

Trees - 4

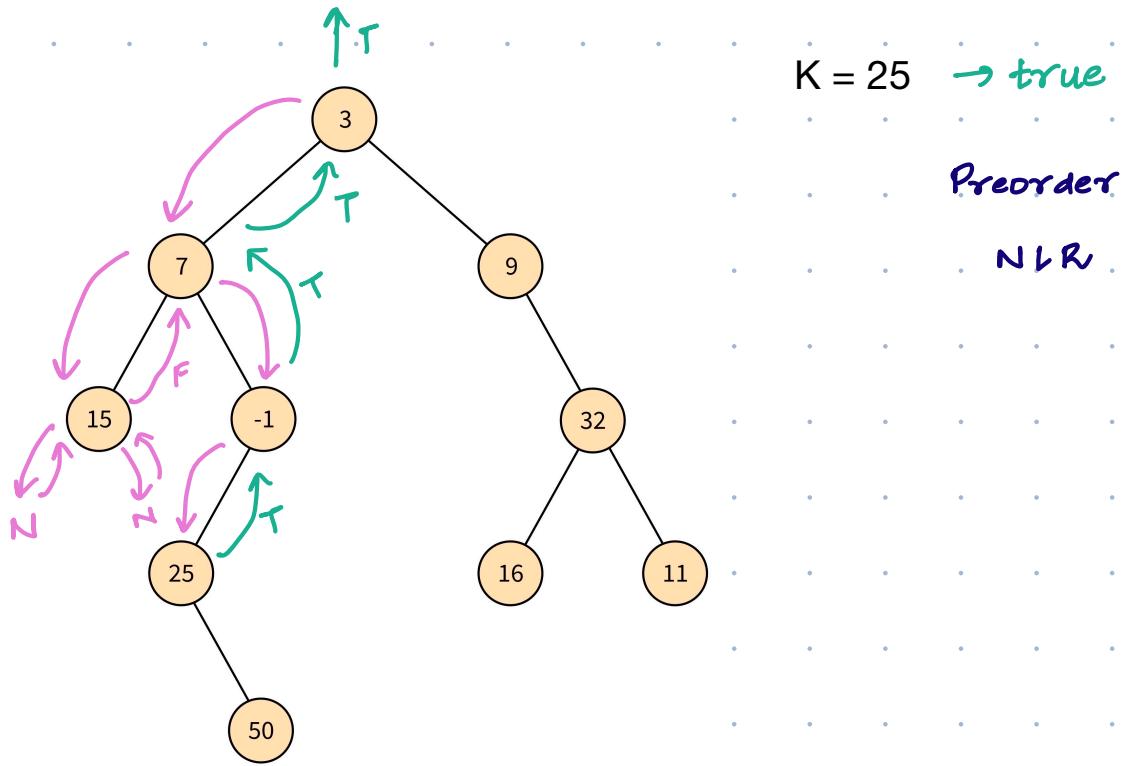
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Search an element in Binary Tree



```
boolean search (Node root, int k) {
```

```
    // Base Case
```

```
    if (root == null) return false;
```

T.C : O(N)
S.C : O(ht of tree)

```
    if (root.val == k) return true;
```

```
    if (search(root.left, k) == true) return true;
```

```
    if (search(root.right, k) == true) return true;
```

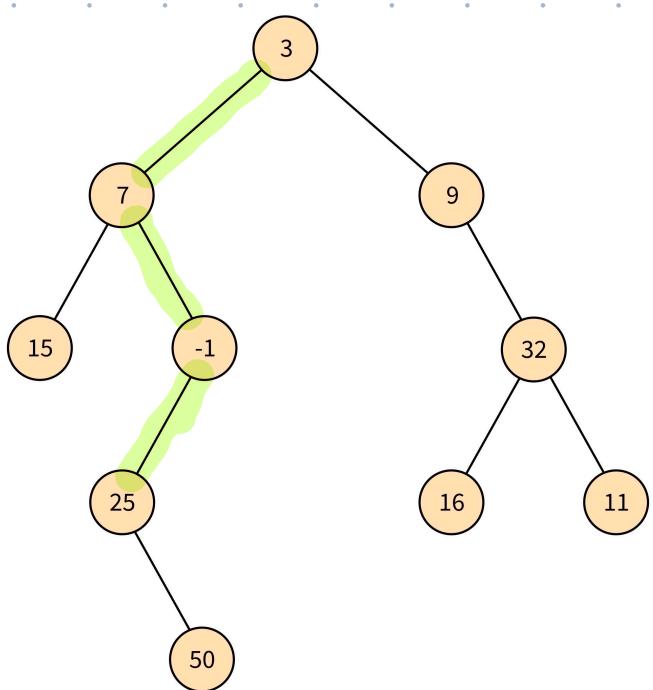
```
    return false;
```

}

return (search(root.left, k) ||
 search(root.right, k));



