

“A LITTLE PROGRESS EACH
DAY ADDS UP TO BIG
RESULTS.”

SATYA NANI



Hello Everyone !!

Class will start at 7:10 IST.

Introduction

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-  Technical Lead at Qorix | Ex - ZF TCI | Ex - Bosch
-  BTech from NIT Jalandhar.
-  Remote Instructor at Scaler
-  Hail from Patiala, Punjab | Current residing in Hyderabad

Few terms that you shall see/hear throughout the course!

1. PSP (Problem Solving Percentage) -

Solved Assignment Problems / Total Open Assignment Problems

- There are two types of section - Assignment and Additional. Assignment section consists of implementation of the problems done in class. PSP is calculated based on only Assignment Problems
- Additional Problems are slight modifications of assignment problems, they are not part of PSP but once you're done with assignment, we highly recommend to complete additional problems as well.
- Try to keep PSP least 80% no matter what. It shall really help you stay focused and we have seen in the past that people with **$\geq 80\%$** , do well in interviews.

2. Attendance

- Try to maintain at least **85% attendance** either through classes or by watching recordings.
- Though I will recommend you to come to classes regularly because otherwise it may create backlogs.
- So, I expect all of you to attend live classes and if for any reasons you are unable to, then please send me a message stating the reason.



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Schedule for next one month

- Introduction to Problem Solving
- Time Complexity
- Introduction to Arrays
- Prefix Sum
- Carry Forward & Subarrays
- Sliding Window & Contribution Technique
- Memory Management
- Sorting Basics
- 2D Matrices
- Bit Manipulation Basics
- Strings Basics
- Interview Problems
- Contest [covers full Intermediate DSA]



Contest will be organised after Intermediate Module

- It will be for **1.5 hours** and will be conducted within class duration followed by Contest Discussion (Instructor shall be discussing contest problems).
- If for any reason you are unable to pass the contest, then we shall be having re-attempts as well, therefore nothing to worry. (We will provide more info on re-attempts and the passing criteria moving forward. Most likely, there will be 4 questions out of which 3 needs to be solved)
- Contests are critical to retain what you have learnt and measuring where you need improvement. Please take contests seriously.

FAQs

- Notes will be uploaded after the class.
- Assignment will be unlocked after the class ends.
- There is no deadline for assignments.

Lecture Days:

Monday } 7:00 AM. IST
Wednesday } We start at sharp 7:05
Friday

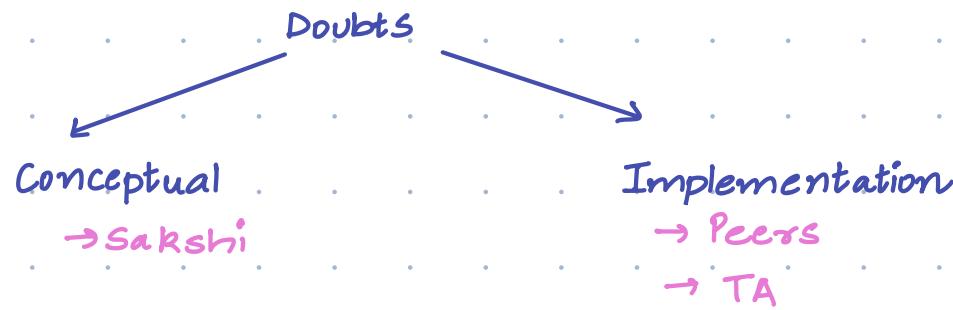
[5-10 min break]

7:05

8:30

9:30

Doubts



Mode of Communication: Whatsapp

- Announcement Group
- Discussion Group
- (Links on Notice Board)

Introduction to Problem Solving

TABLE OF CONTENTS

1. Count the Factors
2. Optimisation for counting the Factors
3. Check if a number is Prime
4. Sum of N natural numbers
5. Definition of AP and GP
6. How to find the number of times a piece of code runs i.e number of iterations
7. How to compare two algorithms



