

$k=3$

n points

(x_1, y_1)

(x_2, y_2)

y

x

$(0,0)$

origin

(x_3, y_3)

$O(n \log n + k \log k)$

$$\sqrt{1^2 + 3^2} \rightarrow \sqrt{10}$$

$$\sqrt{(-2)^2 + 2^2} = \sqrt{8}$$

$[(1, 3) \quad \underline{(-2, 2)}]$

$[\sqrt{10}, \sqrt{8}]$

$(k\text{-smallest})$



→ (manhattan distance)

→ (euclidean dist)

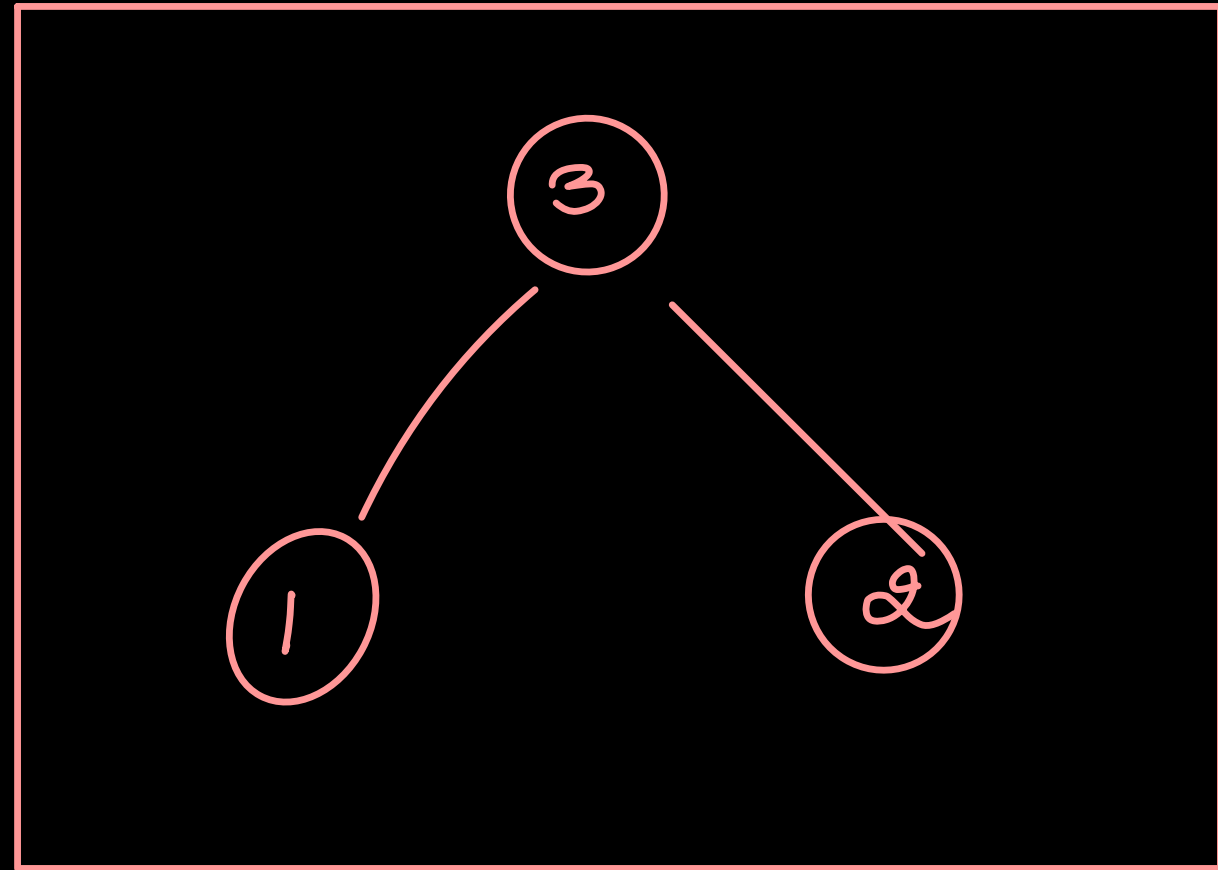
$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\hookrightarrow \sqrt{(x_2 - 0)^2 + (y_2 - 0)^2} \Rightarrow \sqrt{x_2^2 + y_2^2} //$$

