



have a *formula* for $0 + n$ in general, we can only use `add_zero` and `add_succ` once we know whether n is 0 or a successor. The *induction* tactic splits into these two cases.

The base case will require us to prove $0 + 0 = 0$, and the inductive step will ask us to show that if $0 + d = d$ then $0 + \text{succ } d = \text{succ } d$. Because 0 and successor are the only way to make numbers, this will cover all the cases.

See if you can do your first

Theorem `zero_add` : For all natural numbers n , we have $0 + n = n$.

Active Goal

Objects:

`n` : \mathbb{N}

Goal:

$0 + n = n$

`induction n with d hd`

✖ Retry

Active Goal Goal 2

Goal:

$0 + 0 = 0$

`rw [add_zero]`

✖ Retry

Active Goal Goal 2

Goal:

$0 = 0$

`refl`

✖ Retry

intermediate goal solved! 🎉

Active Goal

Objects:

`d` : \mathbb{N}

Assumptions:

`hd` : $0 + d = d$

Goal:

add_succ ✕

$(a\ d : \mathbb{N}) : a + \text{MyNat.succ } d = \text{MyNat.succ } (a + d)$

`add_succ a b` is the proof of $a + \text{succ } b = \text{succ } (a + b)$.