EXP-6 Implementation of unification and resolution for real-world problems

AIM

To implement a program for unification and resolution of real-world problems.

UNIFICATION:

It is a process of making two different logical atomic expressions identical by finding a substitution.

Unification depends on the substitution process.

It takes two literals as input and makes them identical using substitution.

Let Ψ 1 and Ψ 2 be two atomic sentences and σ be a unifier such that, Ψ 1 σ = Ψ 2 σ , then it can be expressed as UNIFY(Ψ 1, Ψ 2)

Example: Find the MGU for Unify{King(x), King(John).

Let $\Psi 1 = \text{King}(x)$, $\Psi 2 = \text{King}(\text{John})$,

Substitution $\theta = \{John/x\}$ is a unifier for these atoms and applying this substitution, both expressions will be identical.

CONDITION FOR UNIFICATION:

Following are some basic conditions for unification:

Predicate symbols must be the same, atoms or expressions with different predicate symbols can never be unified.

The number of Arguments in both expressions must be identical.

Unification will fail if there are two similar variables present in the same expression.

Algorithm

Step 1: If Ψ 1 or Ψ 2 is a variable or constant, then:

- a) If Ψ1 or Ψ2 are identical, then return NIL.
- b) Else if Ψ1 is a variable,
 - i) then if Ψ1 occurs in Ψ2, then return FAILURE
 - ii) Else return { (Ψ2/ Ψ1)}.
- c) Else if Ψ2 is a variable,
 - i) If Ψ2 occurs in Ψ1 then return FAILURE,
 - ii) Else return {(Ψ1/ Ψ2)}.
- d) Else return FAILURE.

Step 2: If the initial Predicate symbol in Ψ1 and Ψ2 are not same, then return FAILURE.

- Step 3: IF Ψ1 and Ψ2 have a different number of arguments, then return FAILURE.
- Step 4: Set Substitution set(SUBST) to NIL.
- Step 5: For i=1 to the number of elements in Ψ 1.
- a) Call Unify function with the ith element of $\Psi 1$ & ith element of $\Psi 2$, & put the result into S.
 - b) If S = failure then returns Failure
 - c) If $S \neq NIL$ then do,
 - i) Apply S to the remainder of both L1 and L2.
 - ii) SUBST= APPEND(S, SUBST).

Step.6: Return SUBST.

Program

```
def get index comma(string):
   index list = list()
   par count = 0
   for i in range(len(string)):
       if string[i] == ',' and par_count == 0:
           index list.append(i)
       elif string[i] == '(':
           par count += 1
       elif string[i] == ')':
           par count -= 1
    return index list
def is variable(expr):
   for i in expr:
       if i == '(' or i == ')':
           return False
    return True
```

```
def process expression(expr):
   expr = expr.replace(' ', '')
    index = None
    for i in range(len(expr)):
        if expr[i] == '(':
            index = i
            break
   predicate symbol = expr[:index]
   expr = expr.replace(predicate symbol, '')
   expr = expr[1:len(expr) - 1]
   arg list = list()
    indices = get_index_comma(expr)
    if len(indices) == 0:
        arg list.append(expr)
   else:
        arg list.append(expr[:indices[0]])
        for i, j in zip(indices, indices[1:]):
            arg list.append(expr[i + 1:j])
        arg list.append(expr[indices[len(indices) - 1] + 1:])
    return predicate_symbol, arg_list
def get arg list(expr):
   _, arg_list = process_expression(expr)
   flag = True
   while flag:
       flag = False
        for i in arg list:
            if not is variable(i):
                flag = True
                _, tmp = process_expression(i)
                for j in tmp:
                    if j not in arg_list:
                        arg list.append(j)
```

```
arg list.remove(i)
    return arg list
def check_occurs(var, expr):
   arg_list = get_arg_list(expr)
   if var in arg list:
        return True
   return False
def unify(expr1, expr2):
    if is variable(expr1) and is variable(expr2):
       if expr1 == expr2:
           return 'Null'
        else:
            return False
    elif is_variable(expr1) and not is_variable(expr2):
        if check occurs(expr1, expr2):
            return False
        else:
            tmp = str(expr2) + '/' + str(expr1)
           return tmp
    elif not is variable(expr1) and is variable(expr2):
        if check occurs(expr2, expr1):
            return False
        else:
            tmp = str(expr1) + '/' + str(expr2)
            return tmp
    else:
        predicate_symbol_1, arg_list_1 = process_expression(expr1)
        predicate symbol 2, arg list 2 = process expression(expr2)
        # Step 2
        if predicate_symbol_1 != predicate_symbol_2:
            return False
```

```
# Step 3
        elif len(arg_list_1) != len(arg_list_2):
            return False
        else:
            # Step 4: Create substitution list
            sub list = list()
            # Step 5:
            for i in range(len(arg_list_1)):
                tmp = unify(arg_list_1[i], arg_list_2[i])
                if not tmp:
                   return False
                elif tmp == 'Null':
                    pass
                else:
                    if type(tmp) == list:
                        for j in tmp:
                            sub_list.append(j)
                    else:
                        sub list.append(tmp)
            # Step 6
            return sub list
if name == ' main ':
    f1 = 'Q(a, g(x, a), f(y))'
   f2 = 'Q(a, g(f(b), a), x)'
   result = unify(f1, f2)
   if not result:
        print('The process of Unification failed!')
    else:
        print('The process of Unification successful!')
        print(result)
```

