



Oh no! On the way to `add_comm`, a wild `succ_add` appears. `succ_add a b` is the proof that  $(\text{succ } a) + b = \text{succ } (a + b)$  for  $a$  and  $b$  numbers. This result is what's standing in the way of  $x + y = y + x$ . Again we have the problem that we are adding  $b$  to things, so we need to use induction to split into the cases where  $b = 0$  and  $b$  is a successor.

Note that `succ a + zb`

### Assumptions:

**nb** : `succ a + zb = succ (a + zb)`

### Goal:

`succ (succ a + zb) = succ (a + succ zb)`

`rw[nb]`

⌕ Retry

### Active Goal

### Objects:

**a zb** :  $\mathbb{N}$

### Assumptions:

**nb** : `succ a + zb = succ (a + zb)`

### Goal:

`succ (succ (a + zb)) = succ (a + succ zb)`

`rw[add_succ a zb]`

⌕ Retry

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`succ (succ (a + zb)) = succ (succ (a + zb))`

`rf1`

⌕ Retry

level completed! 🎉

## add\_succ



$(a \ d : \mathbb{N}) : a + \text{MyNat.succ } d = \text{MyNat.succ } (a + d)$

`add_succ a b` is the proof of  $a + \text{succ } b = \text{succ } (a + b)$ .