

Complexity Analysis

why we need to understand complexity analysis?

→ It helps to measure performance of the algorithms.

→ It's very imp for interviews.



→ photo editor
app

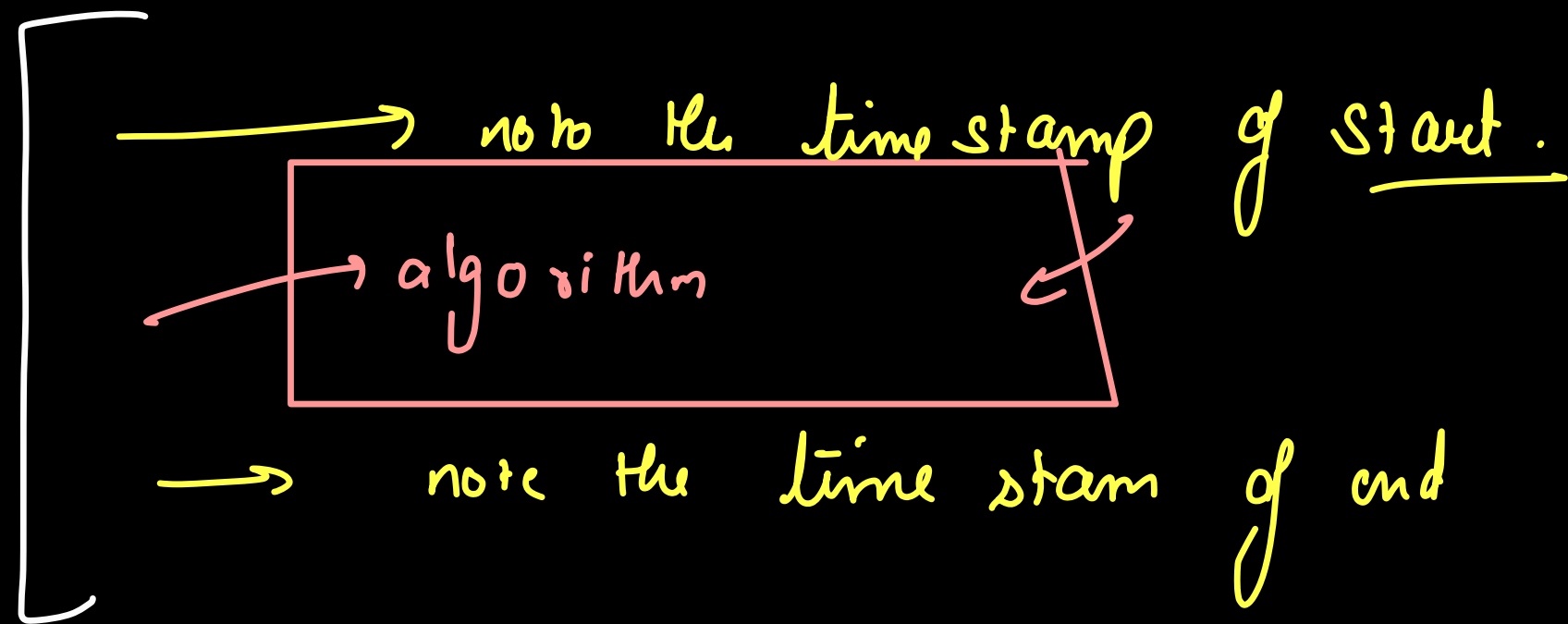
Lightroom

→ we should get the desired output as early as possible.

