Introduction to Data Science

Lab 3 – Basic Statistical Analysis with Microsoft Excel Online

Overview

In the previous labs, you explored a dataset containing details of lemonade sales.

In this lab, you will apply some statistical analysis techniques to gain a better understanding of the data.

What You'll Need

To complete the labs, you will need the following:

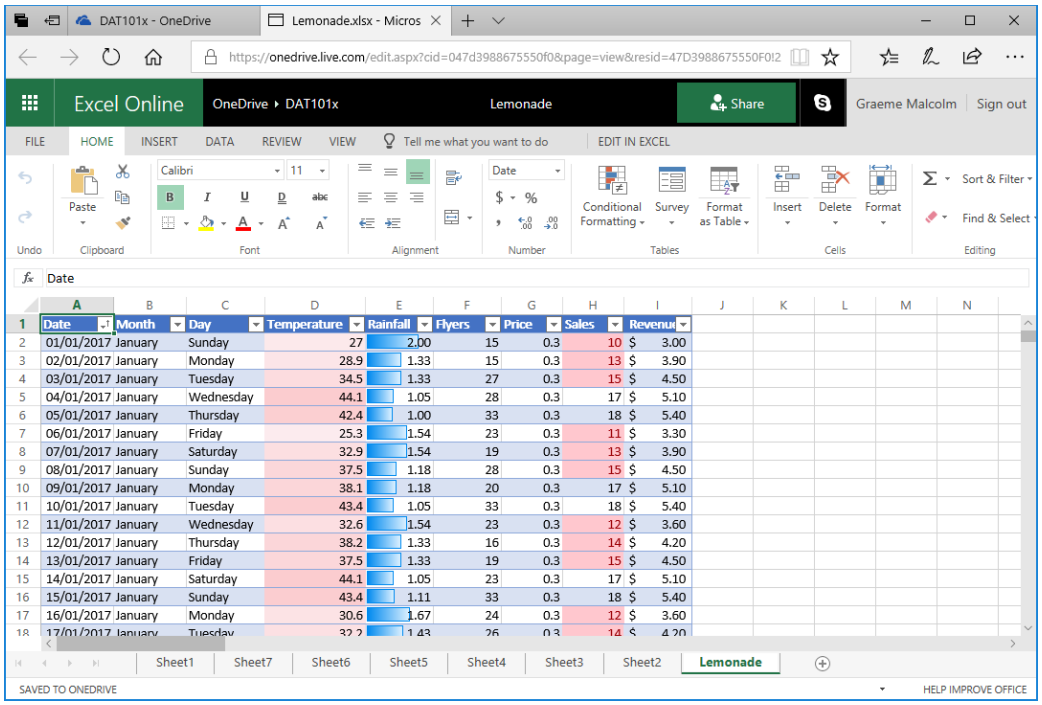
- A Windows, Linux, or Mac OS X computer with a web browser.
- A Microsoft account (for example a *hotmail.com*, *live.com*. or *outlook.com* account). If you do not already have a Microsoft account, sign up for one at https://signup.live.com.
- The **Lemonade.xlsx** workbook from the previous labs in your OneDrive folder.

Exercise 1: Using Descriptive Statistics

Descriptive Statistics help you understand the "shape" or *distribution* of your data; for example, by finding measures on central tendency (the most common "typical" values) and measures of variance (how much difference there is between the most common values and other values that are higher or lower).

Calculate Descriptive Statistics for Sales

1. If you have not already done so, in your web browser, navigate to https://onedrive.live.com, and sign in using your Microsoft account credentials. Then open the **Lemonade.xlsx** workbook in the folder where you uploaded it in the previous labs and view the **Lemonade** worksheet. Your workbook should look like this:



	A	B	C	D	E	F	G	H	I
1	Date	Month	Day	Temperature	Rainfall	Flyers	Price	Sales	Revenue
2	01/01/2017	January	Sunday	27	2.00	15	0.3	10	$ 3.00
3	02/01/2017	January	Monday	28.9	1.33	15	0.3	13	$ 3.90
4	03/01/2017	January	Tuesday	34.5	1.33	27	0.3	15	$ 4.50
5	04/01/2017	January	Wednesday	44.1	1.05	28	0.3	17	$ 5.10
6	05/01/2017	January	Thursday	42.4	1.00	33	0.3	18	$ 5.40
7	06/01/2017	January	Friday	25.3	1.54	23	0.3	11	$ 3.30
8	07/01/2017	January	Saturday	32.9	1.54	19	0.3	13	$ 3.90
9	08/01/2017	January	Sunday	37.5	1.18	28	0.3	15	$ 4.50
10	09/01/2017	January	Monday	38.1	1.18	20	0.3	17	$ 5.10
11	10/01/2017	January	Tuesday	43.4	1.05	33	0.3	18	$ 5.40
12	11/01/2017	January	Wednesday	32.6	1.54	23	0.3	12	$ 3.60
13	12/01/2017	January	Thursday	38.2	1.33	16	0.3	14	$ 4.20
14	13/01/2017	January	Friday	37.5	1.33	19	0.3	15	$ 4.50
15	14/01/2017	January	Saturday	44.1	1.05	23	0.3	17	$ 5.10
16	15/01/2017	January	Sunday	43.4	1.11	33	0.3	18	$ 5.40
17	16/01/2017	January	Monday	30.6	1.67	24	0.3	12	$ 3.60
18	17/01/2017	January	Tuesday	32.2	1.43	26	0.3	14	$ 4.20

2. In cell **K1**, enter the text **Sales Statistics**, and format it as bold.
3. In cell **K2**, enter the text **Mean**, and then in cell **L2**, enter the following formula:

   `=AVERAGE(H2:H366)`

   This calculates the arithmetic mean for sales, which should be slightly over 25.3.

4. In cell **K3**, enter the text **Median**, and then in cell **L3**, enter the following formula:

   `=MEDIAN(H2:H366)`

   This calculates the median for sales, which should be 25.

5. In cell **K4**, enter the text **Mode**, and then in cell **L4**, enter the following formula:

   `=MODE.SNGL(H2:H366)`

   This calculates the mode for sales, which should be 25.

6. In cell **K5**, enter the text **Variance**, and then in cell **L5**, enter the following formula:

   `=VAR.P(H2:H366)`

   This calculates the variance for sales, which should be slightly over 47.39.

   Note that the formula for variance in this case applies to the full *population* of data, hence the **.P** extension in the function name – you'll explore working with data *samples* later in this lab.

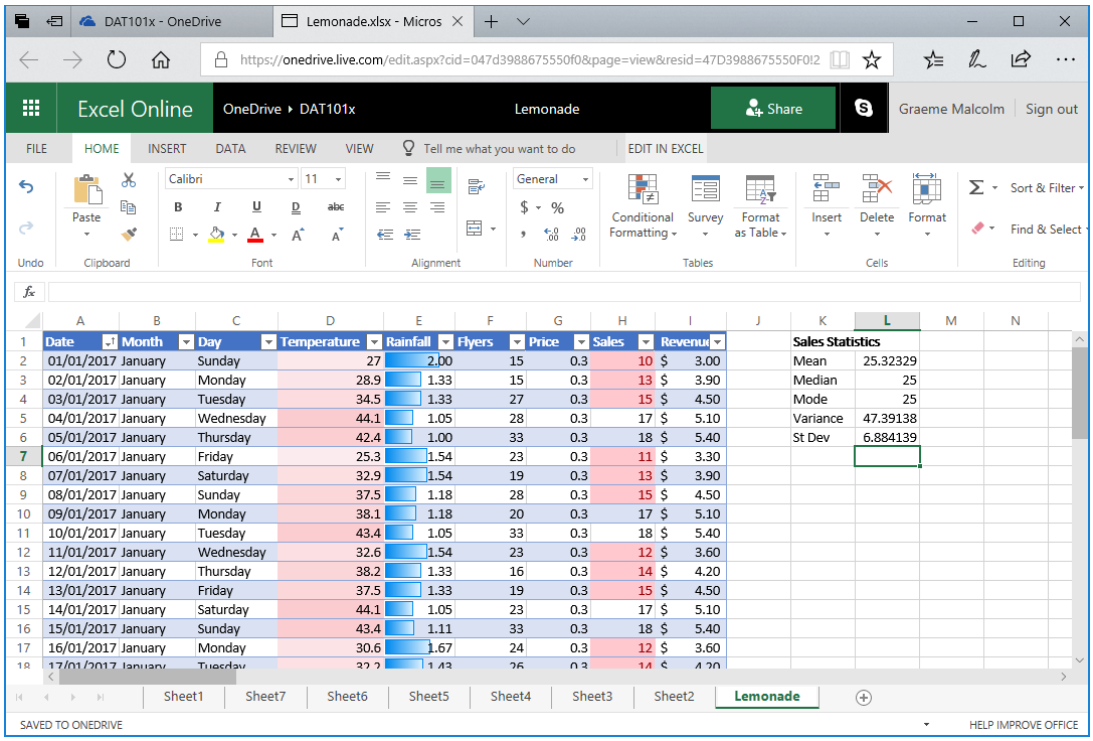
7. In cell **K6**, enter the text **Std Dev**, and then in cell **L6**, enter the following formula:

   `=STDEV.P(H2:H366)`

   This calculates the standard deviation for sales, which should be slightly over 6.88.

Note once again that the formula for standard deviation in this case applies to the full *population* of data.

