

AVL Trees (Not imp for interviews)

↓
Georgy Adelson-Velsky & Landis

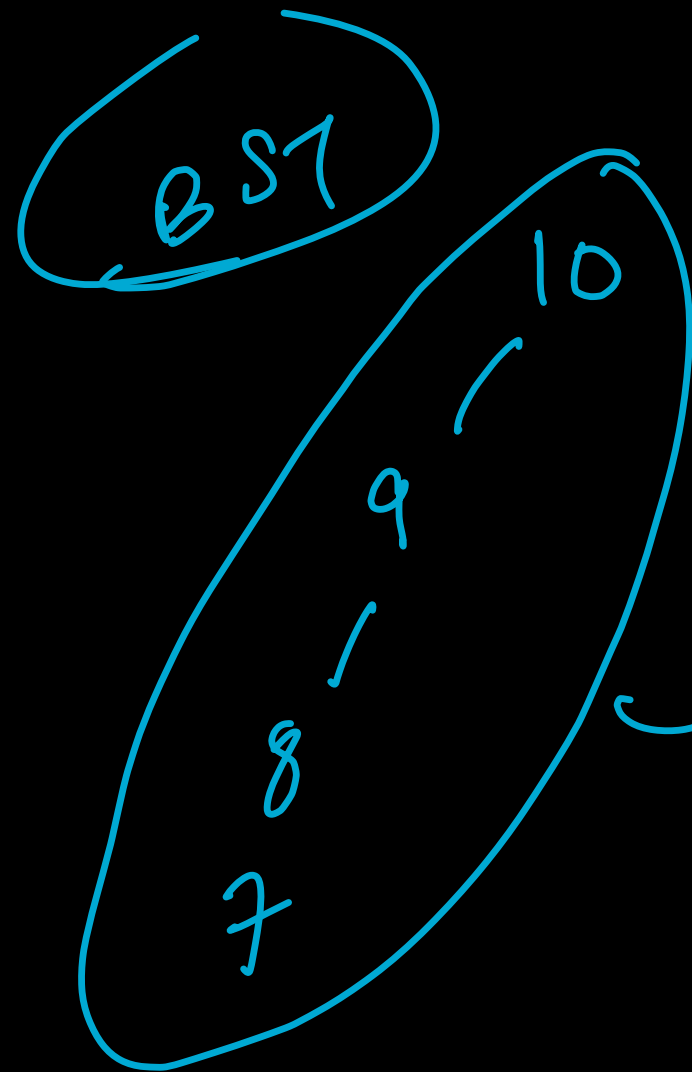
AVL trees are self balancing BST

Balanced B-T → for every subtree of the given
binary tree the balancing factor should be either 0, 1,

-1.
height → $O(\log n)$ always

Balance factor $\rightarrow |h_{\text{leftsubtree}} - h_{\text{rightsubtree}}| \leq 1$