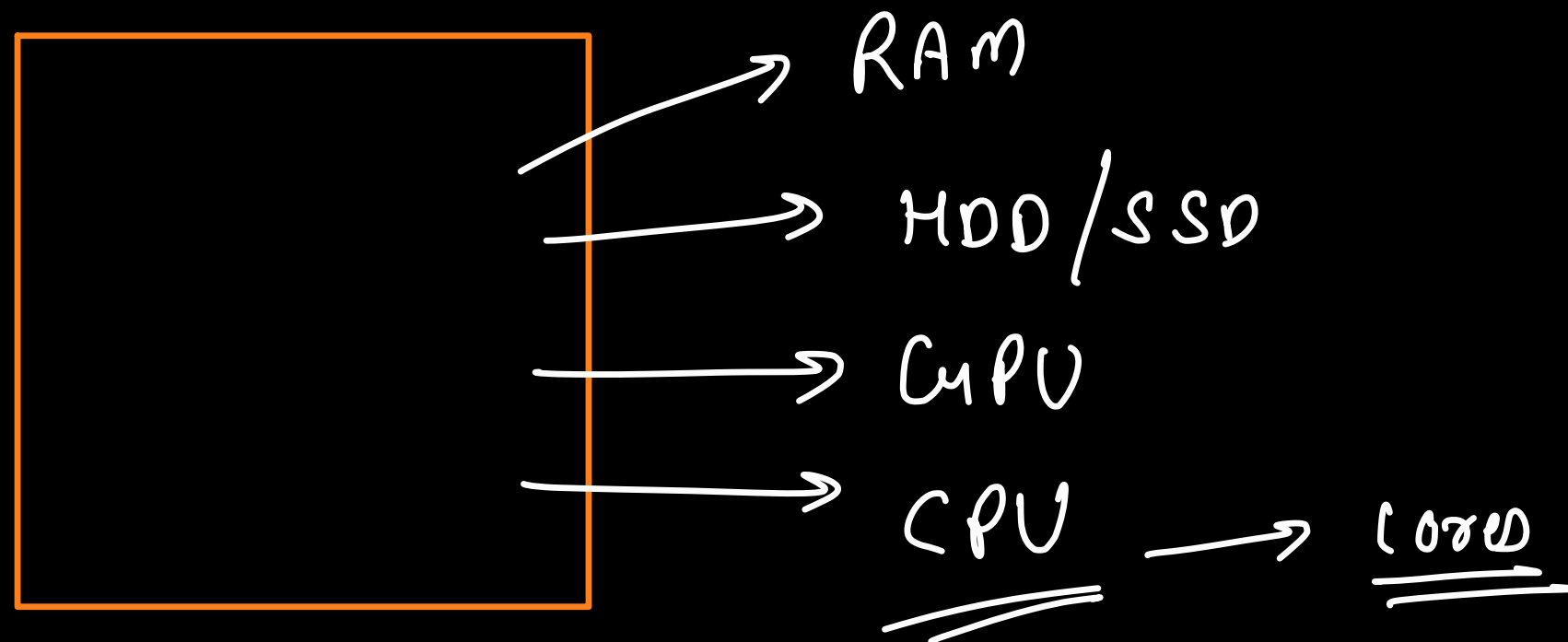
P₂

How to measure performance of an algo ??

