

Will  
start  
7:05 AM  
IST

# Welcome

## Intro. to problem solving

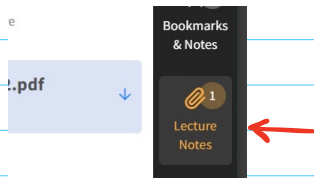
### Instructors

✓ - Amir

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- class time 2.5 hours  $\pm$  10 min

- notes



- Assignments & homework

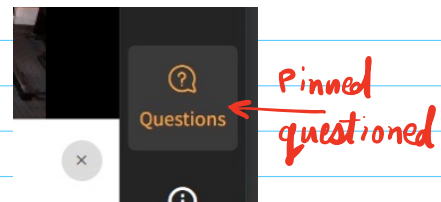
- Peer Learning, class communications

whatsapp group . <https://chat.whatsapp.com/IBt9FwPqNsk6Ne7GrIYBut>

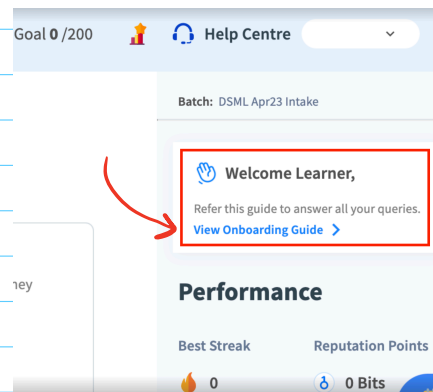
Corrected  
↓

Quick questions: public chat  
Answers: private chat

Questions (Pin your questions  
to be answered at  
the end of session)



- check the onboarding  
guide on your  
dashboard



<sup>int</sup> P1 Count of factors: Given <sup>a</sup> positive integer <sup>> 0</sup> N, return count of

what is factor factors of N.

ex  $N=6$  | 6 2 3 1 ~~ans=4~~

1 2  
 $6/4=1.5$

$a/b=c$   
is a factor of a  
if c is whole int.  
 $a \div b = 0$

Quiz 10 | 10 2 5 1 ans=4  
Correct ↩

Quiz 24 | 1 2 3 4 6 8 12 24 ans=8

Pseudo codes

```

int countFactor(int n){
    count=0
    for(i=1; i<=n; i++){
        if(n%i==0) count+=1
    }
    ret count
}

```

n times

Quiz



I do not run code on my laptop. I run on a super computer 1,000 times faster.

\*Can a really fast processor compensate for inefficient algorithm?

1GHz

N  
 $10^8$   
 $2 \times 10^8$   
 $10^7$   
 $\vdots$   
 $n$   
 $\vdots$   
 $10^{18}$

runtime

1 sec  
 2 sec =  $2 \times 10^8 / 10^8$   
 0.1 sec =  $10^7 / 10^8$   
 $\vdots$   
 $n / 10^8$  sec

$$\frac{10^8}{2} \rightarrow 0.5$$

$$\frac{10^8}{2} = \frac{10 \times 10^7}{2} = 5 \times 10^7$$

Quiz

$$\frac{10^{18}}{10^8} = 10^{10} \text{ sec}$$

years

317 years

optimization?

$n$   $n/i$   
 $24$   $24/i$   
 $i \downarrow$   
 1 24  
 2 12  
 3 8  
 4 6  
 6 4  
 8 3  
 12 2  
 24 1

$$24 \div 1 = 24$$

$$24 \div 6 = 4$$

$$4 \times 6 = 24$$

$n/2$   
 $\sqrt{n}$

24 (1...4)

$$\frac{24}{2} = 12$$

$$24 \quad \frac{n}{2} = \frac{24}{2} = 12$$

16  $16/i$   
 1 16  
 2 8  
 4 4  
 4 4  
 8 2  
 16 1

50  $50/i$   
 1 50  
 2 25  
 5 10  
 10 5  
 25 2  
 50 1

25  $25/i$   
 1 25  
 5 5  
 5 5  
 25 1

$$i \leq \frac{n}{i} \Rightarrow i * i \leq n \Rightarrow i^2 \leq n \Rightarrow i \leq \sqrt{n}$$

1, 2, ..., i

1...  $\sqrt{36}$

36  $36/i$   
 i  
 1 36  
 2 18  
 3 12  
 4 9  
 6 6  
 6 6  
 9 4  
 12 3  
 18 2  
 36 1

pseudo code

```

int countFactor2(int n) {
    Count = 0;
    for (i = 1; i <= sqrt(n); i++) {
        if (n % i == 0) Count += 2;
    }
    if ((i-1) * (i-1) == n) Count += 1;
    return Count;
}
    
```

(X)

Quiz

$$\sqrt{24} = 4.8989...$$

i	24
+1	+24
+2	+12
+3	+8
+4	+6
+5	
	16

N	$\sqrt{N}$	runtime	
$10^8$	$10^4$	$10^4 / 10^8 = 10^{-4}$ Sec	$10^8 \rightarrow 1 \text{ sec}$
$10^{16}$	$10^8$	$10^8 / 10^8 = 1$ Sec	
$\vdots$	$\vdots$		
$10^{18}$	$10^9$	$10^9 / 10^8 = 10$ Sec	

i	9	9/i
+1		+1
2		x
+3		+3
4		

i = 4 Count = 4

true/  
false ↖

P2 check if a number is prime.