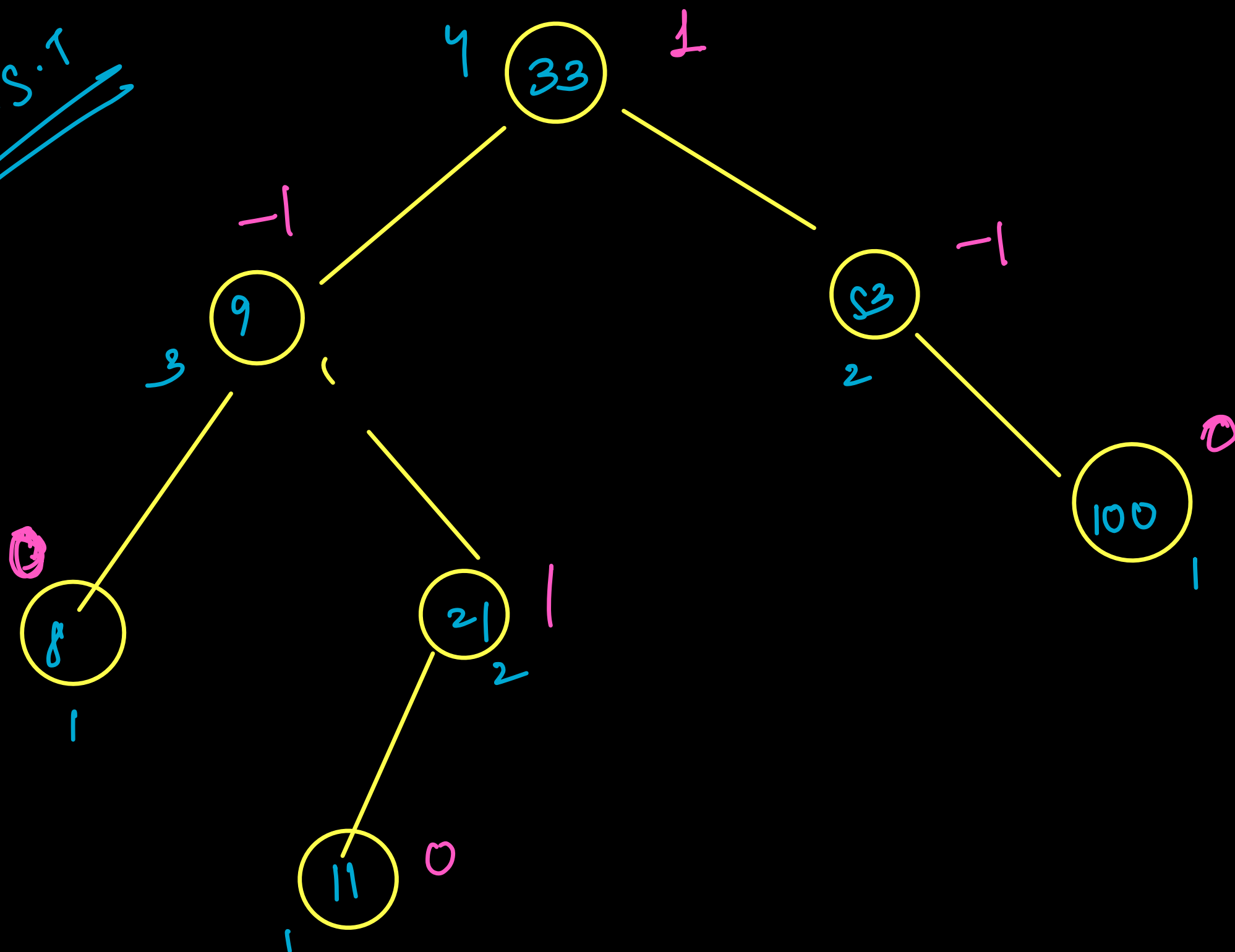
\rightarrow insert
(10)
(9)
(8)
(7)



~~X~~ not balanced
X

skewed tree

Balanced B.S.T



Imp operations on AVL Trees

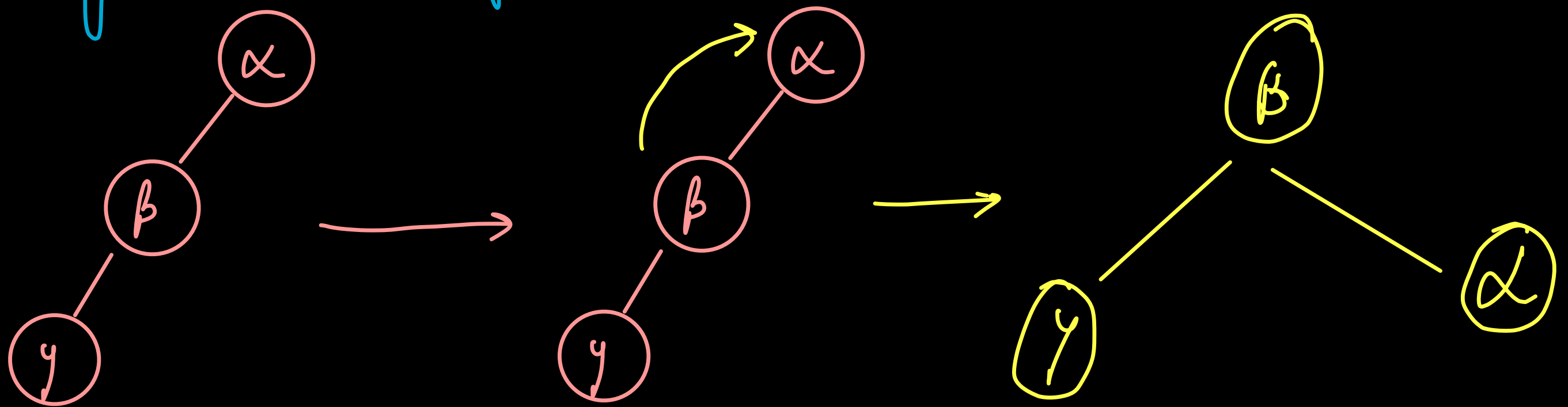
- ① Right Rotation
- ② Left Rotation
- ③ Right Left Rotation
- ④ Left Right Rotation