Input & Output

```
f1 = 'Q(a, g(x, a), f(y))'

f2 = 'Q(a, g(f(b), a), x)'
```

```
RA1911026010021:~/environment/RA1911026010029/exp6 $ python3 exp6-uni.py
The process of Unification successful!
['f(b)/x', 'f(y)/x']
```

AWS Screenshot

```
bash - "ip-172-31-2-88" ×
                              exp6-uni.py
                                                          exp6-res.py
     def get_index_comma(string):
         index_list = list()
         par_count = 0
        for i in range(len(string)):
            if string[i] == ',' and par_count == 0:
    index_list.append(i)
    elif string[i] == '(':
                 par_count += 1
              elif string[i] == ')':
                  par_count -= 1
         return index list
16 def is variable(expr):
         for i in expr:
             if i == '(' or i == ')':
                  return False
         return True
24 def process_expression(expr):
       expr = expr.replace(' ', '')
        index = None
         for i in range(len(expr)):
             if expr[i] == '(':
                  index = i
                  break
       predicate_symbol = expr[:index]
       expr = expr.replace(predicate_symbol, '')
expr = expr[1:len(expr) - 1]
         arg_list = list()
         indices = get_index_comma(expr)
         if len(indices) == 0:
             arg_list.append(expr)
```

RESOLUTION:

Resolution method is an inference rule which is used in both Propositional as well as First-order Predicate Logic in different ways. This method is basically used for proving the satisfiability of a sentence. In the resolution method, we use the Proof by Refutation technique to prove the given statement. The key idea for the resolution method is to use the knowledge base and negated goal to obtain a null clause (which indicates contradiction). The resolution method is also called Proof by Refutation.

Method for Resolution

The process followed to convert the propositional logic into resolution method contains the below steps:

- Convert the given axiom into clausal form, i.e., disjunction form.
- Apply and proof the given goal using negation rule.
- Use those literals which are needed to prove.
- Solve the clauses together and achieve the goal.

Conjunctive Normal Form (CNF)

- 1) Eliminate bi-conditional implication by replacing A? B with (A?B)? (B?A)
- 2) Eliminate implication by replacing A? B with ¬A V B.
- 3) In CNF, negation(¬) appears only in literals, therefore we move it inwards
- 4) Finally, using distributive law on the sentences, and form the CNF

