

# Today's Agenda:-

Starting 7:05

- ① Minimum Spanning Tree
  - a) Kruskal's Algo
  - b) Prim's Algo

- ② Dijkstra's Algorithm

Q:- Given  $N$  islands and cost of construction of a bridge b/w multiple pair of islands. Find minimum cost of construction required such that it is possible to travel from one island to any other island via bridges.  
If not possible, return -1.

Ex:-  $N=7, E=9$

1	<u>3</u>	2
1	<u>5</u>	3
2	<u>1</u>	4
2	<u>5</u>	5
3	<u>3</u>	5

4	<u>2</u>	6
3	<u>8</u>	6
4	<u>5</u>	7
6	<u>3</u>	7

Obs 1:-

All islands must be connected with each other.

⇓  
Graph must be connected.

Obs. 2:- Min Cost  $\Rightarrow$  Min. no. of bridges to construct.

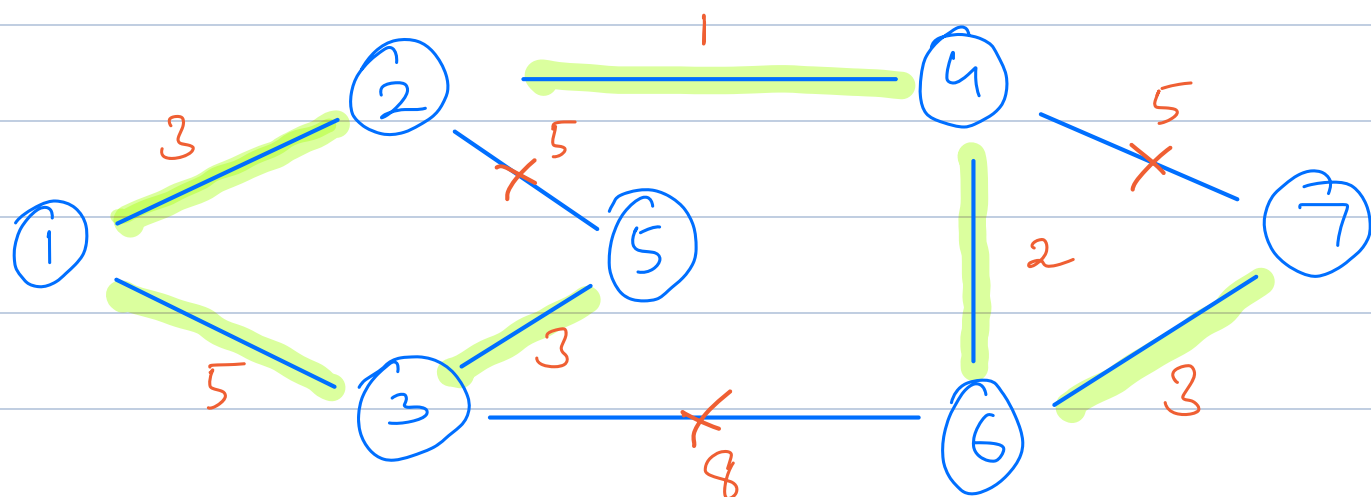
$(N-1)$  edges.

Tree...