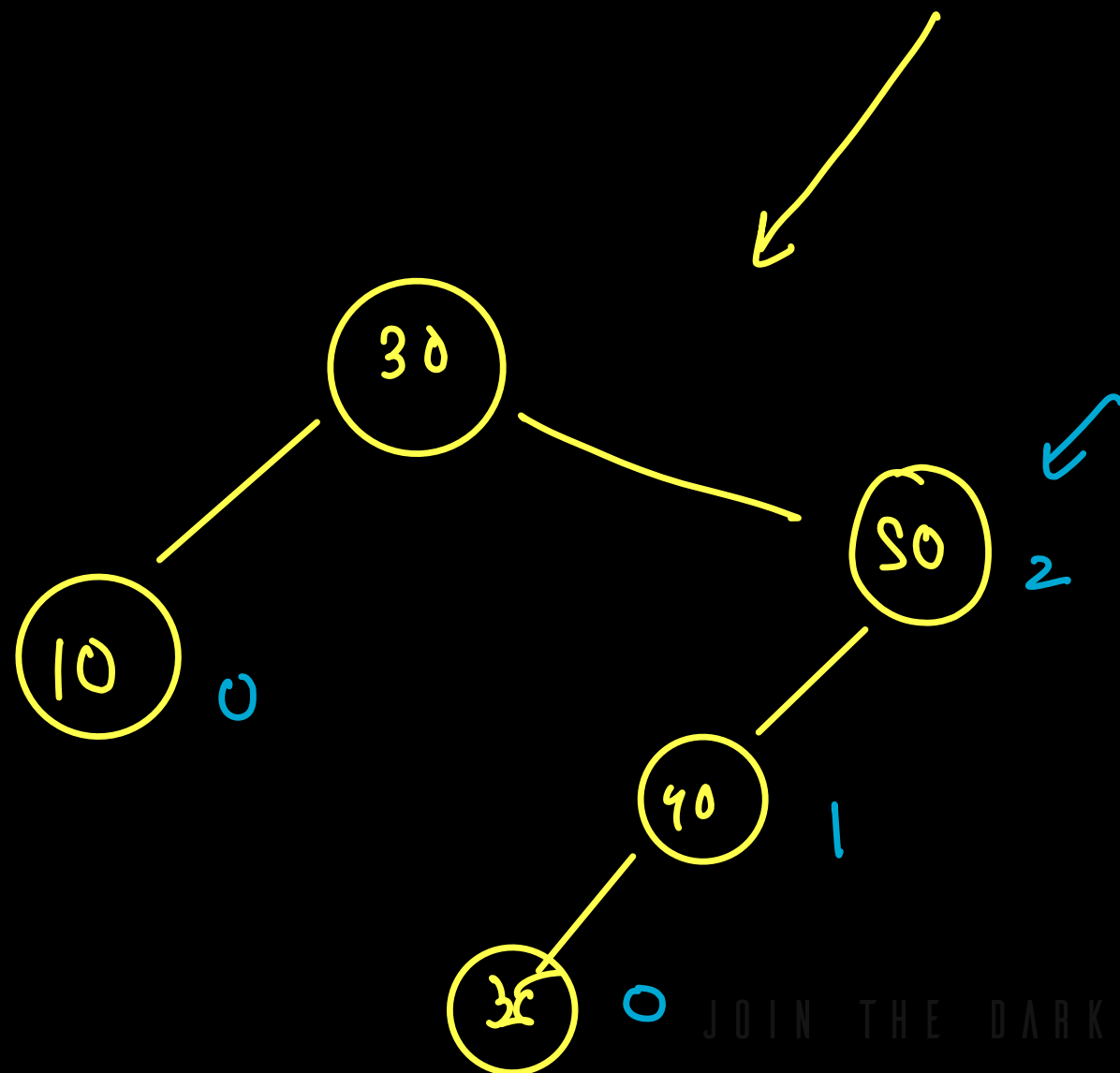
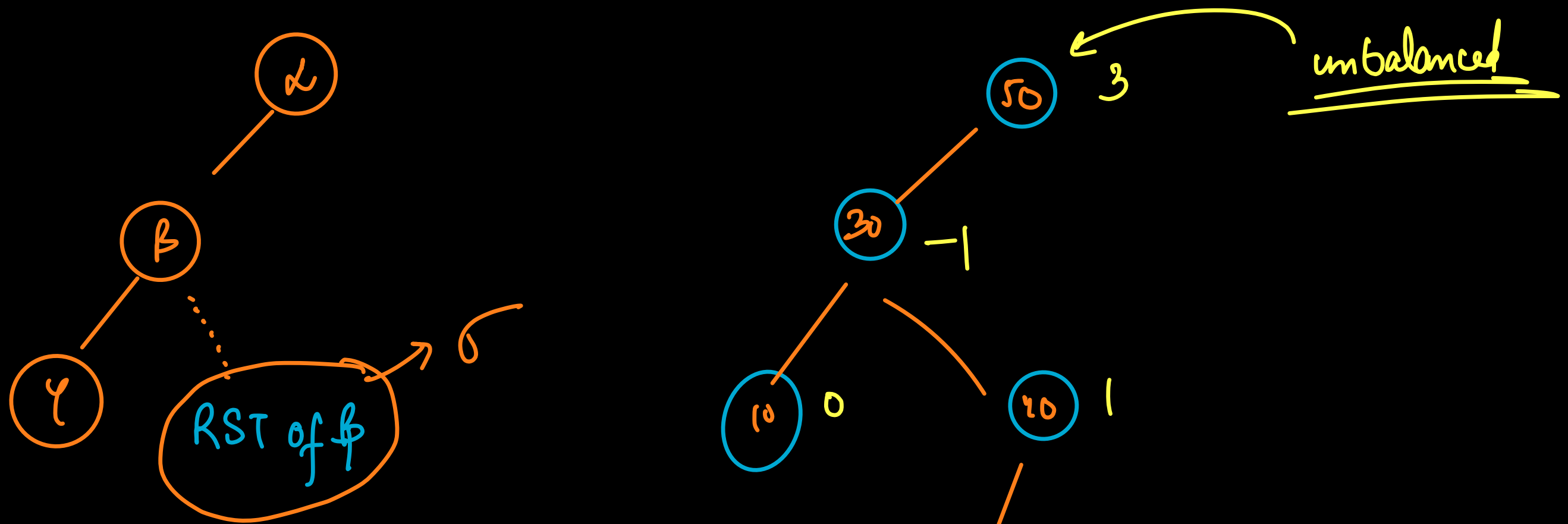
these will be applicable
if and only if we know
it is unbalanced