↳ what is prime?

positive integer  $N$ .

a number  $> 1$  that is divisible only by 1 & itself.

```
bool isPrime(int n){  
    if (countfactor2(n) == 2){  
        ret true;  
    }  
    ret false;  
}
```

$5 \rightarrow 1, 5$

$13 \rightarrow 1, 13$

$12 \rightarrow 1, 12, 2, 6, 3, 4$

$2 \rightarrow 1, 2$

$10 \mid 2 \ 10$   
 $5 \ 1$

# iteration  $\sqrt{n}$

$\log_2 n \rightarrow$  advanced DSA

### P3 sum of $n$ natural numbers

ex  $n = 10$   $S = 1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + 9 + 10 = 55$

$$S = 10 + 9 + 8 + 7 + 6 + 5 + 4 + 3 + 2 + 1$$

$$2S = \underbrace{11 + 11 + 11 + \dots + 11}_{10 \text{ terms}} = 10 \times 11$$

$$2S = 10 \times 11 \Rightarrow S = \frac{10 \times 11}{2} = 55$$

$n$

$$S = 1 + 2 + 3 + \dots + n$$

$$S = n + (n-1) + (n-2) + \dots + 1$$

$$2S = \underbrace{(n+1) + (n+1) + (n+1) + \dots + (n+1)}_{n \text{ terms}} = n \times (n+1)$$

$$2S = n \times (n+1) \Rightarrow S = \frac{n \times (n+1)}{2}$$

$$16 = 4 \times 4$$

$$\sqrt{16} = 4$$

P4.1 Given  $N$  ( $N$  is a perfect square) return  $\text{sqrt\_root}(N)$ .

```
int sqrt1(int n){
```

```
    for(i=1; i<=n; i++){
```

```
        if(i*i==n) return i
```

```
    }
```

```
    return -1
```

```
}
```

i	i*i	n
1	1	16
2	4	16
3	9	16
4	16	16 ✓

#iterations

$$n \rightarrow \sqrt{n}$$

P4.2 Given  $N$  (any positive int) return  $\text{floor}(\text{sqrt\_root}(N))$

$$\lfloor 3.2 \rfloor = 3 \quad \lfloor \sqrt{24} \rfloor = 4$$

what is floor

$$\lfloor 4 \rfloor = 4$$

$$16 < 24 < 25$$

↓                      ↓  
4, 4, ..., 5

50

i	i*i	n=50
1	1	< x
2	4	< x
3	9	< x
4	16	< x
5	25	< x
6	36	< x
7	49	< x
8	64	> x

```
int sqrt2(n){
```

```
    i=1; ans=0
```

```
    while(i*i<=n){
```

```
        ans=i
```

```
        i++
```

```
    }
```

```
    return ans
```

```
}
```

## Log Basics

$$a \leftarrow 2^3 = 8 \rightarrow c$$

$$a \leftarrow 3^2 = 9 \rightarrow c$$

$$2^6 = 64$$

$$10^3 = 1000$$

$$\log_{10} 1000 = 3$$

$$a^b = c$$

$$2^3 = 8 \longleftrightarrow \sqrt[3]{8} = 2$$

$$\sqrt[b]{c} = a$$

$$\log_2 8 = 3$$

$$a \quad a^{10}$$

$$\log_a a^{10} = 10$$

HW

Consider  $n$  (a positive int) how many times can we divide  $n$  by 2 till it reaches 1.

$$\text{ex } 100 \xrightarrow{\substack{12 \\ \underline{\quad}}} 50 \xrightarrow{\substack{12 \\ \underline{\quad}}} 25 \xrightarrow{\substack{12 \\ \underline{\quad}}} 12 \xrightarrow{\substack{12 \\ \underline{\quad}}} 6 \xrightarrow{\substack{12 \\ \underline{\quad}}} 3 \xrightarrow{\substack{12 \\ \underline{\quad}}} 1$$

$$\text{ans} = 6$$

(n)



## intermediate content

Prob solve. 1

- time complexity 2
- Array  $6 + 2 = 8$
- Bit manipulation 2
- math - arithmetic 1
- Sorting 1
- string 1
- Hashing 2
- recursion 2
- classes & Object 1 ←
- Lists (linked List) 1
- Tree Basics 1

HW Assignment

	- hints
	- Peer
	- TA
	- Instructor