IEE Mains 2020

Chapter wise Tests

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1. If the point (x, y) be equidistant from the points (a+b, b-a) and (a-b, a+b), then

- (a) ax + by = 0
- (b) ax by = 0
- (c) bx + ay = 0
- (d) bx ay = 0
- **2.** A triangle with vertices (4, 0); (-1, -1); (3, 5) is
 - (a) Isosceles and right angled
 - (b) Isosceles but not right angled
 - (c) Right angled but not isosceles
 - (d) Neither right angled nor isosceles
- 3. Each vertex of a right angled triangle is reflected in the opposite side. The ratio of the area of the line triangle thus formed and the original triangle is
 - (a) 2 (b) 3
- (c) 4
- (d) None of these
- 4. If A(6, 3), B(-3, 5), C(4, -2) and D(x, 3x) are four points. If the ratio of area of $\triangle DBC$ and $\triangle ABC$ is 1: 2, then the value of x, will
 - 11 (a) 8
- (b) 11
- (c) 3 (d) None of these
- 5. If the three vertices of a rectangle taken in order are the points (2, -2), (8, 4) and (5, 7). The coordinates of the fourth vertex is-(a)(1,1)(b) (1, -1) (c) (-1, 1) (d) None of these
- The extremities of a diagonal of a parallelogram are the points (3, -4) and (-6, 5). If third vertex is (-2, 1), then fourth vertex is: (c) (1, 1) (d) None of these (b) (-1, 0)
- Area of a triangle is 5. Its two vertices are (2, 1) and (3, -2). Third vertex is on line y = x + 3. That vertex will be-

- $\left(-\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$ and $\left(-\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$ is The distance between the orthocenter and circumcentre of the triangle with vertices (1, 0)
 - (a) 2

- (d) 0
- 9. Two vertices of a triangle are (5, -1) and (-2, 3). If orthocentre of the triangle is the origin then coordinates of third vertex, are (a) (-4, -7) (b) (-4, 7) (c) (4, 7) (d) (4, -7)
- 10. A (3, 1), B (6, 5) and C (x, y) are three points such that angle ACB is a right angle and the area of triangle ABC = 7sq. unit. then the number of such points C is-
 - (a) 0 (b) 1 (c) 2
 - (d) 3
- **11.** The area of the pentagon whose vertices are (4, 1)(3, 6) (-5, 1)(-3, -3) and (-3, 0) is
 - (a) 30 unit²
- (b) 60 unit^2 (c) 120 unit^2
- $\sqrt{(x-2)^2 + (y-1)^2}$ $\sqrt{(x+2)^2 + (y-4)^2} = 5$ represents.
 - (a) Circle
- (b) Ellipse
- (c) Line segment (d) None
- 13. Let A(2, 4), B(-3, -8) and C(x, y) are three points such that \angle ACB is a right angle and the area of \triangle ABC = (41/2) units. The number of such points C is
- (b) 2
- (c) 4 (d) Infinite
- 14. If AB = 2a, given the base of \triangle ABP, where P is a variable such that tanA + tanB = λ (constant), then the locus of P is-

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- (a) A circle
- (b) A parabola
- (c) A hyperbola
- (d) None
- 15. A ray of light coming from the point (1, 2) is reflected at a point A on the x-axis and then passes through the point (5, 3). The coordinates of the point A are-
- (c)(-7,0)
- (d) None of these
- 16. If two vertices of an equilateral triangle have integral coordinates then the third vertex will have
 - (a) Integral coordinates
 - (b) Rational coordinates(c) At least one irrational coordinate
 - (d) Irrational coordinates
- 17. The area of the triangle with vertices at the points (a,b+c), (b,c+a), (c,a+b) is-
 - (a) 0
- (b) a + b + c
- (c) ab + bc + ca
- (d) None
- **18.** The incentre of the triangle with vertices $(1, \sqrt{3})$, (0, 0), (2, 0) is-
- $\left(\frac{2}{3}, \frac{1}{\sqrt{3}}\right)$
- $(d) \left(1, \frac{1}{\sqrt{3}}\right)$
- 19. The cartesian co-ordinates of

- **20.** The line x + y = 4 divides the line joining the points (-1, 1) and (5, 7) in the ratio
- (a) 2:1 (b) 1:2 (c) 1:2 externally (d) None



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 $\sqrt{3}\sin\theta + 2\cos\theta = \frac{4}{r}$ $\left[-1,\frac{\pi}{2}\right]$ and perpendicular to The equation of line passing through 1.