Notes



Factor

i is a factor of $N \rightarrow i$ will divide N completely.

$$N \% i == 0$$



Remainder

$$N = 100$$

$$i = 5$$

$$100 \% 5 = 20$$

$$N \% i$$

< Question >: Given N . Find the count of positive factors of N . ($N > 0$)

QUIZ

1. $N = 24$

Factors : 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 12, 24

ans : 8

QUIZ

2. $N = 10$

Factors : 1, 2, 5, 10

ans : 4

Observations :

Min Factor of a No : 1

Max " " " " : N



</> Pseudo Code

```
int CountFactors (int N) {
```

```
    int count = 0;
```

```
    for (i=1; i <= N; i++) { → N iterations
```

```
        if (N % i == 0) {
```

```
            count++;
```

```
y
```

```
return count;
```

```
y
```

$N = 10$

$i : 1 - 10$

$\cancel{1} \cancel{2} \cancel{3} \cancel{4}$

$5 \cancel{6} \cancel{7} \cancel{8} \cancel{9} \cancel{10}$

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Servers → 1 GHz

Assumption: 10^8 iterations are executed in 1s.

N	Iterations (N)	Execution Time
10^8	10^8	1s
10^9	10^9	10s
10^{18}	10^{18}	$10^{10}s$ $\approx 317\text{ yrs}$

5 apples - 50rs

1 apple - $\frac{50}{5}$

= 10

3 apples = $10 * 3$
= 30

$10^8 - 1s$

$1 - \frac{1}{10^8}$

$$\frac{1}{10^{18}} - \frac{1}{10^8} = 1 * 10^8 = 10^{10}$$

$$10^9 - \frac{1 * 10^9}{10^8} = 10$$



Optimisation

$i * j = N \rightarrow i \text{ & } j \text{ are factors of } N$
 $j = \frac{N}{i} \rightarrow i \text{ & } \frac{N}{i} \text{ are factors of } N..$

$$N = 24$$

i	N/i
1	≤ 24
2	≤ 12
3	≤ 8
4	≤ 6
6	4
8	3
12	2
24	1

$$i \leq N/i$$

Part 1

$$N = 100$$

i	N/i
1	≤ 100
2	≤ 50
4	≤ 25
5	≤ 20
10	≤ 10
20	5
25	4
50	2
100	1

Part 2

Observations :

1) Factors are Repeating | Factors exists in pairs.

2) Iterate till $i \leq \frac{N}{i}$

$$\Rightarrow i^2 \leq N$$

$$\Rightarrow i \leq \sqrt{N}$$



</> Pseudo Code

```
int CountFactors (int N) {
```

```
    count = 0;
```

```
    for (i = 1 ; i <= √N ; i++) {
```

$1 : \sqrt{N}$

```
        if (N % i == 0) {
```

\sqrt{N} iterations

```
            if (i == N/i) {
```

```
                count = count + 1;
```

```
y
```

```
            else {
```

```
                count = count + 2;
```

```
y
```

```
y return count;
```

$N = 100$

$i : [1 : \sqrt{100}] = [1 : 10]$

$i = 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$

$count = 0, 4, 6, 8, 10$

N	Iterations (\sqrt{N})	Execution Time
10^{18}	$\sqrt{10^{18}} = 10^9$	$\frac{1}{10^8} \times 10^9 = 10 \text{ s}$

Servers $\rightarrow 1 \text{ GHz}$

Assumption: 10^8 iterations are executed in 1s.



Prime Numbers

Number having 2 factors
(1, N)

QUIZ

How many prime numbers are there?

10, 11, 23, 2, 25, 27, 31

ans : 4

< Question > : Given a number N. Check if it is prime or not.

< /> Pseudo Code

```
boolean CheckPrime(int N) {  
    if (CountFactors(N) == 2)  
        return true;  
    else  
        return false;  
}
```



Range

$[a, b]$ → This type of range means Both a & b INCLUDED.

(a, b) → " " " " " " " " EXCLUDED.

