

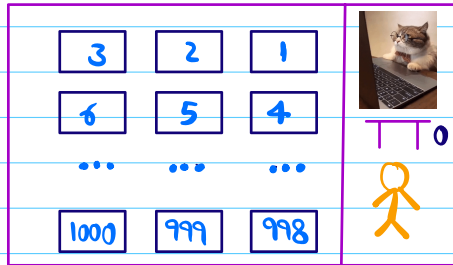
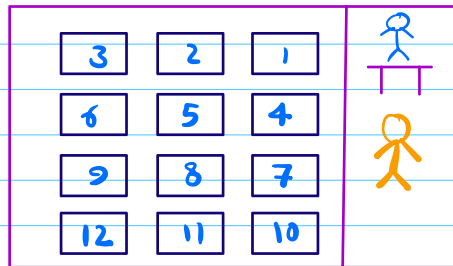
Topics

Intro to hashmaps

- problems
- ① Frequency of each number
 - ② First non-repeating number
 - ③ No. of distinct elements
 - ⚠ ④ No. of subarrays with $\text{sum} \geq 0$

Intro to hashmaps:

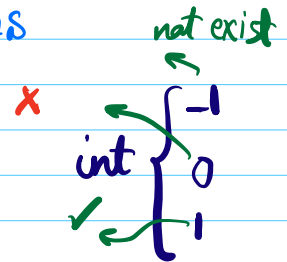
hotel rooms example



bool

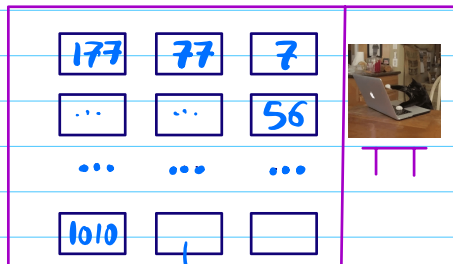
0	1	2	...	999	1000
x	✓	x		x	✓

$O(1)$ fetch
 $O(1)$ update
 SC: $O(n)$ for n rooms
 TC: Search $O(n)$

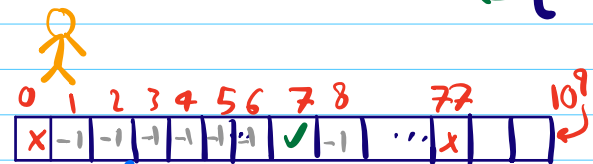


1000

$$\frac{10^3}{10^9} = 10^{-6}$$



1,000,000,000



$O(1)$ fetch
 $O(1)$ update
 SC: $O(\max)$ for n rooms
 TC: Search $O(\max)$

hashMap <key, value>

just pseudocode

donald knuth

⚠ not syntactically correct in any programming language

<77, true>

<177, false>

Storing data in hash map

- ① store population of every country :

$H M \langle \text{String}, \text{lang} \rangle$

HM["India"] = 1,000,000,000
HM["US"] = 300,000,000

- ② # of states/provinces of each country:

HM <String, int>

noOfStates["VS"] = 30

1

- ③ For every country we want to store all state names

HM <string, list<string> >

- ④ For every country store the population of each state :

$$HM \langle \text{string}, \underbrace{HM \langle \text{string}, \text{int} \rangle}_{\text{list}} \rangle$$
$$HM[{}^NVS^N][{}^NWA^N] \rightarrow 8,000,000$$

- ① keys type :: primitive type int, float, double, string, ...
② values type :: any type

→ otherwise
for complex
objects
we need to
define extra
functions so
we can use
them as key

HashSet	<Key>
---------	-------

Time Complexity

	hash map operations	hashSet operations
get size	$O(1)$	$O(1)$
insert \leftarrow put	(key, value) $O(1)$	(key) $O(1)$
\leftarrow ContainsKey	(key) $O(1)$	(key) $O(1)$
$V \leftarrow HM[k] \leftarrow$ get	(key) $O(1)$	- - - -
remove	(key) $O(1)$	(key) $O(1)$
update?	(key) $O(1)$	- - - -

* what if we insert n <key, val> to hash map?

TC: $O(n)$

SC: $O(n)$

HashMap libs in different programming languages:

	Pseudo code	Java	c++ STL	python	JS	C #
HM	hash Map	hashMap	unordered_map	Dictionary	Map	Dictionary
HS	hash Set	hashSet	unordered_set	Set	Set	HashSet

P1 Given an array of integers $a[N]$, and Q queries
 find the frequency of each number that is queried

ex $a[] = \{ \overset{0}{2}, \overset{1}{6}, \overset{2}{3}, \overset{3}{8}, \overset{4}{2}, \overset{5}{8}, \overset{6}{2}, \overset{7}{3}, \overset{8}{8}, \overset{9}{10}, \overset{10}{6} \}$

$1 \leq N \leq 10^5$

$1 \leq Q \leq 10^5$

$1 \leq a[i] \leq 10^9$

Q	freq?
2	3
8	3
3	2
5	0
6	2

ans

brute force

idea 1:

