

## Hashing 2 - problems

- subarray sum eq.  $k$
- longest consecutive sequence
- Shaggy & distances

P1 Given an array of integers  $A$  and a number  $k$   
find total number of subarrays, having  $\text{sum} = k$

ex  $\{10, 2, -2, -20, 10\}$   $k = -10$   
ans = 3

ex  $\{9, 4, 20, 3, 10, 5\}$   $k = 33$  ans = 2

idea1 (brute force)  
for  $i = 0 \rightarrow n-1$   
for  $j = i \rightarrow n-1$   
for  $k = i \rightarrow j$   $\text{sum} += a[k]$   $\text{TC} = O(n^3)$

SC:  $O(n)$  PS  $\rightarrow O(n)$

idea2 PS  
for  $i = 0 \rightarrow n-1$   
for  $j = i \rightarrow n-1$   
 $[i, j] \rightarrow$  only this query can be answered with  $O(1)$   
 $\text{TC} = O(n + n^2) = O(n^2)$

idea3 CF  
for  $i = 0 \rightarrow n-1$   
sumSoFar = 0  
for  $j = i \rightarrow n-1$   
sumSoFar +=  $a[j]$   
... check  $[i, j] \rightarrow k$   
 $\text{TC} = O(n^2)$   
 $\text{SC} = O(1)$

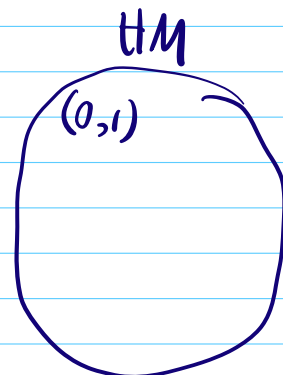
idea3  
3 min  
Calculate PS  $\rightarrow \text{TC} = O(n)$   
inject PS into a hashSet  
meanwhile if PS element  $(\text{PS}_i - k)$  exists then  $\text{ans}++$   
 $\text{PS}_i - k = +\text{PS}_j \rightarrow \text{PS}_i = \text{PS}_j + k$

$HS \rightarrow \begin{pmatrix} 0 & 1 & 2 & 3 & 4 & 5 \\ 9 & 4 & 20 & 3 & 10 & 5 \end{pmatrix} k=33$   
 $PS \rightarrow \{9, 13, 33, 36, 46, 51\}$   
 $ans = 0$   
 $9-33 = -24$   
 $13-33 = -20$   
 $33-33 = 0$   
 $\frac{46}{33} = 1 \frac{13}{33}$

Pro code:

- Calculate P.S as we go
- Count up in hash map

avoid common bug in interview  $\rightarrow$  for true/false  
 note that for  $\neq 0$  HS is enough  
 Count HM is needed



$SC: O(n)$   
 $TC: O(n)$   

```

int countSumK(int a[], int k){
    n = a.len
    hm = new HashMap();
    hm.put(0, 1) // why?  $\rightarrow$  explained
    ans = 0; curSum = 0
    for(i=0; i<n; i++){
        curSum += a[i]
        if(hm.containsKey(curSum - k)){
            ans += hm.get(curSum - k)
        }
        hm.put(curSum, hm.get(curSum) + 1)
    }
    return ans;
  
```

 $\rightarrow$  Care. overflow?!  
 $\downarrow$  default  $\rightarrow$  if not exist ret 0

$HM \rightarrow \begin{pmatrix} (0, 2) & (9, 1) \\ (13, 2) \end{pmatrix}$   
 $\{9, 4, 20, 3, 10, 5, -5\} k=33$   $ans > 1$   
 $curSum = 9, 13, 33, 36, 46, 51, 46$   
 $46 - 33 = 13$   
 good example when Count  $\geq 2$   
 ex  $\{10, 2, -2, -20, 10\} k=-10$   
 $PS \{10, 12, 10, -10, 0\}$

Alternative problem  
rectangle counting distinct elements

P2 Given an integer array  $a$ , find the length of longest chain of consecutive elements.

wait for the example

ex  $a = \{ \overset{0}{100}, \overset{1}{4}, \overset{2}{3}, \overset{3}{6}, \overset{4}{10}, \overset{5}{20}, \overset{6}{11}, \overset{7}{5}, \overset{8}{101} \}$

ans = 4  
 $\{100, 101\}$   
 $\{3, 4, 5, 6\}$   
 $\{10, 11\}$   
 $\{20\}$

idea1

sort  $O(n \log n)$

$\{ \underline{3}, \underline{4}, \underline{5}, \underline{6}, \underline{10}, \underline{11}, \underline{20}, \underline{100}, \underline{101} \}$

idea2

hash set Filled  $O(n)$

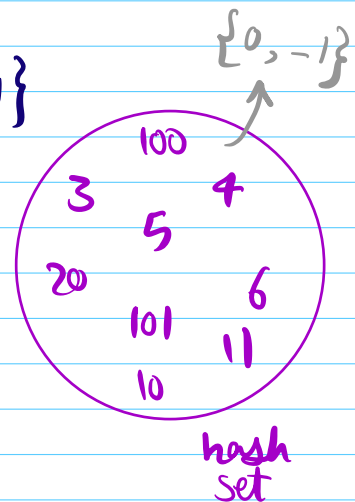
$a = \{ \overset{0}{100}, \overset{1}{4}, \overset{2}{3}, \overset{3}{6}, \overset{4}{10}, \overset{5}{20}, \overset{6}{11}, \overset{7}{5}, \overset{8}{101} \}$