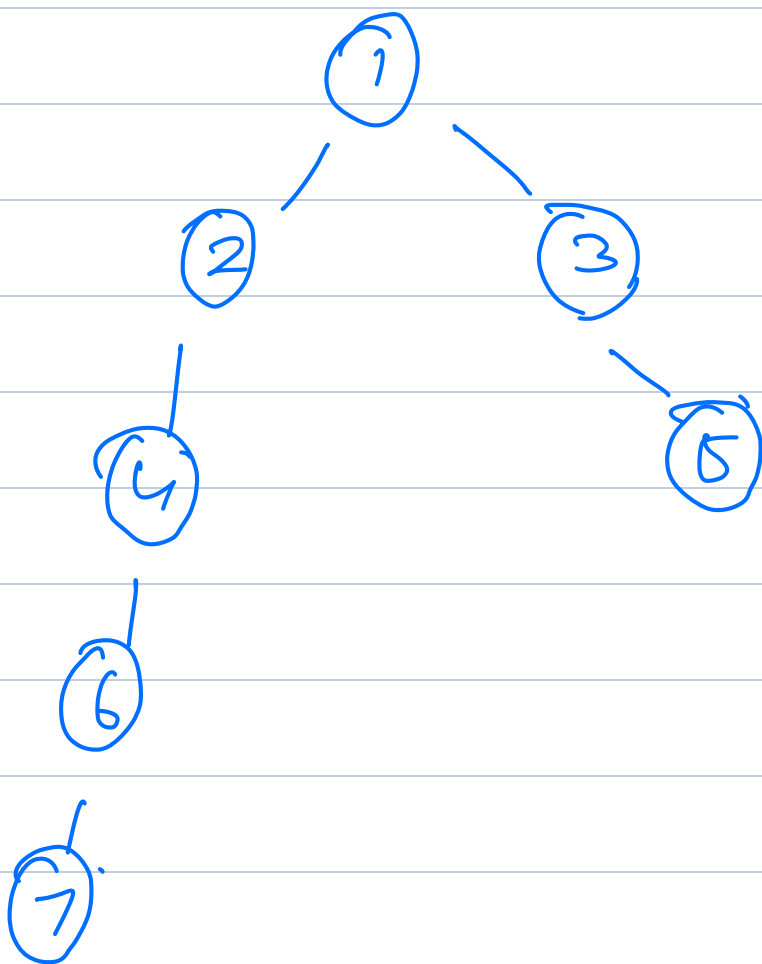
$\leq$  wt of selected edges is minimum



M.S.T.

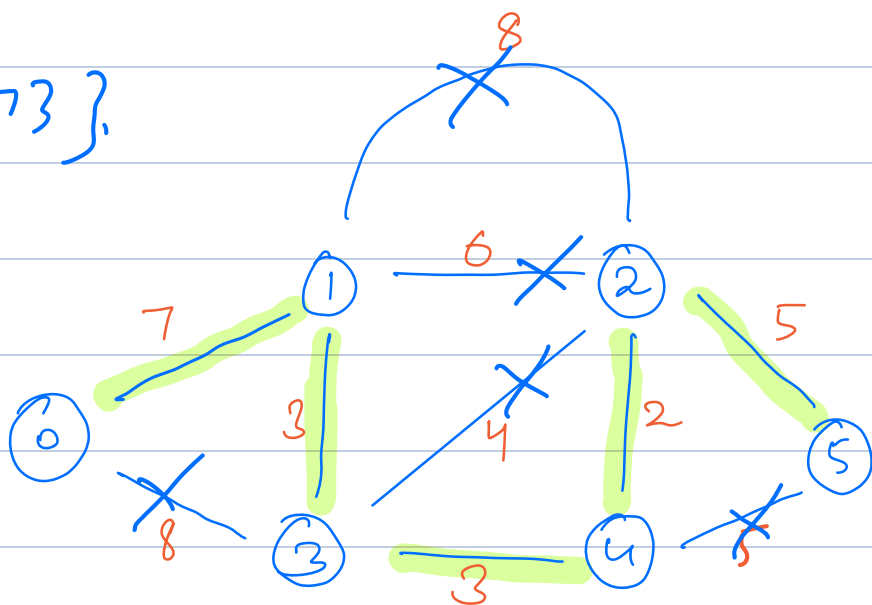


Ans = 17.



# Kruskal's Algorithm

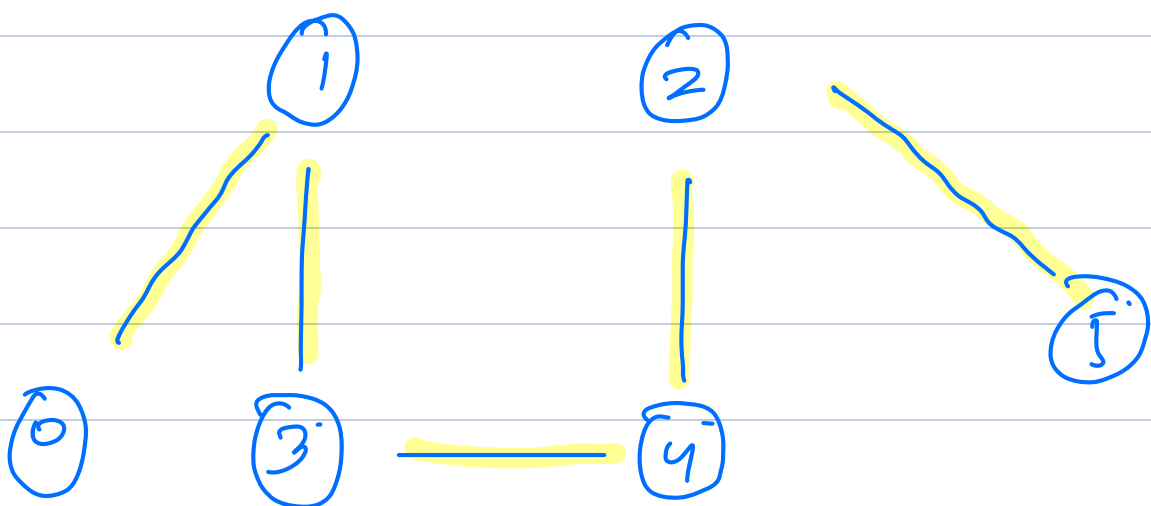
0	- { {1,7}, {3,8} }
1	- { {3,3}, {2,6}, {2,8}, {0,7} }
2	- { {1,8}, {1,6}, {3,4}, {4,2} }
3	- { {0,13}, {1,3}, {2,4}, {4,3} }
4	- { {2,2}, {3,3}, {5,5} }
5	- { {2,5}, {4,5} }



