



is_zero_succ
n, saying
that is_zero
0 = True and
is_zero
(succ n) =
False. Let's
use these
lemmas to
prove
succ_ne_zero,
Peano's Last
Axiom.
Actually, we
have been
using
zero_ne_succ
before, but
it's handy to
have this
opposite
version too,
which can be
proved in the
same way.
Note: you
can cheat
here by using
zero_ne_succ
but the point
of this world
is to show
you how to
prove results
like that.

Objects:

a : \mathbb{N}

Assumptions:

h : $\text{succ } a = 0$

Goal:

is_zero (succ a)

rw[h]

⌫ Retry

Active Goal

Objects:

a : \mathbb{N}

Assumptions:

h : $\text{succ } a = 0$

Goal:

is_zero 0

rw[is_zero_zero]

⌫ Retry

Active Goal

Objects:

a : \mathbb{N}

Assumptions:

h : $\text{succ } a = 0$

Goal:

True

trivial

⌫ Retry

Tactics

apply

cases

contrapose

decide

exact

have

induction

intro

left

rfl

right

rw

simp

simp_add

symm

tauto

trivial

use

Definitions

*

\wedge

+

\neq

\leq

\mathbb{N}

Theorems

* + 012