Your worksheet should now look like this:



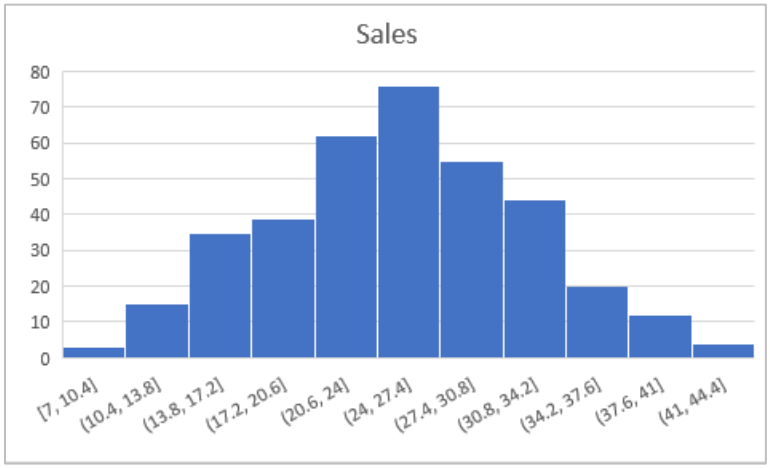
Date	Month	Day	Temperature	Rainfall	Flyers	Price	Sales	Revenue
01/01/2017	January	Sunday	27	2.00	15	0.3	10	$ 3.00
02/01/2017	January	Monday	28.9	1.33	15	0.3	13	$ 3.90
03/01/2017	January	Tuesday	34.5	1.33	27	0.3	15	$ 4.50
04/01/2017	January	Wednesday	44.1	1.05	28	0.3	17	$ 5.10
05/01/2017	January	Thursday	42.4	1.00	33	0.3	18	$ 5.40
06/01/2017	January	Friday	25.3	1.54	23	0.3	11	$ 3.30
07/01/2017	January	Saturday	32.9	1.54	19	0.3	13	$ 3.90
08/01/2017	January	Sunday	37.5	1.18	28	0.3	15	$ 4.50
09/01/2017	January	Monday	38.1	1.18	20	0.3	17	$ 5.10
10/01/2017	January	Tuesday	43.4	1.05	33	0.3	18	$ 5.40
11/01/2017	January	Wednesday	32.6	1.54	23	0.3	12	$ 3.60
12/01/2017	January	Thursday	38.2	1.33	16	0.3	14	$ 4.20
13/01/2017	January	Friday	37.5	1.33	19	0.3	15	$ 4.50
14/01/2017	January	Saturday	44.1	1.05	23	0.3	17	$ 5.10
15/01/2017	January	Sunday	43.4	1.11	33	0.3	18	$ 5.40
16/01/2017	January	Monday	30.6	1.67	24	0.3	12	$ 3.60
17/01/2017	January	Tuesday	32.2	1.43	26	0.3	14	$ 4.20

Sales Statistics	
Mean	25.32329
Median	25
Mode	25
Variance	47.39138
St Dev	6.884139

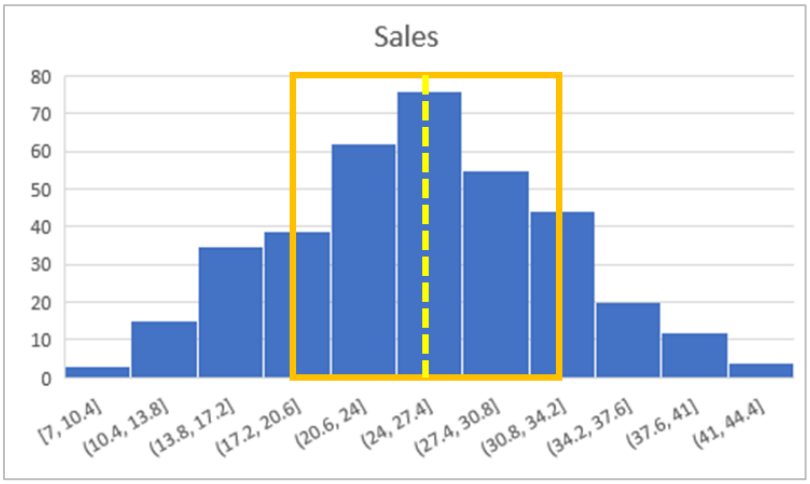
The statistics you have calculated tell you something about the distribution of the sales values, but it can often be easier to visualize the data to get a sense of how the data is distributed.

Visualize the Distribution of Sales Values

1. Select all the data in the **Sales** column, including the header. Then on the **Insert** tab of the ribbon, in the **Other Charts** drop-down list, click the **Histogram** chart (which is the first one in the **Statistical** section).
2. Select the chart that is produced and edit the chart title to change it to **Sales**. Then move the chart so that it is to the right of the statistics you calculated in the previous exercise. The chart should look like this:



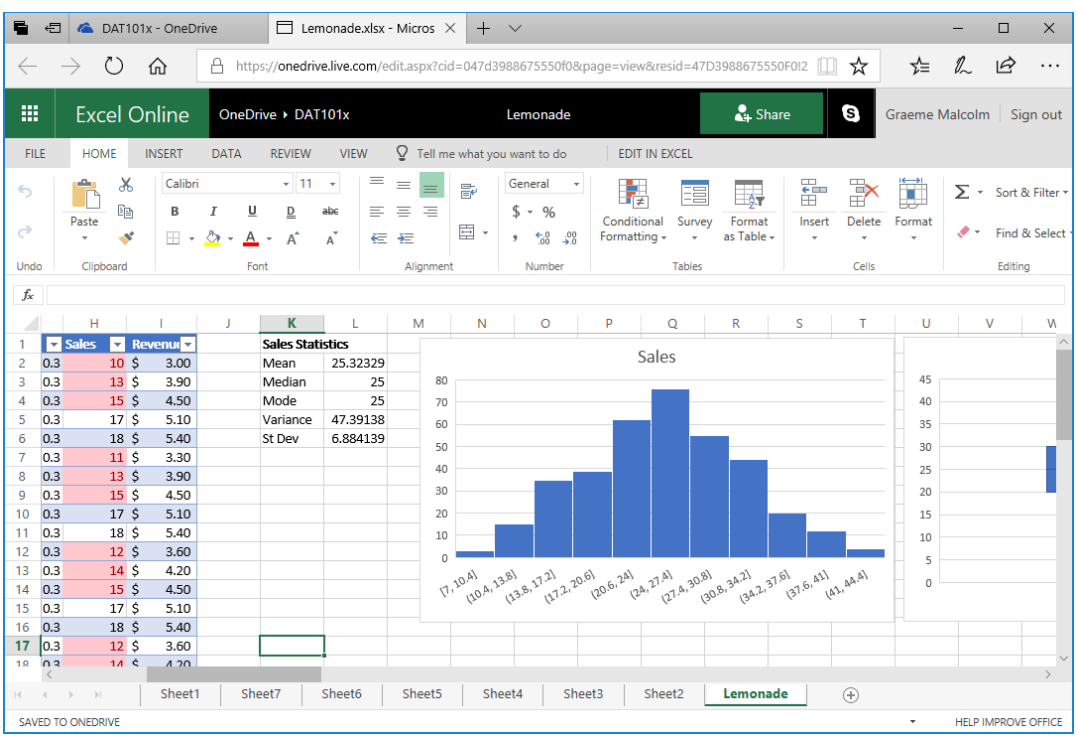
3. Examine the chart, and note the following:
    - The histogram shows the frequency of different values for **Sales** values grouped into ranges, or *bins*. For example, there are around 15 days with a **Sales** value between 10.4 and 13.8; and there are around 20 days with a **Sales** value between 34.2 and 37.6.
    - The most frequently occurring **Sales** values are between 24 and 27.5. This range includes the mean, median, and mode statistics you calculated previously. In other words, on most days, the number of sales was more or less in the middle of the lowest and highest selling days.
    - The distribution is approximately symmetrical around the middle values, forming a "bell-shaped curve" that tapers evenly towards the ends; where there are few occurrences of extreme values for **Sales**. Statisticians refer to this kind of distribution as a *normal* distribution.
    - The standard deviation you calculated previously is just under 6.9. This statistic provides a standard unit of variance around the mean (which is just over 25.3). The data within 1 standard deviation above or below the mean) therefore includes values from approximately 18.4 to around 32.2, as shown here:



    - In a normal distribution, around 68.26% of the data falls within a single standard deviation; so in this case, the number of sales was between 18.4 and 32.2 on 68.26% of the days. Around 95.45% of values fall within 2 standard deviations in a normal distribution, so there were between 11.5 and 39.1 sales on 95.4% of days.
4. Select all the data in the **Sales** column, including the header. Then on the **Insert** tab of the ribbon, in the **Other Charts** drop-down list, click the **Box and Whisker** chart (which is the third one in the **Statistical** section).
5. Select the chart that is produced and edit the chart title to change it to **Sales**. Then move the chart so that it is to the right of the histogram you created previously. The chart should look like this:

6. Examine the chart, and note the following:
    - The horizontal line in the middle indicates the *median* value for sales. This is the 50% *percentile* – in other words, 50% of the values are higher than this, and 50% are lower.
    - The X in the box indicates the mean – this is only slightly higher than the median.
    - The filled box indicates the range of values in the second and third *quartiles* – in other words, from the 25th percentile to the 75th percentile. These values range from around 20 to 30, indicating that the number of sales on half of the days was within this range,
    - The lines extending from the box (known as *whiskers*) show the range for the first and fourth quartiles, on which there were more or fewer sales than in the second and third quartiles.

Your worksheet should now look similar to this (you may need to scroll to the right to see the charts.)



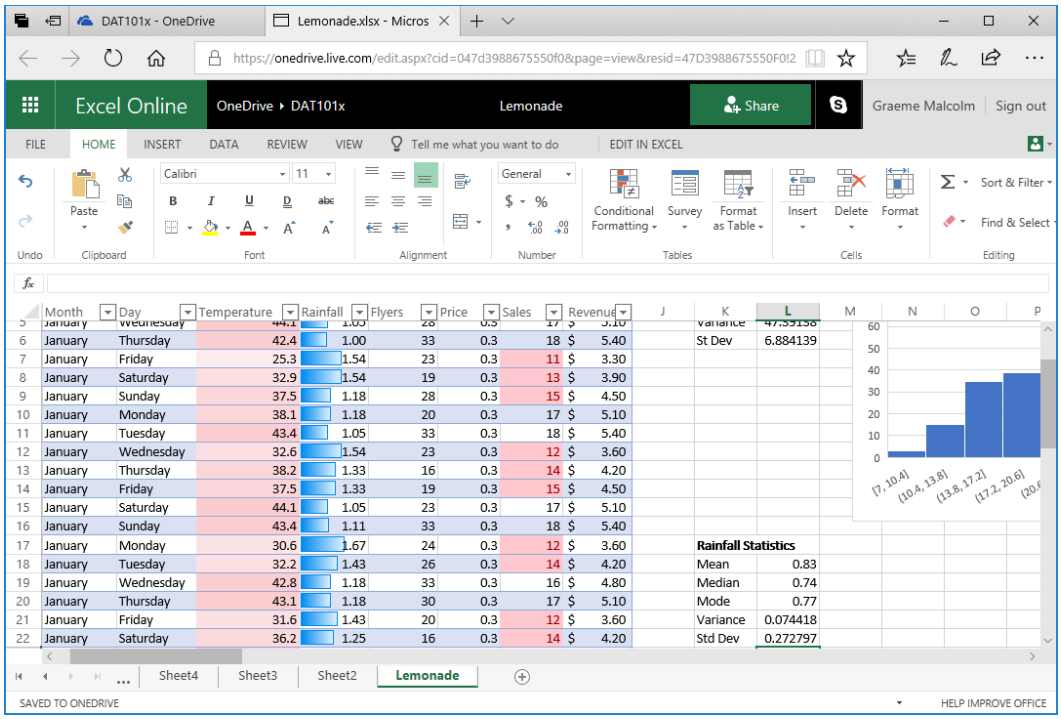
Analyze Statistics for Rainfall

1. Leave some space under the existing statistics, and in cell **K17**, enter the text **Rainfall Statistics**, and format it as bold.
2. In cell **K18**, enter the text **Mean**, and then in cell **L18**, enter the following formula:

   `=AVERAGE(E2:E366)`

   This calculates the arithmetic mean for rainfall, which should be 0.83.