$$\text{Ans} = \underline{\underline{20}}$$

① Sort the edges of the graph in increasing order of wt.

2	2	4	✓
1	3	3	✓
3	3	4	✓
2	4	3	✗
2	5	5	✓
4	5	5	✗
1	6	2	✗
0	7	1	✓
0	8	3	✗
1	8	2	✗



$$\begin{aligned} \text{Ans} &= 0+2+3 \\ &\quad + 3+5 \\ &\quad + 7 \\ &= \underline{\underline{20}} \end{aligned}$$

```

Edge {
    int u;
    int v;
    int wt;
}

```

List <Edges>

Step 2:-

```

for (Edge e : arr) {

```

```

    if (union(e.u, e.v) == true) {

```

```

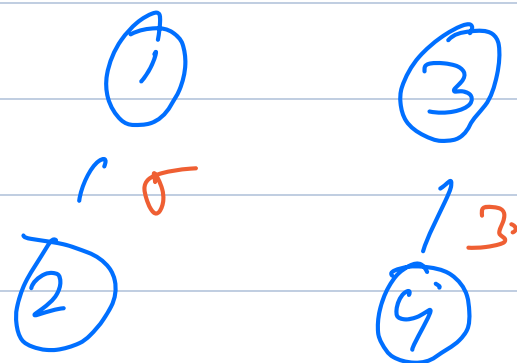
        ans += e.wt;
    }
}

```

}

return ans;

~~\*\*\*~~ → Check for connected graph.