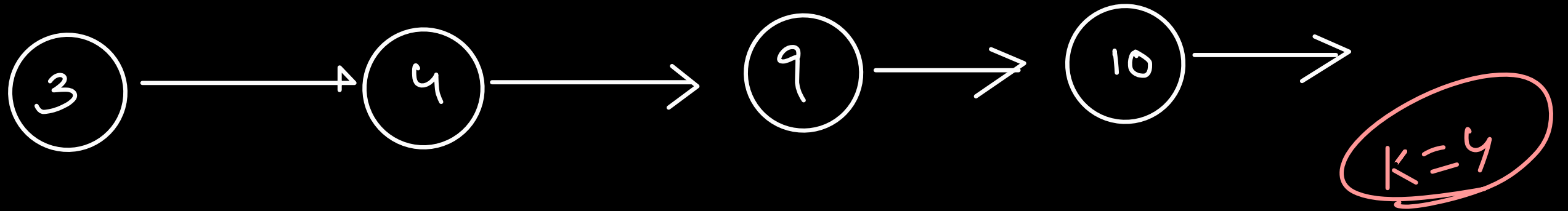
$[3, 2, 6, 1, 9, 4]$

$k=3$

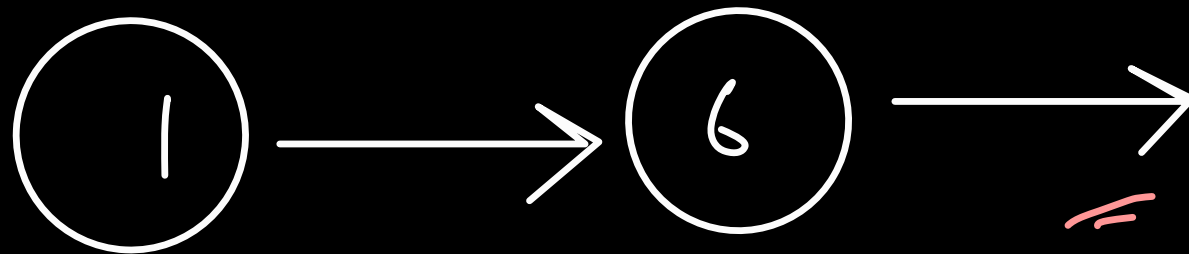
max heap $\Rightarrow 3$



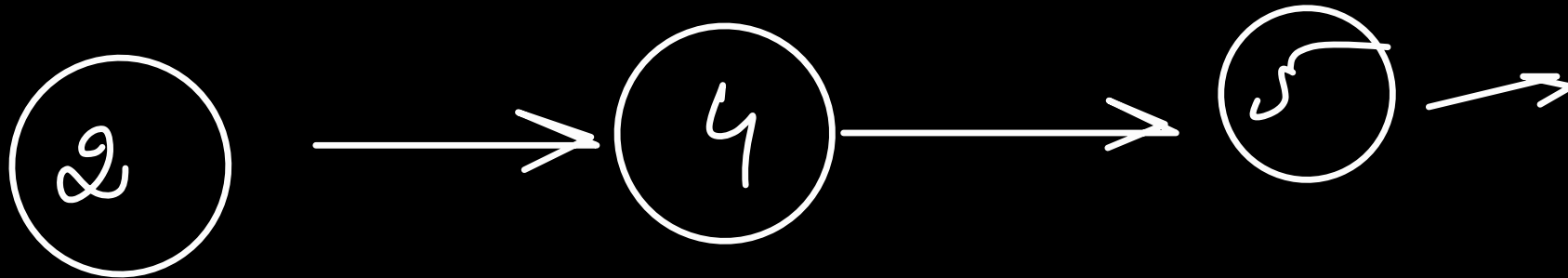
Q0



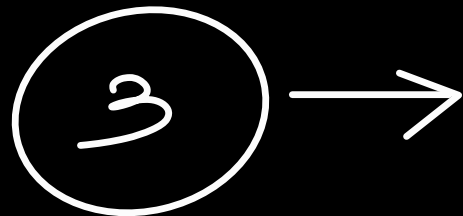
