$$i\partial\psi_i = [F_{\psi_i} + V(t)] \qquad \psi_i(t) = d^i_{mn}(t)e^{i\epsilon_m t}\overline{\psi}_m \qquad F_0\psi_p = \epsilon_p\overline{\psi}_p$$
 (1)

$$i\dot{d}_{m}^{i} = (F_{nm} - \delta_{nm}\epsilon + V_{mn})d_{m}^{i}e^{i(\epsilon_{n} - \epsilon_{m})}t$$
(2)

$$X_{nm} = \langle \psi_n | \hat{X} | \psi_m \rangle \tag{3}$$

$$\langle \overline{\psi}_p | \overline{\psi}_q \rangle = \delta_{pq} \tag{4}$$

$$i\dot{d}_{m}^{0i} = 0$$
  $\psi_{i}(t_{0}) = d_{m}^{0i}\overline{\psi}_{m}$   $\psi_{i}(t_{0}) = d_{m}^{0i} \neq \delta_{mi}$  (5)

$$i\dot{d}_m^{1i} = (F_{nm}^1 + V_{nm}^1)d_m^{0i}e^{i(\epsilon_n - \epsilon_m)}t\tag{6}$$

$$\rho_k = \psi_i^{\dagger} \Sigma_k \psi_i = d_l^{i*} d_s^i e^{i(\epsilon_l - \epsilon_s)} t \overline{\Psi}_l^{\dagger} \Sigma_k \overline{psi}_s$$
 (7)

$$\rho_k = D_{sl}e^{i(\epsilon_l - \epsilon_s)t}\Omega_{ls}^k \tag{8}$$

$$\nabla \rho_k = D_{sk} e^{i(\epsilon_l - \epsilon_s)t} \nabla \Omega_{ls}^k \tag{9}$$

$$F_{nm}^{1} = \frac{dF_{nm}}{dD_{sl}}D_{sl}^{1} = \frac{d\tilde{F}_{nm}}{dD_{sl}}e^{i(\epsilon_{j} - \epsilon_{s})t}((d_{l}^{0j})^{*}d_{s}^{1j} + (d_{l}^{1j})^{*}d_{s}^{0j})$$

$$(10)$$

$$F_{nm}^{1}d_{m}^{0i} = F_{mi}^{1} = K_{mi,sj}e^{i(\epsilon_{j} - \epsilon_{s})t}d_{s}^{1j} + K_{mi,jl}e^{i(\epsilon_{l} - \epsilon_{j})t}(d_{s}^{1j})^{*}$$
(11)

$$K_{mm,ls} = \frac{d\tilde{F}_{nm}}{dD_{sl}} \tag{12}$$

$$i\dot{d}_{m}^{1i} = (K_{mi,lj}e^{i(\epsilon_{j}-\epsilon_{l})t}) + (K_{mi,jl}e^{i(\epsilon_{l}-\epsilon_{j})t})(d_{l}^{1j})^{*}$$

$$(13)$$