3. In cells **K19** to **L22**, calculate the median, mode, population variance, and population standard deviation for rainfall, in the same way you did for sales previously. When you're finished, your worksheet should look like this:

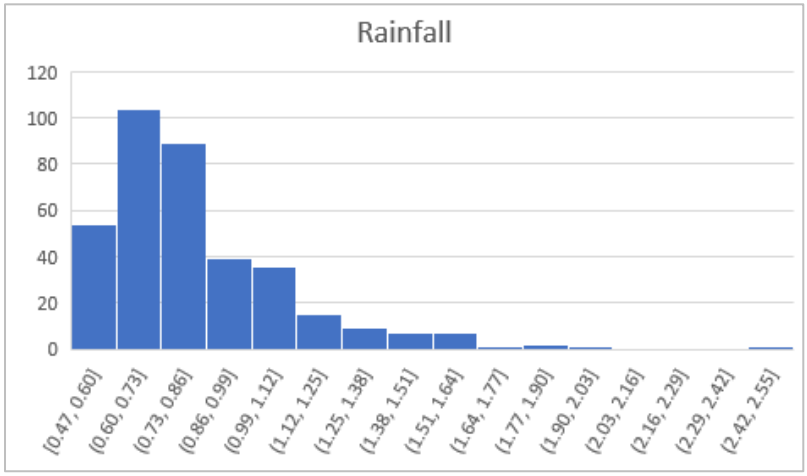


Month	Day	Temperature	Rainfall	Flyers	Price	Sales	Revenue
January	Wednesday	44.1	1.05	28	0.3	17	$ 5.10
January	Thursday	42.4	1.00	33	0.3	18	$ 5.40
January	Friday	25.3	1.54	23	0.3	11	$ 3.30
January	Saturday	32.9	1.54	19	0.3	13	$ 3.90
January	Sunday	37.5	1.18	28	0.3	15	$ 4.50
January	Monday	38.1	1.18	20	0.3	17	$ 5.10
January	Tuesday	43.4	1.05	33	0.3	18	$ 5.40
January	Wednesday	32.6	1.54	23	0.3	12	$ 3.60
January	Thursday	38.2	1.33	16	0.3	14	$ 4.20
January	Friday	37.5	1.33	19	0.3	15	$ 4.50
January	Saturday	44.1	1.05	23	0.3	17	$ 5.10
January	Sunday	43.4	1.11	33	0.3	18	$ 5.40
January	Monday	30.6	1.67	24	0.3	12	$ 3.60
January	Tuesday	32.2	1.43	26	0.3	14	$ 4.20
January	Wednesday	42.8	1.18	33	0.3	16	$ 4.80
January	Thursday	43.1	1.18	30	0.3	17	$ 5.10
January	Friday	31.6	1.43	20	0.3	12	$ 3.60
January	Saturday	36.2	1.25	16	0.3	14	$ 4.20

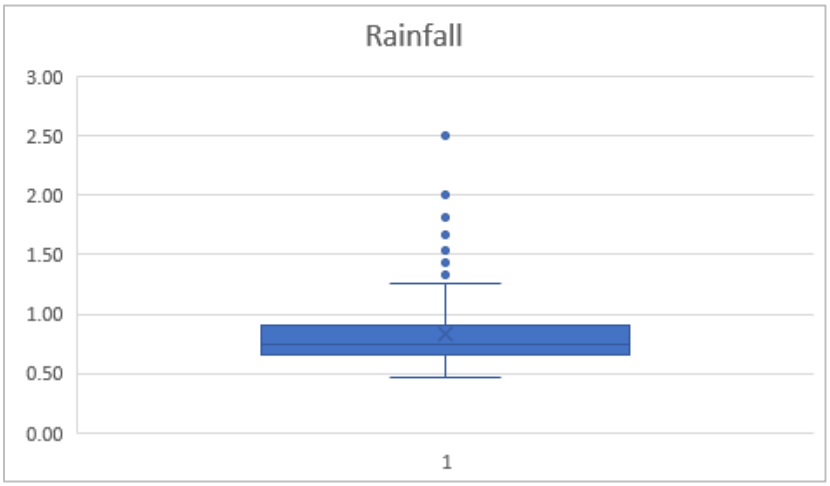
St Dev	6.884139
Rainfall Statistics	
Mean	0.83
Median	0.74
Mode	0.77
Variance	0.074418
Std Dev	0.272797

Note that the mean rainfall is quite a bit higher than the median and mode.

4. Create a histogram of rainfall, and then add an appropriate chart title and move the chart to the right of the rainfall statistics. The rainfall histogram should look like this:



5. Examine the histogram and note that the distribution of the rainfall data is not *normal*. The median value is around 0.74, so on half the days there was less rain than this, and on half there was more; however, on a rare few days, there was much more rain than this - as much as 2.42 to 2.55. These infrequent days of extremely high rainfall are *skewing* the distribution by "pulling" the mean to the right. This results in a long tail of infrequently occurring values that tapers towards the right. We therefore refer to this as a *right-skewed* distribution (had the tail pulled the mean to the left, it would be a *left-skewed* distribution).
6. Create a box and whisker chart of rainfall with an appropriate title; and move it to the right of the rainfall histogram. The box and whisker chart should look like this:



7. Examine the chart and note the following:
    - The line indicating the median (50th percentile) noticeably lower than the X indicating the mean.
    - The filled box, representing the 2nd and 3rd quartiles represents 50% of the data – in other words, on half of the days, the rainfall was between around 0.6 and 0.8.
    - The dots indicate *outliers*; rare values that are considered extreme compared to the typical range of values, which lies within the whiskers.
    - Even discounting the outliers, the range of values in the 4th quartile is larger than that of the other quartiles.

Challenge: Analyze Temperature Statistics

1. Calculate the mean, median, mode, population variance, and population standard deviation of temperature.
2. Create a histogram and a box and whiskers chart for temperature to visualize the distribution.

Exercise 2: Working with Samples

Until now, we've worked with the full *population* of data – in other words, we had all of Rosie's lemonade sales data to work with. In reality, it's more usual to work with a *sample* of data. For example, suppose you needed to conduct some research to determine the most common eye color in the US. It would be unrealistic to examine the eyes of every person in the US, so you would approach this problem by surveying a representative sample of people, and use the statistics collected as approximations for the full population parameters.

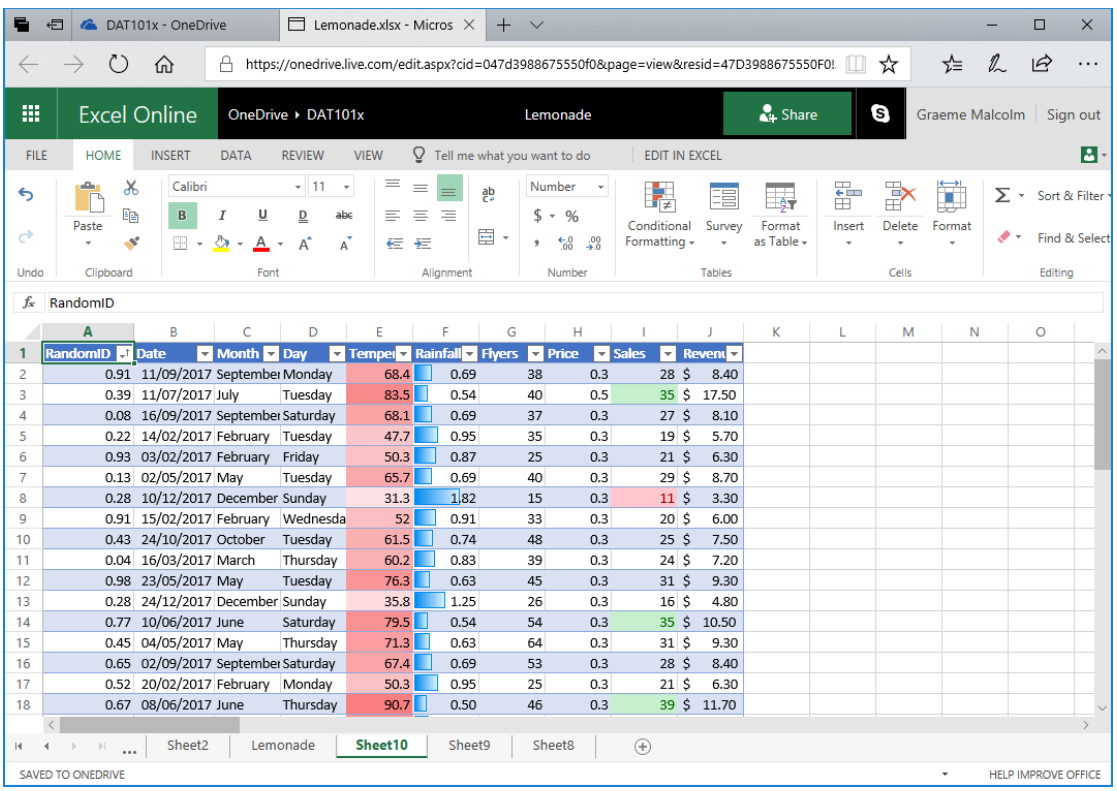
Create a Random Sample

1. On the **Lemonade** worksheet, click in cell **A1** and then press **CTRL+A (⌘ + A** on Mac OSX) to select the entire table of lemonade sales data. Then on the **Home** tab of the ribbon, click **Copy**.
2. Add a new worksheet to the workbook and click cell **A1** of the new worksheet. Then on **Home** tab of the ribbon, click **Paste** to paste the copied table into the new worksheet.
3. Click cell **A1** (the **Date** header), and then on the **Home** tab of the ribbon, in the **Cells** section, click the **Insert** drop-down list and select **Insert Table Columns to the Left**. This inserts a new column for a table field named **Column1**.
4. In the new cell **A1**, rename **Column1** to **RandomID**, and then select column **A** and in the format drop-down list in the **Number** section of the **Home** tab of the ribbon, click **Number**.
5. in cell A2, enter the following formula:

   ```
   =RAND()
   ```

   This will generate random numbers in the **RandomID** column.

