

`int ar[5] =`

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`int ar[N] =`

--	--	--	--	--	--	--	--

`for (i=0; i <= N-1; i++) {`
 `print(A[i])`
`}`

QD Given an array of size N , count number of elements having atleast one element greater than itself?

$A[7] \{ \overset{0}{-3} \overset{1}{-2} \overset{2}{6} \overset{3}{8} \overset{4}{4} \overset{5}{8} \overset{6}{5} \}$

Ans: 5

$$\begin{aligned} \text{Ans} &= N - \text{freq}(8) \\ &= 7 - 2 = 5 \end{aligned}$$

$A[8] \{ 2, 3, 10, 7, 3, 2, 10, 8 \}$

max = 10

$$\begin{aligned} \text{ans} &= N - \text{freq}(\text{max}) \\ &= 8 - 2 = 6 \end{aligned}$$

$A[10] \{ 2, 5, 1, 4, 8, 0, 8, 1, 3, 8 \}$

Max: 8

$$\text{Ans: } 10 - \text{freq}(8) = 10 - 3 = 7$$

$[7, 7, 7, 7, 7]$

Ans: 0

Obs: No element can be greater than max element

obs2: All other (non max) elements will have atleast one element greater than themselves

$ans = N - freq(max)$

5 3 7 2 4

↑
i $max = 7$

$max = A[0]$

for ($i=0; i < N; i++$) {

 if ($A[i] > max$) {

$max = A[i]$

TC: $O(N)$

SC: $O(1)$

// freq of max

count = 0

for ($i=0; i < N; i++$) {

 if ($A[i] == max$) {

 count++

return $N - count$

HW: do it in a single loop

bool

Q2) Given N array elements, check if there exists a pair (i, j) such that $A[i] + A[j] = k$ & $i \neq j$

Note: i, j are index values and k is given sum

A: $\{ \overset{0}{3} \overset{1}{2} \overset{2}{1} \overset{3}{4} \overset{4}{3} \overset{5}{6} \overset{6}{8} \}$ Sum

$i = 4$ $j = 5$

$k = 9$

$$A[i] + A[j] = 9$$

A: $\{ \overset{0}{3} \overset{1}{5} \overset{2}{2} \overset{3}{7} \overset{4}{3} \}$

$k = 6$

$k = 5$

$i = 0$, $j = 4$

$$A[i] + A[j] = 6$$

A: $\{ \overset{0}{3} \overset{1}{5} \overset{2}{2} \overset{3}{7} \overset{4}{3} \}$

$k = 14$

$i = 3$ $j = 3$

$$7 + 7 = 14$$

$i \neq j$ fails

A: $\{ \overset{0}{5} \overset{1}{7} \overset{2}{9} \overset{3}{3} \overset{4}{2} \}$

$k = 12$

Index: i j

2 3

True

0 1

Check all pairs

$$A[i] + A[j] == k$$

$$N=5$$

i \ j	0	1	2	3	4
0	0 0	0 1	0 2	0 3	0 4
1	1 0	1 1	1 2	1 3	1 4
2	2 0	2 1	2 2	2 3	2 4
3	3 0	3 1	3 2	3 3	3 4
4	4 0	4 1	4 2	4 3	4 4

Lower Triangle HW

```

for (i = 0; i < N; i++) {
    for (j = 0; j < N; j++) {
        if (A[i] + A[j] == k && i != j)
            return true
    }
}
return false

```

TC: $O(N^2)$
 SC: $O(1)$
 Correct

```

for (i = 0; i < N-1; i++) {
    for (j = i+1; j < N; j++) {
        if (A[i] + A[j] == k)
            return true
    }
}
return false

```

i	j	$[i+1, N-1]$	
0	$[1, N-1]$	$N-1$	$+ 1$ (outer)
1	$[2, N-1]$	$N-2$	$+ 1$ (outer)
2	$[3, N-1]$	$N-3$	$+ 1$ (outer)
\vdots			
$N-2$	$[N-1, N-1]$	<u>1</u>	$+ 1$