- (a) $2 = \sqrt{3} r \cos \theta 2r \sin \theta$
- (b) $5 = -2\sqrt{3} r \sin\theta + 4r \cos\theta$
- (c) $2 = \sqrt{3} r \cos \theta + 2r \sin \theta$
- (d) $5 = 2\sqrt{3} r \sin\theta + 4r \cos\theta$
- If the lines x = a + m, y = -2 and y = mx are concurrent, the least value of |a| is
- (b) $\sqrt{2}$ (c) $2\sqrt{2}$
- (d) None of these
- If the line passing through (4, 3) and (2, k) is perpendicular to y = 2x + 3, then k = 1
- (b) 1
- (c) -4
- (d) 4
- The equation of the base of an equilateral triangle ABC is
 - x + y = 2 and the vertex is (2, -1). The area of the triangle ABC is

- If a point P moves such that its distance from line $y = \sqrt{3} x$ -7 is same as its distance from $(2\sqrt{3}, -1)$, then area of curve described by P, enclosed between coordinate axes is-
 - $\sqrt{3}$ (a) 2

(b) $2^{\sqrt{3}}$

(c) 6

- (d) None of these
- The circum-center of the triangle formed by the lines xy + 2x + 2y + 4 = 0 and x + y + 2 = 0 is -
 - (a) (-2, -2)(b)(0,0)
 - (c)(-1,-2)
 - (d)(-1,-1)
- Equation of line inclined at an angle of 45° with positive x-axis and dividing the line joining the points (3, -1) and (8, 9) in the ratio
 - (a) x y 2 = 0
- (b) 3x 3y + 1 = 0
- (c) $\sqrt{3} x \sqrt{3} y + 2 = 0$
- (d) None of these
- The straight lines represented by $(y mx)^2 = a^2 (1 + m^2)$ and $(y nx)^2 = a^2 (1 + n^2)$ form a-
 - (a) Rectangle
- (b) Trapezium
- (c) Rhombus
- (d) None of these
- A line which is parallel to the line common to pair of lines given by $6x^2 xy 12y^2 = 0$ and $15x^2 + 14xy 8y^2 = 0$ and makes intercepts on axes whose sum of length is 7,is
 - (a) 2x 3y = 42
- (b) 3x + 4y = 12
- (c) 5x 2y = 10
- (d) None of these
- 10. The point $(a^2, a + 1)$ lies in the angle between the lines 3x y + 1 = 0 and x + 2y 5 = 0 containing the origin, if-

- 11. For how many integral values of m do the lines y + mx 1
 - = 0 and 3x + 4y = 9 intersect in points having integral coordinates -
- (b) 1
- (c) 2
- (d) Infinite
- 12. Consider the locus of a moving point P(x, y) in the plane which satisfies the condition

$$2x^2 = r^2 + r^4$$
, where $r^2 = x^2 + y^2$

Then, only one of the following statement is true-

- (a) For every 0 < r < 1, there are exactly four points on the
- curve
- (b) For every $0 < r \le 1$, there are exactly four points on the curve
- (c) The locus is a pair of straight lines

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(d) None of these

13. A (a, 0), B (b, 0), C (c, 0) and D(d, 0) are four given points. If $\frac{CA}{CB} + \frac{DA}{DB} = 0$, then-

$$\frac{1}{a} + \frac{1}{b} = \frac{1}{c} + \frac{1}{d}$$

- (b) (a + b) (c + d) = 2 (ab + cd)
- (c) (a + b) ab = (c + d) cd
- (d) None of these
- 14. Number of lines drawn from the point (4, -5) so that its distance from (-2, 3) will be equal to 12 are-
 - (a) 2
- (c) 4
- (d) None of these
- 15. The equation of the lines which passes through the point (3, -2) and are inclined at 60^0 to the line $\sqrt{3}x + y = 1$