Q1



Q2



Q3



Heap of size k



Combined list

$$nk(\log(nk) + \cancel{nk})$$

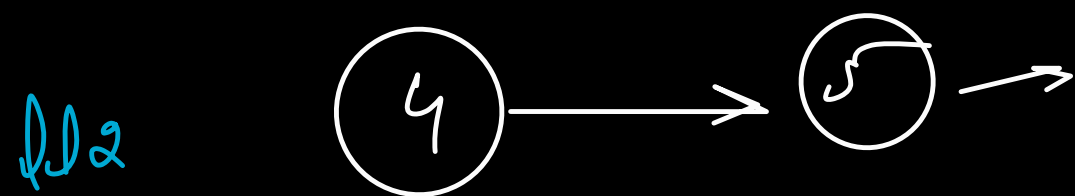
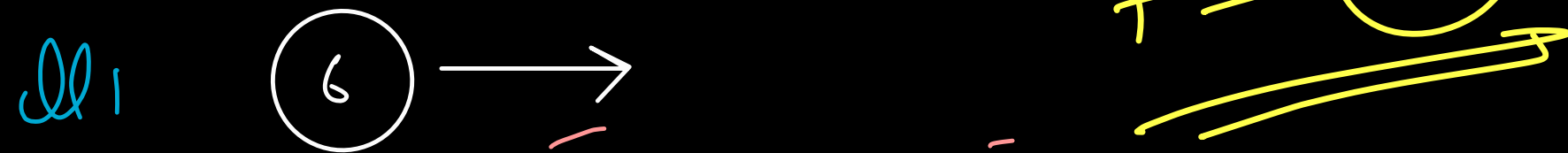
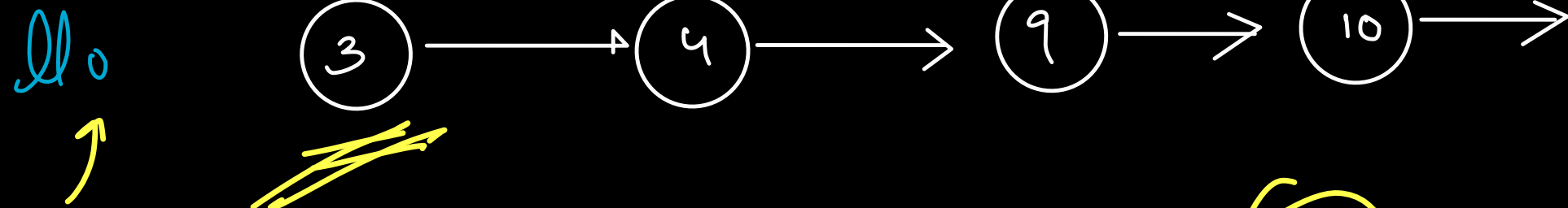
merge sort