for checker balancing of any node
we need height.

df

Right Rotation \rightarrow if an element is added to the left side of my left subtree, then the tree becomes heavy on the left side.





right rotate (alpha) ↺

→ beta = alpha.left

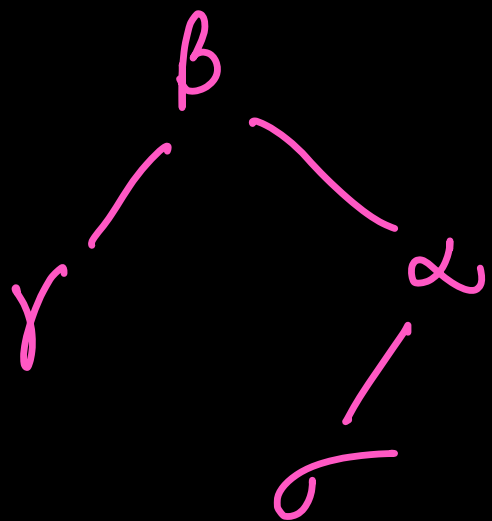
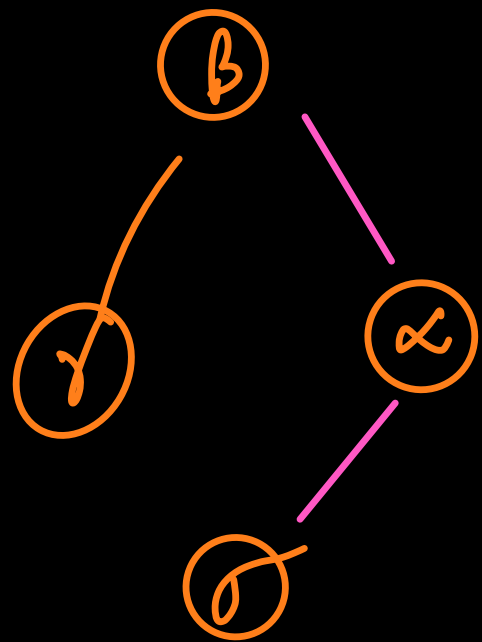
sigma = beta.right

