q3

April 3, 2020

0.1 Question 3 - MNIST Classification using PyTorch

```
[0]: import torch import numpy as np
```

Load Data Sets

```
[2]: from torchvision import datasets
     import torchvision.transforms as transforms
     # number of subprocesses to use for data loading
     num_workers = 0
     # how many samples per batch to load
     batch size = 20
     # convert data to torch.FloatTensor
     transform = transforms.ToTensor()
     # choose the training and test datasets
     train_data = datasets.MNIST(root='data', train=True,
                                        download=True, transform=transform)
     test_data = datasets.MNIST(root='data', train=False,
                                       download=True, transform=transform)
     # prepare data loaders
     train_loader = torch.utils.data.DataLoader(train_data, batch_size=batch_size,
         num_workers=num_workers)
     test_loader = torch.utils.data.DataLoader(test_data, batch_size=batch_size,
         num_workers=num_workers)
```

HBox(children=(IntProgress(value=1, bar_style='info', max=1), HTML(value='')))

Extracting data/MNIST/raw/train-images-idx3-ubyte.gz to data/MNIST/raw Downloading http://yann.lecun.com/exdb/mnist/train-labels-idx1-ubyte.gz to data/MNIST/raw/train-labels-idx1-ubyte.gz

```
HBox(children=(IntProgress(value=1, bar_style='info', max=1), HTML(value='')))
```

Extracting data/MNIST/raw/train-labels-idx1-ubyte.gz to data/MNIST/raw Downloading http://yann.lecun.com/exdb/mnist/t10k-images-idx3-ubyte.gz to data/MNIST/raw/t10k-images-idx3-ubyte.gz

```
HBox(children=(IntProgress(value=1, bar_style='info', max=1), HTML(value='')))
```

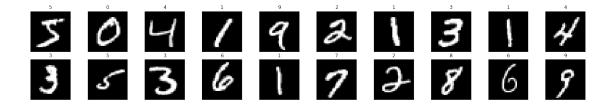
Extracting data/MNIST/raw/t10k-images-idx3-ubyte.gz to data/MNIST/raw Downloading http://yann.lecun.com/exdb/mnist/t10k-labels-idx1-ubyte.gz to data/MNIST/raw/t10k-labels-idx1-ubyte.gz

```
HBox(children=(IntProgress(value=1, bar_style='info', max=1), HTML(value='')))
```

Extracting data/MNIST/raw/t10k-labels-idx1-ubyte.gz to data/MNIST/raw Processing...

Done!

Visualize a batch of Training Set



Define the Network Architecture

```
[0]: import torch.nn as nn
     import torch.nn.functional as F
     ## Define the NN architecture
     class Net(nn.Module):
         def __init__(self):
             super(Net, self).__init__()
             self.fc1 = nn.Linear(28 * 28, 512)
             # linear layer (n_hidden -> hidden_2)
             self.fc2 = nn.Linear(512, 512)
             # linear layer (n_hidden -> 10)
             self.fc3 = nn.Linear(512, 10)
             # dropout layer (p=0.2)
             # dropout prevents overfitting of data
             self.dropout = nn.Dropout(0.2)
         def forward(self, x):
             # flatten image input
             x = x.view(-1, 28 * 28)
             # add hidden layer, with relu activation function
             x = F.relu(self.fc1(x))
             return x
[5]: # initialize the NN
     model = Net()
     print(model)
    Net(
      (fc1): Linear(in_features=784, out_features=512, bias=True)
      (fc2): Linear(in_features=512, out_features=512, bias=True)
      (fc3): Linear(in_features=512, out_features=10, bias=True)
      (dropout): Dropout(p=0.2, inplace=False)
    )
    Specify Loss Function and Optimizer
[0]: criterion = nn.CrossEntropyLoss()
     # specify optimizer
     optimizer = torch.optim.SGD(model.parameters(), lr=0.01)
```

Train the Network

```
[7]: n_epochs = 30 # suggest training between 20-50 epochs
     model.train() # prep model for training
     for epoch in range(n_epochs):
         # monitor training loss
         train loss = 0.0
         ####################
         # train the model #
         ####################
         for data, target in train_loader:
             # clear the gradients of all optimized variables
             optimizer.zero_grad()
             # forward pass: compute predicted outputs by passing inputs to the model
             output = model(data)
             # calculate the loss
             loss = criterion(output, target)
             # backward pass: compute gradient of the loss with respect to model_{\sqcup}
      \rightarrow parameters
             loss.backward()
             # perform a single optimization step (parameter update)
             optimizer.step()
             # update running training loss
             train_loss += loss.item()*data.size(0)
         # print training statistics
         # calculate average loss over an epoch
         train_loss = train_loss/len(train_loader.dataset)
         print('Epoch: {} \tTraining Loss: {:.6f}'.format(
             epoch+1,
             train_loss
             ))
```

```
Epoch: 1
                Training Loss: 0.804222
Epoch: 2
                Training Loss: 0.411707
Epoch: 3
                Training Loss: 0.370065
Epoch: 4
                Training Loss: 0.348959
Epoch: 5
                Training Loss: 0.335502
Epoch: 6
                Training Loss: 0.325918
Epoch: 7
                Training Loss: 0.318626
Epoch: 8
                Training Loss: 0.312826
Epoch: 9
                Training Loss: 0.308064
Epoch: 10
                Training Loss: 0.304058
Epoch: 11
                Training Loss: 0.300624
Epoch: 12
                Training Loss: 0.297635
```

```
Epoch: 13
                Training Loss: 0.294999
Epoch: 14
                Training Loss: 0.292651
Epoch: 15
                Training Loss: 0.290539
Epoch: 16
                Training Loss: 0.288626
Epoch: 17
                Training Loss: 0.286881
Epoch: 18
                Training Loss: 0.285279
Epoch: 19
                Training Loss: 0.283802
Epoch: 20
                Training Loss: 0.282434
Epoch: 21
                Training Loss: 0.281160
                Training Loss: 0.279970
Epoch: 22
Epoch: 23
                Training Loss: 0.278856
Epoch: 24
                Training Loss: 0.277808
Epoch: 25
                Training Loss: 0.276820
Epoch: 26
                Training Loss: 0.275887
Epoch: 27
                Training Loss: 0.275002
Epoch: 28
                Training Loss: 0.274163
Epoch: 29
                Training Loss: 0.273365
Epoch: 30
                Training Loss: 0.272604
```

Test the Trained Network¶

```
[8]: test_loss = 0.0
     class_correct = list(0. for i in range(10))
     class_total = list(0. for i in range(10))
     model.eval() # prep model for *evaluation*
     for data, target in test_loader:
         # forward pass: compute predicted outputs by passing inputs to the model
         output = model(data)
         # calculate the loss
         loss = criterion(output, target)
         # update test loss
         test_loss += loss.item()*data.size(0)
         # convert output probabilities to predicted class
         _, pred = torch.max(output, 1)
         # compare predictions to true label
         correct = np.squeeze(pred.eq(target.data.view_as(pred)))
         # calculate test accuracy for each object class
         for i in range(batch_size):
             label = target.data[i]
             class_correct[label] += correct[i].item()
             class_total[label] += 1
     # calculate and print avg test loss
     test_loss = test_loss/len(test_loader.dataset)
     print('Test Loss: {:.6f}\n'.format(test_loss))
```

Test Loss: 0.274007

```
Test Accuracy of
                    0: 98% (962/980)
Test Accuracy of
                    1: 97% (1109/1135)
Test Accuracy of
                    2: 88% (918/1032)
Test Accuracy of
                   3: 90% (914/1010)
Test Accuracy of
                   4: 92% (909/982)
Test Accuracy of
                    5: 87% (781/892)
                    6: 94% (910/958)
Test Accuracy of
Test Accuracy of
                   7: 92% (946/1028)
Test Accuracy of
                    8: 88% (864/974)
Test Accuracy of
                    9: 90% (916/1009)
```