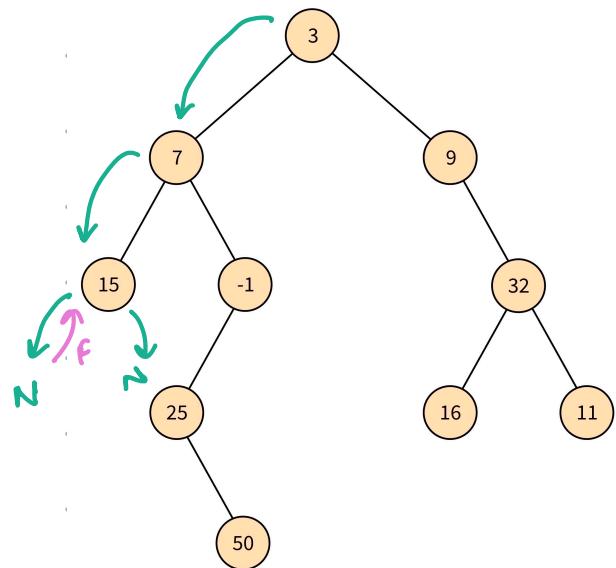
Path from Root to Node



$K = 25$

[3, 7, -1, 25]

Approach: We search for an element & when the element is found we will return back & on returning back we will also add elements in an arraylist. Then Reverse the list.



$K = 25$

ans = { 3 }

</> Code

```
boolean search (Node root, int K, vector<int> ans) {
```

```
    if (root == NULL) returns false;
```

T.C : O(N)

S.C : O(ht of tree)

```
    if (root.val == K) {
```

```
        ans.push(root.val);
```

```
        return true;
```

```
}
```

```
bool x = search (root.left, K, ans) || search (root.right, K, ans);
```

```
if (x == true) {
```

```
    ans.push (root.val);
```

```
    return true;
```

```
y  
return false;
```

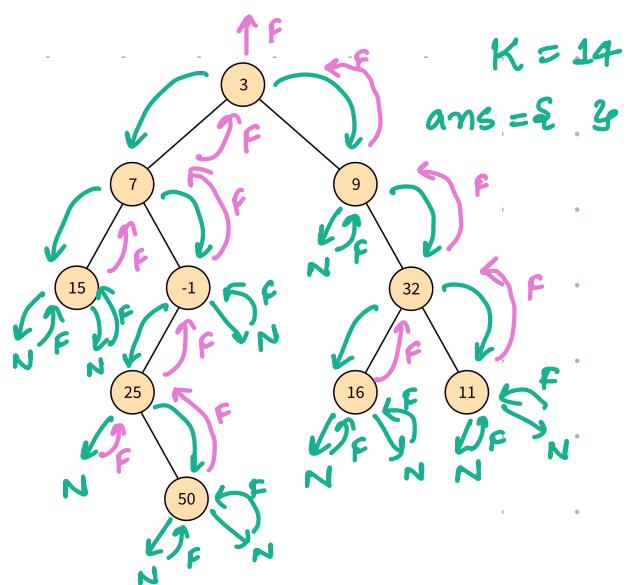
```
vector<int> RootToNodePath (Node root, int K) {
```

```
    vector<int> ans;
```

```
    search (root, K, ans);
```

```
    reverse (ans);
```

```
    return ans;
```