6. Click the drop-down arrow in the **RandomID** column header and click **Sort Ascending**. The data in the table is then sorted by the **RandomID** field, which randomizes the order of the data records. This makes it easier to select a random sample of records (a random sample is more likely to be representative of the population than a sample that is based on some inherent order in the data itself). Your worksheet should now look like this:



	A	B	C	D	E	F	G	H	I	J
1	RandomID	Date	Month	Day	Tempe	Rainfall	Flyers	Price	Sales	Revenu
2	0.91	11/09/2017	Septembe	Monday	68.4	0.69	38	0.3	28	$ 8.40
3	0.39	11/07/2017	July	Tuesday	83.5	0.54	40	0.5	35	$ 17.50
4	0.08	16/09/2017	Septembe	Saturday	68.1	0.69	37	0.3	27	$ 8.10
5	0.22	14/02/2017	February	Tuesday	47.7	0.95	35	0.3	19	$ 5.70
6	0.93	03/02/2017	February	Friday	50.3	0.87	25	0.3	21	$ 6.30
7	0.13	02/05/2017	May	Tuesday	65.7	0.69	40	0.3	29	$ 8.70
8	0.28	10/12/2017	December	Sunday	31.3	1.82	15	0.3	11	$ 3.30
9	0.91	15/02/2017	February	Wednesda	52	0.91	33	0.3	20	$ 6.00
10	0.43	24/10/2017	October	Tuesday	61.5	0.74	48	0.3	25	$ 7.50
11	0.04	16/03/2017	March	Thursday	60.2	0.83	39	0.3	24	$ 7.20
12	0.98	23/05/2017	May	Tuesday	76.3	0.63	45	0.3	31	$ 9.30
13	0.28	24/12/2017	December	Sunday	35.8	1.25	26	0.3	16	$ 4.80
14	0.77	10/06/2017	June	Saturday	79.5	0.54	54	0.3	35	$ 10.50
15	0.45	04/05/2017	May	Thursday	71.3	0.63	64	0.3	31	$ 9.30
16	0.65	02/09/2017	Septembe	Saturday	67.4	0.69	53	0.3	28	$ 8.40
17	0.52	20/02/2017	February	Monday	50.3	0.95	25	0.3	21	$ 6.30
18	0.67	08/06/2017	June	Thursday	90.7	0.50	46	0.3	39	$ 11.70

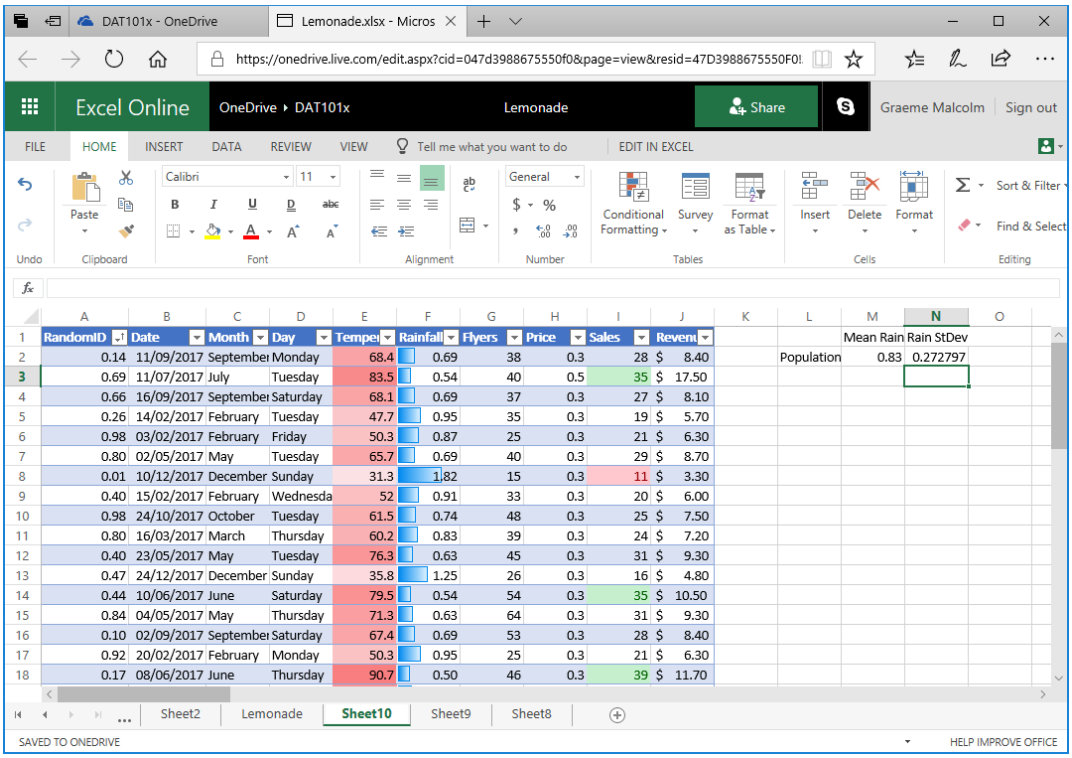
7. In Cell **M1**, enter the text **Mean Rain**, and in cell **N1** enter the text **Rain StDev**.
8. In cell **L2**, enter the text **Population**.
9. Then in cell **M2**, enter the following formula:

   ```
   =AVERAGE(F2:F366)
   ```

10. In cell **N2**, enter the following formula:

```
=STDEV.P(F2:F366)
```

This gives you full population parameters for the mean and standard deviation of rainfall, so you can compare them with sample statistics. Your workbook should now look like this:



RandomID	Date	Month	Day	Tempe	Rainfall	Flyers	Price	Sales	Revenu			Mean Rain	Rain StDev
0.14	11/09/2017	September	Monday	68.4	0.69	38	0.3	28	$ 8.40		Population	0.83	0.272797
0.69	11/07/2017	July	Tuesday	83.5	0.54	40	0.5	35	$ 17.50				
0.66	16/09/2017	September	Saturday	68.1	0.69	37	0.3	27	$ 8.10				
0.26	14/02/2017	February	Tuesday	47.7	0.95	35	0.3	19	$ 5.70				
0.98	03/02/2017	February	Friday	50.3	0.87	25	0.3	21	$ 6.30				
0.80	02/05/2017	May	Tuesday	65.7	0.69	40	0.3	29	$ 8.70				
0.01	10/12/2017	December	Sunday	31.3	1.82	15	0.3	11	$ 3.30				
0.40	15/02/2017	February	Wednesda	52	0.91	33	0.3	20	$ 6.00				
0.98	24/10/2017	October	Tuesday	61.5	0.74	48	0.3	25	$ 7.50				
0.80	16/03/2017	March	Thursday	60.2	0.83	39	0.3	24	$ 7.20				
0.40	23/05/2017	May	Tuesday	76.3	0.63	45	0.3	31	$ 9.30				
0.47	24/12/2017	December	Sunday	35.8	1.25	26	0.3	16	$ 4.80				
0.44	10/06/2017	June	Saturday	79.5	0.54	54	0.3	35	$ 10.50				
0.84	04/05/2017	May	Thursday	71.3	0.63	64	0.3	31	$ 9.30				
0.10	02/09/2017	September	Saturday	67.4	0.69	53	0.3	28	$ 8.40				
0.92	20/02/2017	February	Monday	50.3	0.95	25	0.3	21	$ 6.30				
0.17	08/06/2017	June	Thursday	90.7	0.50	46	0.3	39	$ 11.70				

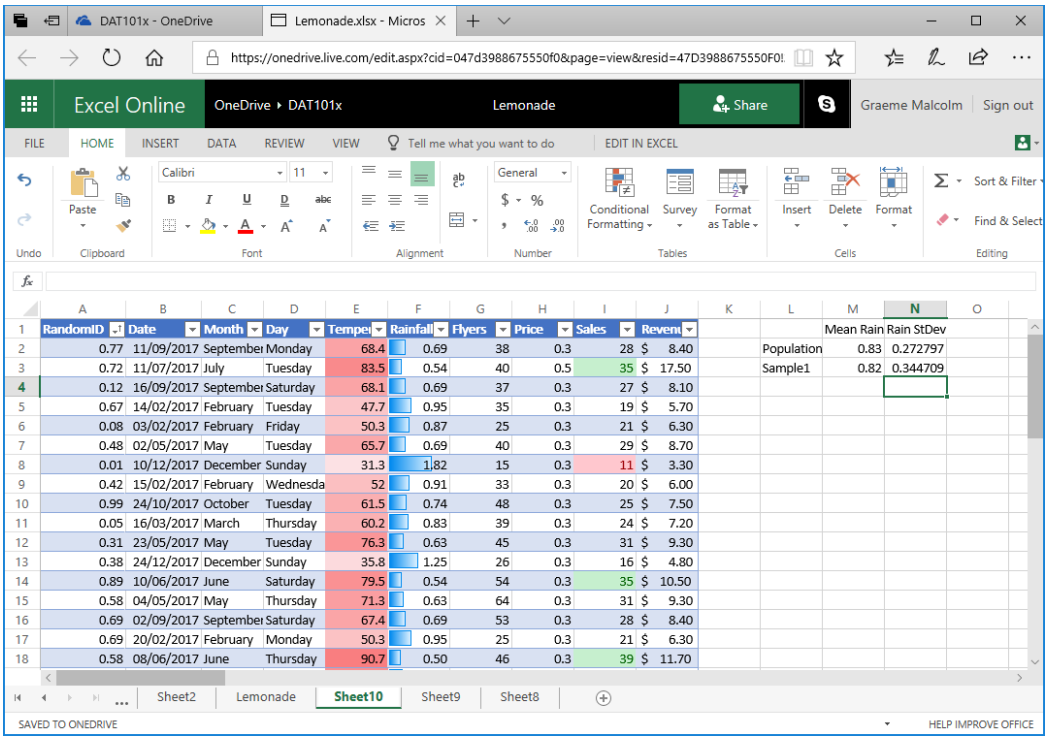
11. In cell **L3**, enter the text **Sample1**.
12. Then in cell **M3**, enter the following formula:

```
=AVERAGE(F2:F41)
```