Test Accuracy (Overall): 92% (9229/10000)

Visualize Sample Test Results

```
[9]: dataiter = iter(test_loader)
     images, labels = dataiter.next()
     # get sample outputs
     output = model(images)
     # convert output probabilities to predicted class
     _, preds = torch.max(output, 1)
     # prep images for display
     images = images.numpy()
     # plot the images in the batch, along with predicted and true labels
     fig = plt.figure(figsize=(25, 4))
     for idx in np.arange(20):
         ax = fig.add_subplot(2, 20/2, idx+1, xticks=[], yticks=[])
         ax.imshow(np.squeeze(images[idx]), cmap='gray')
         ax.set_title("{} ({})".format(str(preds[idx].item()), str(labels[idx].
      \rightarrowitem()),
                      color=("green" if preds[idx]==labels[idx] else "red"))
```



0.2 MNIST Classification using CNN

```
[0]: import numpy as np # to handle matrix and data operation
     import pandas as pd # to read csv and handle dataframe
     import torch
     import torch.nn as nn
     import torch.nn.functional as F
     import torch.utils.data
     from torch.autograd import Variable
     from sklearn.model_selection import train_test_split
[0]: from keras.datasets import mnist
     (x_train, y_train), (x_test, y_test) = mnist.load_data()
[0]: x_train = x_train.reshape(60000,784)
     x_{test} = x_{test.reshape}(10000,784)
[0]: BATCH_SIZE = 32
[0]: torch_X_train = torch.from_numpy(x_train).type(torch.LongTensor)
     torch_y_train = torch.from_numpy(y_train).type(torch.LongTensor)
[0]: torch_X_test = torch.from_numpy(x_test).type(torch.LongTensor)
     torch_y_test = torch.from_numpy(y_test).type(torch.LongTensor)
[0]: train = torch.utils.data.TensorDataset(torch_X_train,torch_y_train)
     test = torch.utils.data.TensorDataset(torch_X_test,torch_y_test)
[0]: train_loader = torch.utils.data.DataLoader(train, batch_size = BATCH_SIZE,_u
     ⇒shuffle = False)
     test_loader = torch.utils.data.DataLoader(test, batch_size = BATCH_SIZE,__
     ⇒shuffle = False)
```

```
[59]: class MLP(nn.Module):
          def __init__(self):
              super(MLP, self).__init__()
              self.linear1 = nn.Linear(784,250)
              self.linear2 = nn.Linear(250,100)
              self.linear3 = nn.Linear(100,10)
          def forward(self,X):
              X = F.relu(self.linear1(X))
              X = F.relu(self.linear2(X))
              X = self.linear3(X)
              return F.log softmax(X, dim=1)
      mlp = MLP()
      print(mlp)
     MLP(
       (linear1): Linear(in_features=784, out_features=250, bias=True)
       (linear2): Linear(in_features=250, out_features=100, bias=True)
       (linear3): Linear(in_features=100, out_features=10, bias=True)
     )
 [0]: def fit(model, train_loader):
          optimizer = torch.optim.Adam(model.parameters())#, lr=0.001, betas=(0.9,0.
       →999))
          error = nn.CrossEntropyLoss()
          EPOCHS = 5
          model.train()
          for epoch in range(EPOCHS):
              correct = 0
              for batch_idx, (X_batch, y_batch) in enumerate(train_loader):
                  var_X_batch = Variable(X_batch).float()
                  var_y_batch = Variable(y_batch)
                  optimizer.zero_grad()
                  output = model(var_X_batch)
                  loss = error(output, var_y_batch)
                  loss.backward()
                  optimizer.step()
                  # Total correct predictions
                  predicted = torch.max(output.data, 1)[1]
                  correct += (predicted == var_y_batch).sum()
                  #print(correct)
                  if batch_idx % 50 == 0:
                      print('Epoch : {} [{}/{} ({:.0f}%)]\tLoss: {:.6f}\t Accuracy:{:.
       \hookrightarrow3f}%'.format(
```

```
epoch, batch_idx*len(X_batch), len(train_loader.dataset),__

100.*batch_idx / len(train_loader), (loss.data), float(correct*100) /__
float(BATCH_SIZE*(batch_idx+1))))
```