(a)
$$y + 2 = 0$$
, $\sqrt{3}x - y - 2 - 3\sqrt{3} = 0$

(b)
$$x - 2 = 0$$
, $\sqrt{3}x - y + 2 + 3\sqrt{3} = 0$

(c)
$$\sqrt{3}x - y - 2 - 3\sqrt{3} = 0$$

(d) None of these

16. If
$$\frac{1}{ab'} + \frac{1}{ba'} = 0$$
, then lines $\frac{x}{a} + \frac{y}{b} = 1$ and $\frac{x}{b'} + \frac{y}{a'} = 1$ are

- (a) Parallel
 - (b) Inclined at 600 to each other
 - (c) Perpendicular to each other
 - (d) Inclined at 300 to each other
- 17. The distance between 4x + 3y = 11 and 8x + 6y = 15, is
 - (a) 7/2 (b) 4 (c) 7/10 (d) None of these
- 18. The straight lines $y = m_1 x + c_1$ and $y = m_2 x + c_2$ will meet the co-ordinate axis in concyclic points if -
 - (a) $m_1 m_2 = 2$
 - (b) $c_1 c_2 = 2$
 - (c) $m_1 m_2 = 1$
- (d) $c_1 c_2 = 1$
- 19. A line segment of length (a + b) moves in such a way that its ends are always on two fixed perpendicular straight lines. Then the locus of the point on this line which divide it into portions of lengths a and b is-
 - (a) A parabola
- (b) A circle
- (c) An ellipse
- (d) None of these
- 20. If the algebraic sum of distances of points (2,1), (3,2) and (-4,7) from the line y=mx+c is zero, then this line will always pass through a fixed point whose co-ordinate is-
 - (a)(1,3)

(b) (1, 10)

(c)(1,6)



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1. Let f(x,y) = 0 be the equation of a circle. If $f(0,\lambda) = 0$ has equal roots $\lambda = 2,2$ and $f(\lambda,0) = 0$ has roots of the circle is

$$(a) \left(2, \frac{29}{10}\right)$$

$$(b)^{\left(\frac{29}{10},2\right)}$$

(b)
$$\left(\frac{29}{10}, 2\right)$$
 (c) $\left(-2, \frac{29}{10}\right)$ (d) None

The polar of the point $\left(5, -\frac{1}{2}\right)$ with respect to circle $(x-2)^2 + y^2 = 4$ is

(a)
$$5x - 10y + 2 = 0$$

(b)
$$6x - y - 20 = 0$$

(c)
$$10x - y - 10 = 0$$

(d)
$$x - 10y - 2 = 0$$

If circles $x^2 + y^2 + 2ax + c = 0$ and $x^2 + y^2 + 2by + c = 0$ touch each other, then

$$\frac{1}{a} + \frac{1}{b} = \frac{1}{c}$$

(b)
$$\frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{c^2}$$

$$(c) \frac{1}{a} + \frac{1}{b} = c^2$$

(d)
$$\frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{c}$$

The common chord of $x^2 + y^2 - 4x - 4y = 0$ and $x^2 + y^2 = 16$ subtends at the origin an angle equal to

$$\frac{\pi}{6}$$

$$\frac{\pi}{4}$$

$$\frac{\pi}{(c)}$$
 3

5. If the tangent at the point P on the circle $x^2 + y^2 + 6x + 6y = 2$ meets the straight line 5x - 2y + 6 = 0 at a point on the y-axis, then the length of PQ is

$$_{(b)} \sqrt{5}$$

(c) 5 (d)
$$3\sqrt{5}$$

6. If length of common chord of two circles

 $x^2+y^2+8x+1=0$ and $x^2+y^2+2\mu y$ -1 = 0 is $\sqrt[2]{6}$, then value of μ are

$$(a) \pm 2$$

(b)
$$\pm 3$$

$$(c) \pm 4$$

7. The range of parameter 'a' for which the variable line

y = 2x + a lies between the circle

 $x^2 + y^2 - 2x - 2y + 1 = 0$ and $x^2 + y^2 - 16x - 2y + 61 = 0$ without intersecting or touching either circle, is -

