

Wednesday

Contest 9-10:30

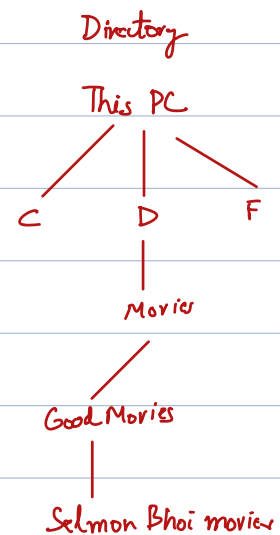
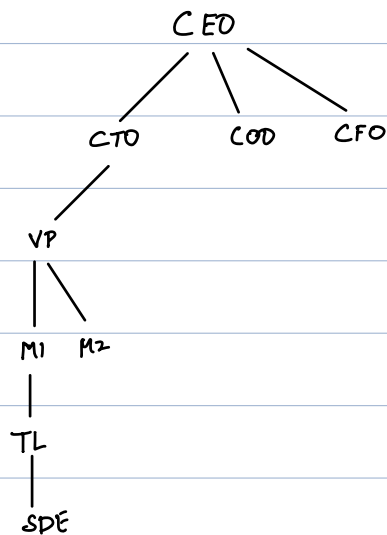
[Strings to LL]

Trees

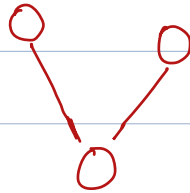
Strings, Arrays, LL

Hierarchical DS

Trees, Graphs



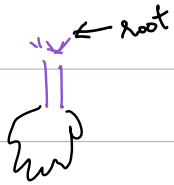
SQL {Relation DB}



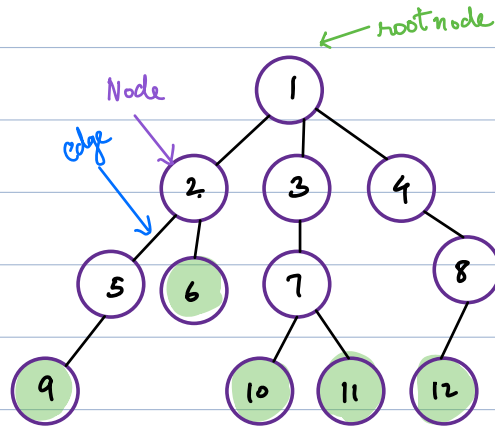
Not a tree

Every node of a tree has only one parent

Naming conventions



1 is ancestor to every one



4 related to 1
$$\begin{array}{ccc} & \text{parent} & \\ 1 & \longleftrightarrow & 4 \\ & \text{child} & \end{array}$$

8 is a grand child of 1

12 " " descendent of 1

8 " " " " "

4 " " " " "