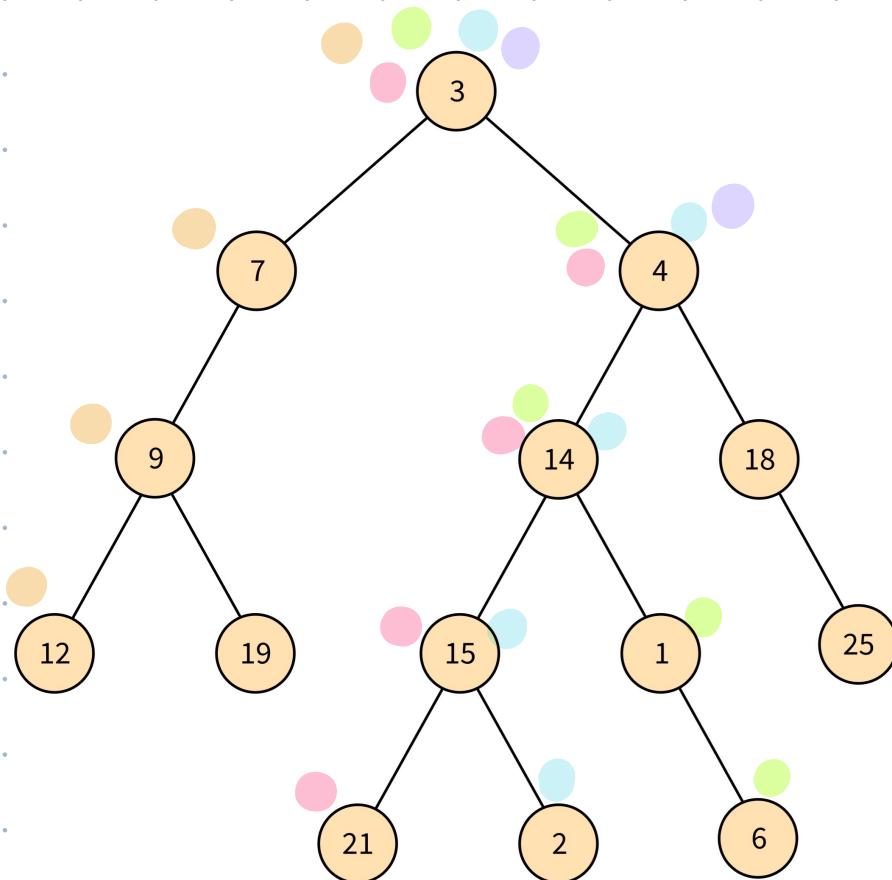


Lowest Common Ancestor (LCA)

| | | | | | | |
|----------|----------------|--------|-----------|-----------|----------|------------------|
| Flipkart | Acolite | Amazon | Microsoft | OYO Rooms | Snapdeal | MakeMyTrip |
| PayU | Times Internet | Cisco | PayPal | Expedia | Twitter | American Express |

Note : All values are distinct.

Both v_1 & v_2 will exist.



$$\text{L.C.A}(21, 6) \rightarrow 14$$

$$\text{L.C.A}(2, 6) \rightarrow 14$$

$$\text{L.C.A}(21, 4) \rightarrow 4$$

$$\text{L.C.A}(12, 6) \rightarrow 3$$

$$21 \rightarrow [3 \ 4 \ 14 \ 15 \ 21]$$

$$6 \rightarrow [3 \ 4 \ 14 \ 1 \ 6]$$

Root \rightarrow Node

$$[21 \ 15 \ 14 \ 4 \ 3] \leftarrow$$

$$[6 \ 1 \ 14 \ 4 \ 3]$$

$$4 [4 \ 3]$$

Approach :

Find Root \rightarrow Node Path for both v_1 & v_2 .

Iterate on both arrays & check for last common value.

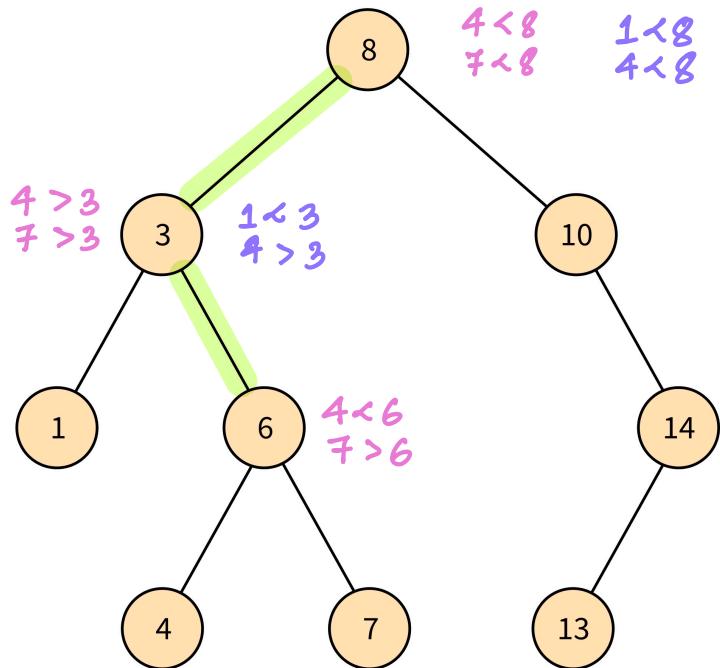
T.C : O(N)