[67]: fit(mlp, train_loader)

```
Epoch: 0 [0/60000 (0%)]
                                Loss: 0.028779
                                                  Accuracy: 100.000%
Epoch: 0 [1600/60000 (3%)]
                                                 Accuracy:96.875%
                                Loss: 0.135546
Epoch: 0 [3200/60000 (5%)]
                                Loss: 0.161492
                                                 Accuracy:97.061%
Epoch: 0 [4800/60000 (8%)]
                                Loss: 0.029837
                                                 Accuracy: 97.144%
Epoch: 0 [6400/60000 (11%)]
                                Loss: 0.251311
                                                  Accuracy:97.233%
Epoch: 0 [8000/60000 (13%)]
                                Loss: 0.288707
                                                  Accuracy:96.987%
Epoch: 0 [9600/60000 (16%)]
                                                  Accuracy:96.564%
                                Loss: 0.001341
Epoch: 0 [11200/60000 (19%)]
                                Loss: 0.147621
                                                  Accuracy:96.270%
Epoch: 0 [12800/60000 (21%)]
                                                  Accuracy:96.213%
                                Loss: 0.162637
Epoch: 0 [14400/60000 (24%)]
                                Loss: 0.040754
                                                 Accuracy:96.182%
Epoch: 0 [16000/60000 (27%)]
                                Loss: 0.053642
                                                  Accuracy:96.214%
Epoch: 0 [17600/60000 (29%)]
                                Loss: 0.021809
                                                  Accuracy:96.257%
Epoch: 0 [19200/60000 (32%)]
                                Loss: 0.007951
                                                  Accuracy:96.339%
Epoch: 0 [20800/60000 (35%)]
                                                  Accuracy:96.376%
                                Loss: 0.117186
Epoch: 0 [22400/60000 (37%)]
                                Loss: 0.001032
                                                  Accuracy:96.438%
Epoch: 0 [24000/60000 (40%)]
                                Loss: 0.240103
                                                  Accuracy:96.451%
Epoch: 0 [25600/60000 (43%)]
                                Loss: 0.097887
                                                 Accuracy:96.497%
Epoch: 0 [27200/60000 (45%)]
                                Loss: 0.023727
                                                 Accuracy:96.500%
Epoch: 0 [28800/60000 (48%)]
                                Loss: 0.015119
                                                 Accuracy:96.528%
Epoch: 0 [30400/60000 (51%)]
                                Loss: 0.070183
                                                  Accuracy:96.537%
Epoch: 0 [32000/60000 (53%)]
                                Loss: 0.012500
                                                  Accuracy:96.544%
Epoch: 0 [33600/60000 (56%)]
                                Loss: 0.110607
                                                  Accuracy:96.530%
Epoch: 0 [35200/60000 (59%)]
                                Loss: 0.357193
                                                  Accuracy:96.540%
Epoch: 0 [36800/60000 (61%)]
                                Loss: 0.010914
                                                  Accuracy:96.549%
Epoch: 0 [38400/60000 (64%)]
                                Loss: 0.176304
                                                  Accuracy:96.555%
Epoch: 0 [40000/60000 (67%)]
                                Loss: 0.098055
                                                  Accuracy:96.530%
Epoch: 0 [41600/60000 (69%)]
                                Loss: 0.044533
                                                  Accuracy:96.539%
Epoch: 0 [43200/60000 (72%)]
                                                  Accuracy:96.551%
                                Loss: 0.099969
Epoch: 0 [44800/60000 (75%)]
                                Loss: 0.024746
                                                  Accuracy:96.576%
Epoch: 0 [46400/60000 (77%)]
                                Loss: 0.333618
                                                  Accuracy: 96.550%
Epoch: 0 [48000/60000 (80%)]
                                Loss: 0.118122
                                                  Accuracy:96.565%
Epoch: 0 [49600/60000 (83%)]
                                Loss: 0.100130
                                                 Accuracy:96.555%
Epoch: 0 [51200/60000 (85%)]
                                Loss: 0.101556
                                                 Accuracy:96.549%
Epoch: 0 [52800/60000 (88%)]
                                Loss: 0.163493
                                                  Accuracy:96.555%
Epoch: 0 [54400/60000 (91%)]
                                Loss: 0.001940
                                                 Accuracy:96.550%
Epoch: 0 [56000/60000 (93%)]
                                Loss: 0.151699
                                                  Accuracy:96.552%
Epoch: 0 [57600/60000 (96%)]
                                Loss: 0.085508
                                                  Accuracy:96.577%
Epoch: 0 [59200/60000 (99%)]
                                Loss: 0.006413
                                                  Accuracy:96.607%
Epoch: 1 [0/60000 (0%)]
                                Loss: 0.066838
                                                  Accuracy:96.875%
Epoch: 1 [1600/60000 (3%)]
                                Loss: 0.038393
                                                  Accuracy:95.895%
Epoch: 1 [3200/60000 (5%)]
                                Loss: 0.088629
                                                 Accuracy:96.566%
```

```
Epoch: 1 [4800/60000 (8%)]
                                Loss: 0.073845
                                                  Accuracy:96.978%
Epoch: 1 [6400/60000 (11%)]
                                Loss: 0.323887
                                                  Accuracy:97.015%
Epoch: 1 [8000/60000 (13%)]
                                Loss: 0.080831
                                                  Accuracy:97.049%
Epoch: 1 [9600/60000 (16%)]
                                                  Accuracy:97.103%
                                Loss: 0.028484
Epoch: 1 [11200/60000 (19%)]
                                Loss: 0.217653
                                                  Accuracy: 97.044%
Epoch: 1 [12800/60000 (21%)]
                                                  Accuracy:97.015%
                                Loss: 0.015726
Epoch: 1 [14400/60000 (24%)]
                                Loss: 0.031854
                                                  Accuracy: 96.993%
Epoch: 1 [16000/60000 (27%)]
                                Loss: 0.102694
                                                  Accuracy:97.050%
Epoch: 1 [17600/60000 (29%)]
                                Loss: 0.314560
                                                  Accuracy:97.164%
Epoch: 1 [19200/60000 (32%)]
                                Loss: 0.043562
                                                  Accuracy:97.192%
Epoch: 1 [20800/60000 (35%)]
                                Loss: 0.078116
                                                  Accuracy:97.211%
Epoch: 1 [22400/60000 (37%)]
                                                  Accuracy:97.214%
                                Loss: 0.010395
Epoch: 1 [24000/60000 (40%)]
                                Loss: 0.008545
                                                  Accuracy:97.241%
Epoch: 1 [25600/60000 (43%)]
                                Loss: 0.087680
                                                  Accuracy: 97.285%
Epoch: 1 [27200/60000 (45%)]
                                Loss: 0.016307
                                                  Accuracy:97.264%
Epoch: 1 [28800/60000 (48%)]
                                Loss: 0.070700
                                                  Accuracy: 97.295%
Epoch: 1 [30400/60000 (51%)]
                                Loss: 0.283281
                                                  Accuracy:97.315%
Epoch: 1 [32000/60000 (53%)]
                                Loss: 0.124514
                                                  Accuracy:97.331%
Epoch: 1 [33600/60000 (56%)]
                                                  Accuracy:97.265%
                                Loss: 0.077984
Epoch: 1 [35200/60000 (59%)]
                                Loss: 0.018130
                                                  Accuracy: 97.272%
Epoch: 1 [36800/60000 (61%)]
                                Loss: 0.063739
                                                  Accuracy: 97.277%
Epoch: 1 [38400/60000 (64%)]
                                Loss: 0.262766
                                                  Accuracy: 97.250%
Epoch: 1 [40000/60000 (67%)]
                                Loss: 0.040512
                                                  Accuracy:97.252%
Epoch: 1 [41600/60000 (69%)]
                                Loss: 0.088825
                                                  Accuracy:97.235%
Epoch: 1 [43200/60000 (72%)]
                                Loss: 0.161225
                                                  Accuracy:97.213%
Epoch: 1 [44800/60000 (75%)]
                                Loss: 0.050391
                                                  Accuracy:97.232%
Epoch: 1 [46400/60000 (77%)]
                                Loss: 0.577136
                                                  Accuracy: 97.194%
Epoch: 1 [48000/60000 (80%)]
                                Loss: 0.154128
                                                  Accuracy: 97.183%
Epoch: 1 [49600/60000 (83%)]
                                Loss: 0.199059
                                                  Accuracy: 97.155%
Epoch: 1 [51200/60000 (85%)]
                                Loss: 0.163394
                                                  Accuracy:97.146%
                                Loss: 0.163188
Epoch: 1 [52800/60000 (88%)]
                                                  Accuracy: 97.161%
Epoch: 1 [54400/60000 (91%)]
                                Loss: 0.007887
                                                  Accuracy:97.163%
Epoch: 1 [56000/60000 (93%)]
                                Loss: 0.123494
                                                  Accuracy: 97.150%
Epoch: 1 [57600/60000 (96%)]
                                Loss: 0.084630
                                                  Accuracy:97.167%
Epoch: 1 [59200/60000 (99%)]
                                Loss: 0.041318
                                                  Accuracy: 97.197%
Epoch: 2 [0/60000 (0%)]
                                Loss: 0.101924
                                                  Accuracy:93.750%
Epoch: 2 [1600/60000 (3%)]
                                Loss: 0.192111
                                                  Accuracy: 96.078%
Epoch: 2 [3200/60000 (5%)]
                                Loss: 0.070167
                                                  Accuracy:97.123%
Epoch: 2 [4800/60000 (8%)]
                                Loss: 0.023145
                                                  Accuracy:97.413%