$[a, b)$ → Include a & Exclude b

$(a, b]$ → Exclude a & Include b .

QUIZ

How many numbers are in range?

$[3, 10] \rightarrow 3, 4, 5, 6, 7, 8, 9, 10$

ans : 8

QUIZ

How many numbers are in range?

$[a, b] \rightarrow b - a + 1$

$$[3, 10] \rightarrow 10 - 3 + 1 = 8$$

$$[a, b) \rightarrow b - a + 1 - 1 = b - a$$

$$(a, b] \rightarrow b - a + 1 - 1 = b - a$$

$$(a, b) \rightarrow b - a - 1$$

Sum of first N numbers

.Gauss

QUIZ

$$1 + 2 + 3 + 4 + 5 - - - - - \quad 98 + 99 + 100$$

$$S = 1 + 2 + 3 + 4 + 5 - - - - - 98 + 99 + 100 - \textcircled{1}$$

$$S = 100 + 99 + 98 + 97 + 96 - - - - - \cdot 3 + 2 + 1 - ②$$

① + ②

$$2S = \underline{101 + 101 + 101 + 101} \quad - \quad \underline{\dots} \quad 101 + 101 + 101$$

100 times

$$2S = 101 * 100$$

$$S = \frac{101 * 100}{2} = 5050$$

Sum of 1st N natural no's

$$S = 1 + 2 + 3 - \dots - (n-1) + n$$

$$S = N + (N-1) + (N-2) \quad - - - - - \quad 2 + 1$$

$$2S = (N+1) + (N+1) + (N+1) = \dots - \dots - \dots - (N+1) + (N+1)$$

N times

$$g_C = z^* (N+1)$$

$$S = \frac{N * (N+1)}{2}$$



What is a iteration?

The no OF times loop runs.

Quiz- 7

How many times will the below loop run ?

```
for(i -> 1 to N)      for (i=1 ; i≤N ; i++)
{
    if(i == N) break;
}
```

$i : [a, b]$

$$\begin{aligned} \text{No. of times loop} &= b-a+1 \\ \text{will run} &= n-1+1 = n. \end{aligned}$$

Quiz- 8

How many iterations will be there in this loop ?

```
for(i -> 0 to 100){
    s = s + i + i^2;
}
```

$i : [a, b]$

$$\begin{aligned} \text{No. of times loop} &= b-a+1 \\ \text{will run} &= 100-0+1 \\ &= 101 \end{aligned}$$



Quiz- 9 How many iterations will be there in this loop?

```
func(){
    for(i -> 1 to N){
        if(i % 2 == 0){
            print(i);
        }
    }
    for(j -> 1 to M){
        if(j % 2 == 0){
            print(j);
        }
    }
}
```

i: [1, N]
N iterations

j: [1, M]
M iterations .

Total iterations : N+M.



Geometric Progression

- Series where the ratio of two consecutive terms remains same.

$$\begin{array}{cccc} a & ar & ar^2 & ar^3 \\ 5, 10, 20, 40, 80, 160, 320, 640 \end{array}$$

$$\frac{10}{5} = 2$$

r : Common ratio = 2

a : First term of GP = 5

$$\frac{20}{10} = 2$$

$$\frac{40}{20} = 2$$

$$a, ar, ar^2, ar^3, \dots$$

Sum of first N terms of a GP :