beta.right = alpha

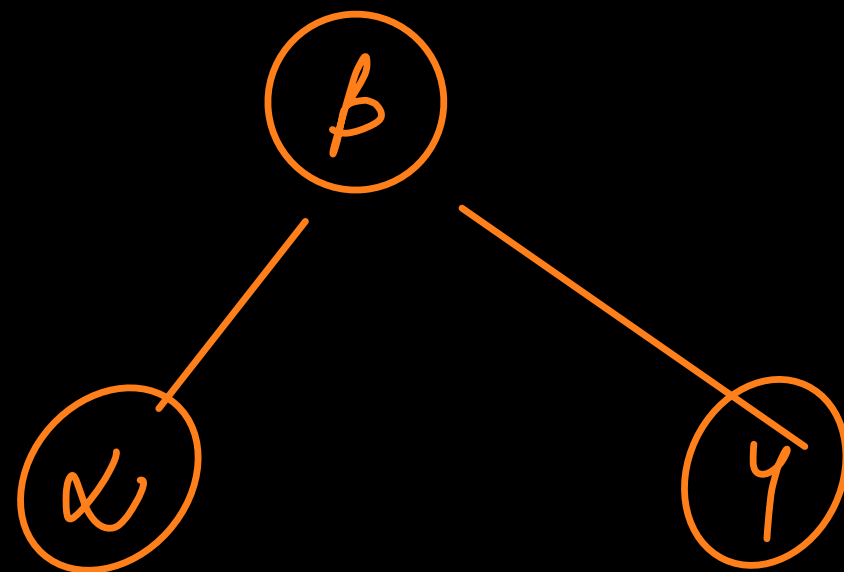
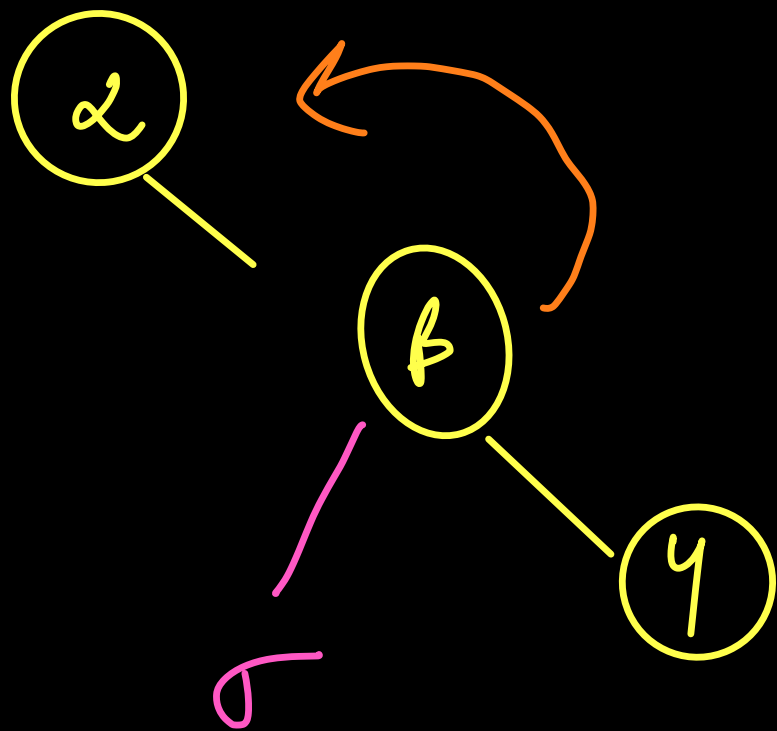
alpha.left = sigma