Epoch: 2 [6400/60000 (11%)]
                                Loss: 0.164375
                                                  Accuracy:97.217%
Epoch: 2 [8000/60000 (13%)]
                                Loss: 0.206731
                                                  Accuracy:97.261%
Epoch: 2 [9600/60000 (16%)]
                                Loss: 0.013814
                                                  Accuracy: 97.228%
Epoch: 2 [11200/60000 (19%)]
                                Loss: 0.189980
                                                  Accuracy:97.302%
Epoch: 2 [12800/60000 (21%)]
                                Loss: 0.094958
                                                  Accuracy:97.319%
Epoch: 2 [14400/60000 (24%)]
                                Loss: 0.015213
                                                  Accuracy:97.367%
Epoch: 2 [16000/60000 (27%)]
                                Loss: 0.093988
                                                  Accuracy:97.287%
Epoch: 2 [17600/60000 (29%)]
                                Loss: 0.621408
                                                  Accuracy:97.221%
Epoch: 2 [19200/60000 (32%)]
                                Loss: 0.108640
                                                  Accuracy:97.223%
```

```
Epoch: 2 [20800/60000 (35%)]
                                Loss: 0.021036
                                                  Accuracy:97.216%
Epoch: 2 [22400/60000 (37%)]
                                Loss: 0.001247
                                                  Accuracy:97.209%
Epoch: 2 [24000/60000 (40%)]
                                Loss: 0.015268
                                                  Accuracy: 97.233%
Epoch: 2 [25600/60000 (43%)]
                                                  Accuracy:97.261%
                                Loss: 0.101386
Epoch: 2 [27200/60000 (45%)]
                                Loss: 0.131324
                                                  Accuracy: 97.239%
Epoch: 2 [28800/60000 (48%)]
                                                  Accuracy:97.243%
                                Loss: 0.069168
Epoch: 2 [30400/60000 (51%)]
                                Loss: 0.025075
                                                  Accuracy: 97.282%
Epoch: 2 [32000/60000 (53%)]
                                Loss: 0.016453
                                                  Accuracy:97.300%
Epoch: 2 [33600/60000 (56%)]
                                Loss: 0.020328
                                                  Accuracy:97.273%
Epoch: 2 [35200/60000 (59%)]
                                Loss: 0.872610
                                                  Accuracy:97.298%
Epoch: 2 [36800/60000 (61%)]
                                Loss: 0.101088
                                                  Accuracy:97.296%
Epoch: 2 [38400/60000 (64%)]
                                                  Accuracy:97.294%
                                Loss: 0.088246
Epoch: 2 [40000/60000 (67%)]
                                Loss: 0.119826
                                                  Accuracy:97.302%
Epoch: 2 [41600/60000 (69%)]
                                Loss: 0.052212
                                                  Accuracy: 97.324%
Epoch: 2 [43200/60000 (72%)]
                                Loss: 0.325394
                                                  Accuracy:97.305%
Epoch: 2 [44800/60000 (75%)]
                                Loss: 0.062563
                                                  Accuracy:97.310%
Epoch: 2 [46400/60000 (77%)]
                                Loss: 0.133759
                                                  Accuracy:97.273%
Epoch: 2 [48000/60000 (80%)]
                                Loss: 0.219807
                                                  Accuracy:97.271%
Epoch: 2 [49600/60000 (83%)]
                                                  Accuracy:97.288%
                                Loss: 0.019319
Epoch: 2 [51200/60000 (85%)]
                                Loss: 0.045573
                                                  Accuracy: 97.273%
Epoch: 2 [52800/60000 (88%)]
                                Loss: 0.129453
                                                  Accuracy: 97.265%
Epoch: 2 [54400/60000 (91%)]
                                Loss: 0.037412
                                                  Accuracy: 97.270%
Epoch: 2 [56000/60000 (93%)]
                                Loss: 0.061451
                                                  Accuracy:97.275%
Epoch: 2 [57600/60000 (96%)]
                                Loss: 0.268131
                                                  Accuracy:97.278%
Epoch: 2 [59200/60000 (99%)]
                                Loss: 0.029599
                                                  Accuracy:97.316%
Epoch: 3 [0/60000 (0%)]
                                Loss: 0.151179
                                                  Accuracy:93.750%
Epoch: 3 [1600/60000 (3%)]
                                Loss: 0.128003
                                                  Accuracy:96.446%
Epoch: 3 [3200/60000 (5%)]
                                Loss: 0.006657
                                                  Accuracy:97.308%
Epoch: 3 [4800/60000 (8%)]
                                Loss: 0.015271
                                                  Accuracy:97.392%
Epoch: 3 [6400/60000 (11%)]
                                Loss: 0.127014
                                                  Accuracy:97.404%
Epoch: 3 [8000/60000 (13%)]
                                Loss: 0.137492
                                                  Accuracy:97.323%
Epoch: 3 [9600/60000 (16%)]
                                Loss: 0.011746
                                                  Accuracy:97.290%
Epoch: 3 [11200/60000 (19%)]
                                Loss: 0.193034
                                                  Accuracy:97.391%
Epoch: 3 [12800/60000 (21%)]
                                Loss: 0.151988
                                                  Accuracy:97.506%
Epoch: 3 [14400/60000 (24%)]
                                Loss: 0.001826
                                                  Accuracy: 97.561%
Epoch: 3 [16000/60000 (27%)]
                                Loss: 0.038850
                                                  Accuracy: 97.493%
Epoch: 3 [17600/60000 (29%)]
                                Loss: 0.005036
                                                  Accuracy: 97.533%
Epoch: 3 [19200/60000 (32%)]
                                Loss: 0.041748
                                                  Accuracy:97.577%
Epoch: 3 [20800/60000 (35%)]
                                Loss: 0.061989
                                                  Accuracy:97.552%
Epoch: 3 [22400/60000 (37%)]
                                Loss: 0.000083
                                                  Accuracy:97.562%
Epoch: 3 [24000/60000 (40%)]
                                Loss: 0.010684
                                                  Accuracy:97.562%
Epoch: 3 [25600/60000 (43%)]
                                Loss: 0.035633
                                                  Accuracy: 97.554%
Epoch: 3 [27200/60000 (45%)]
                                Loss: 0.003687
                                                  Accuracy: 97.536%
Epoch: 3 [28800/60000 (48%)]
                                Loss: 0.059841
                                                  Accuracy: 97.562%
Epoch: 3 [30400/60000 (51%)]
                                Loss: 0.055981
                                                  Accuracy:97.581%
Epoch: 3 [32000/60000 (53%)]
                                Loss: 0.057697
                                                  Accuracy: 97.596%
Epoch: 3 [33600/60000 (56%)]
                                Loss: 0.099345
                                                  Accuracy:97.589%
Epoch: 3 [35200/60000 (59%)]
                                Loss: 0.004503
                                                  Accuracy:97.593%
```

```
Epoch: 3 [36800/60000 (61%)]
                                Loss: 0.132729
                                                  Accuracy:97.597%
Epoch: 3 [38400/60000 (64%)]
                                Loss: 0.078958
                                                  Accuracy:97.580%
Epoch: 3 [40000/60000 (67%)]
                                Loss: 0.049452
                                                  Accuracy:97.577%
Epoch: 3 [41600/60000 (69%)]
                                                  Accuracy:97.574%
                                Loss: 0.001719
Epoch: 3 [43200/60000 (72%)]
                                Loss: 0.175857
                                                  Accuracy: 97.580%
Epoch: 3 [44800/60000 (75%)]
                                Loss: 0.034069
                                                  Accuracy:97.589%
Epoch: 3 [46400/60000 (77%)]
                                Loss: 0.021272
                                                  Accuracy: 97.599%
Epoch: 3 [48000/60000 (80%)]
                                Loss: 0.064088
                                                  Accuracy:97.620%
Epoch: 3 [49600/60000 (83%)]
                                Loss: 0.003137
                                                  Accuracy:97.625%
Epoch: 3 [51200/60000 (85%)]
                                Loss: 0.014169
                                                  Accuracy:97.628%
Epoch: 3 [52800/60000 (88%)]
                                Loss: 0.221221
                                                  Accuracy: 97.625%
Epoch: 3 [54400/60000 (91%)]
                                Loss: 0.001268
                                                  Accuracy: 97.612%
Epoch: 3 [56000/60000 (93%)]
                                Loss: 0.063965
                                                  Accuracy: 97.596%
Epoch: 3 [57600/60000 (96%)]
                                Loss: 0.254212
                                                  Accuracy: 97.604%
Epoch: 3 [59200/60000 (99%)]
                                Loss: 0.000153
                                                  Accuracy:97.633%
Epoch: 4 [0/60000 (0%)]
                                Loss: 0.077204
                                                  Accuracy:96.875%
Epoch: 4 [1600/60000 (3%)]
                                Loss: 0.160978
                                                  Accuracy:97.059%
                                Loss: 0.022128
Epoch: 4 [3200/60000 (5%)]
                                                  Accuracy: 97.463%
Epoch: 4 [4800/60000 (8%)]
                                                  Accuracy:97.641%
                                Loss: 0.087849
Epoch: 4 [6400/60000 (11%)]
                                Loss: 0.282174
                                                  Accuracy: 97.512%
Epoch: 4 [8000/60000 (13%)]
                                Loss: 0.022924
                                                  Accuracy: 97.572%
Epoch: 4 [9600/60000 (16%)]
                                Loss: 0.057789
                                                  Accuracy: 97.456%
Epoch: 4 [11200/60000 (19%)]
                                Loss: 0.173873