total nodes $\Rightarrow nk$

$$O((nk) \log(nk))$$

Space $\rightarrow \underline{O(nk)}$

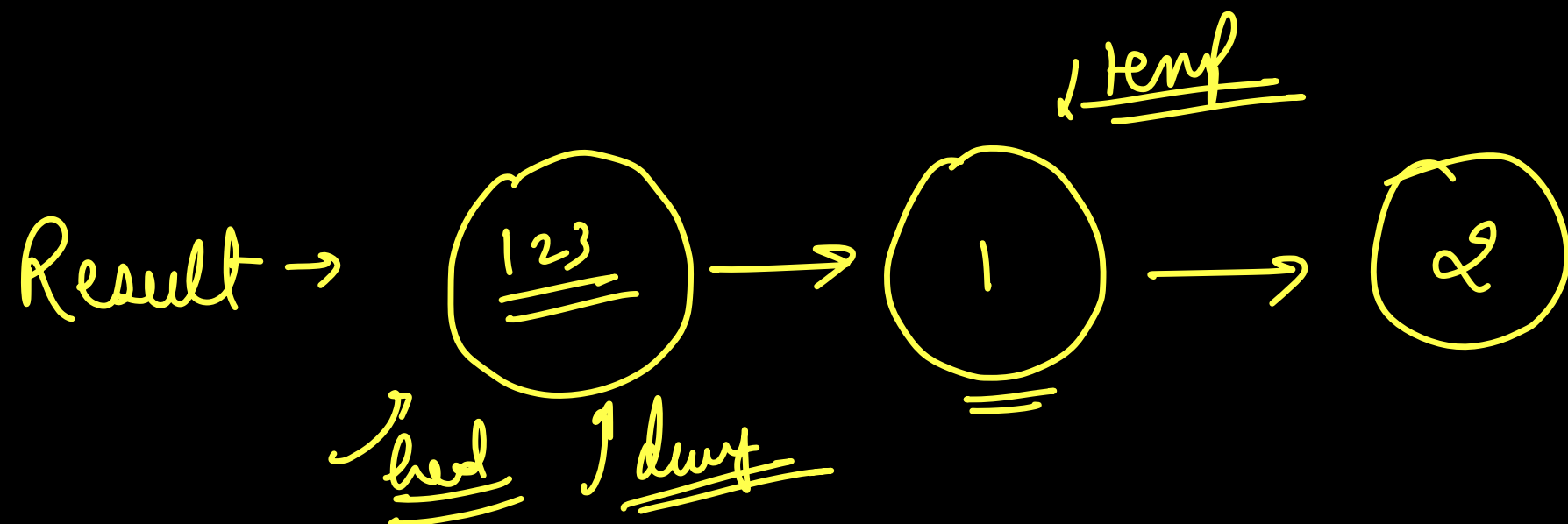
Can we improve



7 = 3

(2, 2)

<u>K</u>
(3, 0)
(6, 1)
(3, 3)



$O(nk \log k)$

[1, 2, 3, 5]

→ $O(n^2)$

$$\log(n^2) \approx \frac{1}{2} \log n$$

$\frac{1}{5}$ $\frac{1}{3}$ $\frac{1}{2}$ 1

$\frac{2}{5}$ $\frac{2}{3}$ 1

$\frac{3}{5}$

1

$n^2 \log n + (k-1) \log n$

$[\overset{0}{1}, \overset{1}{2}, \overset{2}{3}, \overset{3}{5}]$

$\rightarrow 1/5 \quad 2/5 \quad 3/5 \quad 5/5 \rightarrow \text{sorted}$

$\rightarrow 1/3 \quad 2/3 \quad 3/3 \rightarrow \text{sorted}$

$\rightarrow 1/2 \quad 2/2 \rightarrow \text{sorted}$

$\rightarrow 1/1$

$(0, 2, 1/3)$

$K=0$

min heap

$(1, 3, 2/5) \quad (0, 1, 1/2)$
 $(1, 2, 2/3) \quad (0, 0, 1)$

$2/5 \rightarrow 0.4$

$1/2 \rightarrow 0.5$

$1/3 \rightarrow 0.3$

$1 \rightarrow 1$

$$(n \log n + (k-1) \log n)$$

$$O((n+k) \log n)$$