1 is an ancestor of 7

" " " " " 10

10 is not a descendant of 4, 2

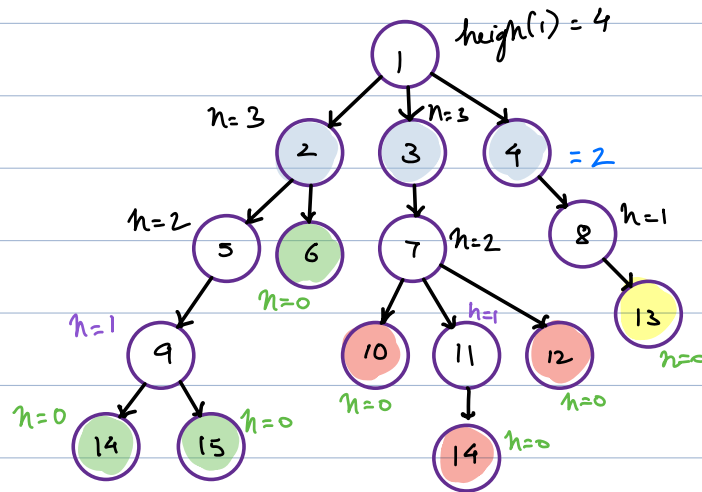
why? Not in same branch

Leaf nodes: Nodes with 0 children

Height

Height of a node is max path length between a node to its descendant leaf node

Path len: No. of edges b/w nodes



$$\text{height}(\text{node}) = \max(\text{height of its children}) + 1$$

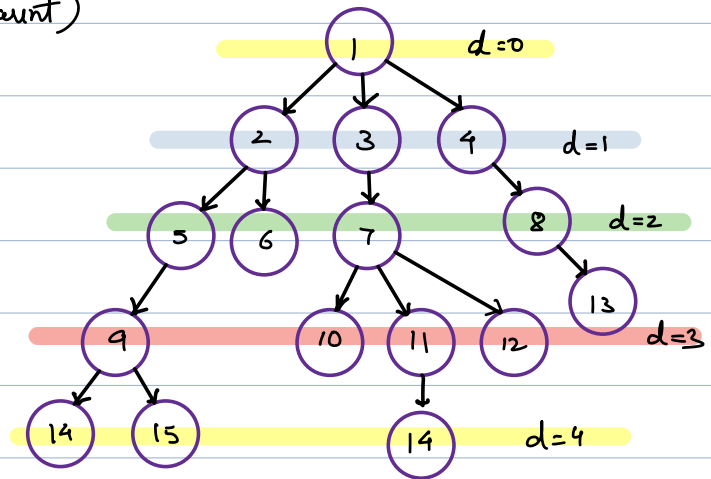
Depth

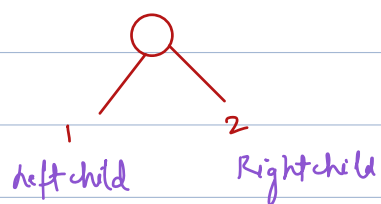
Distance of any node to root node

$$\text{depth}(\text{node}) = 1 + \text{depth}(\text{parent})$$

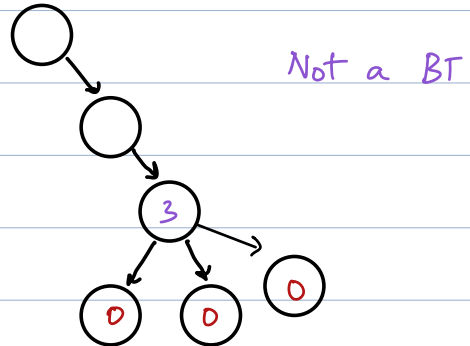
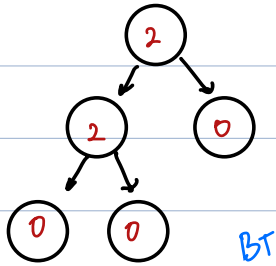
$$d(\text{root}) = 0$$

by definition



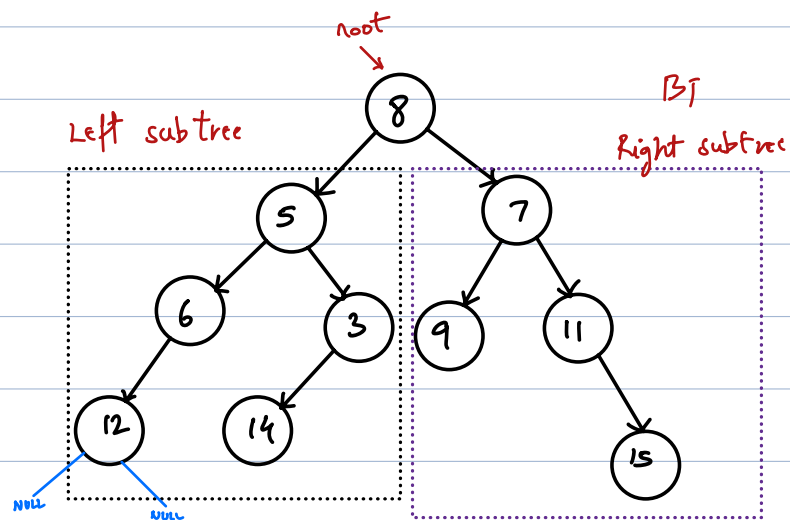


Binary Tree: A tree having all nodes ≤ 2 children



0 BT

NULL smallest Binary Tree



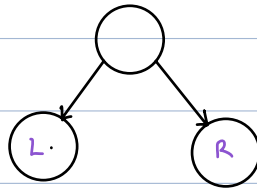
Recursive DS



Traversal in a BT

- 1) Preorder : Root \longrightarrow Left subtree \longrightarrow Right subtree
- 2) Inorder : Left Subtree \longrightarrow Root \longrightarrow Right subtree
- 3) Postorder : Left Subtree \longrightarrow Right Subtree \longrightarrow Root
- 4) level order \longrightarrow Advance [Queue]

Tree Modeling



```
class TreeNode {
```

```
    int data;
```

```
    TreeNode left;
```

```
    TreeNode right;
```

```
    TreeNode(int x) {
```

```
        data = x;
```

```
        left = null;
```

```
        right = null;
```

```
    }
```

```
}
```