                                                  Accuracy:97.480%
Epoch: 4 [12800/60000 (21%)]
                                Loss: 0.177891
                                                  Accuracy:97.498%
Epoch: 4 [14400/60000 (24%)]
                                Loss: 0.058999
                                                  Accuracy:97.568%
Epoch: 4 [16000/60000 (27%)]
                                Loss: 0.087360
                                                  Accuracy:97.493%
Epoch: 4 [17600/60000 (29%)]
                                Loss: 0.002993
                                                  Accuracy: 97.544%
Epoch: 4 [19200/60000 (32%)]
                                Loss: 0.007460
                                                  Accuracy:97.577%
Epoch: 4 [20800/60000 (35%)]
                                Loss: 0.172938
                                                  Accuracy: 97.576%
Epoch: 4 [22400/60000 (37%)]
                                Loss: 0.003647
                                                  Accuracy:97.597%
Epoch: 4 [24000/60000 (40%)]
                                Loss: 0.003558
                                                  Accuracy:97.616%
Epoch: 4 [25600/60000 (43%)]
                                Loss: 0.123521
                                                  Accuracy:97.651%
Epoch: 4 [27200/60000 (45%)]
                                Loss: 0.062108
                                                  Accuracy:97.650%
Epoch: 4 [28800/60000 (48%)]
                                Loss: 0.079932
                                                  Accuracy:97.683%
Epoch: 4 [30400/60000 (51%)]
                                Loss: 0.002716
                                                  Accuracy: 97.703%
Epoch: 4 [32000/60000 (53%)]
                                Loss: 0.218044
                                                  Accuracy: 97.687%
Epoch: 4 [33600/60000 (56%)]
                                Loss: 0.009926
                                                  Accuracy: 97.693%
Epoch: 4 [35200/60000 (59%)]
                                Loss: 0.001960
                                                  Accuracy:97.707%
Epoch: 4 [36800/60000 (61%)]
                                Loss: 0.003491
                                                  Accuracy:97.706%
Epoch: 4 [38400/60000 (64%)]
                                Loss: 0.193213
                                                  Accuracy:97.684%
Epoch: 4 [40000/60000 (67%)]
                                Loss: 0.121122
                                                  Accuracy:97.677%
Epoch: 4 [41600/60000 (69%)]
                                Loss: 0.058635
                                                  Accuracy: 97.672%
Epoch: 4 [43200/60000 (72%)]
                                Loss: 0.121910
                                                  Accuracy:97.668%
Epoch: 4 [44800/60000 (75%)]
                                Loss: 0.020887
                                                  Accuracy:97.711%
Epoch: 4 [46400/60000 (77%)]
                                Loss: 0.099990
                                                  Accuracy:97.676%
Epoch: 4 [48000/60000 (80%)]
                                Loss: 0.167490
                                                  Accuracy:97.677%
Epoch: 4 [49600/60000 (83%)]
                                Loss: 0.096079
                                                  Accuracy:97.671%
Epoch: 4 [51200/60000 (85%)]
                                Loss: 0.009618
                                                  Accuracy:97.687%
```

```
Epoch: 4 [52800/60000 (88%)] Loss: 0.322359
                                                      Accuracy:97.714%
     Epoch: 4 [54400/60000 (91%)] Loss: 0.001315 Accuracy:97.702%
     Epoch: 4 [56000/60000 (93%)] Loss: 0.065532
                                                      Accuracy:97.717%
     Epoch: 4 [57600/60000 (96%)] Loss: 0.120293
                                                      Accuracy:97.729%
     Epoch: 4 [59200/60000 (99%)] Loss: 0.000217
                                                      Accuracy:97.758%
[68]: def evaluate(model):
      #model = mlp
          correct = 0
          for test_imgs, test_labels in test_loader:
              #print(test_imgs.shape)
              test_imgs = Variable(test_imgs).float()
              output = model(test_imgs)
              predicted = torch.max(output,1)[1]
              correct += (predicted == test_labels).sum()
          print("Test accuracy:{:.3f}% ".format( float(correct) /_
       →(len(test_loader)*BATCH_SIZE)))
      evaluate(mlp)
     Test accuracy:0.971%
     ##Since a CNN needs a image shape as input let's reshape our flatten images to real image
[69]: torch_X_train = torch_X_train.view(-1, 1,28,28).float()
      torch_X_test = torch_X_test.view(-1,1,28,28).float()
      print(torch_X_train.shape)
      print(torch_X_test.shape)
      # Pytorch train and test sets
      train = torch.utils.data.TensorDataset(torch_X_train,torch_y_train)
      test = torch.utils.data.TensorDataset(torch_X_test,torch_y_test)
      # data loader
      train_loader = torch.utils.data.DataLoader(train, batch_size = BATCH_SIZE,__
       ⇒shuffle = False)
      test loader = torch.utils.data.DataLoader(test, batch size = BATCH SIZE,
       \rightarrowshuffle = False)MB
     torch.Size([60000, 1, 28, 28])
     torch.Size([10000, 1, 28, 28])
[70]: class CNN(nn.Module):
          def init (self):
              super(CNN, self).__init__()
              self.conv1 = nn.Conv2d(1, 32, kernel_size=5)
              self.conv2 = nn.Conv2d(32, 32, kernel_size=5)
              self.conv3 = nn.Conv2d(32,64, kernel_size=5)
              self.fc1 = nn.Linear(3*3*64, 256)
```

```
self.fc2 = nn.Linear(256, 10)
          def forward(self, x):
              x = F.relu(self.conv1(x))
              \#x = F.dropout(x, p=0.5, training=self.training)
              x = F.relu(F.max_pool2d(self.conv2(x), 2))
              x = F.dropout(x, p=0.5, training=self.training)
              x = F.relu(F.max_pool2d(self.conv3(x),2))
              x = F.dropout(x, p=0.5, training=self.training)
              x = x.view(-1,3*3*64)
              x = F.relu(self.fc1(x))
              x = F.dropout(x, training=self.training)
              x = self.fc2(x)
              return F.log_softmax(x, dim=1)
      cnn = CNN()
      print(cnn)
      it = iter(train_loader)
      X_batch, y_batch = next(it)
      print(cnn.forward(X_batch).shape)
     CNN(
       (conv1): Conv2d(1, 32, kernel_size=(5, 5), stride=(1, 1))
       (conv2): Conv2d(32, 32, kernel_size=(5, 5), stride=(1, 1))
       (conv3): Conv2d(32, 64, kernel_size=(5, 5), stride=(1, 1))
       (fc1): Linear(in_features=576, out_features=256, bias=True)
       (fc2): Linear(in_features=256, out_features=10, bias=True)
     torch.Size([32, 10])
[71]: fit(cnn,train_loader)
     Epoch : 0 [0/60000 (0%)]
                                     Loss: 24.703955 Accuracy:6.250%
     Epoch: 0 [1600/60000 (3%)]
                                                       Accuracy: 17.279%
                                     Loss: 1.980315
                                                       Accuracy: 29.115%
     Epoch: 0 [3200/60000 (5%)]
                                     Loss: 1.460487
     Epoch: 0 [4800/60000 (8%)]
                                     Loss: 0.748759
                                                       Accuracy: 38.949%
     Epoch: 0 [6400/60000 (11%)]
                                     Loss: 1.238455
                                                       Accuracy: 45.553%
     Epoch: 0 [8000/60000 (13%)]
                                     Loss: 0.865389
                                                       Accuracy:50.461%
     Epoch: 0 [9600/60000 (16%)]
                                     Loss: 0.764462
                                                       Accuracy: 54.485%
     Epoch: 0 [11200/60000 (19%)]
                                     Loss: 0.602340
                                                       Accuracy: 58.191%
     Epoch: 0 [12800/60000 (21%)]
                                     Loss: 0.548422
                                                       Accuracy: 60.793%
     Epoch: 0 [14400/60000 (24%)]
                                     Loss: 0.491586
                                                       Accuracy:63.089%
     Epoch: 0 [16000/60000 (27%)]
                                     Loss: 0.702923
                                                       Accuracy: 64.814%
     Epoch: 0 [17600/60000 (29%)]
                                     Loss: 0.591373
                                                       Accuracy:66.640%
     Epoch: 0 [19200/60000 (32%)]
                                     Loss: 0.427941
                                                       Accuracy: 68.225%
     Epoch: 0 [20800/60000 (35%)]
                                     Loss: 0.508253
                                                       Accuracy:69.772%
     Epoch: 0 [22400/60000 (37%)]
                                     Loss: 0.220711
                                                       Accuracy:71.122%
```

```
Epoch: 0 [24000/60000 (40%)]
                                Loss: 0.182511
                                                  Accuracy: 72.121%
Epoch: 0 [25600/60000 (43%)]
                                Loss: 0.578731
                                                  Accuracy:73.174%
Epoch: 0 [27200/60000 (45%)]
                                Loss: 0.405716
                                                  Accuracy: 74.104%
Epoch: 0 [28800/60000 (48%)]
                                                  Accuracy: 75.035%
                                Loss: 0.335528
Epoch: 0 [30400/60000 (51%)]
                                Loss: 0.524058
                                                  Accuracy: 75.710%
Epoch: 0 [32000/60000 (53%)]
                                                  Accuracy: 76.346%
                                Loss: 0.522807
Epoch: 0 [33600/60000 (56%)]
                                Loss: 0.353773
                                                  Accuracy: 77.019%
Epoch: 0 [35200/60000 (59%)]
                                Loss: 0.348661
                                                  Accuracy:77.677%
Epoch: 0 [36800/60000 (61%)]
                                Loss: 0.335008
                                                  Accuracy: 78.307%
Epoch: 0 [38400/60000 (64%)]
                                Loss: 0.295484
                                                  Accuracy: 78.841%
Epoch: 0 [40000/60000 (67%)]
                                Loss: 0.330925
                                                  Accuracy: 79.359%
Epoch: 0 [41600/60000 (69%)]
                                Loss: 0.761555
                                                  Accuracy: 79.790%
Epoch: 0 [43200/60000 (72%)]
                                Loss: 0.308168
                                                  Accuracy:80.204%
Epoch: 0 [44800/60000 (75%)]
                                Loss: 0.039641
                                                  Accuracy:80.661%
Epoch: 0 [46400/60000 (77%)]
                                Loss: 0.347005
                                                  Accuracy:81.032%