$i$

left

right

$\underline{3} \quad \underline{4} \quad \underline{5} \quad \underline{6}$



- insert all elements in hash set  $O(n)$

- for  $i = 0 \rightarrow n-1$  { not

if ( $a[i]-1$  is Present in set) continue // skip

else // first number in consec. series

| while ( $a[i]+next$  is in set)  $next++$

| maxlen

TC:  $O(n)$

SC:  $O(n)$

Already discussed last session!

P3 Shaggy & distances!

Given an integer array  $a$ , find  $\min |i-j|$  st.

$i \neq j$ ,  $a[i] = a[j]$  &  $|i-j|$  is minimum.

ABSolute wait for this!

$a = \{2, 3, 5, 7, 2, 6, 8, 7, 3, 5, 2, 3\}$



Brute Force For  $i = 0 \rightarrow n-1$   
 $j = i+1 \rightarrow n-1$   
 $a[i] = a[j] \dots$

hash: key value  
 $a[i]$

```
int getMinDistance(int a[]) {  
    n = a.len
```

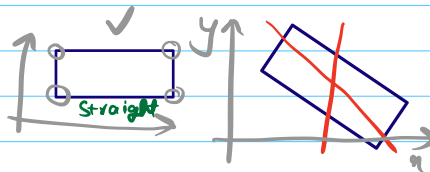
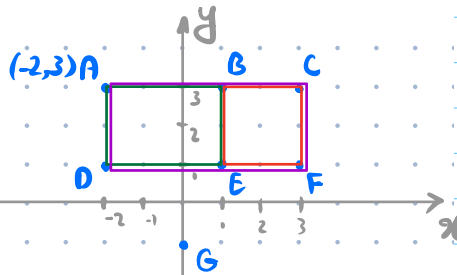
TC:

SC:

# Optionals

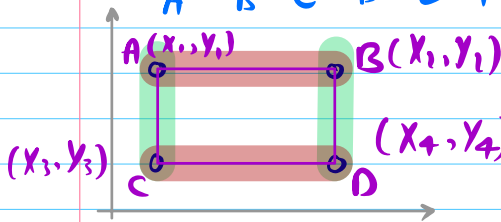
P1 Given  $n$  points in a 2D plane, count the number of rectangles with sides parallel to xy axis. All four corners must be part of input & two rectangles are different if one point is different.

Amir  
Microsoft  
screening



ans = 3

input  $x = \{-2, 1, 3, -2, 1, 3, 0\}$   
 $y = \{3, 3, 3, 1, 1, 1, -1\}$



$$\begin{cases} x_1 = x_3 \\ x_2 = x_4 \\ y_1 = y_2 \\ y_3 = y_4 \end{cases}$$

$\&\& Y_1 \neq Y_3$   
 $\&\& X_1 \neq X_2$

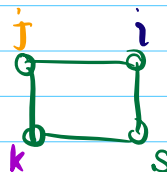
idea 1:  $\forall$  four point in input test

Count++

→ ret Count?

TC:  $O(N^4)$

SC:  $O(1)$



for  $i = 0 \rightarrow n-1$

$j = 0 \rightarrow n-1$

$k = 0 \rightarrow n-1$

$s = 0 \rightarrow n-1$

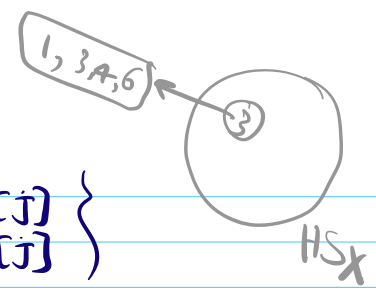
if (check  $(x[i], x[j], x[k], x[s])$   
 $(y[i], y[j], y[k], y[s])$ )

Count++

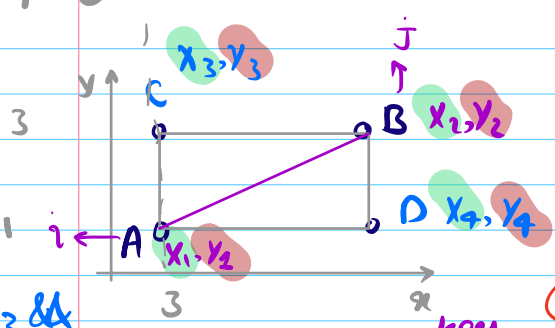
Q1

ret Count / 4 // because each  $\square$  will be counted 4 times

Assume Points are distinct



idea 2



$$\left\{ \begin{matrix} x[i] & , & x[j] \\ y[i] & , & y[j] \end{matrix} \right\}$$

