

Expected no. of empty boxes:

for $i = 1, 2, 3, \dots, 50$

now let a random variable X_i such that

*

$$X_i = \begin{cases} 1 & \text{if box } i \text{ contains no balls.} \\ 0 & \text{otherwise} \end{cases}$$

let $X = X_1 + X_2 + X_3 + \dots + X_{50}$

Then X is the total no. of boxes which don't have balls

$$E(X) = E(X_1) + E(X_2) + \dots + E(X_{50})$$

now we can find $E(X_i)$ for any i

$X_i = 1$, if 100 times on a row we choose one of the other boxes

Then $P(X_i = 1) = \left(\frac{49}{50}\right)^{100}$

now $E(X) = 50 \left(\frac{49}{50}\right)^{100}$