(a)
$$(-15 + 2\sqrt{5}, -\sqrt{5} - 1)$$
 (b) $(15 + 2\sqrt{5}, \sqrt{5} - 1)$

(b)
$$(15 + 2\sqrt{5}, \sqrt{5} - 1)$$

(c)
$$(-15-2\sqrt{5}, -\sqrt{5}+1)$$
 (d) $(-15+2\sqrt{5}, \sqrt{5}-1)$

(d)
$$(-15+2\sqrt{5}, \sqrt{5}-1)$$

8. If equation $(a+1)x^2 + (b-1)y^2 + (a-2b)xy - 6x + 9y - 3 = 0$ represent a circle then its radius is

(a) 3/2

(b)
$$2/3$$

(d)
$$\sqrt{a^2 + b^2}$$

9. If a circle of constant radius 3k passes through the origin and meets the axes at A and B, the locus of centroid of ΔOAB is-

(a)
$$x^2 + y^2 = k^2$$

(b)
$$x^2 + y^2 = 2k^2$$

(c)
$$x^2 + y^2 = 3k^2$$

(d)
$$x^2 + y^2 = 4k^2$$

10. If the circle $x^2 + y^2 - 4x - 6y + \lambda = 0$ touches x- axis then the value of λ is

11. The equation of the line parallel to the line 3x + 4y = 0 and touching the circle $x^2 + y^2 = 9$ in the first quadrant is -

(a)
$$3x + 4y = 9$$

(b)
$$3x + 4y = 45$$

(c)
$$3x + 4y = 15$$

12. The locus of the centre of a circle which touches externally the circle $x^2 + y^2 - 6x - 6y + 14 = 0$ and also touches the y-axis is given by the equation -

(a)
$$x^2 - 6x - 10y + 14 = 0$$

(b)
$$x^2 - 10x - 6y + 14 = 0$$



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for

which

(c)
$$y^2 - 6x - 10y + 14 = 0$$
 (d) y^2

(d)
$$y^2 - 10x - 6y + 14 = 0$$

- (a) 0
- (b) 25
- (c) 25
- (d) None of these
- 14. The equation of the diameter of the circle

$$x^2 + y^2 - 6x + 2y - 8 = 0$$
 is given by

- (a) x + 3y = 0
- (b) x 3y = 0
- (c) x 2y = 0
- (d) x + 2y = 0
- 15. If the chord y = mx + 1 of the circle $x^2 + y^2 = 1$ subtends an angle of measure 45° at the major segment of the circle then value of m

13. The circle $x^2 + y^2 - 6x - 10y + p = 0$ does not touch nor intersect the coordinate axes if the point (1, 4) lies inside the circle then -

- (a) 2
- (b) 2 (c) ± 1 (d) None of these
- **16.** If the distances from the origin to the centres of three circles $x^2 + y^2 + 2\lambda_i x c^2 = 0$ (i = 1, 2, 3) are in G.P. then the lengths of the tangents drawn to them from any point on the circle $x^2 + y^2 = c^2$ are in
- (c)H.P.
- (d) None of these
- 17. A foot of the normal from the point (4, 3) to a circle is (2, 1) and a diameter of the circle has the equation 2x y = 2. Then the equation of the circle is
 - (a) $x^2 + y^2 + 2x 1 = 0$
- (b) $x^2 + y^2 2x 1 = 0$
- (c) $x^2 + y^2 2y 1 = 0$
- (d) None of these
- **18.** The number
- of integral
- $x^2 + y^2 + 2\lambda x + 2(1 \lambda)y 1 = 0$ is the equation of a circle whose radius can not exceed 3
 - (a) 3 (b) 4 (c) 5 (d) None
- **19.** In a triangle ABC, $r^2 + r_1^2 + r_2^2 + r_3^2 + a^2 + b^2 + c^2$ is equal to -
 - (a) $4R^2$ (b) $8R^2$ (c) $12R^2$ (d) $16R^2$
- 20. The area of the circle and the area of a regular polygon of n sides, and of perimeter equal to that of the circle are in the ratio of
 - (a) $\tan \left(\frac{\pi}{3}\right) : \frac{\pi}{n}$ (b) $\cot \left(\frac{\pi}{n}\right) : \frac{\pi}{n}$