□ → null

Java: null

C++/C/C#: NULL

Python: None

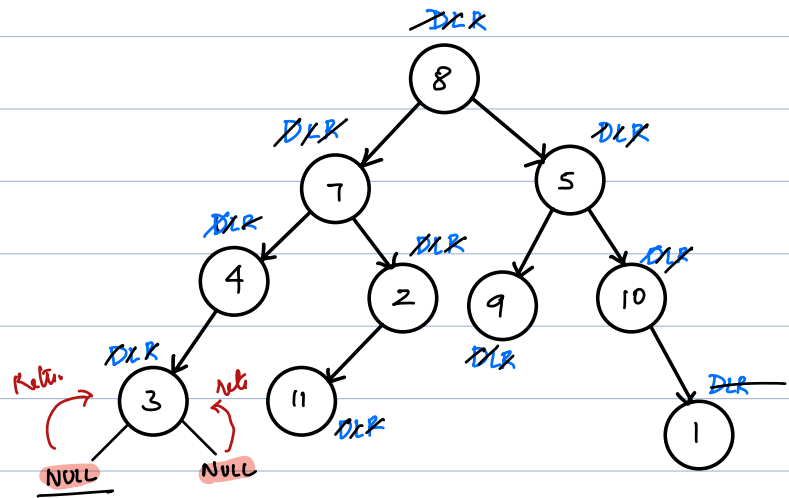
TREE TRAVERSALS

preorder: DLR
 inorder: LDR HW
 postorder: LRD

Preorder

Preorder

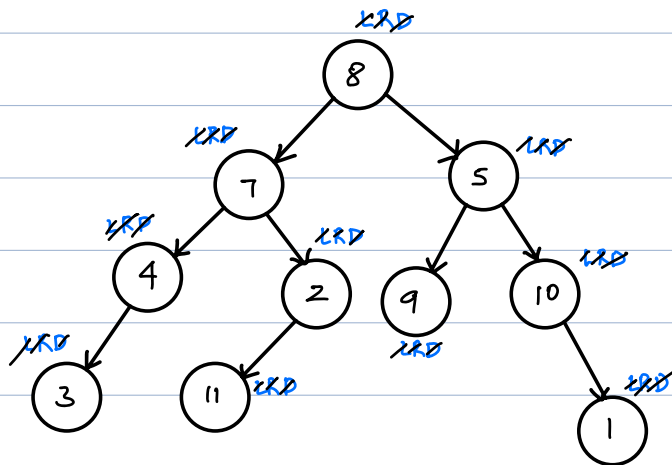
Print : 8 7 4 3 2 11 5 9 10 1



Post order

Postorder

Print : 3 4 11 2 7 9 1 10 5 8



Back (10:18 - 10:30)

Preorder:

Assumption: preorder(root) will print all the elements of the tree having "root" as its root node in preorder manner

D L R

TC: $O(N)$

	void preorder (root) {	
Base case	if (root == null) { return }	
	print (root.data)	# D
Main logic	preorder (root.left)	# L
	preorder (root.right)	# R
	}	

	void inorder (root) {	
	if (root == null) { return }	
	inorder (root.left)	# L
	print (root.data)	# D
	inorder (root.right)	# R
	}	

Post order is HW

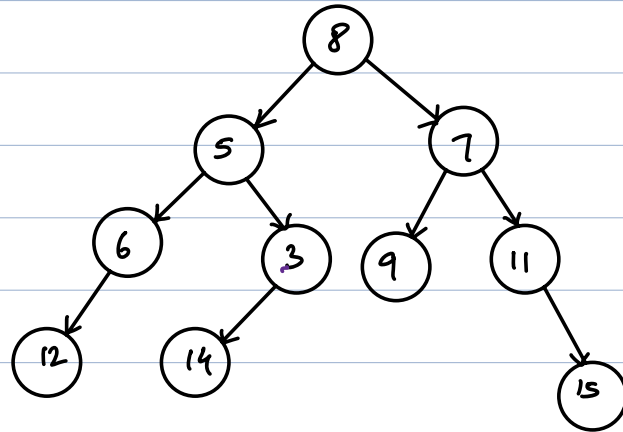
HW

Stack dy ren

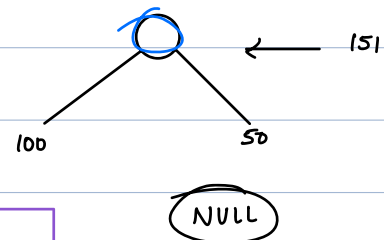
SC: _____

Calculate size of a tree:

Size = 10



Assumption: `size(root)` return no. of nodes in tree

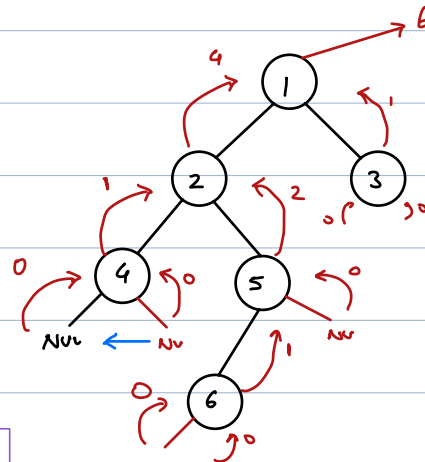


```
int size(root) {  
    if (root == NULL) { return 0 }  
    int lsize = size(root->left)  
    int rsize = size(root->right)  
    return lsize + rsize + 1  
}
```

```

int size(root) { root=1
1 if (root == NULL) { return 0; }
2 int lsize = size(root.left);
3 int rsize = size(root.right);
4 return lsize + rsize + 1;
}

```



```

int size(root) { root=2
1 if (root == NULL) { return 0; }
2 int lsize = size(root.left);
3 int rsize = size(root.right);
4 return lsize + rsize + 1;
}

```

```

size(root) { root=5
1 if (root == NULL) { return 0; }
2 int lsize = size(root.left);
3 int rsize = size(root.right);
4 return lsize + rsize + 1;
}

```

```

int size(root) { root=4
1 if (root == NULL) { return 0; }
2 int lsize = size(root.left);
3 int rsize = size(root.right);
4 return lsize + rsize + 1;
}

```

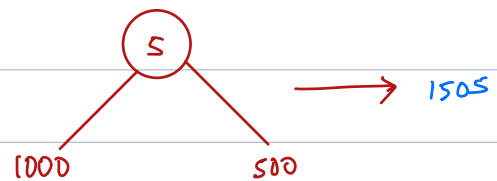
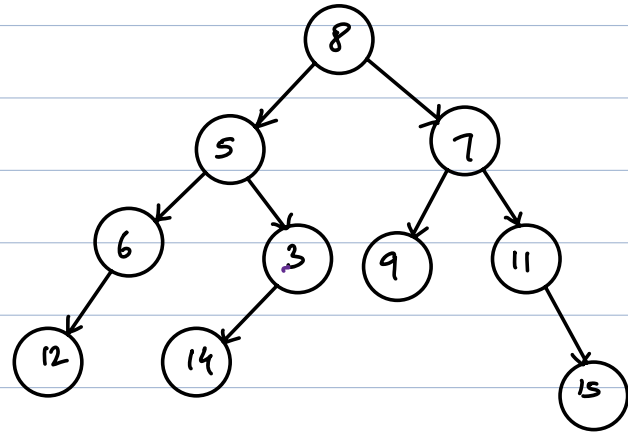
```

int size(root) { root=NULL
1 if (root == NULL) { return 0; }
2 int lsize = size(root.left);
3 int rsize = size(root.right);
4 return lsize + rsize + 1;
}

```

Find sum of all nodes

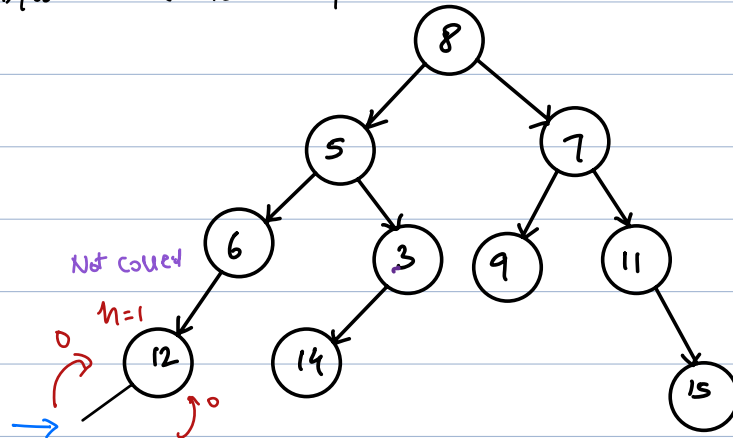
Ans: 90



```
int sum(root) {  
    if (root == NULL) { return 0; }  
    int l = sum(root->left);  
    int r = sum(root->right);  
    return l + r + root->data;  
}
```

Find height of a tree

Path len b/w node to leaf



$\text{height}(\text{node}) = \max(\text{height of its children}) + 1$

```
int height(root) {  
    if (root == null) {  
        return 0;  
    }  
    int lh = height(root->left);  
    int rh = height(root->right);  
    return max(lh, rh) + 1;  
}
```

hw
Base case!

Def: No. of nodes b/w root to leaf node