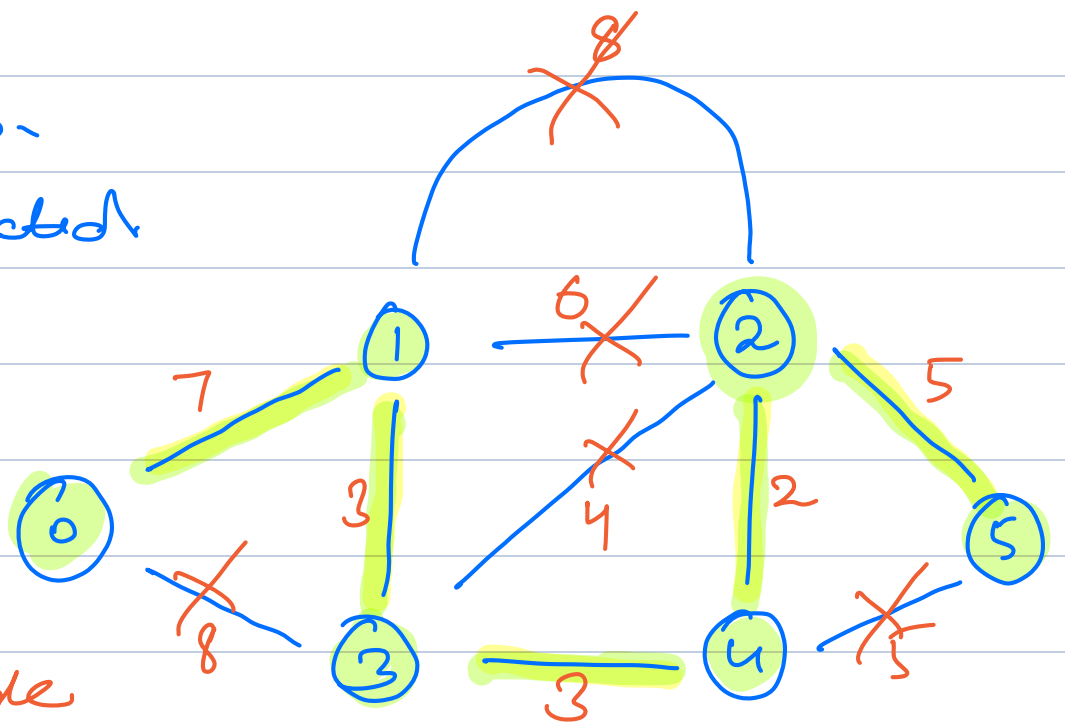


T.C. →  $O(E \log E)$

S.C. →  $O(E + V)$

# Prim's Algorithm

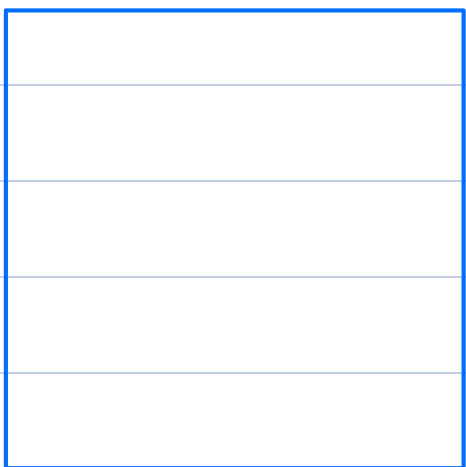
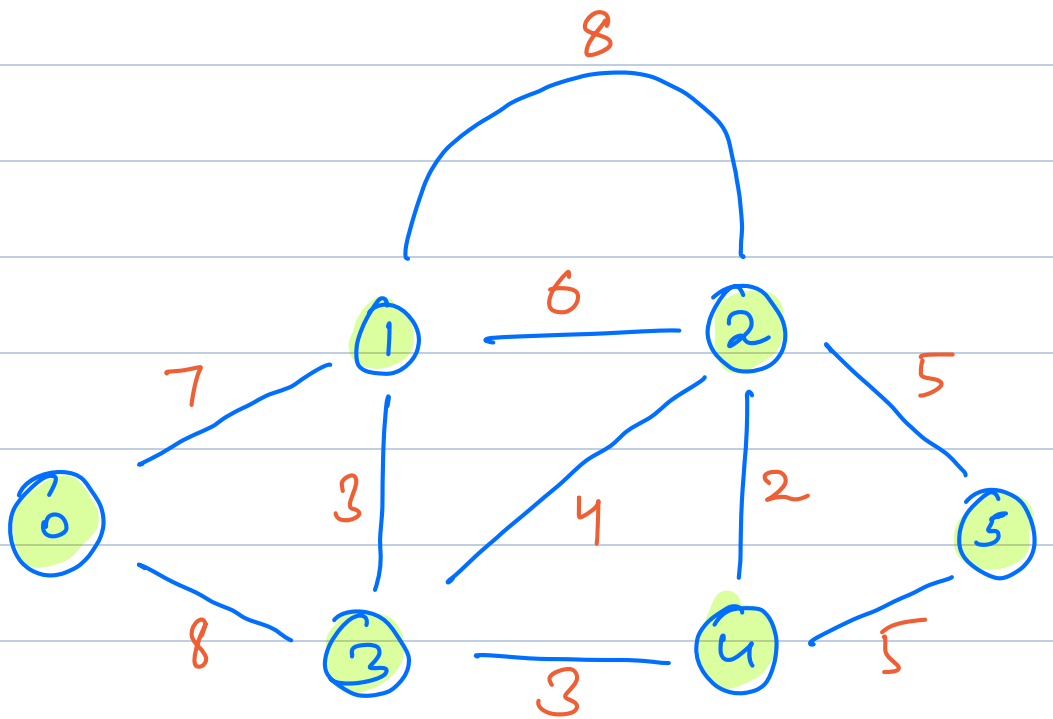
yellow  $\rightarrow$  In collection  
 green  $\rightarrow$  Already selected



$\rightarrow$  Start with any node as root node  
 \* Keep on adding the other nodes with min. wt;

visited.

t	t	t	t	t	t
0	1	2	3	4	5



ans

$$0 + 7 + 3 + 3 + 2 + 5$$

priority Q.