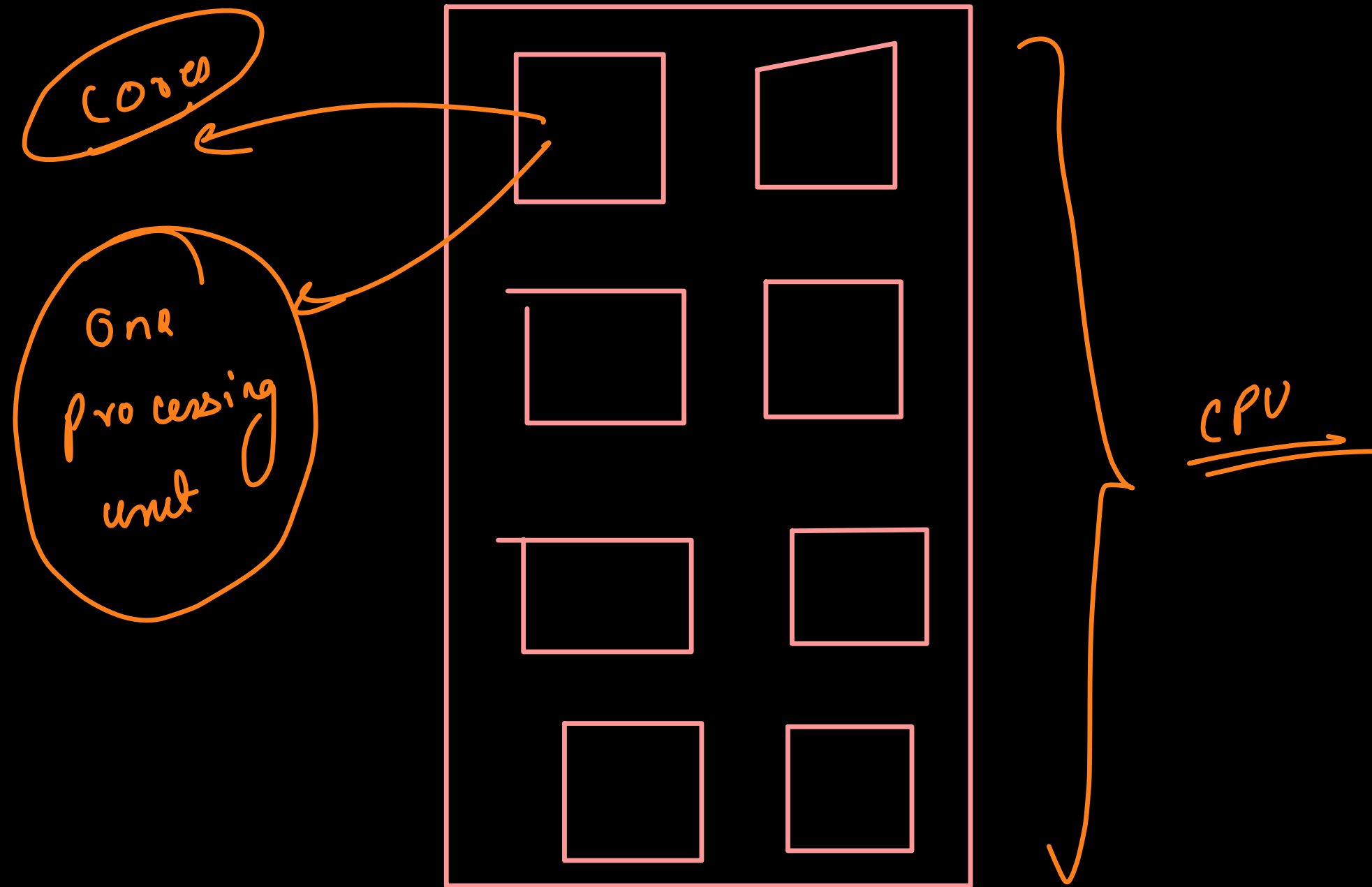
experimental analysis



this is not accurate. why??



dual core → 2
quad core → 4
octa core → 8



for simplicity let's consider a system with a single core.

1 core

In a single core, 2 or more processes cannot run at the same point of time.

then why we don't feed a lag??

Content Switching \rightarrow 1 sec $\rightarrow \approx 10^8$ instructions

≡

P₂ P₄ P₁ P₃

Waiting State

Process → Program under execution

Asymptotic Analysis

a line that
curve
approaches
at infinity

Asymptote

→ in asymptotic analysis, we try to
analyse algorithms for very large

input

→ why we are dealing with very large inputs??

→ bear as a general trend we can see that
for large input, algorithms take more instructions
to execute.

```
for (i=0 ; i<n ; i++)  
    console.log(i)
```

