



Let's see if you can use the tactics we've learnt to prove $x + 1 = y + 1 \implies x = y$. Try this one by yourself; if you need help then click on "Show more help!".

Level completed!



Here's a completely backwards proof:

```
intro h
apply succ_inj
repeat rw [succ_add_one]
exact h
```



Objects:

$y x : \mathbb{N}$

Assumptions:

$h : \text{succ } x = y + 1$

Goal:

$x = y$

`rw[<-succ_eq_add_one y]`
`at h`

✖ Retry

Active Goal

Objects:

$y x : \mathbb{N}$

Assumptions:

$h : \text{succ } x = \text{succ } y$

Goal:

$x = y$

`apply succ_inj at h`

✖ Retry

Active Goal

Objects:

$y x : \mathbb{N}$

Assumptions:

$h : x = y$

Goal:

$x = y$

`exact h`

✖ Retry

level completed! 🎉

succ_inj ✕

$(a \ b : \mathbb{N}) (h : \text{MyNat.succ } a = \text{MyNat.succ } b) : a = b$

Statement

If a and b are numbers, then `succ_inj a b` is the proof that $(\text{succ}(a) = \text{succ}(b)) \implies a = b$.

More technical details

There are other ways to think about `succ_inj`.

You can think about `succ_inj` itself as a function which takes two numbers a and b as input, and outputs a proof of $(\text{succ}(a) = \text{succ}(b)) \implies a = b$.