S.C : O(N)



L.C.A in B.S.T

Both v_1 & v_2 will exist.



$\text{LCA}(4, 7) \rightarrow 6$

$\text{LCA}(1, 4) \rightarrow 3$

Idea 1 : Same approach as BT.

Idea 2 : Make use of BST property for searching & find the point where diversion pt.

</> Code

```

int LCA(Node root, int v1, int v2) {
    Node curr = root;
    while (true) {
        if (v1 < curr.val && v2 < curr.val)
            curr = curr.left;
        else if (v1 > curr.val && v2 > curr.val)
            curr = curr.right;
        else
            return curr.val;
    }
}
  
```

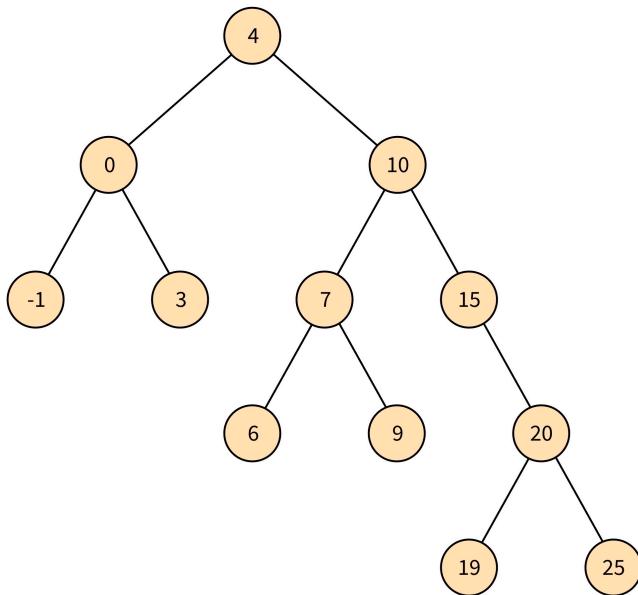
T.C : O(ht of tree)
S.C : O(1)



< Question > : Find Kth smallest element in B.S.T

K = 3

3rd smallest element : 3



Inorder of BST is sorted in Ascending Order

Inorder : [0 1 2 3 4 5 6 7 8 9 10 11]
 [-1 0 3 4 6 7 9 10 15 19 20 25]



BF Idea

Find Inorder of the BST & store it in ArrayList.

value at $(K-1)^{\text{th}}$ index of this arraylist is k^{th} smallest value.

T.C. : O(N)

S.C. : O(N)



Idea -2

While doing Inorder traversal, keep track of count of nodes.



L N R

</> Code

```
void Inorder(Node root, int &K, int &ans) {
```

```
    if (root == NULL) return;
```

```
    Inorder(root.left, K, ans);
```

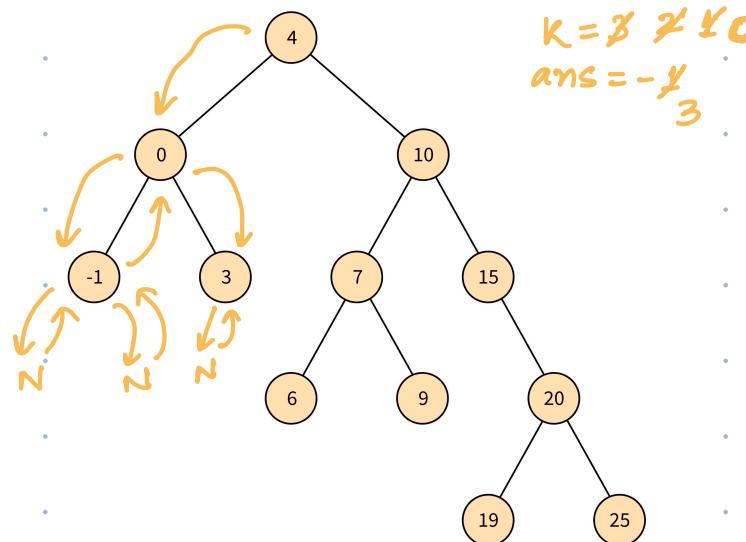
```
K--;
```

```
if (K == 0) {
```

```
    ans = root.val;
    return;
}
```

```
Inorder(root.right, K, ans);
```