Epoch: 0 [48000/60000 (80%)]
                                Loss: 0.695292
                                                  Accuracy:81.404%
Epoch: 0 [49600/60000 (83%)]
                                Loss: 0.664559
                                                  Accuracy:81.742%
Epoch: 0 [51200/60000 (85%)]
                                Loss: 0.267460
                                                  Accuracy:82.083%
Epoch: 0 [52800/60000 (88%)]
                                                  Accuracy:82.418%
                                Loss: 0.457143
Epoch: 0 [54400/60000 (91%)]
                                Loss: 0.123103
                                                  Accuracy:82.742%
Epoch: 0 [56000/60000 (93%)]
                                Loss: 0.171987
                                                  Accuracy:83.040%
Epoch: 0 [57600/60000 (96%)]
                                Loss: 0.293099
                                                  Accuracy:83.320%
Epoch: 0 [59200/60000 (99%)]
                                Loss: 0.139004
                                                  Accuracy:83.656%
Epoch: 1 [0/60000 (0%)]
                                Loss: 0.197437
                                                  Accuracy: 93.750%
Epoch: 1 [1600/60000 (3%)]
                                Loss: 0.182057
                                                  Accuracy:93.137%
Epoch: 1 [3200/60000 (5%)]
                                Loss: 0.449420
                                                  Accuracy:94.028%
Epoch: 1 [4800/60000 (8%)]
                                Loss: 0.116307
                                                  Accuracy:93.729%
Epoch: 1 [6400/60000 (11%)]
                                Loss: 0.029951
                                                  Accuracy:93.797%
Epoch: 1 [8000/60000 (13%)]
                                Loss: 0.101050
                                                  Accuracy:93.875%
Epoch: 1 [9600/60000 (16%)]
                                Loss: 0.333615
                                                  Accuracy:93.625%
Epoch: 1 [11200/60000 (19%)]
                                Loss: 0.426801
                                                  Accuracy:93.643%
Epoch: 1 [12800/60000 (21%)]
                                Loss: 0.298322
                                                  Accuracy:93.462%
Epoch: 1 [14400/60000 (24%)]
                                Loss: 0.108020
                                                  Accuracy:93.528%
Epoch: 1 [16000/60000 (27%)]
                                Loss: 0.474114
                                                  Accuracy:93.469%
Epoch: 1 [17600/60000 (29%)]
                                Loss: 0.277469
                                                  Accuracy: 93.455%
Epoch: 1 [19200/60000 (32%)]
                                Loss: 0.163615
                                                  Accuracy: 93.506%
Epoch: 1 [20800/60000 (35%)]
                                Loss: 0.227395
                                                  Accuracy: 93.568%
Epoch: 1 [22400/60000 (37%)]
                                Loss: 0.010190
                                                  Accuracy:93.630%
Epoch: 1 [24000/60000 (40%)]
                                Loss: 0.085058
                                                  Accuracy:93.633%
Epoch: 1 [25600/60000 (43%)]
                                Loss: 0.092341
                                                  Accuracy:93.606%
Epoch: 1 [27200/60000 (45%)]
                                Loss: 0.161767
                                                  Accuracy:93.548%
Epoch: 1 [28800/60000 (48%)]
                                Loss: 0.029576
                                                  Accuracy:93.573%
Epoch: 1 [30400/60000 (51%)]
                                Loss: 0.205116
                                                  Accuracy:93.589%
Epoch: 1 [32000/60000 (53%)]
                                Loss: 0.252389
                                                  Accuracy:93.581%
Epoch: 1 [33600/60000 (56%)]
                                Loss: 0.318719
                                                  Accuracy:93.583%
Epoch: 1 [35200/60000 (59%)]
                                Loss: 0.124187
                                                  Accuracy:93.583%
Epoch: 1 [36800/60000 (61%)]
                                Loss: 0.110199
                                                  Accuracy:93.636%
Epoch: 1 [38400/60000 (64%)]
                                Loss: 0.135114
                                                  Accuracy:93.633%
```

```
Epoch: 1 [40000/60000 (67%)]
                                Loss: 0.337480
                                                  Accuracy:93.608%
Epoch: 1 [41600/60000 (69%)]
                                Loss: 0.151904
                                                  Accuracy:93.637%
Epoch: 1 [43200/60000 (72%)]
                                Loss: 0.201784
                                                  Accuracy:93.651%
Epoch: 1 [44800/60000 (75%)]
                                Loss: 0.120788
                                                  Accuracy:93.670%
Epoch: 1 [46400/60000 (77%)]
                                Loss: 0.631979
                                                  Accuracy:93.638%
Epoch: 1 [48000/60000 (80%)]
                                Loss: 0.330198
                                                  Accuracy:93.644%
Epoch: 1 [49600/60000 (83%)]
                                Loss: 0.092436
                                                  Accuracy:93.667%
Epoch: 1 [51200/60000 (85%)]
                                Loss: 0.046334
                                                  Accuracy:93.693%
Epoch: 1 [52800/60000 (88%)]
                                Loss: 0.316572
                                                  Accuracy:93.701%
Epoch: 1 [54400/60000 (91%)]
                                Loss: 0.114109
                                                  Accuracy:93.695%
Epoch: 1 [56000/60000 (93%)]
                                Loss: 0.394695
                                                  Accuracy:93.727%
Epoch: 1 [57600/60000 (96%)]
                                Loss: 0.083526
                                                  Accuracy:93.792%
Epoch: 1 [59200/60000 (99%)]
                                Loss: 0.015199
                                                  Accuracy:93.860%
Epoch: 2 [0/60000 (0%)]
                                Loss: 0.217455
                                                  Accuracy: 90.625%
Epoch: 2 [1600/60000 (3%)]
                                Loss: 0.406698
                                                  Accuracy:94.056%
Epoch: 2 [3200/60000 (5%)]
                                Loss: 0.423212
                                                  Accuracy: 94.864%
Epoch: 2 [4800/60000 (8%)]
                                Loss: 0.065729
                                                  Accuracy:94.454%
                                Loss: 0.006236
Epoch: 2 [6400/60000 (11%)]
                                                  Accuracy: 94.325%
Epoch: 2 [8000/60000 (13%)]
                                Loss: 0.204239
                                                  Accuracy:94.410%
Epoch: 2 [9600/60000 (16%)]
                                Loss: 0.303900
                                                  Accuracy: 94.248%
Epoch: 2 [11200/60000 (19%)]
                                Loss: 0.255757
                                                  Accuracy: 94.436%
Epoch: 2 [12800/60000 (21%)]
                                Loss: 0.152741
                                                  Accuracy: 94.459%
Epoch: 2 [14400/60000 (24%)]
                                Loss: 0.082564
                                                  Accuracy:94.471%
Epoch: 2 [16000/60000 (27%)]
                                Loss: 0.283941
                                                  Accuracy:94.374%
Epoch: 2 [17600/60000 (29%)]
                                Loss: 0.014378
                                                  Accuracy:94.380%
Epoch: 2 [19200/60000 (32%)]
                                Loss: 0.083600
                                                  Accuracy: 94.452%
Epoch: 2 [20800/60000 (35%)]
                                Loss: 0.360928
                                                  Accuracy: 94.556%
Epoch: 2 [22400/60000 (37%)]
                                Loss: 0.102351
                                                  Accuracy: 94.593%
Epoch: 2 [24000/60000 (40%)]
                                Loss: 0.109202
                                                  Accuracy: 94.653%
Epoch: 2 [25600/60000 (43%)]
                                Loss: 0.092279
                                                  Accuracy:94.714%
Epoch: 2 [27200/60000 (45%)]
                                Loss: 0.241476
                                                  Accuracy: 94.679%
Epoch: 2 [28800/60000 (48%)]
                                Loss: 0.107590
                                                  Accuracy:94.704%
Epoch: 2 [30400/60000 (51%)]
                                Loss: 0.188392
                                                  Accuracy:94.759%
Epoch: 2 [32000/60000 (53%)]
                                Loss: 0.298663
                                                  Accuracy:94.699%
Epoch: 2 [33600/60000 (56%)]
                                Loss: 0.165397
                                                  Accuracy: 94.690%
Epoch: 2 [35200/60000 (59%)]
                                Loss: 0.109414
                                                  Accuracy: 94.738%
Epoch: 2 [36800/60000 (61%)]
                                Loss: 0.111880
                                                  Accuracy: 94.790%
Epoch: 2 [38400/60000 (64%)]
                                Loss: 0.247883
                                                  Accuracy:94.786%
Epoch: 2 [40000/60000 (67%)]
                                Loss: 0.241609
                                                  Accuracy:94.799%
Epoch: 2 [41600/60000 (69%)]
                                Loss: 0.274725
                                                  Accuracy:94.809%
Epoch: 2 [43200/60000 (72%)]
                                Loss: 0.335197
                                                  Accuracy:94.828%
Epoch: 2 [44800/60000 (75%)]
                                                  Accuracy:94.872%
                                Loss: 0.005174
Epoch: 2 [46400/60000 (77%)]
                                Loss: 1.024677
                                                  Accuracy:94.889%
Epoch: 2 [48000/60000 (80%)]
                                Loss: 0.283337
                                                  Accuracy:94.860%
Epoch: 2 [49600/60000 (83%)]
                                Loss: 0.264172
                                                  Accuracy:94.854%
Epoch: 2 [51200/60000 (85%)]
                                Loss: 0.145659
                                                  Accuracy: 94.857%
Epoch: 2 [52800/60000 (88%)]
                                Loss: 0.662844
                                                  Accuracy:94.893%
