



is an axiom of Lean that recursion is a valid way to define functions from types such as the naturals.

Let's define a new function `pred` from the naturals to the naturals, which attempts to subtract 1 from the input. The definition is this:

```
pred 0 := 37
pred (succ n)
```



We cannot subtract one from 0, so we just return a junk value. As well as this

Objects:

**a b** :  $\mathbb{N}$

Assumptions:

**h** : `succ a = succ b`

Goal:

`pred (succ a) = b`

`rw[h]`

⌕ Retry

Active Goal

Objects:

**a b** :  $\mathbb{N}$

Assumptions:

**h** : `succ a = succ b`

Goal:

`pred (succ b) = b`

`rw[pred_succ b]`

⌕ Retry

Active Goal

Objects:

**a b** :  $\mathbb{N}$

Assumptions:

**h** : `succ a = succ b`

Goal:

`b = b`

`rf1`

⌕ Retry

level completed! 🎉

**pred\_succ** ✕

```
(n :  $\mathbb{N}$ ) :
MyNat.pred
(MyNat.succ n) =
n
```

`pred_succ n` is a proof of `pred (succ n) = n`.