y



```
int Kth Smallest Element (Node root, int K) {
```

```
    int ans = -1;
```

```
    Inorder(root, K, ans);
```

```
    return ans;
```

y

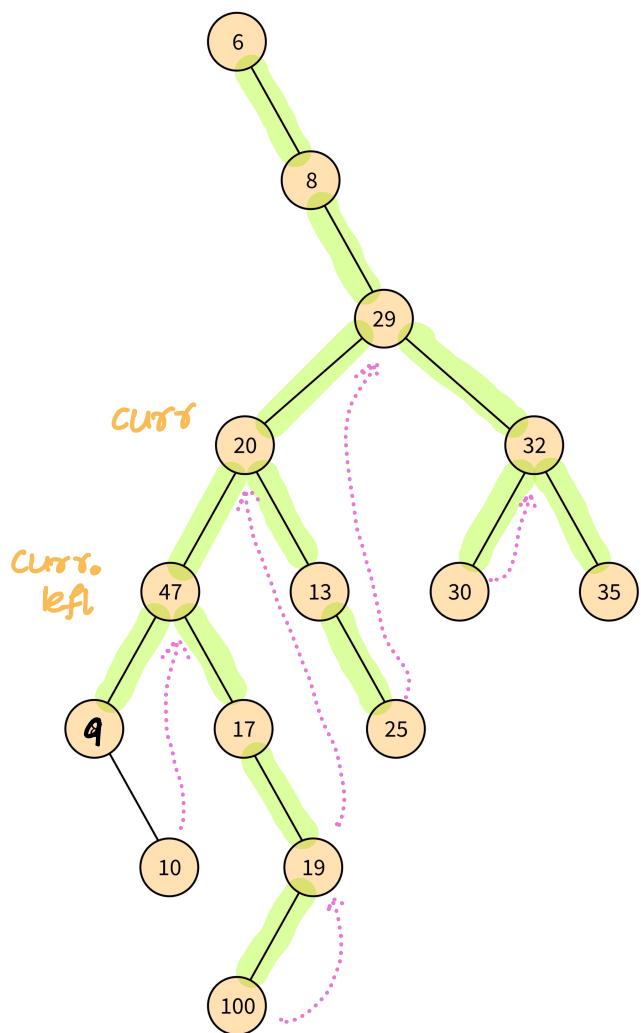


Morris Traversal

S.C of Recursive : O(int of tree)
" " Iterative : O(int of tree)

In-Order Traversal of a Binary Tree

Expected S.C $\rightarrow O(1)$



Can we use Recursion? ✗

Iteration ✓

Inorder : [6, 8, 9, 10, 47, 17, 100, 19, 20, 13, 25, 29, 30, 32, 35]

L N R

Inorder Predecessor : Node that comes just before the given node in its Inorder.