TC: $O(Q \times N)$

SC: $O(1)$

idea 2:

```

for (q = 0; q < Q; q++) {
    k = Query[q]; Count = 0;
    for (i = 0; i < N; i++) {
        if (a[i] == k) Count++;
    }
    print("k: " + Count);
}
    
```

hashMap < $\underset{\substack{\downarrow \\ \text{number}}}{\text{int}}, \underset{\substack{\downarrow \\ \text{freq}}}{\text{int}} \rangle$

Quiz

TC: $O(N+Q)$

SC: $O(N)$

```
void printFreqForQuery(int a[], int q[]){
```

```
    int n = a.Length
```

```
    HashMap hm <int, int> = ...
```

```
    for (i = 0; i < n; i++) {
```

```
        key = a[i]
```

```
        if (!hm.ContainsKey(key)) {  $O(n)$ 
```

```
            hm[key] = 0
```

```
        }
```

```
        hm[key]++
```

```
    }
```

```
    for (q = 0; q < Q; q++) {
```

```
        k = Query[q]
```

$O(Q)$

Q

```
        if (!hm.ContainsKey(k)) print("invalid")
```

```
        else print(hm[k])
```

```
    }
```

```
}
```

from left close to index 0

P2 Find the first non-repeating element in a given array

ex $a[]: \{ \overset{0}{\underline{1}}, \overset{1}{\underline{2}}, \overset{2}{\underline{3}}, \overset{3}{\underline{1}}, \overset{4}{\underline{2}}, \overset{5}{\underline{5}} \}$ ans=3

Quiz $a[]: \{ \underline{4}, \underline{3}, \underline{3}, \underline{2}, 5, 6, \underline{4}, 5 \}$ ans=2

Quiz $a[]: \{ \underline{2}, \underline{6}, 8, 4, 7, \underline{2}, 9 \}$ ans=6

ideas: ① $freq[]$

wrongx
foreach entry $\langle k, v \rangle$ in $freq$
if ($v == 1$) ret k
}

Hash Map
doesn't keep
the same order

$\{2, 2, 3, 3\}$

② $freq[]$..

$O(n+n)$

TC: $O(n)$

SC: $O(n)$

```
for (i=0; i<n; i++) {  
    if ( freq[ a[i] ] == 1) ret a[i]  
}
```

key

ret ... (not exist)

P3 Given an array $a[n]$, find number of distinct elements:

ex as $\{ \overset{0}{\underline{3}}, \overset{1}{\underline{5}}, \overset{2}{\underline{6}}, \overset{3}{\underline{5}}, \overset{4}{\underline{4}} \}$ ans = 4

Quiz $a = \{ \underline{6}, \underline{3}, \underline{7}, \underline{3}, \underline{8}, \underline{6}, \underline{9} \}$ ans = 5

Quiz $a = \{ \underline{1}, \underline{1}, \underline{1}, \underline{2}, \underline{2} \}$ ans = 2

ex $\{ 3, 3, 3 \}$ ans = 1

idea:

```
HashSet<int> hs = ...  
for(i=0; i<n; i++){  
    hs.put(a[i])  
}  
ret hs.size()
```


true/false

P3.2 Given an array $a[n]$, check if all elements are distinct?

ex $\{6, 8, 3, 2, 7\} \rightarrow \text{true}$

ex $\{3, \underline{1}, 6, \underline{1}, 4, 9, 6\} \rightarrow \text{false}$

ret $hs.size() == arr.len$

true/false

P4 Given an array $a[n]$, check if there is a subarray with sum $= 0$.

ex $a[]: \{ 2, 2, 1, -3, 4, 3, 1, -2, -3, 2 \}$

idea 1

```
void sumOfEachSubarray1(int a[]) {
    n = a.len
    for (i = 0; i < n; i++) {
        for (j = i; j < n; j++) {
            sum = 0
            for (k = i; k <= j; k++) {
                sum += a[k]
            }
            if (sum == 0) ret true
        }
    }
}
```

Carry Forward
 $O(n^2)$

idea 2

```
} ret false
```

ex $a[]: \{ 2, 2, 1, -3, 4, 3, 1, -2, -3, 2 \}$
 $PS[]: \{ 2, 4, 5, 2, 6, 9, 10, 8, 5, 7 \}$

case I

obs $PS[2] = 5 \rightarrow \text{sum}[0, 2]$
 $PS[8] = 5 \rightarrow \text{sum}[0, 8] = \text{sum}[0, 2] + \text{sum}[3, 8]$

special case

$a \{ 2, -5, 3, 6 \}$

$PS \{ 2, -3, 0, 6 \}$

case II

Quiz

Tc: $O(n)$

Sc: $O(n+n)$

$= O(n)$

```
bool subArrZero(int a[]){
```

```
    n = a.Len
```

```
    int[] PS = ...
```

// PS $O(n)$

```
    hashSet<int> hs = ...
```

```
    for(i=0; i<n; i++){
```

```
        if(PS[i] == 0) ret true case II
```

```
        if(hs.contains(PS[i])) ret true
```

```
        hs.put(PS[i])
```

```
    }
```

```
    ret false
```

```
}
```