13. In cell **N3**, enter the following formula:

```
=STDEV.S(F2:F41)
```

This gives you sample statistics for the mean and standard deviation of rainfall based on the first 40 random rows of data. Note that you use the same AVERAGE function to calculate a sample mean or population mean, but you use the STDEV.S function to calculate the standard deviation for a sample – this incorporates some additional variance to allow for sample bias. Your spreadsheet should now look similar to this (the figures may not be exactly the same because of the randomization of the data):



RandomID	Date	Month	Day	Tempe	Rainfall	Flyers	Price	Sales	Revenu
0.77	11/09/2017	September	Monday	68.4	0.69	38	0.3	28	$ 8.40
0.72	11/07/2017	July	Tuesday	83.5	0.54	40	0.5	35	$ 17.50
0.12	16/09/2017	September	Saturday	68.1	0.69	37	0.3	27	$ 8.10
0.67	14/02/2017	February	Tuesday	47.7	0.95	35	0.3	19	$ 5.70
0.08	03/02/2017	February	Friday	50.3	0.87	25	0.3	21	$ 6.30
0.48	02/05/2017	May	Tuesday	65.7	0.69	40	0.3	29	$ 8.70
0.01	10/12/2017	December	Sunday	31.3	1.82	15	0.3	11	$ 3.30
0.42	15/02/2017	February	Wednesda	52	0.91	33	0.3	20	$ 6.00
0.99	24/10/2017	October	Tuesday	61.5	0.74	48	0.3	25	$ 7.50
0.05	16/03/2017	March	Thursday	60.2	0.83	39	0.3	24	$ 7.20
0.31	23/05/2017	May	Tuesday	76.3	0.63	45	0.3	31	$ 9.30
0.38	24/12/2017	December	Sunday	35.8	1.25	26	0.3	16	$ 4.80
0.89	10/06/2017	June	Saturday	79.5	0.54	54	0.3	35	$ 10.50
0.58	04/05/2017	May	Thursday	71.3	0.63	64	0.3	31	$ 9.30
0.69	02/09/2017	September	Saturday	67.4	0.69	53	0.3	28	$ 8.40
0.69	20/02/2017	February	Monday	50.3	0.95	25	0.3	21	$ 6.30
0.58	08/06/2017	June	Thursday	90.7	0.50	46	0.3	39	$ 11.70

	Mean Rain	Rain StDev
Population	0.83	0.272797
Sample1	0.82	0.344709

Compare the sample statistics with the population parameters.

14. In cell **L4**, enter the text **Sample2**.
15. Then in cell **M4** enter the following formula:

```
=AVERAGE(F35:F74)
```

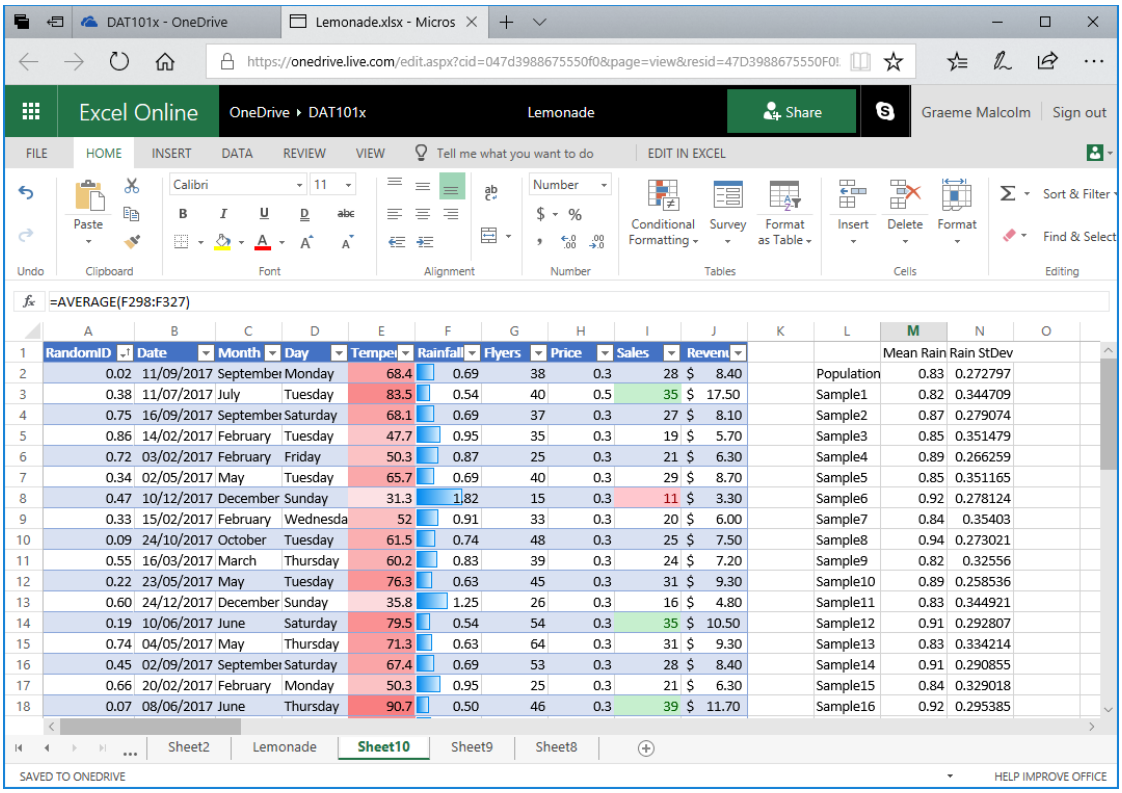
16. In cell **N4**, enter the following formula:

```
=STDEV.S(F35:F74)
```

This produces statistics from a different sample. Note that the closeness of the sample statistics to the population parameters varies depending on the sample. In this case, both samples include 40 observations - using larger samples generally results in statistics that are closer to their actual population parameters.

Create a Sampling Distribution

1. Select cells **L3** to **N4** (the **Sample1** and **Sample2** statistics you created previously; but <u>not</u> the population parameters), and then drag the small square "handle" at the bottom right of the selected cells down to row 292. This creates 290 samples as shown here:



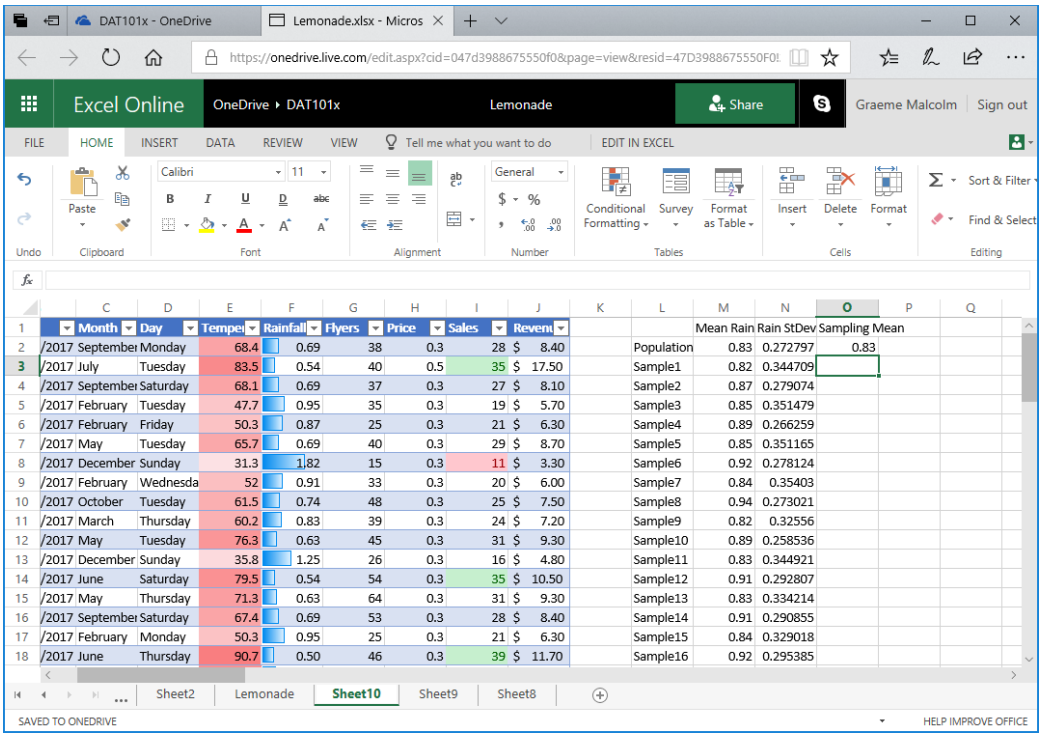
	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
1	RandomID	Date	Month	Day	Tempe	Rainfall	Flyers	Price	Sales	Revenu			Mean Rain	Rain StDev	
2	0.02	11/09/2017	September	Monday	68.4	0.69	38	0.3	28	$ 8.40		Population	0.83	0.272797	
3	0.38	11/07/2017	July	Tuesday	83.5	0.54	40	0.5	35	$ 17.50		Sample1	0.82	0.344709	
4	0.75	16/09/2017	September	Saturday	68.1	0.69	37	0.3	27	$ 8.10		Sample2	0.87	0.279074	
5	0.86	14/02/2017	February	Tuesday	47.7	0.95	35	0.3	19	$ 5.70		Sample3	0.85	0.351479	
6	0.72	03/02/2017	February	Friday	50.3	0.87	25	0.3	21	$ 6.30		Sample4	0.89	0.266259	
7	0.34	02/05/2017	May	Tuesday	65.7	0.69	40	0.3	29	$ 8.70		Sample5	0.85	0.351165	
8	0.47	10/12/2017	December	Sunday	31.3	1.82	15	0.3	11	$ 3.30		Sample6	0.92	0.278124	
9	0.33	15/02/2017	February	Wednesda	52	0.91	33	0.3	20	$ 6.00		Sample7	0.84	0.35403	
10	0.09	24/10/2017	October	Tuesday	61.5	0.74	48	0.3	25	$ 7.50		Sample8	0.94	0.273021	
11	0.55	16/03/2017	March	Thursday	60.2	0.83	39	0.3	24	$ 7.20		Sample9	0.82	0.32556	
12	0.22	23/05/2017	May	Tuesday	76.3	0.63	45	0.3	31	$ 9.30		Sample10	0.89	0.258536	
13	0.60	24/12/2017	December	Sunday	35.8	1.25	26	0.3	16	$ 4.80		Sample11	0.83	0.344921	
14	0.19	10/06/2017	June	Saturday	79.5	0.54	54	0.3	35	$ 10.50		Sample12	0.91	0.292807	
15	0.74	04/05/2017	May	Thursday	71.3	0.63	64	0.3	31	$ 9.30		Sample13	0.83	0.334214	
16	0.45	02/09/2017	September	Saturday	67.4	0.69	53	0.3	28	$ 8.40		Sample14	0.91	0.290855	
17	0.66	20/02/2017	February	Monday	50.3	0.95	25	0.3	21	$ 6.30		Sample15	0.84	0.329018	
18	0.07	08/06/2017	June	Thursday	90.7	0.50	46	0.3	39	$ 11.70		Sample16	0.92	0.295385	

The means of the samples form a *sampling distribution* of the mean – in other words, a new data distribution that consists of the sample means.