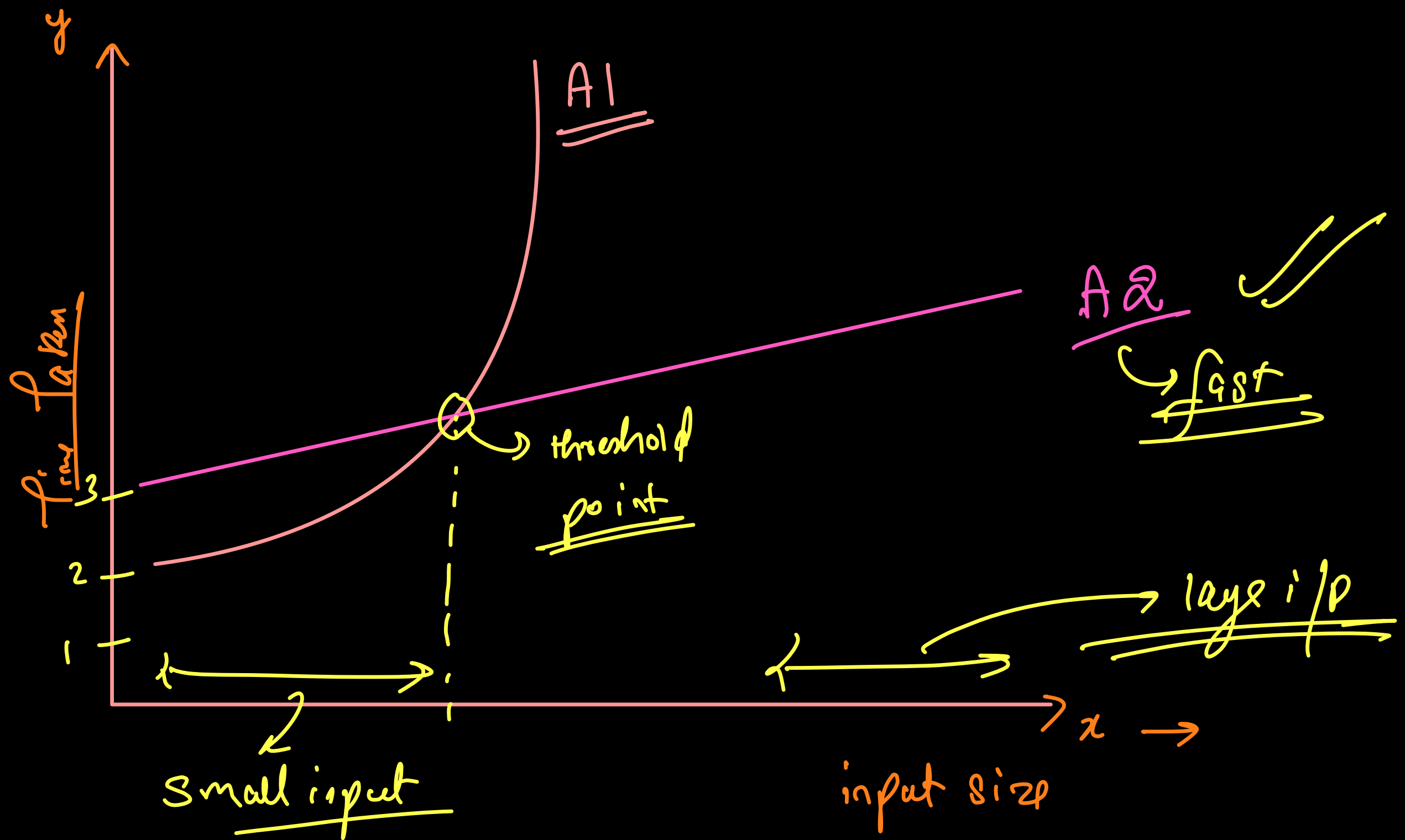
$n \rightarrow 10$

$n \rightarrow 10^6$

```
if (n % 2 == 0)  
    console.log("even")
```

$n \rightarrow 10$

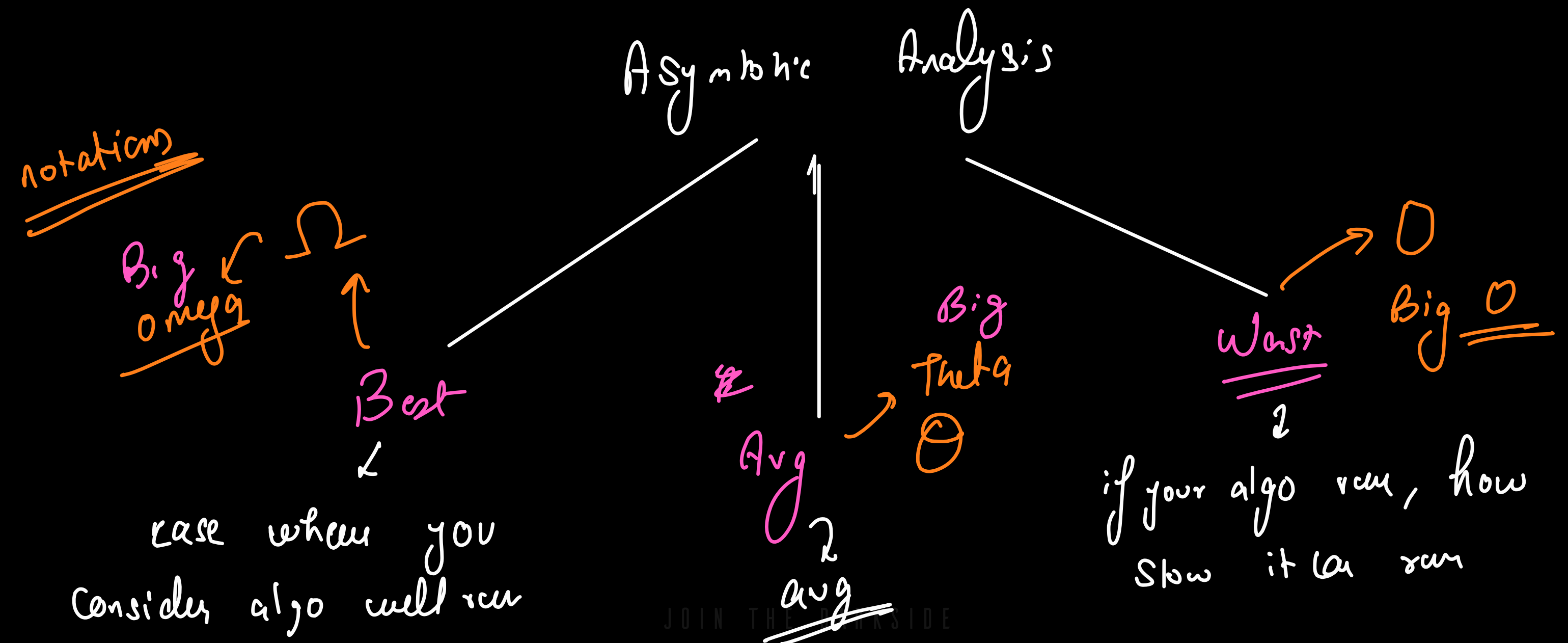
$n \rightarrow 10^9$



Before threshold pt. A1 is faster than A2
 But before threshold the input size is
 Small. & for small i/p size we do not

Case who is fast.

After threshold pt, input size increases. & then A1 is taking too much time. So after threshold A2 is bro.



as fast as possible

Ques Given an array of elements (integers). Apart from the array you've an element x , return the index at which x is present in the array. If not present return -1.

worst $x = 100, 200, 101 \dots$

$x = 6$

ans \rightarrow 5

$x = 4$
 \downarrow
Best Case

4	1	3	0	-2	6	8	9
0	1	2	3	4	5	6	7

$i \uparrow$

now about, we one by one go to every index & check if x is present.

Time Complexity

Worst

you will go to every index & still not find any any

```
n = arr.length → 1
for (i = 0; i < n; i++) {
    if (arr[i] == x) {
        return i;
    }
}
return -1;
```

(linear search)

length of arr → 1 + 1 + 3n + 1
i = 0 → for loop → return

n → large value
n → 10⁹

$$\underbrace{1+1}_{\text{const}} + \underbrace{3 \times 10^7}_{\text{const}} + \underbrace{1}_{\text{const}} \approx \underline{\underline{10^8}}$$

→ avoid constant terms

$$\rightarrow \underline{\underline{3 \times 10^7}} \approx \underline{\underline{10^8}}$$

~~Worst Case~~ → $O(n)$ → Big O of n

Best Case → $\Omega(\text{constant})$ → $\Omega(1)$

← 6 instructions

→ for linear search
is independent of
input

→ Constant time and
are taken for every n.