$$1 + 2 + 3 + 4 \dots N-1 \quad N-1$$

AP

$$\frac{N \times (N-1)}{2} + N-1$$

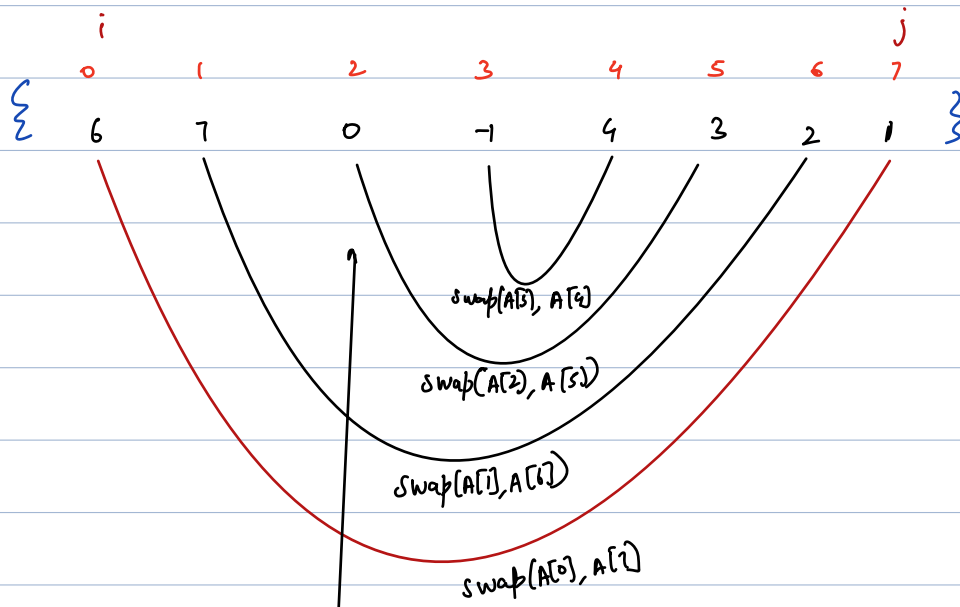
$$TC: O(N^2)$$

Q3) Given an array, reverse it

SC: $O(1)$

A: $\{ \overset{0}{1} \overset{1}{2} \overset{2}{3} \overset{3}{4} \overset{4}{-1} \overset{5}{0} \overset{6}{7} \overset{7}{6} \}$

rev(A): $\{ 6, 7, 0, -1, 4, 3, 2, 1 \}$



$i = 0$ $j = N - 1$

TC: $O(N)$

while $(i < j)$ {

$\text{swap}(A[i], A[j])$

$i++$

$j--$

}

$$i \neq j$$

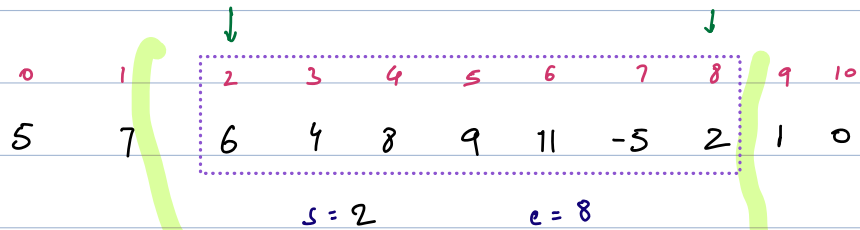
0	1	2	3
4	1	2	3

	↑ i	↑ j	
--	--------	--------	--

< =

Break(10:25 - 10:35)

Q4) Reverse a part of an array between [s, e]



output: 5, 7, 2, -5, 11, 9, 8, 4, 6, 1, 0

```
void reverse (A, s, e) {  
    i = s    j = e    TC: O(N)  
    while (i < j) {  
        swap (A[i], A[j])  
        i++  
        j--  
    }  
}
```

Google / Microsoft

Q5) Rotate an array from left to right by k times

$$A = \{ 3 \quad -2 \quad 1 \quad 4 \quad 6 \quad 9 \quad 8 \} \quad k=3$$

$$k=1 \quad \{ 8 \quad 3 \quad -2 \quad 1 \quad 4 \quad 6 \quad 9 \}$$

$$k=2 \quad \{ 9 \quad 8 \quad 3 \quad -2 \quad 1 \quad 4 \quad 6 \}$$

$$k=3 \quad \{ 6 \quad 9 \quad 8 \quad 3 \quad -2 \quad 1 \quad 4 \}$$

Ans

$$\begin{array}{cccccccc} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ \{ 4, & 1, & 6, & 9, & 2, & 14, & 7, & 8, & 3 \} \end{array}$$

$$k=4$$

$$k=1 \quad \{ 3 \quad 4, 1, 6, 9, 2, 14, 7, 8 \}$$

$$k=2 \quad \{ 8 \quad 3 \quad 4, 1, 6, 9, 2, 14 \quad 7 \}$$

$$k=3 \quad \{ 7 \quad 8 \quad 3 \quad 4, 1, 6, 9, 2, 14 \}$$

$$k=4 \quad \{ 14 \quad 7 \quad 8 \quad 3 \quad 4, 1, 6, 9, 2 \}$$

$$k < N$$

$$\{ 8 \quad 7 \quad 9 \quad 3 \quad -2 \quad 3 \quad 1 \quad 4 \quad 6 \quad 2 \} \quad k=4$$

