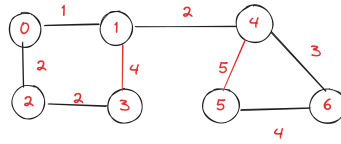


Minimum Spanning Trees

Kruskals (sparse)

Prims (dense)



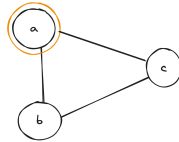
[[0, 1, 1], [0, 2, 2], [2, 3, 2], [1, 3, 4], [1, 4, 2] ...]

Kruskals

Kruskals is done using the edge list representation of graph.

kruskals internally use DSU.

A tree is a graph without cycles. So to convert a graph into a tree, we need cycle detection. DSU can help u find cycles very easily

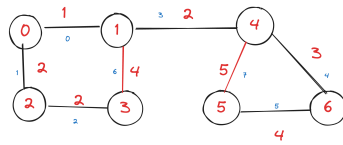


union(a, b)
union (b, c) ✓
union(a, c)

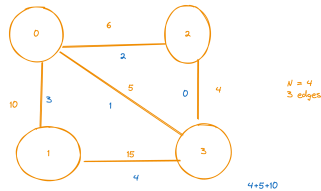
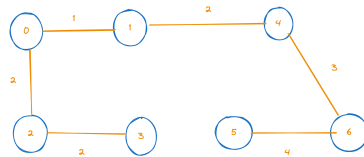
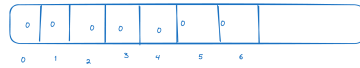
DSU can be used to do cycle detection, because DSU can check if two elements are in same group or not, if yes and we add a direct edge between then its a cycle.

Sort the edge list based on weight (inc order)

- one by one keep picking the edges from smaller weight to larger weight
- while picking an edge check if it creates cycle or not using DSU
- And then if it doesn't creates a cycle add that edge to the ans.



Trees which are connected graphs always have $N-1$ edges

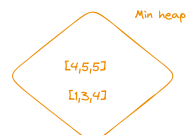
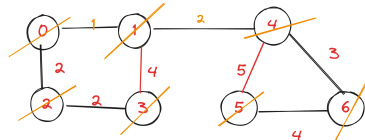


$N = 4$
3 edges

$4+5+10$

Prims

BFS + PQ



Min heap

[0, 1, 1]

[0, 2, 2]

[2, 3, 2]

[1, 4, 2]

[4, 6, 3]

[6, 5, 4]