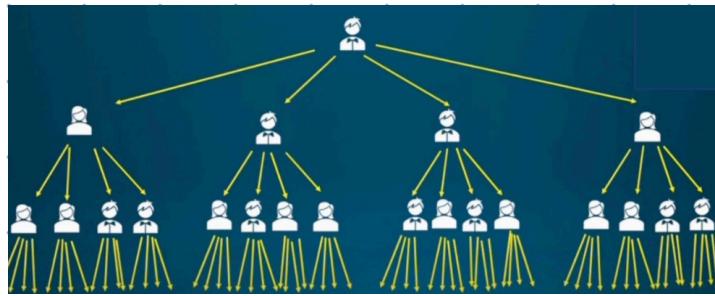
$$\frac{a(r^n - 1)}{r - 1}$$

$$r \neq 1$$

$$N^{\text{th}} \text{ term of GP} : ar^{N-1}$$



Real life example of GP



1, 4, 16, - - -

$$a = 1$$

$$r = 4/1 = 4$$

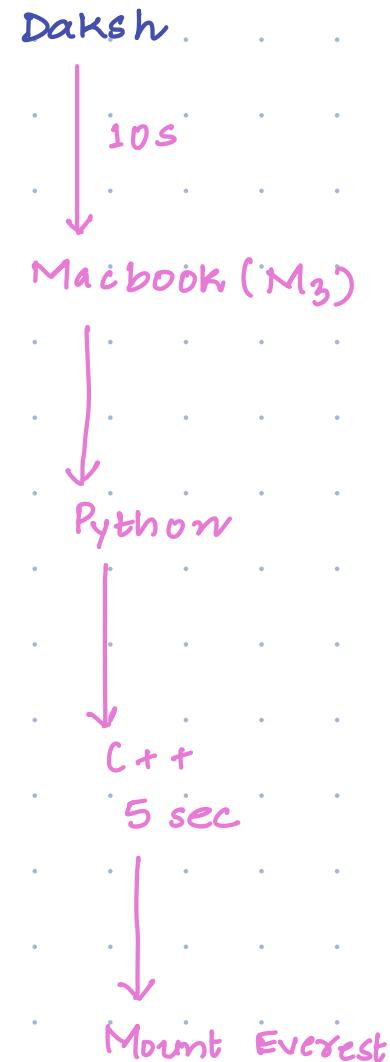
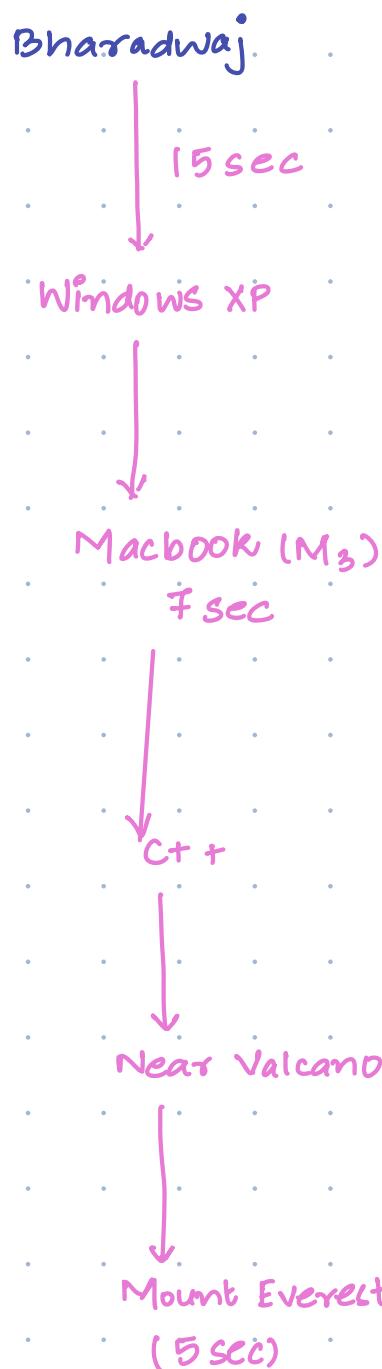
Number of people at 8th level: $a r^7 = 1 * 4^7 = 4^7$

Sum till 8th level: $\frac{a(r^N - 1)}{r - 1} = \frac{1(4^8 - 1)}{4 - 1} = \frac{4^8 - 1}{3}$



How to compare two algorithms?

$N = 10^8$. Given N elements, sort the elements in increasing order.



Execution time is not the good criteria to compare a algo. Since it depends on many external factors.

Criteria to compare a algo: No of Iterations