Edge {  
 int v;  
 int wt

return 20;

3.

```
# visited[N];   ∀i   visited[i] = false;
```

```
minHeap < Edge > heap;
```

```
visited[0] = true;
```

```
for (Edge e : graph[0]) {
```

```
    |   heap.insert(e);
```

```
    }
```

```
int ans = 0;
```

```
while (heap.size() > 0) {
```

```
    Edge re = heap.remove();
```

```
    if (visited[re.v] == true) {
```

```
        continue;
```

```
    } else {
```

```
        visited[re.v] = true;
```

```
        ans += re.wt;
```

```
        for (Edge e : graph[re.v]) {
```

```
            |   if (visited[e.v] == false) {
```

```
                |   heap.insert(e);
```

```
                |   }
```

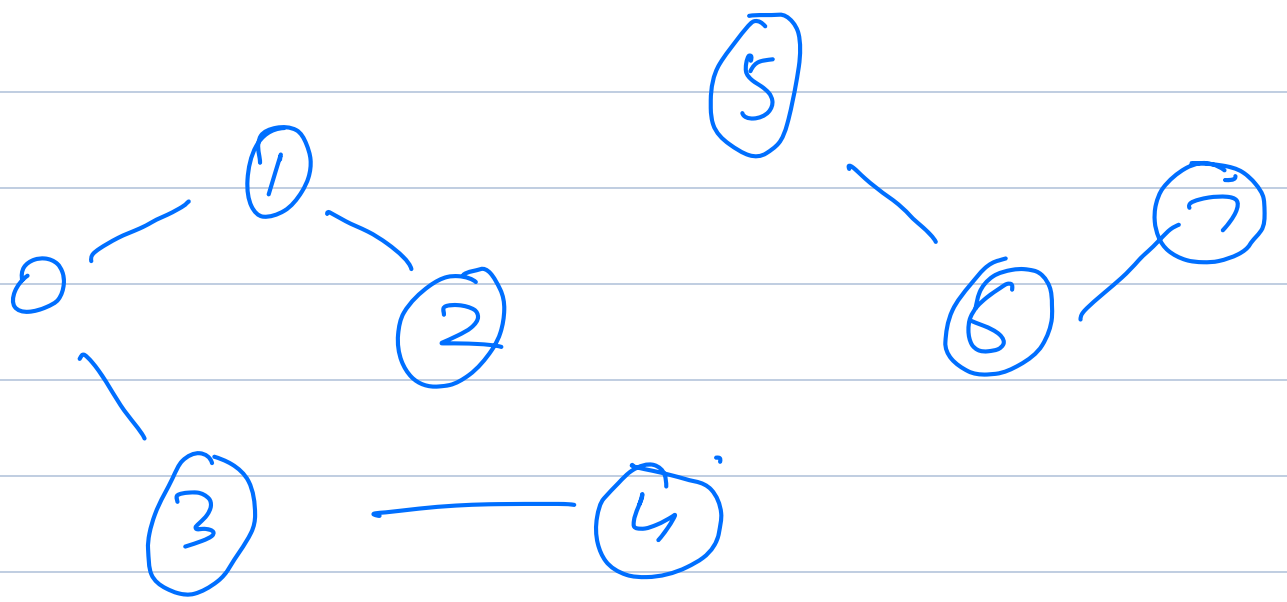
```
            |   }
```

```
        }
```

```
    }
```

```
    return ans
```