Avg \rightarrow $\Theta(n)$

Fastest

$\log(\log(n))$

$\log(n)$
 \sqrt{n}

n

$n \log n$

$n \sqrt{n}$

n^2

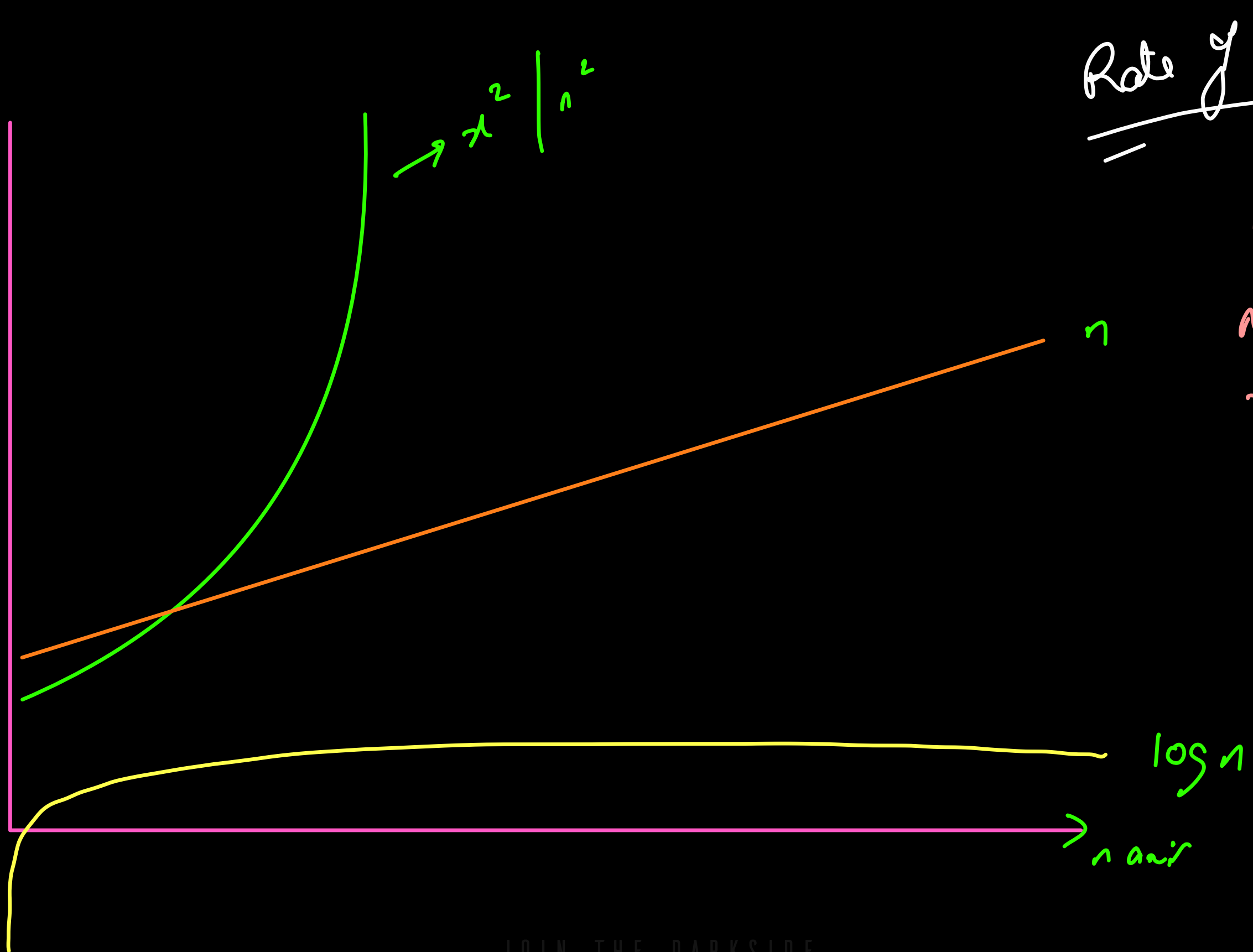
n^3

\vdots

$n!$

$2^n, 3^n, \dots$

Slowest



Rate of growth
↓
is also we
need slow
rate of growth.

Worst
Case

```
for (i=0 ; i<n ; i++) {  
    for (j=0 ; j<n ; j++) {  
        console.log(i,j);  
    }  
}
```

HW
↓
DSA classes

$O(n^2)$

$i=0$	→	$3n$
$i=1$	→	$3n$
$i=2$	→	$3n$
⋮		
$i=n-1$	→	$3n$

$3n + 3n + 3n + \dots + 3n$
 $3(n + n + n + \dots + n)$
↪ n times

$3n^2$ → $\approx \frac{n^2}{1}$


```
for ( i = 1 ; i <= n ; i *= 2 )
    console.log ( i )
```

$i = 1 \rightarrow$ first iteration

$i = 2 \rightarrow$ 2nd "

$i = 4 \rightarrow$ 3rd "

$i = 8 \rightarrow$ 4th "

$i = 2^{(k-1)} \rightarrow$ kth iteration

$$1 \rightarrow 2 \rightarrow 4 \rightarrow 8 \rightarrow 16 \dots$$

$$\hookrightarrow 2^{k-1} < n$$

\log_2 on both sides

$$\log_2(2^{k-1}) < \log_2 n$$

$$(k-1) \log_2 2 < \log_2 n$$

$$(k-1) < \log_2 n$$

$$\textcircled{K} < \frac{\log_2 n + 1}{}$$

the highest value of K

$$3K \rightarrow 3(\log_2 n + 1)$$

$$3 \log_2 n \rightarrow \log_2 n \rightarrow \underline{\underline{O(\log n)}}$$