

Unitary RG Approach to Quantum Impurity Problems

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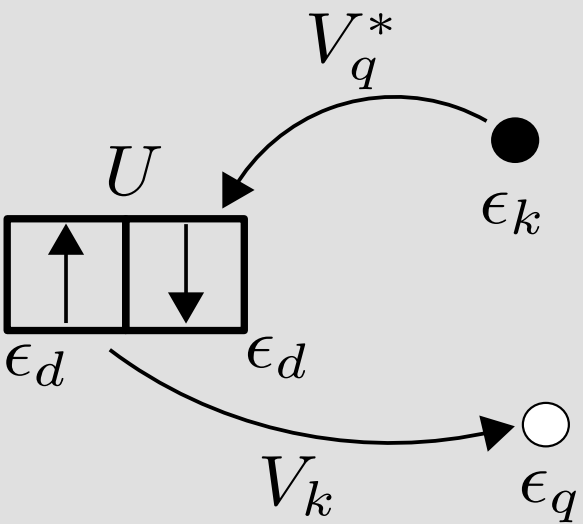


[1] Department of Physical Sciences, IISER Kolkata

[2] Theoretical Sciences Unit, JNCASR

[3] Department of Physics, IIT Kharagpur

The Anderson impurity model (SIAM)

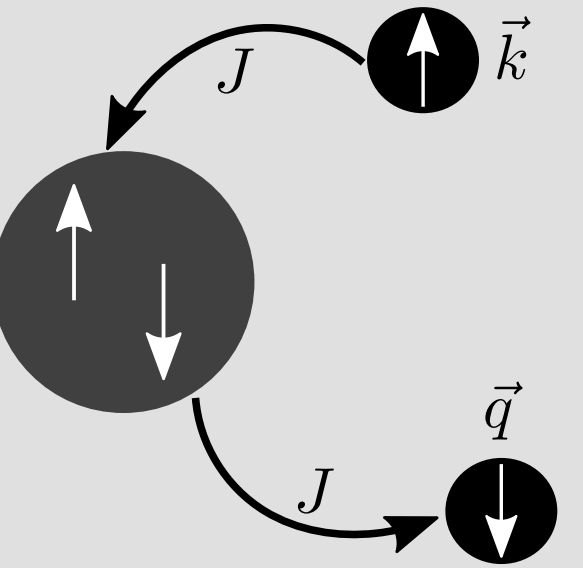


- Local impurity interacting with bath: $H_{\text{bath}} = \sum_{k\sigma} \epsilon_k \hat{n} k \sigma$
- Hubbard repulsion U on impurity and 1-particle hybridisation V with bath

$$H = H_{\text{bath}} + \epsilon_d \hat{n}_d + U \hat{n}_{d\uparrow} \hat{n}_{d\downarrow} + V \sum_{k\sigma} \left(c_{k\sigma}^\dagger c_{d\sigma} + \text{h.c.} \right)$$

- ## ● Microscopic origin of local moments in metals

The (spin) Kondo model

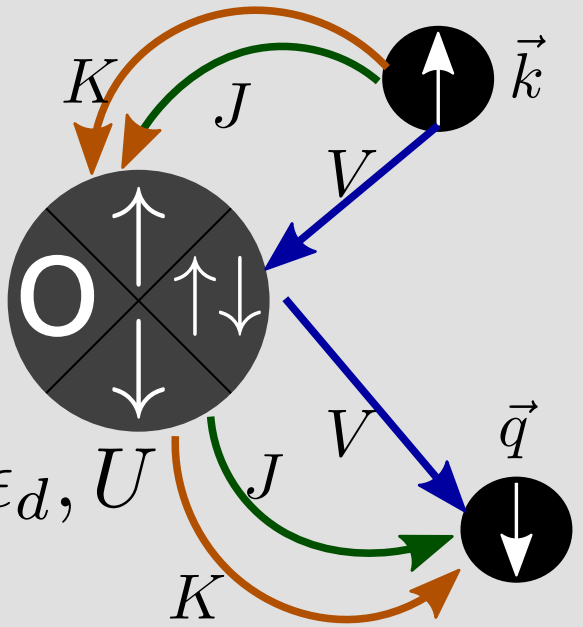


- Impurity projected to spin-half Hilbert space
- **Spin-exchange coupling** with conduction bath spin

$$H = H_{\text{bath}} + J \vec{S}_d \cdot \vec{s}$$
- Ground state is a **macroscopic singlet** formed by the impurity and the conduction bath
- Charge variant involves **isospin exchange**

$$H = H_{\text{bath}} + J\vec{S}_d \cdot \vec{s}$$

Generalised Kondo-SIAM model

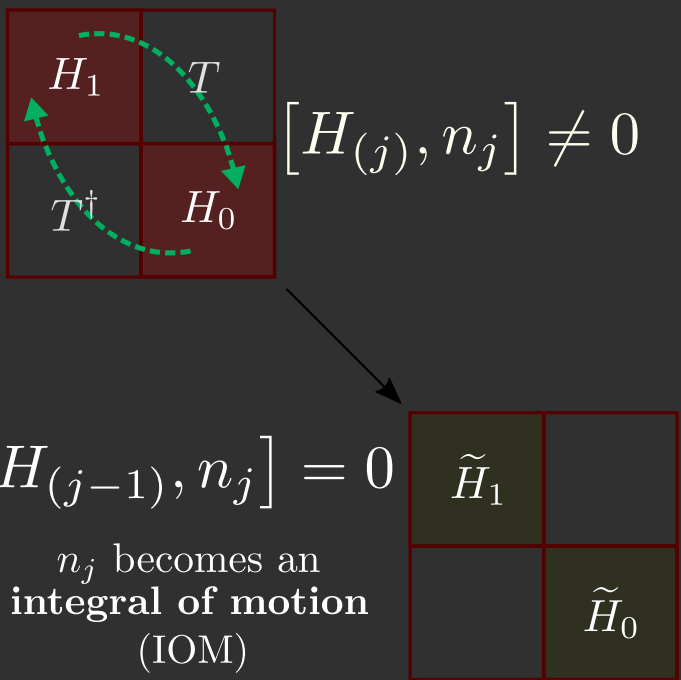


- Add spin and isospin exchange J and K to SIAM
- Exchange couplings are **dynamically generated under RG**, simpler to keep them at the start
- V renormalises at lowest order
- Describes **both spin and charge screening** in one model

Outstanding Questions

- What's the **effective Hamiltonian** for the conduction electrons that screen the impurity?
- What is the **nature of the metal** responsible for this screening?
- Quantitative insight into **many-particle entanglement** at and near the fixed point
- Does the interplay of V , J and K change the phase diagram in the generalised SIAM?
- Is there any **topological quantity** that changes in the process of screening?
- Can the inclusion of J lead to a local **metal-insulator transition** on the impurity?

The Unitary Renormalisation Group (URG) Method



- Proceeds by **applying unitary transformations** U_j on the Hamiltonian to generate RG flow H_j

$$H_{j-1} = U_j H_j U_j^*$$

- U_j are defined so as to **remove quantum fluctuations** of high energy k -states

- Continues until fixed point where denominator of RG equation vanishes

- Fixed point Hamiltonian describes **emergent theory** at low energy