Epoch: 2 [54400/60000 (91%)]
                                Loss: 0.017660
                                                  Accuracy:94.922%
```

```
Epoch: 2 [56000/60000 (93%)]
                                Loss: 0.118975
                                                  Accuracy:94.960%
Epoch: 2 [57600/60000 (96%)]
                                Loss: 0.390172
                                                  Accuracy:94.961%
Epoch: 2 [59200/60000 (99%)]
                                Loss: 0.000941
                                                  Accuracy:95.016%
Epoch: 3 [0/60000 (0%)]
                                                  Accuracy:96.875%
                                Loss: 0.039304
                                                  Accuracy:94.424%
Epoch: 3 [1600/60000 (3%)]
                                Loss: 0.274808
Epoch: 3 [3200/60000 (5%)]
                                                  Accuracy:95.142%
                                Loss: 0.082404
Epoch: 3 [4800/60000 (8%)]
                                Loss: 0.180459
                                                  Accuracy: 95.281%
Epoch: 3 [6400/60000 (11%)]
                                Loss: 0.055648
                                                  Accuracy:95.134%
Epoch: 3 [8000/60000 (13%)]
                                Loss: 0.032606
                                                  Accuracy:95.219%
Epoch: 3 [9600/60000 (16%)]
                                Loss: 0.057986
                                                  Accuracy:94.975%
Epoch: 3 [11200/60000 (19%)]
                                Loss: 0.275520
                                                  Accuracy:95.103%
Epoch: 3 [12800/60000 (21%)]
                                                  Accuracy:94.950%
                                Loss: 0.070716
Epoch: 3 [14400/60000 (24%)]
                                Loss: 0.027030
                                                  Accuracy:94.928%
Epoch: 3 [16000/60000 (27%)]
                                Loss: 0.066866
                                                  Accuracy:94.941%
Epoch: 3 [17600/60000 (29%)]
                                Loss: 0.028506
                                                  Accuracy:94.941%
Epoch: 3 [19200/60000 (32%)]
                                Loss: 0.219603
                                                  Accuracy:94.998%
Epoch: 3 [20800/60000 (35%)]
                                Loss: 0.051435
                                                  Accuracy:94.993%
                                Loss: 0.011864
Epoch: 3 [22400/60000 (37%)]
                                                  Accuracy: 95.047%
Epoch: 3 [24000/60000 (40%)]
                                Loss: 0.177396
                                                  Accuracy:95.073%
Epoch: 3 [25600/60000 (43%)]
                                Loss: 0.050125
                                                  Accuracy: 95.154%
Epoch: 3 [27200/60000 (45%)]
                                Loss: 0.215653
                                                  Accuracy: 95.131%
Epoch: 3 [28800/60000 (48%)]
                                Loss: 0.357761
                                                  Accuracy: 95.106%
Epoch: 3 [30400/60000 (51%)]
                                Loss: 0.303260
                                                  Accuracy:95.127%
Epoch: 3 [32000/60000 (53%)]
                                Loss: 0.435719
                                                  Accuracy:95.042%
Epoch: 3 [33600/60000 (56%)]
                                Loss: 0.038899
                                                  Accuracy:95.008%
Epoch: 3 [35200/60000 (59%)]
                                Loss: 0.157955
                                                  Accuracy:95.084%
Epoch: 3 [36800/60000 (61%)]
                                Loss: 0.065332
                                                  Accuracy: 95.127%
Epoch: 3 [38400/60000 (64%)]
                                Loss: 0.087521
                                                  Accuracy: 95.145%
Epoch: 3 [40000/60000 (67%)]
                                Loss: 0.119639
                                                  Accuracy: 95.131%
Epoch: 3 [41600/60000 (69%)]
                                Loss: 0.089203
                                                  Accuracy:95.143%
Epoch: 3 [43200/60000 (72%)]
                                Loss: 0.412446
                                                  Accuracy:95.152%
Epoch: 3 [44800/60000 (75%)]
                                Loss: 0.103714
                                                  Accuracy:95.211%
Epoch: 3 [46400/60000 (77%)]
                                Loss: 0.355738
                                                  Accuracy:95.202%
Epoch: 3 [48000/60000 (80%)]
                                Loss: 0.139295
                                                  Accuracy:95.191%
Epoch: 3 [49600/60000 (83%)]
                                Loss: 0.194295
                                                  Accuracy: 95.189%
Epoch: 3 [51200/60000 (85%)]
                                Loss: 0.083338
                                                  Accuracy: 95.181%
Epoch: 3 [52800/60000 (88%)]
                                Loss: 0.779976
                                                  Accuracy: 95.192%
Epoch: 3 [54400/60000 (91%)]
                                Loss: 0.033422
                                                  Accuracy:95.196%
Epoch: 3 [56000/60000 (93%)]
                                Loss: 0.117889
                                                  Accuracy:95.208%
Epoch: 3 [57600/60000 (96%)]
                                Loss: 0.146757
                                                  Accuracy:95.232%
Epoch: 3 [59200/60000 (99%)]
                                Loss: 0.007108
                                                  Accuracy:95.286%
Epoch: 4 [0/60000 (0%)]
                                Loss: 0.037586
                                                  Accuracy:96.875%
Epoch: 4 [1600/60000 (3%)]
                                Loss: 0.532983
                                                  Accuracy:95.282%
Epoch: 4 [3200/60000 (5%)]
                                Loss: 0.141879
                                                  Accuracy: 95.575%
Epoch: 4 [4800/60000 (8%)]
                                Loss: 0.068667
                                                  Accuracy:95.882%
                                Loss: 0.088112
Epoch: 4 [6400/60000 (11%)]
                                                  Accuracy:95.740%
Epoch: 4 [8000/60000 (13%)]
                                Loss: 0.112370
                                                  Accuracy:95.754%
Epoch: 4 [9600/60000 (16%)]
                                Loss: 0.098440
                                                  Accuracy:95.650%
```

```
Epoch: 4 [11200/60000 (19%)]
                                Loss: 0.284854
                                                 Accuracy:95.593%
Epoch: 4 [12800/60000 (21%)]
                                Loss: 0.082128
                                                 Accuracy:95.605%
Epoch: 4 [14400/60000 (24%)]
                                Loss: 0.066085
                                                 Accuracy:95.468%
Epoch: 4 [16000/60000 (27%)]
                                Loss: 0.137398
                                                 Accuracy:95.422%
Epoch: 4 [17600/60000 (29%)]
                                                 Accuracy:95.389%
                                Loss: 0.083179
Epoch: 4 [19200/60000 (32%)]
                                Loss: 0.296649
                                                 Accuracy:95.372%
Epoch: 4 [20800/60000 (35%)]
                                Loss: 0.079538
                                                 Accuracy: 95.387%
Epoch: 4 [22400/60000 (37%)]
                                Loss: 0.021219
                                                 Accuracy:95.399%
Epoch: 4 [24000/60000 (40%)]
                                Loss: 0.045635
                                                 Accuracy:95.460%
Epoch: 4 [25600/60000 (43%)]
                                Loss: 0.025185
                                                 Accuracy:95.431%
Epoch: 4 [27200/60000 (45%)]
                                Loss: 0.313549
                                                 Accuracy:95.384%
Epoch: 4 [28800/60000 (48%)]
                                                 Accuracy:95.384%
                                Loss: 0.358900
Epoch: 4 [30400/60000 (51%)]
                                Loss: 0.290802
                                                 Accuracy:95.354%
Epoch: 4 [32000/60000 (53%)]
                                Loss: 0.031017
                                                 Accuracy:95.367%
Epoch: 4 [33600/60000 (56%)]
                                Loss: 0.085758
                                                 Accuracy:95.362%
Epoch: 4 [35200/60000 (59%)]
                                Loss: 0.152539
                                                 Accuracy:95.416%
Epoch: 4 [36800/60000 (61%)]
                                Loss: 0.162986
                                                 Accuracy:95.441%
Epoch: 4 [38400/60000 (64%)]
                                Loss: 0.174990
                                                 Accuracy:95.444%
Epoch: 4 [40000/60000 (67%)]
                                Loss: 0.521610
                                                 Accuracy: 95.456%
Epoch: 4 [41600/60000 (69%)]
                                Loss: 0.122210
                                                 Accuracy:95.484%
Epoch: 4 [43200/60000 (72%)]
                                Loss: 0.318961
                                                 Accuracy: 95.503%
Epoch: 4 [44800/60000 (75%)]
                                                 Accuracy:95.550%
                                Loss: 0.035795
Epoch: 4 [46400/60000 (77%)]
                                Loss: 0.384703
                                                 Accuracy:95.535%
Epoch: 4 [48000/60000 (80%)]
                                Loss: 0.491851
                                                 Accuracy:95.561%
Epoch: 4 [49600/60000 (83%)]
                                Loss: 0.055732
                                                 Accuracy:95.561%
Epoch: 4 [51200/60000 (85%)]
                                Loss: 0.087599
                                                 Accuracy:95.583%
Epoch: 4 [52800/60000 (88%)]
                                Loss: 0.285666
                                                 Accuracy:95.597%
Epoch: 4 [54400/60000 (91%)]
                                Loss: 0.043655
                                                 Accuracy:95.602%
Epoch: 4 [56000/60000 (93%)]
                                Loss: 0.363469
                                                 Accuracy: 95.604%
Epoch: 4 [57600/60000 (96%)]
                                Loss: 0.103343
                                                 Accuracy:95.624%
Epoch: 4 [59200/60000 (99%)]
                                Loss: 0.018067
                                                 Accuracy:95.676%
```