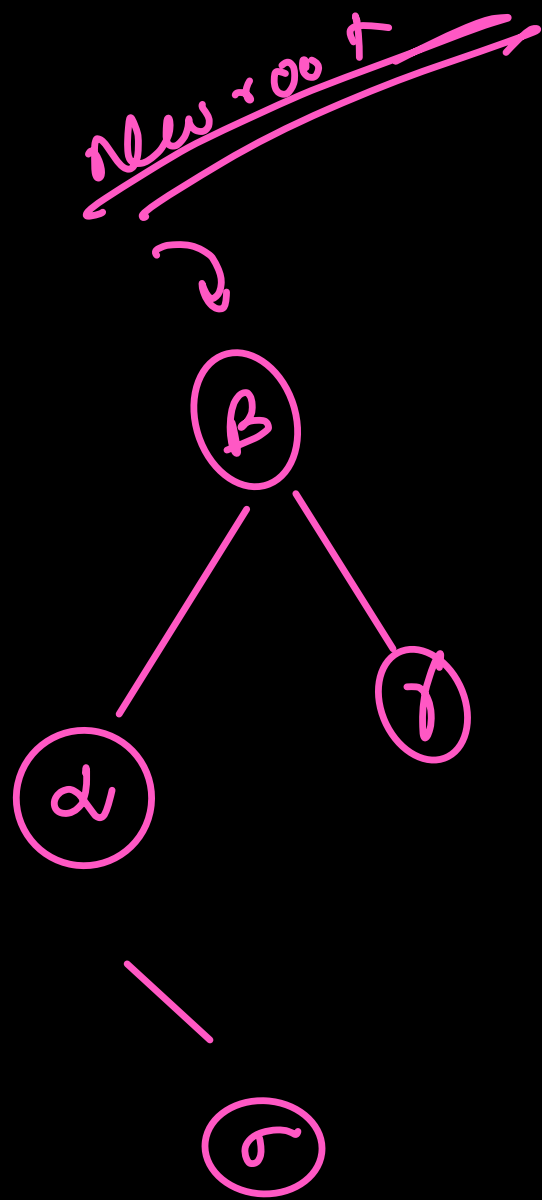
// more ops

return beta;



Left Rotation \rightarrow if node is added to right side of my
BST, we have a right-heavy tree





left Rotate (alpha) {

beta = alpha.right;

Sigma = beta.left;