2. In cell **O1**, enter the text **Sampling Mean**. Then in cell **O2**, enter the following formula:

```
=AVERAGE(M3:M292)
```

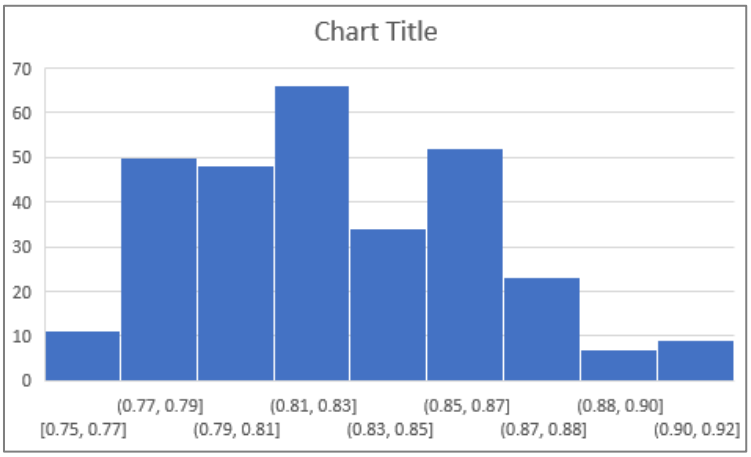
This calculates the mean of the sample means; in other words, the mean of the sampling distribution. This should be fairly close to the population mean as shown here (yours may not be exactly the same as the population mean, but it should be close!)



	Month	Day	Tempe	Rainfall	Flyers	Price	Sales	Revenu
2	/2017 September	Monday	68.4	0.69	38	0.3	28	$ 8.40
3	/2017 July	Tuesday	83.5	0.54	40	0.5	35	$ 17.50
4	/2017 September	Saturday	68.1	0.69	37	0.3	27	$ 8.10
5	/2017 February	Tuesday	47.7	0.95	35	0.3	19	$ 5.70
6	/2017 February	Friday	50.3	0.87	25	0.3	21	$ 6.30
7	/2017 May	Tuesday	65.7	0.69	40	0.3	29	$ 8.70
8	/2017 December	Sunday	31.3	1.82	15	0.3	11	$ 3.30
9	/2017 February	Wednesda	52	0.91	33	0.3	20	$ 6.00
10	/2017 October	Tuesday	61.5	0.74	48	0.3	25	$ 7.50
11	/2017 March	Thursday	60.2	0.83	39	0.3	24	$ 7.20
12	/2017 May	Tuesday	76.3	0.63	45	0.3	31	$ 9.30
13	/2017 December	Sunday	35.8	1.25	26	0.3	16	$ 4.80
14	/2017 June	Saturday	79.5	0.54	54	0.3	35	$ 10.50
15	/2017 May	Thursday	71.3	0.63	64	0.3	31	$ 9.30
16	/2017 September	Saturday	67.4	0.69	53	0.3	28	$ 8.40
17	/2017 February	Monday	50.3	0.95	25	0.3	21	$ 6.30
18	/2017 June	Thursday	90.7	0.50	46	0.3	39	$ 11.70

	Mean Rain	Rain StDev	Sampling Mean
Population	0.83	0.272797	0.83
Sample1	0.82	0.344709	
Sample2	0.87	0.279074	
Sample3	0.85	0.351479	
Sample4	0.89	0.266259	
Sample5	0.85	0.351165	
Sample6	0.92	0.278124	
Sample7	0.84	0.35403	
Sample8	0.94	0.273021	
Sample9	0.82	0.32556	
Sample10	0.89	0.258536	
Sample11	0.83	0.344921	
Sample12	0.91	0.292807	
Sample13	0.83	0.334214	
Sample14	0.91	0.290855	
Sample15	0.84	0.329018	
Sample16	0.92	0.295385	

3. Click cell **M3** (the Sample1 mean) and then hold the **Shift** and **Ctrl** keys and press the **Down-Arrow** key to select all the other sample means (if you are using a Mac OSX computer, hold the **Shift** and ⌘ keys, and press the **Down-Arrow** key).
4. In the **Insert** tab of the ribbon, in the **Other Charts** drop-down list, select **Histogram** (the first chart in the **Statistical** section) and view the histogram that is created, as shown here (yours may look a little different):



The histogram may not look exactly symmetrical; but when you create a sampling distribution from a sufficiently large number of reasonably-sized samples, you'll find that it has a bell-curved appearance. We won't discuss this any further in this course, but it's useful to know that with enough random samples, a sampling distribution generally takes on a *normal* distribution due to something called the *central limit theorem* – even when (as in this case), the population data from which the sample means are derived is not normally distributed.

Challenge: Analyze Temperature Samples

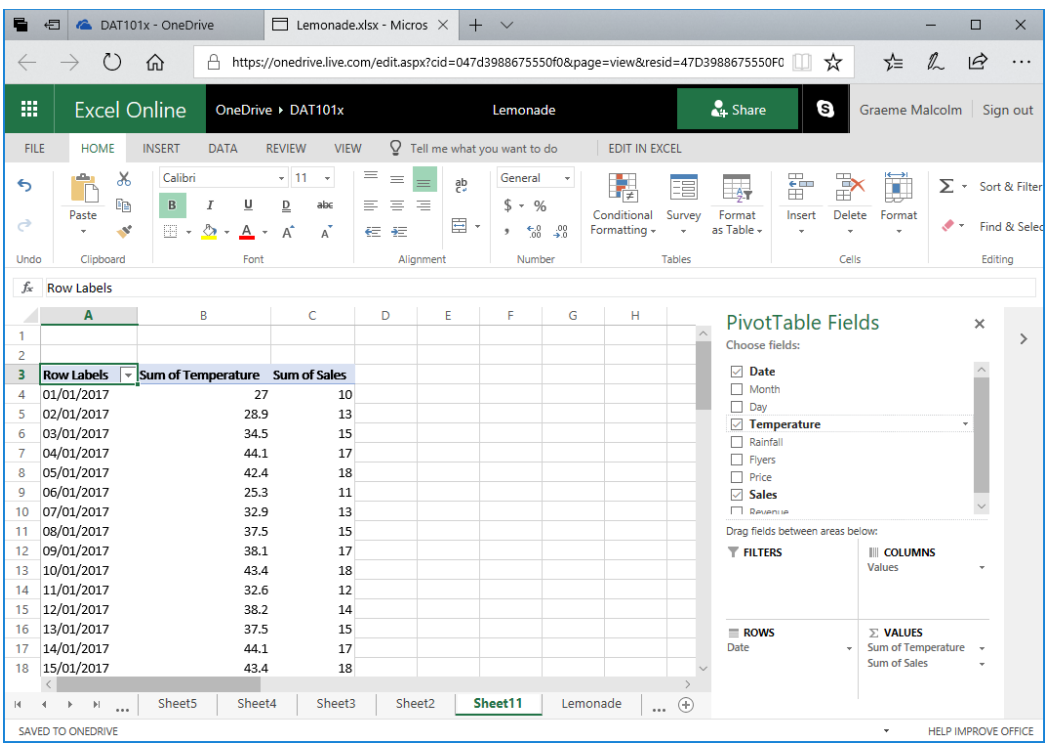
1. Create a sampling distribution based on 290 samples of mean **Temperature**. Each sample should be based on 40 random observations.
2. Calculate the mean of the temperature sampling distribution.

Exercise 3: Inferential Statistics and Hypothesis Testing

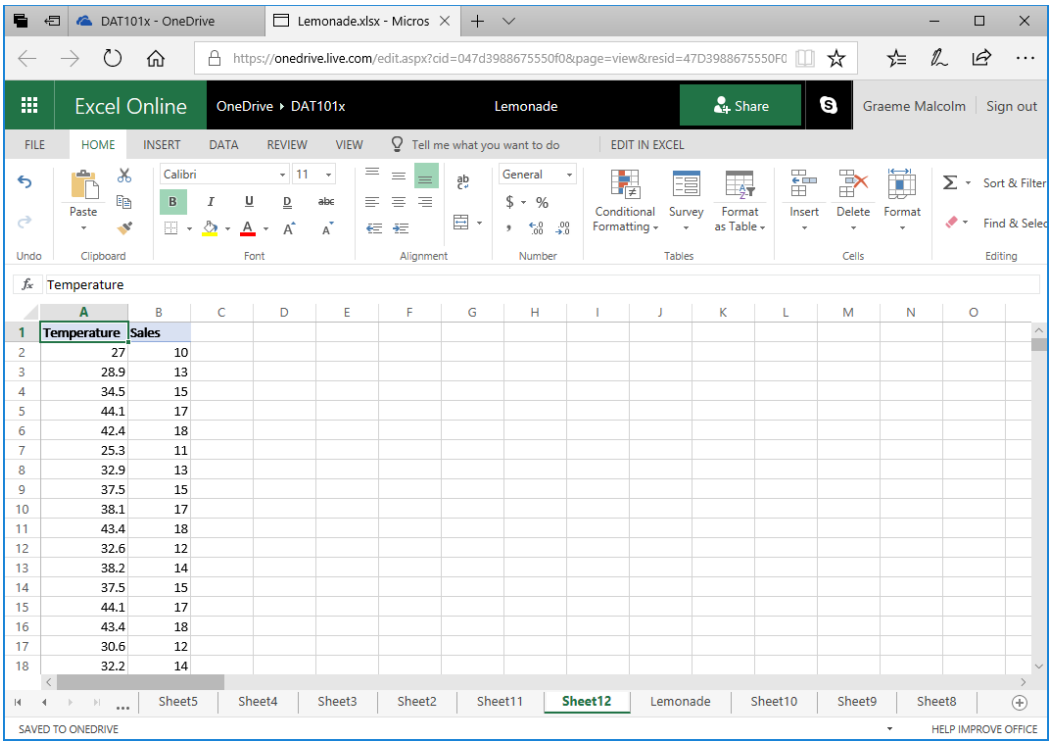
So far, we've explored *descriptive* statistics that describe the distribution of data in a full population or a sample. *Inferential* statistics, as the name suggests, are used to make inferences, or predictions, from data based on statistical relationships between fields (or *features*) of the data.