# Check for connectivity safely  
point away.



T.C  $\rightarrow O(E \log E)$

S.C  $\rightarrow O(N + E)$

8:50

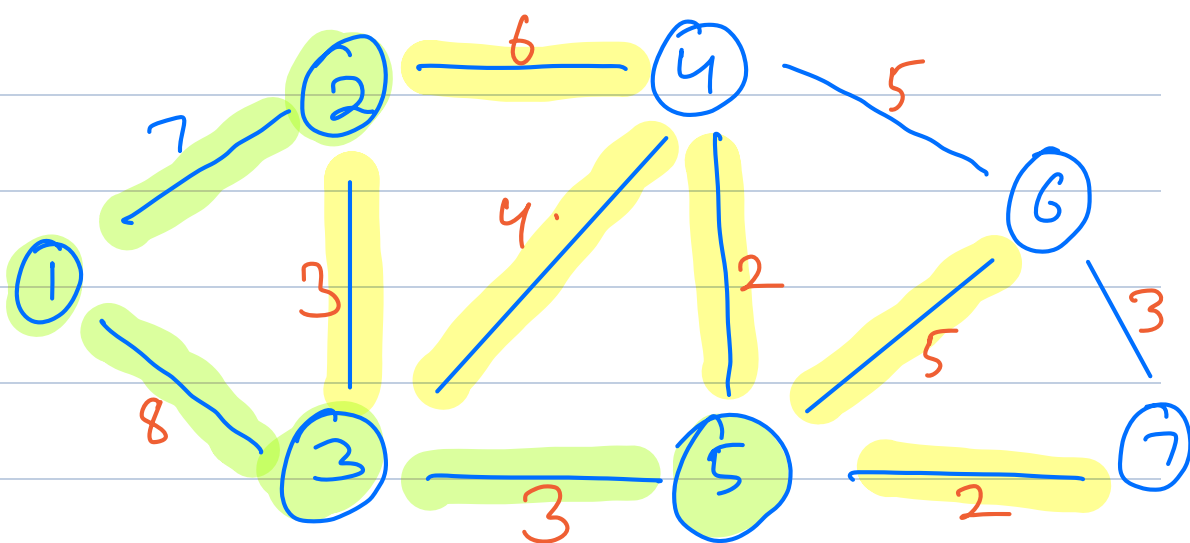


# Dijkstra's Algorithm

(Single source shortest path)

(Edge wt 70)

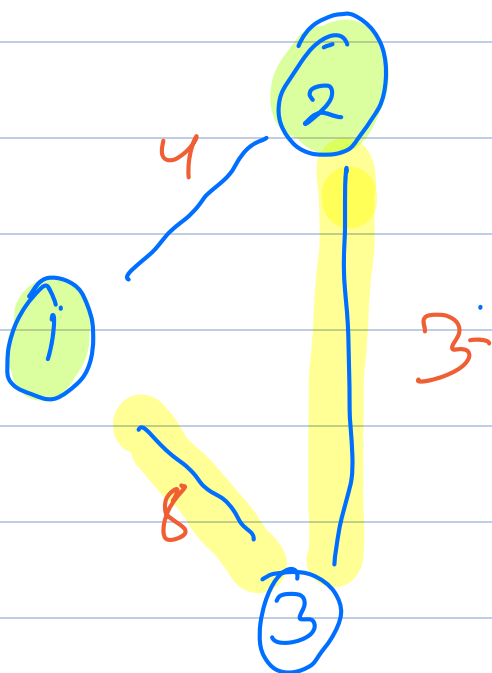
Q1. There are  $N$  cities in a country, you are living in city 1. Find min. distance to reach every other city from city 1.



Expected Output

dist;