beta.left = alpha

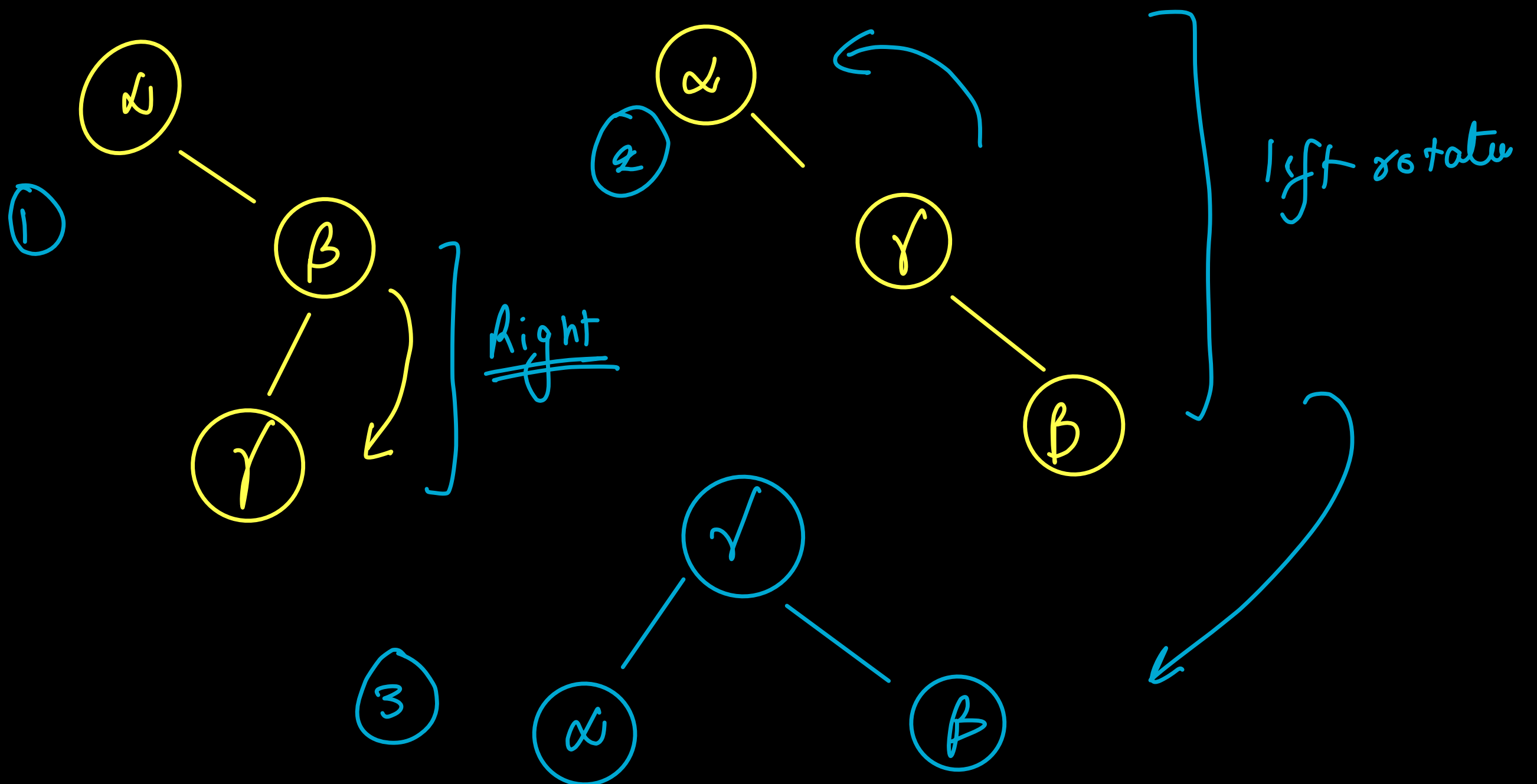
alpha.right = Sigma

// more ops

return beta;