Measure Correlation

1. Switch back to the **Lemonade** worksheet in the **Lemonade.xlsx** workbook and select cell **A1** (the **Date** column header).
2. On the **Insert** tab of the ribbon, click **PivotTable**; and insert a PivotTable for the lemonade sales table into a new worksheet.
3. In the **PivotTable Fields** pane, drag **Date** to the **ROWS** area and drag **Temperature** and **Sales** to the **VALUES** area so that your worksheet looks like this:

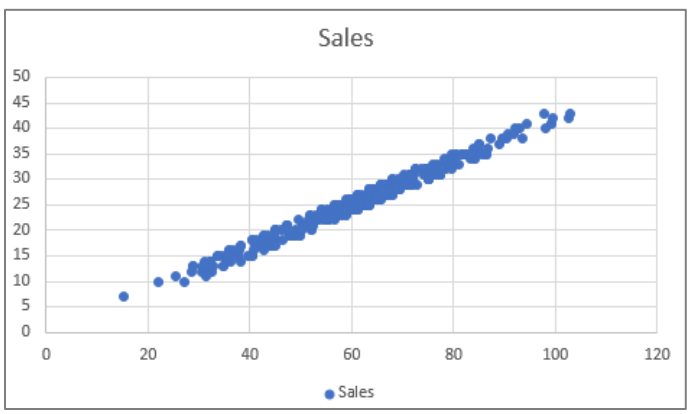


4. Scroll to the bottom of the PivotTable until you can see the **Grand Total** row. You need to copy the temperature and sales values, *excluding* this grand total to a new worksheet.
5. Click cell **B368**, which should contain the **Temperature** value for December 12th 2017 (above the grand total). Then press **SHIFT + CTRL + ↑** (**SHIFT + ⌘ + ↑** on Mac OSX) to select the column of temperature values, and then press **SHIFT + →** to extend the selection to include the sales values. Finally, copy the selected cells to the clipboard.
6. Create a new worksheet, and then on the new worksheet click cell **A1** and paste the copied data. Then change the columns headers to **Temperature** and **Sales** as shown here:



	A	B
1	Temperature	Sales
2	27	10
3	28.9	13
4	34.5	15
5	44.1	17
6	42.4	18
7	25.3	11
8	32.9	13
9	37.5	15
10	38.1	17
11	43.4	18
12	32.6	12
13	38.2	14
14	37.5	15
15	44.1	17
16	43.4	18
17	30.6	12
18	32.2	14

7. Select cell **A1** (the **Temperature** column header) and press **CTRL + A** (**⌘ + A** on Mac OSX) to select the data, and then on the **Insert** tab of the ribbon, in the **Scatter** drop-down list, click the first scatter plot. This inserts a scatter plot that looks like this:



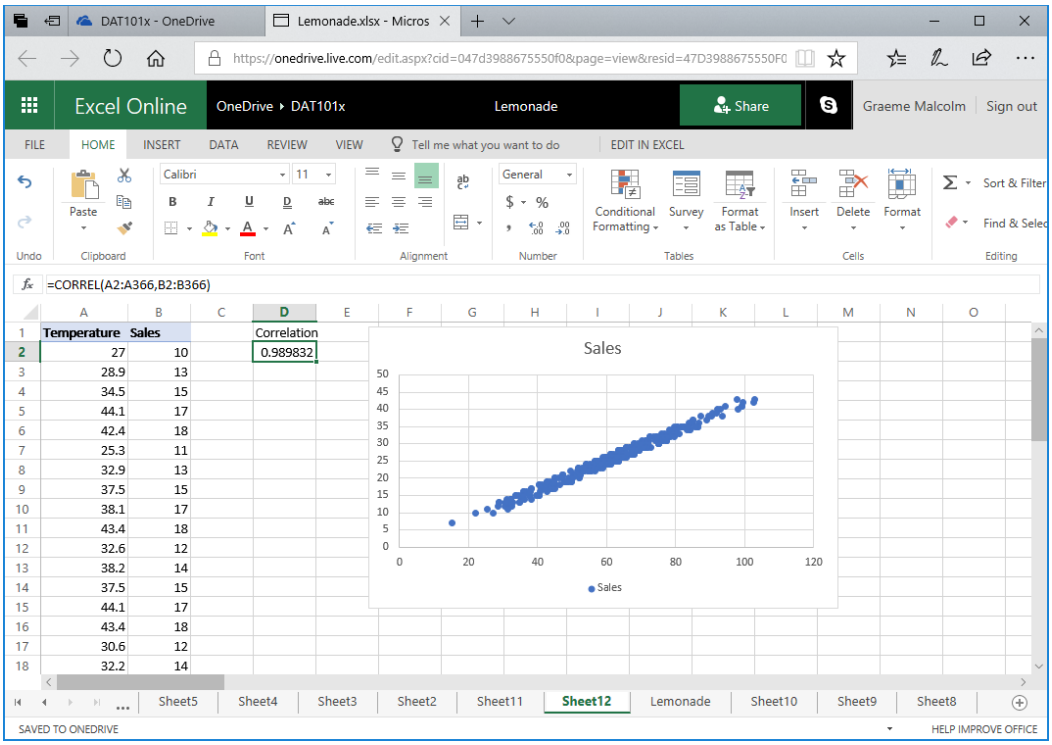
Note that the scatter plot seems to reflect a linear relationship between temperature and sales, in which the higher the temperature, the more sales there are.

8. Move the chart to the side of the worksheet to create some space, and then in cell **D1**, enter the text **Correlation** and in cell **D2**, enter the following formula:

```
=CORREL(A2:A366,B2:B366)
```

This calculates the *correlation* between temperature and sales; and should produce a value of around 0.989832. Correlation is a statistical measurement of the strength of an apparent relationship between two numeric variables – in this case, temperature and sales.

Your worksheet should look like this:



Correlation is measured as a value between -1 and 1. A value close to 1 indicates a *positive* correlation; in other words, high values for one variable seem to correspond with high values for the other variable. A value close to -1 on the other hand indicates a *negative* correlation, in which high values for one variable correspond to low values for the other variable. A value close to 0 indicates the lack of any discernible relationship between the variables.

With a correlation of almost 0.99, there is a strong positive relationship between temperature and sales.

Note: Statisticians often quote the mantra "correlation is not causation". We can use correlation to determine that days with high sales volumes tend to have high temperatures; but we can't say that Rosie sold a lot of lemonade on a particular day *because* the temperature was high – just as we can't say that a day was particularly hot *because* Rosie sold a lot of lemonade. In fact, there could be a "hidden" third factor that affects both sales of lemonade and temperature. For example, during the summer months, when lemons are in season, the temperature tends to be higher.

Challenge: Calculate Rainfall / Sales Correlation

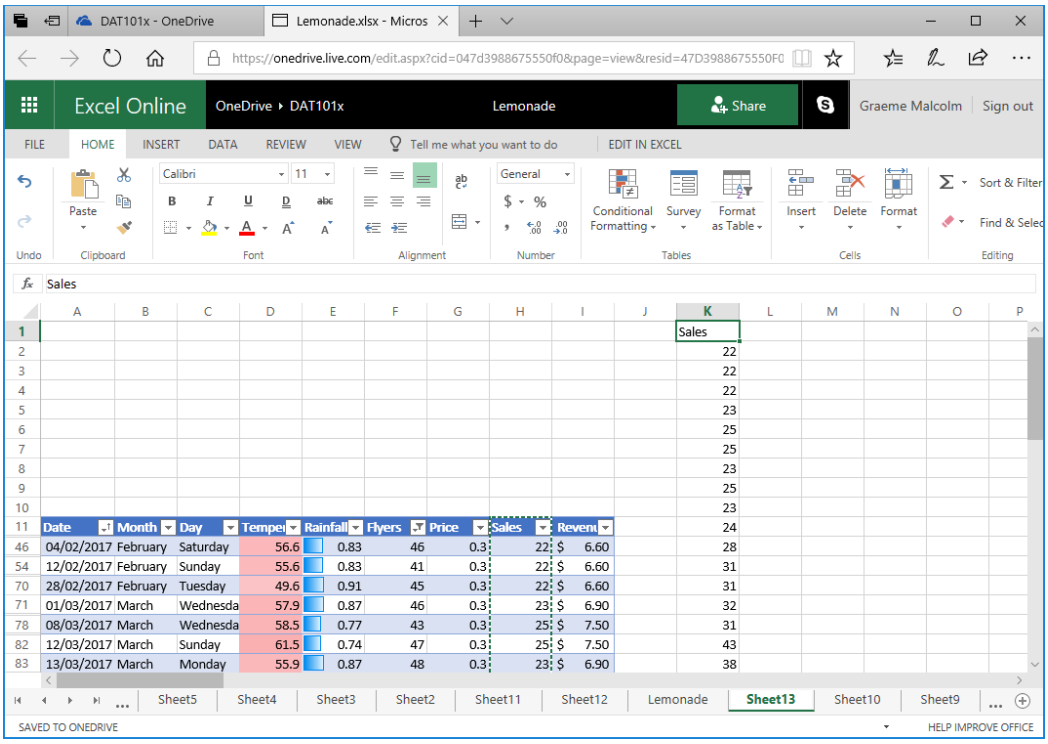
1. Calculate the correlation between **Rainfall** and **Sales**.
2. What does the correlation indicate?