Program

```
import copy
import time
class Parameter:
  variable count = 1
  def init (self, name=None):
    if name:
      self.type = "Constant"
       self.name = name
    else:
      self.type = "Variable"
       self.name = "v" + str(Parameter.variable count)
      Parameter.variable count += 1
  def isConstant(self):
    return self.type == "Constant"
  def unify(self, type , name):
    self.type = type
```

```
self.name = name
  def eq (self, other):
    return self.name == other.name
  def str (self):
    return self.name
class Predicate:
  def init (self, name, params):
    self.name = name
    self.params = params
  def eq (self, other):
    return self.name == other.name and all(a == b for a, b in zip(self.params,
other.params))
  def str (self):
    return self.name + "(" + ",".join(str(x) for x in self.params) + ")"
  def getNegatedPredicate(self):
    return Predicate(negatePredicate(self.name), self.params)
class Sentence:
  sentence count = 0
  def init (self, string):
    self.sentence index = Sentence.sentence count
    Sentence.sentence count += 1
    self.predicates = []
    self.variable_map = {}
    local = {}
    for predicate in string.split("|"):
       name = predicate[:predicate.find("(")]
      params = []
      for param in predicate[predicate.find("(") + 1:
predicate.find(")")].split(","):
         if param[0].islower():
           if param not in local: # Variable
              local[param] = Parameter()
              self.variable_map[local[param].name] = local[param]
           new param = local[param]
```

```
else:
           new param = Parameter(param)
           self.variable map[param] = new param
         params.append(new param)
      self.predicates.append(Predicate(name, params))
  def getPredicates(self):
    return [predicate.name for predicate in self.predicates]
  def findPredicates(self, name):
    return [predicate for predicate in self.predicates if predicate.name == name]
  def removePredicate(self, predicate):
    self.predicates.remove(predicate)
    for key, val in self.variable map.items():
      if not val:
         self.variable_map.pop(key)
  def containsVariable(self):
    return any(not param.isConstant() for param in self.variable map.values())
  def eq (self, other):
    if len(self.predicates) == 1 and self.predicates[0] == other:
      return True
    return False
  def str (self):
    return "".join([str(predicate) for predicate in self.predicates])
class KB:
  def init (self, inputSentences):
    self.inputSentences = [x.replace(" ", "") for x in inputSentences]
    self.sentences = []
    self.sentence map = {}
  def prepareKB(self):
    self.convertSentencesToCNF()
    for sentence_string in self.inputSentences:
       sentence = Sentence(sentence string)
      for predicate in sentence.getPredicates():
         self.sentence map[predicate] = self.sentence map.get(
           predicate, []) + [sentence]
```

```
def convertSentencesToCNF(self):
  for sentenceIdx in range(len(self.inputSentences)):
    # Do negation of the Premise and add them as literal
    if "=>" in self.inputSentences[sentenceldx]:
      self.inputSentences[sentenceIdx] = negateAntecedent(
         self.inputSentences[sentenceldx])
def askQueries(self, queryList):
  results = []
  for query in queryList:
    negatedQuery = Sentence(negatePredicate(query.replace(" ", "")))
    negatedPredicate = negatedQuery.predicates[0]
    prev sentence map = copy.deepcopy(self.sentence map)
    self.sentence map[negatedPredicate.name] = self.sentence map.get(
       negatedPredicate.name, []) + [negatedQuery]
    self.timeLimit = time.time() + 40
       result = self.resolve([negatedPredicate], [
                   False * (len(self.inputSentences) + 1))
    except:
       result = False
    self.sentence map = prev sentence map
    if result:
       results.append("TRUE")
    else:
       results.append("FALSE")
  return results
def resolve(self, queryStack, visited, depth=0):
  if time.time() > self.timeLimit:
    raise Exception
  if queryStack:
    query = queryStack.pop(-1)
    negatedQuery = query.getNegatedPredicate()
    queryPredicateName = negatedQuery.name
    if queryPredicateName not in self.sentence_map:
      return False
    else:
       queryPredicate = negatedQuery
      for kb sentence in self.sentence map[queryPredicateName]:
         if not visited[kb sentence.sentence index]:
```

```
for kbPredicate in
kb sentence.findPredicates(queryPredicateName):
               canUnify, substitution = performUnification(
                  copy.deepcopy(queryPredicate),
copy.deepcopy(kbPredicate))
               if canUnify:
                  newSentence = copy.deepcopy(kb sentence)
                  newSentence.removePredicate(kbPredicate)