0	7	8	12	11	16	13
1	2	3	4	5	6	7

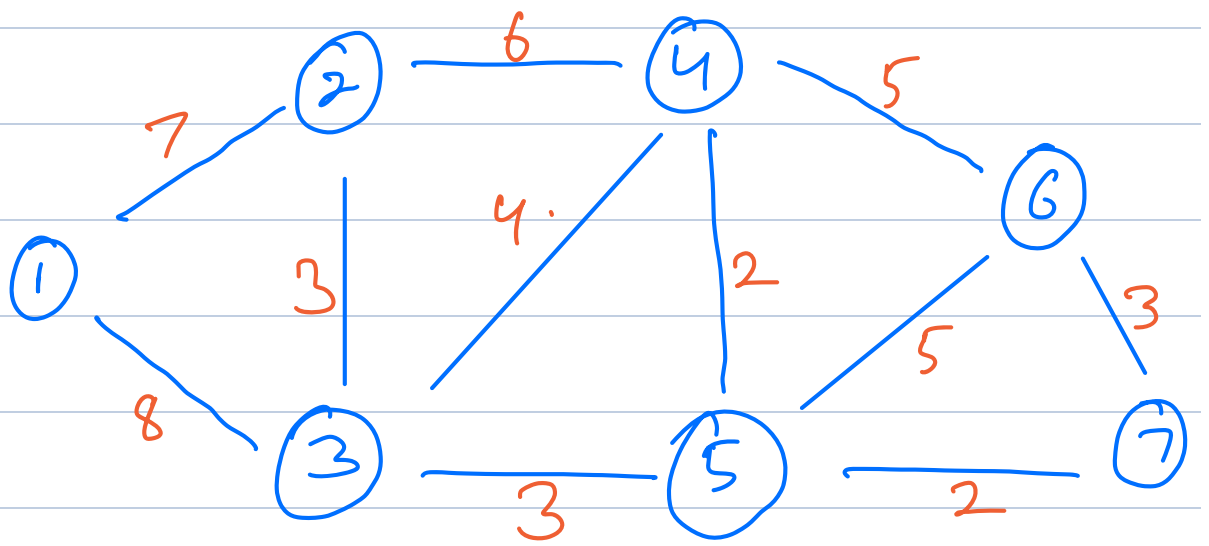


more connections

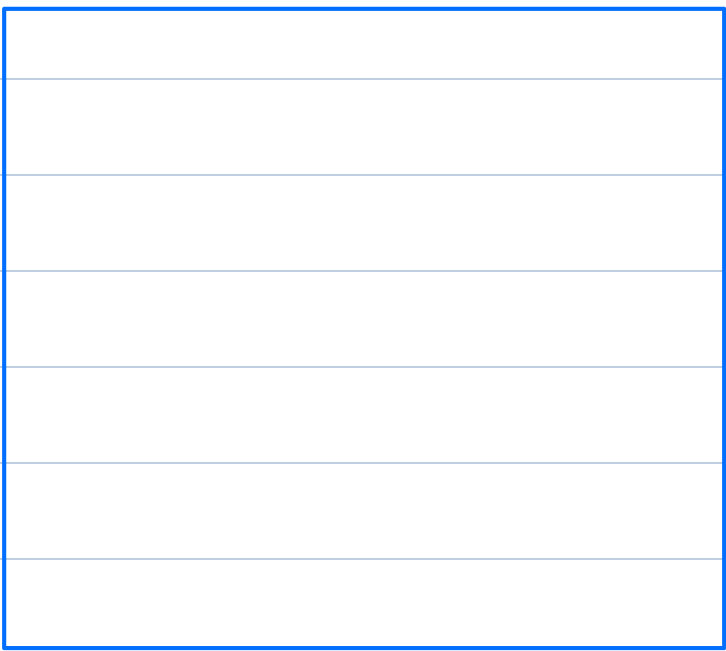
8, 4+3

Pair {  
 int v;  
 int wsf;

3.



		7	8	12	11	16	13
dist:	$\infty$	0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
	0	1	2	3	4	5	6



min heap.

# Code:

```
dist[N+1];   $\forall i$  dist[i] = INT_MAX;
```

```
minHeap < Pair > heap;
```

```
heap.insert(new Pair(src, 0));
```

```
while (heap.size() > 0) {
```

```
    Pair op = heap.removeMin();
```

```
    if (dist[op.v] != INT_MAX)
        continue; }
```

```
    else {
```

```
        dist[op.v] = op.wsf;
```

```
        for (int nbr: graph[op.v]) {
```

```
            if (dist[nbr] == INT_MAX) {
```

```
                heap.insert(new Pair
                    (nbr, op.wsf
                     + wt. of current
                     edge));
```

```
            }
```

```
        }
```

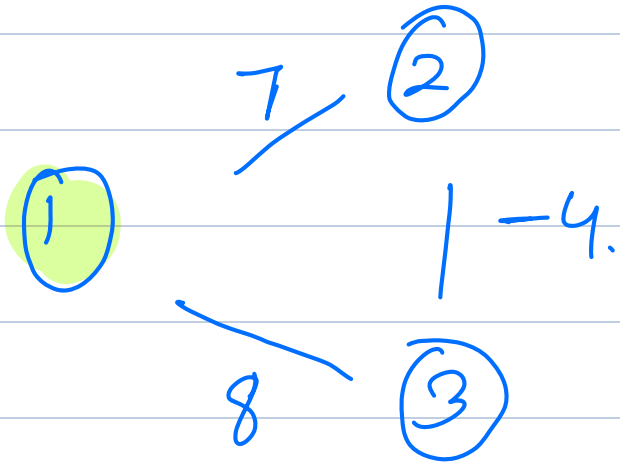
```
    }
```

```
} return dist;
```

T.C  $\rightarrow O(E \log E)$ .

S.C.  $\rightarrow O(E)$ .

Can it work for -ve edge weight?



0	7	3
1	2	3

# Dijkstra's algorithm is not going to give the correct answer.