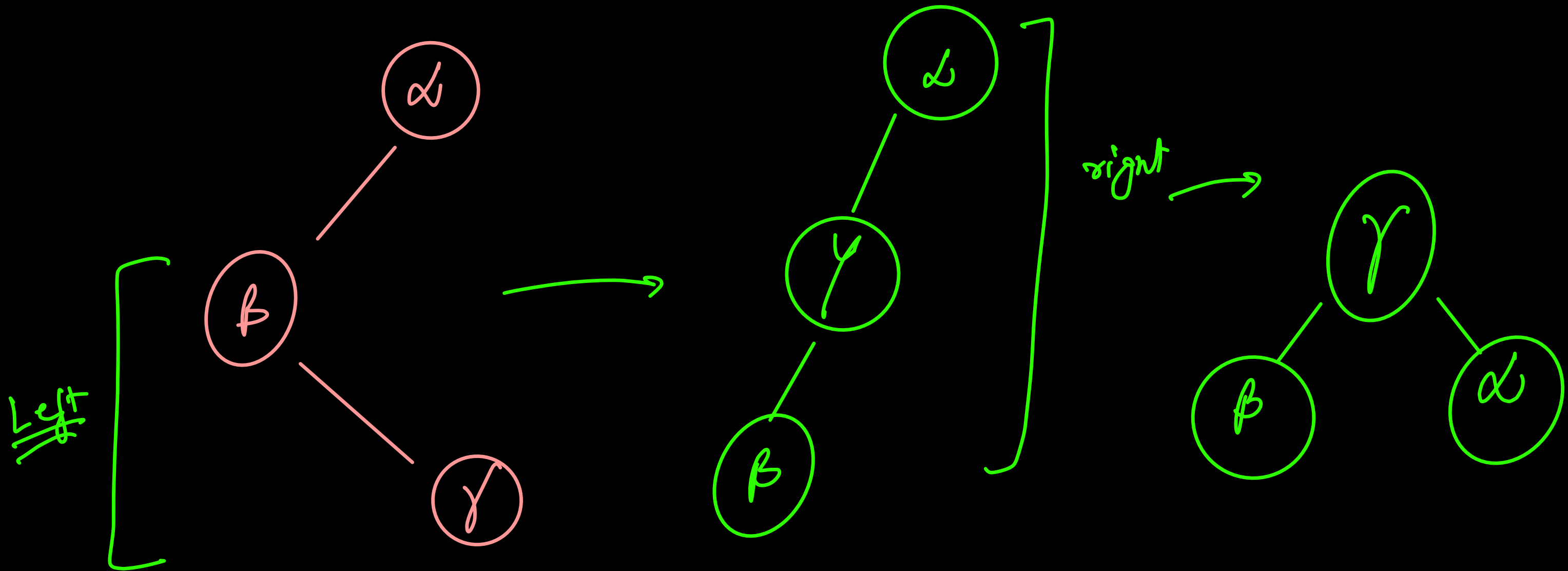
}

Right-Left Rotation \rightarrow Right heavy here but with diff
orientation



$$\left(\begin{array}{l} \alpha.\text{right} = \text{rightRotate}(\alpha.\text{right}) \\ \text{return leftRotate}(\alpha) \end{array} \right)$$

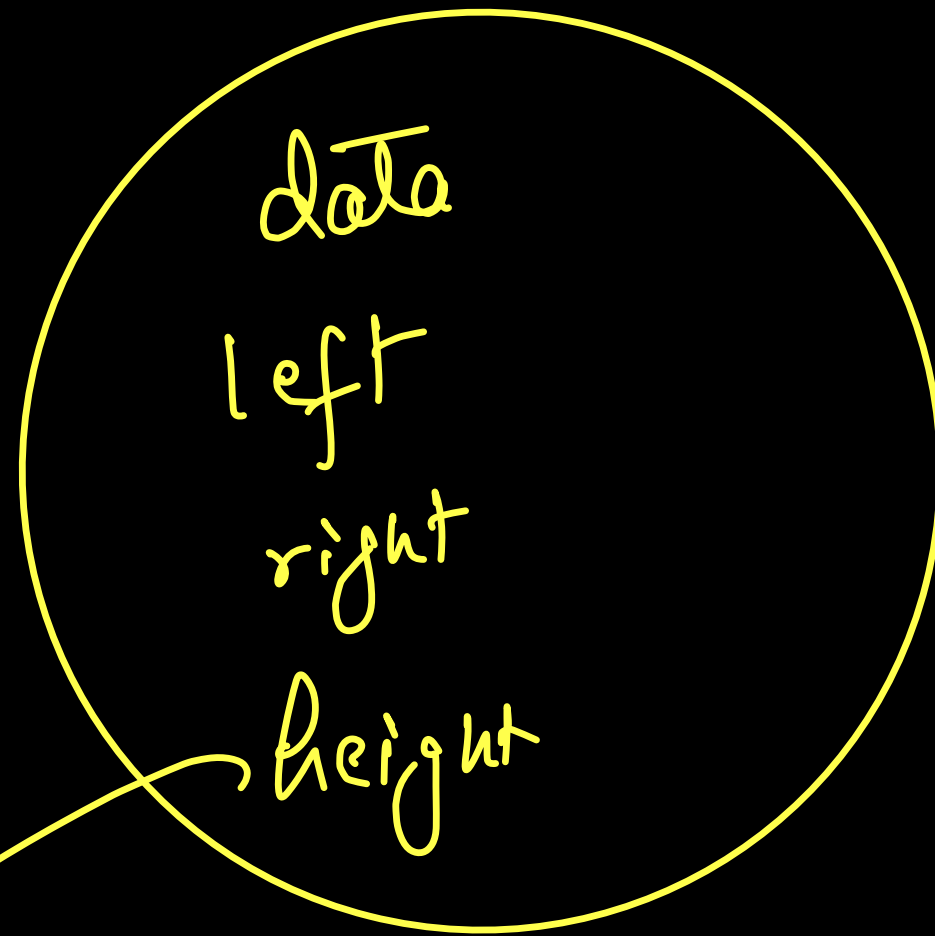
→ Left-Right Rotation



$\alpha.\text{left} = \text{leftrotate}(\alpha.\text{left})$

return $\text{rightrotate}(\alpha)$

Node



height of tree rooted
here