                  newQueryStack = copy.deepcopy(queryStack)
                  if substitution:
                    for old, new in substitution.items():
                      if old in newSentence.variable map:
                         parameter = newSentence.variable map[old]
                         newSentence.variable map.pop(old)
                        parameter.unify(
                           "Variable" if new[0].islower() else "Constant", new)
                         newSentence.variable map[new] = parameter
                    for predicate in newQueryStack:
                      for index, param in enumerate(predicate.params):
                         if param.name in substitution:
                           new = substitution[param.name]
                           predicate.params[index].unify(
                             "Variable" if new[0].islower() else "Constant",
new)
                  for predicate in newSentence.predicates:
                    newQueryStack.append(predicate)
                  new visited = copy.deepcopy(visited)
                  if kb sentence.containsVariable() and
len(kb sentence.predicates) > 1:
                    new visited[kb sentence.sentence index] = True
                  if self.resolve(newQueryStack, new visited, depth + 1):
                    return True
         return False
    return True
def performUnification(queryPredicate, kbPredicate):
  substitution = {}
  if queryPredicate == kbPredicate:
```

```
return True, {}
  else:
    for query, kb in zip(queryPredicate.params, kbPredicate.params):
       if query == kb:
         continue
       if kb.isConstant():
         if not query.isConstant():
           if query.name not in substitution:
              substitution[query.name] = kb.name
           elif substitution[query.name] != kb.name:
              return False, {}
           query.unify("Constant", kb.name)
           return False, {}
       else:
         if not query.isConstant():
           if kb.name not in substitution:
              substitution[kb.name] = query.name
           elif substitution[kb.name] != query.name:
              return False, {}
           kb.unify("Variable", query.name)
         else:
           if kb.name not in substitution:
              substitution[kb.name] = query.name
           elif substitution[kb.name] != query.name:
              return False, {}
  return True, substitution
def negatePredicate(predicate):
  return predicate[1:] if predicate[0] == "~" else "~" + predicate
def negateAntecedent(sentence):
  antecedent = sentence[:sentence.find("=>")]
  premise = []
  for predicate in antecedent.split("&"):
    premise.append(negatePredicate(predicate))
  premise.append(sentence[sentence.find("=>") + 2:])
  return "|".join(premise)
def getInput(filename):
  with open(filename, "r") as file:
```

```
noOfQueries = int(file.readline().strip())
    inputQueries = [file.readline().strip() for in range(noOfQueries)]
    noOfSentences = int(file.readline().strip())
    inputSentences = [file.readline().strip()
               for in range(noOfSentences)]
    return inputQueries, inputSentences
def printOutput(filename, results):
  print(results)
  with open(filename, "w") as file:
    for line in results:
      file.write(line)
      file.write("\n")
  file.close()
if name == ' main ':
  inputQueries_, inputSentences_ = getInput("input.txt")
  knowledgeBase = KB(inputSentences )
  knowledgeBase.prepareKB()
  results = knowledgeBase.askQueries(inputQueries )
  printOutput("output.txt", results_)
```

Input & Output

```
RA1911026010029:~/environment/RA1911026010029/exp6 $ python3 exp6-res.py
['TRUE']
RA1911026010029:~/environment/RA1911026010029/exp6 $
```

```
def __init__(self, name=None):
    if name:
             self.type = "Constant"
              self.name = name
              self.type = "Variable"
self.name = "v" + str(Parameter.variable_count)
Parameter.variable_count += 1
    def isConstant(self):
          return self.type == "Constant"
    def unify(self, type_, name):
         self.type = type_
self.name = name
    def __eq__(self, other):
         return self.name == other.name
    def __str__(self):
         return self.name
class Predicate:
    def __init__(self, name, params):
    self.name = name
    self.params = params
    def __eq__(self, other):
    return self.name == other.name and all(a == b for a, b in zip(self.params, other.params))
    def __str__(self):
    return self.name + "(" + ",".join(str(x) for x in self.params) + ")"
    def getNegatedPredicate(self):
```

Observation

The concept of unification and resolution has been studied and understood through this experiment.

Result

Thus the program for unification and resolution has been successfully implemented and verified with manual calculation.