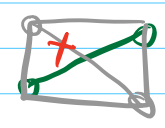
Condition of being diag. of a  $\square$

$$x[i] \neq x[j] \ \&\& \ y[i] \neq y[j]$$

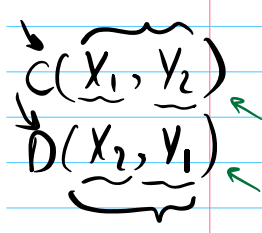
$$\begin{cases} x_1 = x_3 \ \&\& \\ y_2 = y_3 \\ x_2 = x_4 \\ y_1 = y_4 \end{cases}$$

HashSet < Pair < X, Y > > <sup>key</sup> <sup>HS</sup> // whole Pair < X, Y > is object for key.

insert all points to HashSet  $\rightarrow O(n)$



form j  $\rightarrow$  i



$i = 0 \rightarrow n-1$   
 $j = i+1 \rightarrow n-1$

if (check diag (  $\begin{pmatrix} x[i] \\ y[i] \end{pmatrix} , \begin{pmatrix} x[j] \\ y[j] \end{pmatrix} \end{pmatrix} ) \{$

HS.Contains ( new Pair (  $x[i]$ ,  $y[i]$  ) ) &&

HS.Contains ( new Pair (  $x[j]$ ,  $y[j]$  ) )

ans++

st all A, B, C, D form  $\square$

$O(n^2)$  TC

$O(n)$  SC

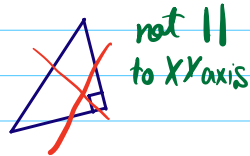
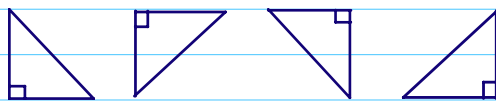
}

ret ans/2;



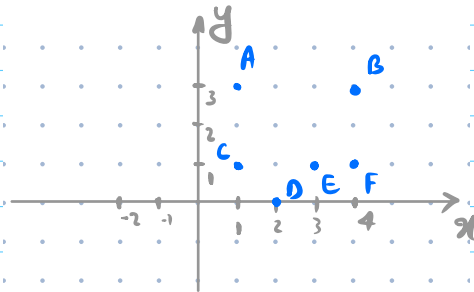
right angle

P2 Given  $n$  points in a 2D plane, count the number of triangles with sides parallel to  $xy$  axis. All three corners must be part of input & two triangles are different if one point is different. points are distinct

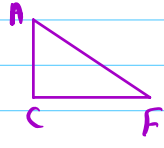
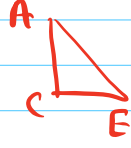


not || to XY axis

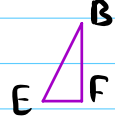
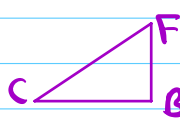
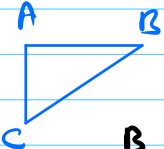
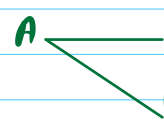
Q2



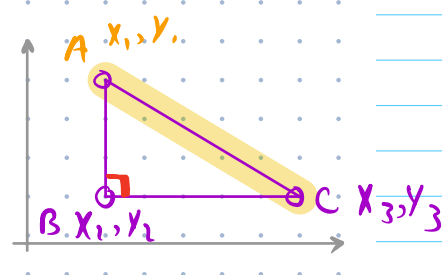
$X = \{ \overset{A}{1}, \overset{B}{4}, \overset{C}{1}, \overset{D}{2}, \overset{E}{3}, \overset{F}{4} \}$   
 $Y = \{ \overset{A}{3}, \overset{B}{3}, \overset{C}{1}, \overset{D}{0}, \overset{E}{0}, \overset{F}{0} \}$



ans = 6



$A(x_1, y_1)$   
 $C(x_3, y_3)$   
 $B(x_2, y_2)$



$\begin{cases} x_1 = x_2 \text{ \& \& } x_1 \neq x_3 \\ y_2 = y_3 \end{cases}$

idea 1

similar to prev solution with modification for  $TC: O(n^2)$   
 $SC: O(n)$

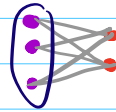
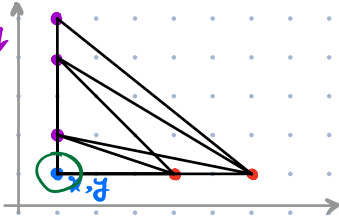
idea 2

hash map for Freq  
x of all point

x HM ←

y HM ←

hash map for Freq  
y of all point



$$3 \times 2 = 6$$

different

$x, y \leftarrow \Delta$

x HM → Hash map for all X coordinations  $O(n)$

y HM → Hash map for all y coordinations  $O(n)$

for  $i = 0 \rightarrow n-1$  // focus on each corner

$$ans += (xHM[x[i]] - 1) * (yHM[y[i]] - 1)$$

ret ans;

for  $i = 0 \rightarrow n-1$

$x[i]$

$y[i]$

$$\begin{cases} xHM[x[i]] + \\ yHM[y[i]] \end{cases}$$

exclude the current point i