0.3 SVM Classifer for MNIST DATA SET

```
[0]: from keras.datasets import mnist
   (x_train, y_train), (x_test, y_test) = mnist.load_data()

[0]: x_train = x_train.reshape(60000,784)
   x_test = x_test.reshape(10000,784)

[0]: ## Applying HOG feature extraction

[0]: from sklearn.svm import SVC
   from sklearn.metrics import accuracy_score
   from skimage.feature import hog
   from sklearn import preprocessing
```

```
from collections import Counter
[38]: list hog train = []
      for feature in x train:
          fd = hog(feature.reshape((28,28)), orientations=10,__
       →pixels_per_cell=(7,7),cells_per_block=(1,1),visualize=False )
          list_hog_train.append(fd)
      hog_features = np.array(list_hog_train, 'float64')
      preProcess = preprocessing.MaxAbsScaler().fit(hog_features)
      hog_features_transformed_train = preProcess.transform(hog_features)
      print(hog_features_transformed_train.shape)
     (60000, 160)
 [0]: ## Extracting hog feature for test data
[41]: | list_hog_test = []
      for feature in x_test:
          fd = hog(feature.reshape((28,28)), orientations=10,__
       →pixels_per_cell=(7,7),cells_per_block=(1,1),visualize=False )
          list_hog_test.append(fd)
      hog_features_test = np.array(list_hog_test, 'float64')
      preProcess = preprocessing.MaxAbsScaler().fit(hog_features_test)
      hog_features_transformed_test = preProcess.transform(hog_features_test)
      print(hog_features_transformed_test.shape)
     (10000, 160)
 [0]: model = SVC()
      model.fit(hog_features_transformed_train,y_train)
      y_pred = model.predict(hog_features_transformed_test)
     Fitting the model with best parameters
[43]: print(accuracy_score(y_test, y_pred))
```

0.9713