

SOLVING LCR CIRCUIT USING RUNGE KUTTA METHOD-19003//ABHISEK PRAHARAJ

Charging of Capacitor in LCR circuit. The enf equation for the circuit is

$$L \frac{d^2 q}{dt^2} + R \frac{dq}{dt} + \frac{q}{C} = E \text{ -----1}$$

Where $q(t)$ is the instantaneous charge on the capacitor. The second order oDE can be split into 2 first order coupled ODEs

$$\frac{dq}{dt} = i = f_1(q, i, t) \text{ -----2}$$

$$\frac{di}{dt} = (E - Ri - q/C)/L = f_2(q, i, t) \text{ -----3}$$

There are 3 cases on interest-

- OverDamped when $R > 2 \sqrt{L/C}$
- CriticalDamped when $R = 2 \sqrt{L/C}$
- UnderDamped when $R < 2 \sqrt{L/C}$