10 is IP of 47

100 " 19

19 " 20

25 " 29

30 " 32



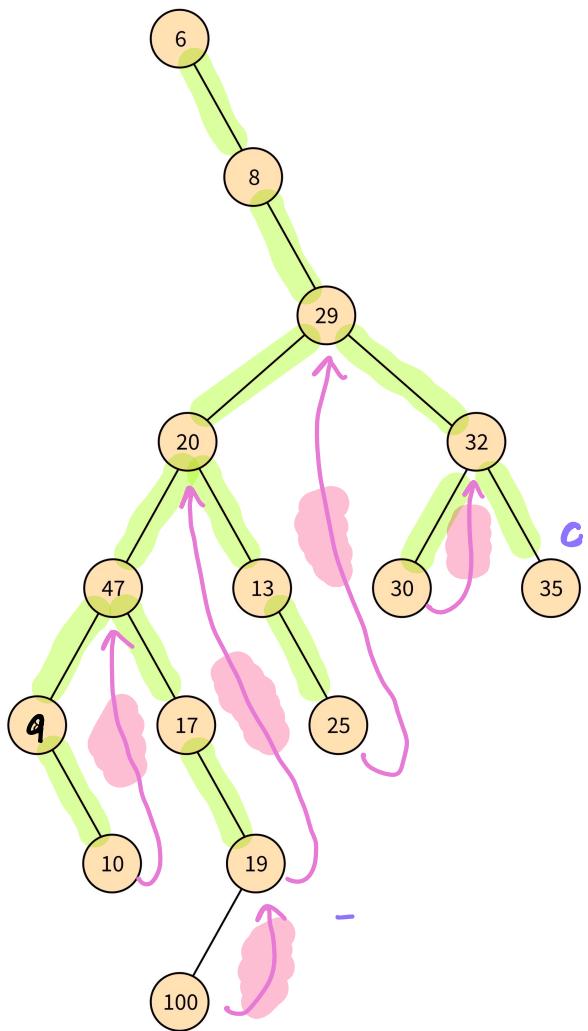
Observations :

For Nodes with LEFT CHILD

- Inorder Predecessor of a node = Rightmost child of curr.left
- Inorder Predecessor of a node doesn't have RIGHT CHILD

Right child = NULL

We can use this to make connection to the next node in its Inorder.

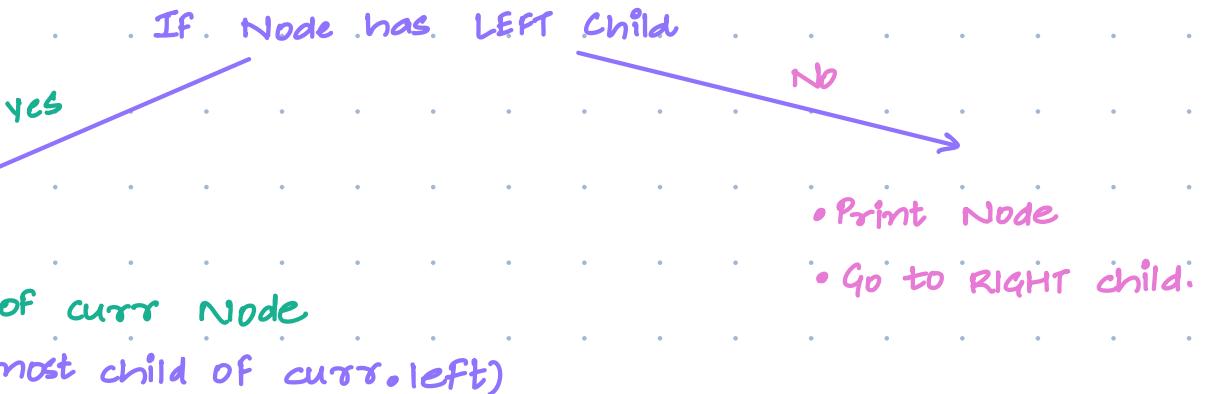


6 8 9 10 47 17 100
19 20 13 25 29
30 32 35

Node temp = curr.left
while (temp.right != NULL)
temp = temp.right;



Approach:



Check if the connection exists b/w IP & curr node

- YES →
- Break the connection
 - Print the curr node value.
 - Go to RIGHT child
 $curr = curr.right$
- NO →
- Make Connection
 - $curr = curr.left$
-
- ```
graph TD; A[Check if the connection exists b/w IP & curr node] -- YES --> B["• Break the connection
• Print the curr node value."]; A -- NO --> C["• Make Connection
• curr = curr.left"]; B --> D["• Go to RIGHT child
curr = curr.right"];
```



&lt;/&gt; Code

void MorrisInorder (Node root) {

Node curr = root;

while (curr != NULL) {

if (curr.left == NULL) {

print (curr.val);

curr = curr.right;

}

else {     || Curr has left child

|| Find IP

Node temp = curr.left;

while (temp.right != NULL &amp;&amp; temp.right != curr)

temp = temp.right;

|| Connection doesn't exist

if (temp.right == NULL) {

temp.right = curr;

curr = curr.left;

}

|| Connection already exist

else if (temp.right == curr) {

temp.right = NULL;

print (curr.val);

curr = curr.right;

}

T.C : O(N)  
S.C : O(1)

y

-3