0	1	2	3	4	5	6	7	8	9	
-2	3	1	4	6	2	8	7	9	3	$k=4$

$\{ 3 \quad 9 \quad 7 \quad 8 \quad 2 \quad 6 \quad 4 \quad 1 \quad 3 \quad -2 \}$ $rev(A, 0, N-1)$

$\{ 8 \quad 7 \quad 9 \quad 3 \quad 2 \quad 6 \quad 4 \quad 1 \quad 3 \quad -2 \}$ $rev(A, 0, k-1)$

$\{ 8 \quad 7 \quad 9 \quad 3 \quad -2 \quad 3 \quad 1 \quad 4 \quad 6 \quad 2 \}$ $rev(A, k, N-1)$

Input

$k=5$

$A = \{ \boxed{a_0 \ a_1 \ a_2 \ a_3 \ a_4 \ a_5 \ a_6 \ a_7} \ \boxed{a_8 \ a_9 \ a_{10} \ a_{11} \ a_{12}} \}$

$k=5$

i) Reverse array $rev(A, 0, N-1)$

$\{ \boxed{a_{12} \ a_{11} \ a_{10} \ a_9 \ a_8} \ \boxed{a_7 \ a_6 \ a_5 \ a_4 \ a_3 \ a_2 \ a_1 \ a_0} \}$

$[0, k-1]$

$rev(A, 0, k-1)$

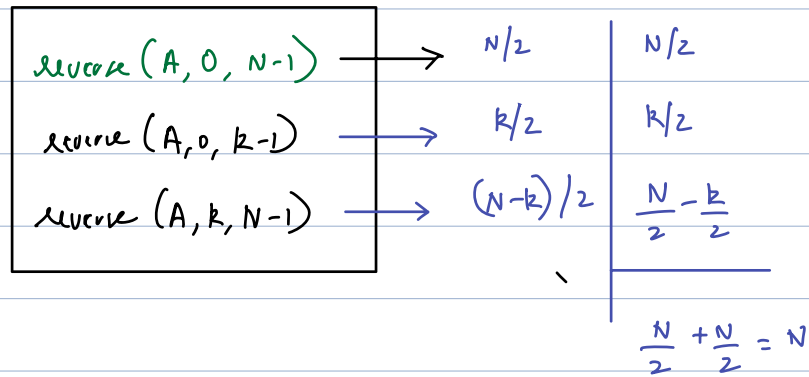
$rev(A, k, N-1)$

$\{ \boxed{a_8 \ a_9 \ a_{10} \ a_{11} \ a_{12}} \ \boxed{a_0 \ a_1 \ a_2 \ a_3 \ a_4 \ a_5 \ a_6 \ a_7} \}$



$\{a_8, a_9, a_{10}, a_{11}, a_{12}, a_0, a_1, a_2, a_3, a_4, a_5, a_6, a_7\}$

Output



TC: $O(N)$

SC: $O(1)$

$k > N$

k=0	1	2	3	4	5	k=5	1	2	3	4	5
k=1	5	1	2	3	4	k=6	5	1	2	3	4
k=2	4	5	1	2	3	k=7	4	5	1	2	3
k=3	3	4	5	1	2						
k=4	2	3	4	5	1						

$k > N$

HW

Division: Repeated subtraction
 Multia: Repeated addition

$$3 = \frac{15}{5} \Rightarrow$$

$$15 - 5 - 5 - 5 = 0$$

$$\frac{15}{7} \Rightarrow$$

$$15 - 7 - 7 = 1$$

$$15 \% 7 =$$

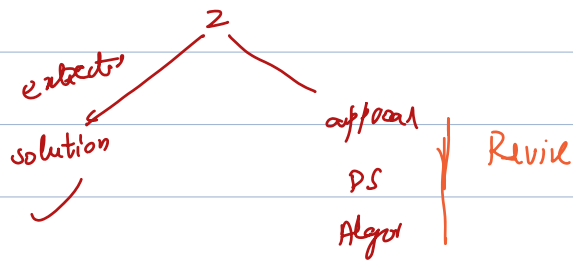
$$(18) \rightarrow (13) \rightarrow 8 \rightarrow (3)$$

$$18 \% 5 = 3$$

i	j	
0	0	-
⋮		⋮
N		N
[0 N)		
		(N+1)

for





big O ✓

for $(i=0; i < N; i+=1) \rightarrow O(N)$

for $(i=1; i < N; i*=c) O(\log_c N)$