Conduct a Hypothesis Test

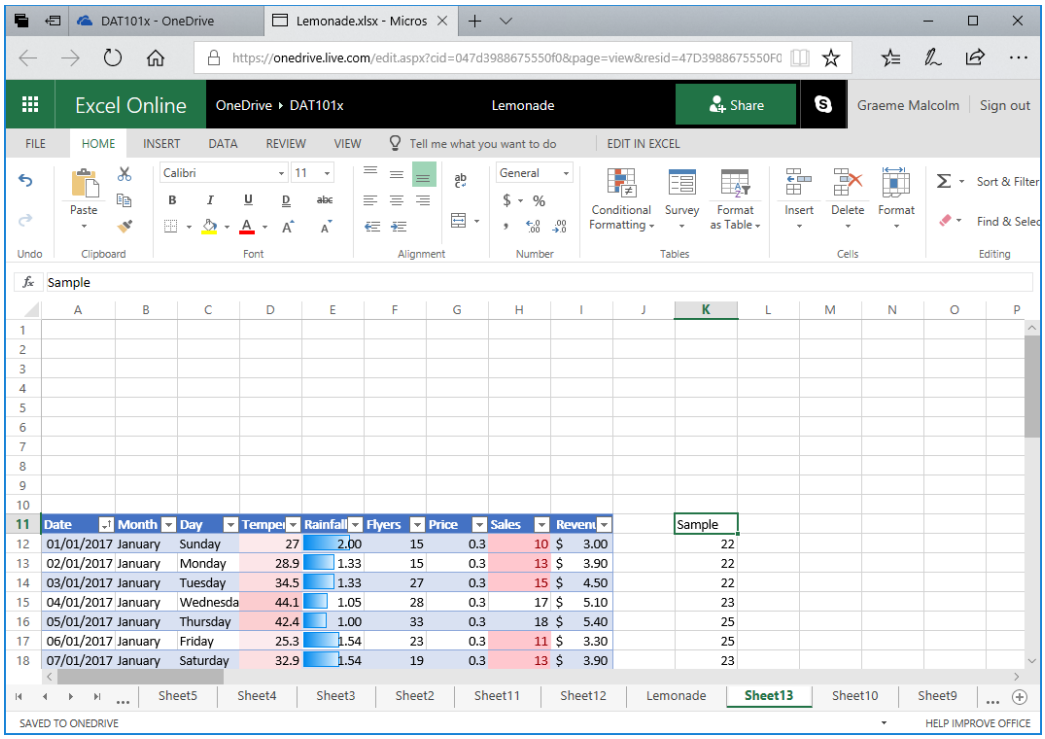
1. On the **Lemonade** worksheet, clear any filters from the table of lemonade sales data. Then click in cell **A1** and then press **CTRL+A (⌘ + A** on Mac OSX) to select the entire table of lemonade sales data. Then on the **Home** tab of the ribbon, click **Copy**.
2. Add a new worksheet to the workbook and paste the copied data into cell **A11** of the new worksheet (leaving ten blank rows above the pasted data).

You have hypothesized that on days where Rosie distributes a higher than average number of flyers, sales are higher. You need to test this hypothesis to determine if any increase in sales on days with higher than average flyer distribution can be explained by chance, or if the variation in sales is too improbable to be explained by chance alone. To help determine this, you need to create a data sample containing sales for days with higher than average flyer distribution.

3. In the drop-down list for the **Flyers** column header, in the **Number Filters** sub-menu, click **Above Average**.
4. Select the **Sales** column (including the header), and then select cell **K1** and in the **Paste** drop-down list, click **Paste Values**. This pastes the filtered sales data sample (which contains the observations from days with higher than average leaflet distribution) as shown here:

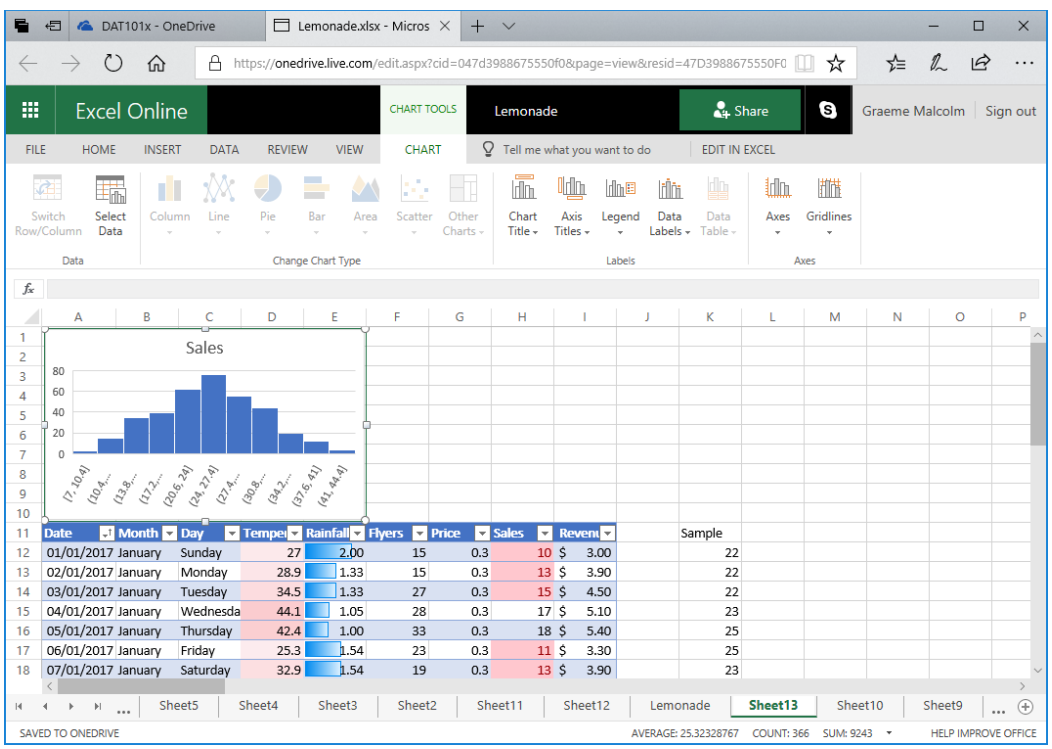


5. Clear the filter from the **Flyers** column so that the table starting in row 11 shows the full population of sales data.
6. In cell **K1**, change the column header to **Sample**. Then select the sample data (including the header) and move it to cell **K11** as shown here:



Date	Month	Day	Tempe	Rainfall	Flyers	Price	Sales	Revenu	Sample
01/01/2017	January	Sunday	27	2.00	15	0.3	10	$ 3.00	22
02/01/2017	January	Monday	28.9	1.33	15	0.3	13	$ 3.90	22
03/01/2017	January	Tuesday	34.5	1.33	27	0.3	15	$ 4.50	22
04/01/2017	January	Wednesda	44.1	1.05	28	0.3	17	$ 5.10	23
05/01/2017	January	Thursday	42.4	1.00	33	0.3	18	$ 5.40	25
06/01/2017	January	Friday	25.3	1.54	23	0.3	11	$ 3.30	25
07/01/2017	January	Saturday	32.9	1.54	19	0.3	13	$ 3.90	23

7. Select the **Sales** column of data (including the header), and insert a histogram showing the distribution of sales. Change the chart title to **Sales**, and then resize and position the histogram in the space above the data, like this:



8. In cell **G2**, enter the text **Mean**, and then in cell **H2** enter the following formula:

```
=AVERAGE(H12:H376)
```

9. In cell **G3**, enter the text **StDev**, and then in cell **H3** enter the following formula:

```
=STDEV.P(H12:H376)
```

10. In cell **G4**, enter the text **Sample**, and then in cell **H4** enter the following formula to calculate the sample mean of sales for days with higher than average flyer distribution (of which there are 172):

    ```
    =AVERAGE(K12:K183)
    ```

    In cells G2 to H4, you should now have the following values:

Mean	25.32329
StDev	6.884139
Sample	29.99419

From this, you can see that the sample mean of approximately 29.99 (the mean number of sales on days with higher than average flyer distribution) is indeed greater than the population mean of around 25.32 (the mean number of sales on all days). You can also see in the histogram that the population mean is in the middle, and the sample mean is to the right. However, there is some variance in the population data resulting in a standard deviation of around 6.88. So can the higher sales on days where Rosie distributed more flyers be explained simply by this normal variance (we'll call this our *null hypothesis*), or is there enough evidence to reject that explanation in favor of an *alternative hypothesis* that the sales increase on these days is statistically significant enough to have been caused by something other than random chance?

To determine this, we'll conduct something called a Z-Test.

11. In cell **G5**, enter the text **P-Value**, and then in cell **H5** enter the following formula:

    ```
    =Z.TEST(K12:K183, H2, H3)
    ```

    This calculates a p-value, which is the probability of observing a sample mean at least as high as our value of 29.99 in a 172 sample distribution from a population with a mean of 25.32, and a standard deviation of 6.88.

    The p-value is probably displayed in scientific notation, with a value similar to 2.83128E-19. To view this as a regular decimal number, select the p-value (in cell **H4**) and on the **Home** tab of the ribbon, in the **Number** section select the **Number** format and then repeatedly click the **Increase Decimal** button until the first non-zero decimal place is shown. It should be close to 0.0000000000000000003.

    This is clearly a very small probability, and in fact it is common to use a value of 0.05 (or 5%) as the threshold for rejecting the null hypothesis in favor of the alternative hypothesis. So in this case, the p-value is much lower than this threshold and we can reject the hypothesis that the increase in sales can be explained by random variance and conclude that there is some non-random factor at work here. Note that we *can't* categorically say that the increase in sales is because of the higher number of flyers distributed; but we can say that on the days where more leaflets were distributed, there was a statistically significant increase in sales.

    It's worth briefly thinking a little bit about what this means. What does this show? We have shown that, *had the results been due to chance* (i.e., H_0 = true), we could *possibly* still get these results. In other words, we haven't disproven chance as an explanation. However, we showed

that the probability of getting these results is very, very, very small…only 0.0000000000000000003. We are safe in rejecting chance as an explanation for our results here.

Note: There's a lot more to hypothesis testing than we have room to discuss here. The example above is a 1-sample test (it tests a single sample of data to compare the sample mean with a hypothesized mean). The example is also a 1-tailed test, and in this case, the test is *right*-tailed (our p-value describes the probability of a sample mean being significantly *higher* than the hypothesized mean, which means the critical area for rejection of the null hypothesis is under the *right* tail of a normal distribution curve.

You can also use the Excel Z.TEST function to perform a two-tailed test, in which the alternative hypothesis is that the sample mean is *not equal* to the hypothesized mean (so there are critical areas under both the right and left tails of the normal distribution curve). To perform 2-tailed tests in Excel, you need to manipulate the value retuned by the Z.TEST function to calculate the correct p-value as follows:

```
= 2*MIN(Z.TEST(SampleRange, HypothesizedMean [,PopStDev]),
   1-Z.TEST(SampleRange, HypothesizedMean [,PopStDev]))
```

For more information about using the Z.TEST function in Excel, see the documentation at https://support.office.com/en-us/article/Z-TEST-function-D633D5A3-2031-4614-A016-92180AD82BEE.

Challenge: Test Rainfall Hypothesis

1. Test the following hypotheses:
    - H_0 (null hypothesis): Higher mean sales on days with lower than average rainfall can be explained by random variance.
    - H_1 (alternative hypothesis): Mean sales on days with lower than average rainfall are *significantly* higher than the population mean and can't be explained by random variance.
2. You should reject the null hypothesis if the p-value for your test is less than 0.05.