

Searching - 1

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Notes



Searching

finding something

Phone lost

Brand, IMEI, Model

(what to search)

Target

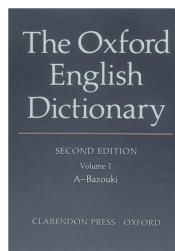
Lost Location.

(where to search)

Search Space.

1. Searching a word in newspaper

Searching a word in dictionary



Target : Word

Search Space : Dictionary / Newspaper.

2. Search phone no in Contact List

Search phone no in diary

Target : Phone NO

Search Space : Contact List, Diary.

Obs :

Searching becomes easy if the search space is SORTED



Search "Dog" in Physical Dictionary

dict = { A B C D E F G H - - - - Y Z }

↑ ↑ ↑

We randomly open a page & discard one of the sides & move to the other side.

Binary Search

Dividing the array into 2 halves & based on some condition we discard one of the half.

When can we apply Binary Search?

After dividing the array into 2 halves, if we are able to discard one of the half using some conditions we can apply BS.

Note: Data may or mayn't be sorted.



< Question > : Given a sorted arr[]. Search if an element K is present or not.

0	1	2	3	4	5	6	7
3	6	9	12	14	19	20	23

K = 12 True.

K = 17 False.

💡 BF Approach

Linear Search

T.C : O(N)

S.C : O(1)

💡 Idea - 2 Binary Search

Target : K

Search Space : Entire Array

== K.



A[mid] == k Return True.

< K



A[mid] < k Discard Left
Move towards Right.

> K



A[mid] > k Discard Right side
Move towards Left.

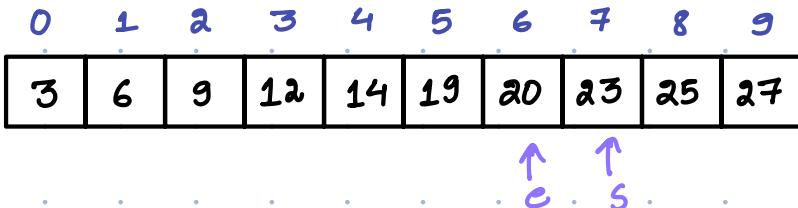


0	1	2	3	4	5	6	7	8	9
3	6	9	12	14	19	20	23	25	27

 $K = 12$

↑
me
↑
s

s	e	$m = s + e / 2$	A[m]	r	A[m]	
0	9	4	14	12 < 14	Go to LHS. $e = m - 1$	
0	3	1	6	12 > 6	Go to RHS $s = m + 1$	
2	3	2	9	12 > 9	Go to RHS $s = m + 1$	
3	3	3	12	12 == 12	Return True	



$K = 21 \rightarrow \text{False.}$

s	e	$m = s + e / 2$	$A[m]$	K	$A[m]$	
0	9	4	14	21	$21 > 14$	Go to RHS $s = m + 1$
5	9	7	23	21	$21 < 23$	Go to LHS. $e = m - 1$
5	6	5	19	21	$21 > 19$	Go to RHS $s = m + 1$
6	6	6	20	21	$21 > 20$	Go to RHS $s = m + 1$
7	6	Search Space Exhausted. ($s > e$)				Return False.



</> Code

```
boolean search ( int [ ] A , int K ) {  
    int n = A . size ( ) ;  
    int s = 0 , e = n - 1 ;  
    while ( s <= e ) {  
        m = ( s + e ) / 2 ;  
        if ( A [ m ] == K ) {  
            return True ;  
        }  
        else if ( A [ m ] < K ) { // Move to RHS .  
            s = m + 1 ;  
        }  
        else { // A [ m ] > K  
            e = m - 1 ; // Move to LHS .  
        }  
    }  
    return False ;  
}
```

$$N \rightarrow \frac{N}{2} \rightarrow \frac{N}{4} - \dots = 1$$

T.C : $O(\log N)$
S.C : $O(1)$



< Question > : Given a sorted arr[N]. Find first occurrence of K.

If K is not present in array then return -1

$\text{arr[]} \rightarrow [$	-5	-5	-3	0	0	1	5	5	5	5	8	10	10	15]
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
$K = 5 \rightarrow 6$															
$K = -5 \rightarrow 0$															
$K = 20 \rightarrow -1$															

m

BF Approach

linear Search

T.C : O(N)

S.C : O(1)

Idea - 2

Target : 1st occ. of K.

Search Space : Entire Array.



$A[\text{mid}] < k$ Discard Left Move to RHS.
 $s = m + 1$.



$A[\text{mid}] > k$ Discard Right Move to LHS.
 $e = m - 1$



$A[\text{mid}] == k$ Store Mid. as an Ans.
Discard Right & Move to LHS.



</> Code

```
int firstOccurrence (int [ ] A, int K) {
```

```
    int s = 0, e = n - 1;
```

```
    int ans = -1;
```

```
    while (s <= e) {
```

```
        m = (s + e) / 2;
```

```
        if (A[m] == K) {
```

```
            ans = m;
```

```
            e = m - 1;
```

```
}
```

```
        else if (A[m] < K) {
```

```
            s = m + 1;
```

```
}
```

```
        else {
```

```
            e = m - 1;
```

```
}
```

```
}
```

```
    return ans;
```

```
}
```

T.C.: O(log N)

S.C.: O(1)



Unique Element

< Question > : Every element occurs twice except for 1. Find that unique element.



Note : Duplicates are adjacent to each other and array isn't necessarily sorted.

arr[] →	[8	8	5	5	9	9	6	2	2	4	4]
		0	1	2	3	4	5	6	7	8	9	10	

ans : 6.

Idea -1 XOR of all elements.

T.C : O(N)

S.C : O(1)

Idea -2 Hashmap.

T.C : O(N)

S.C : O(N)

Idea -3 binary Search

T.C : O(N)

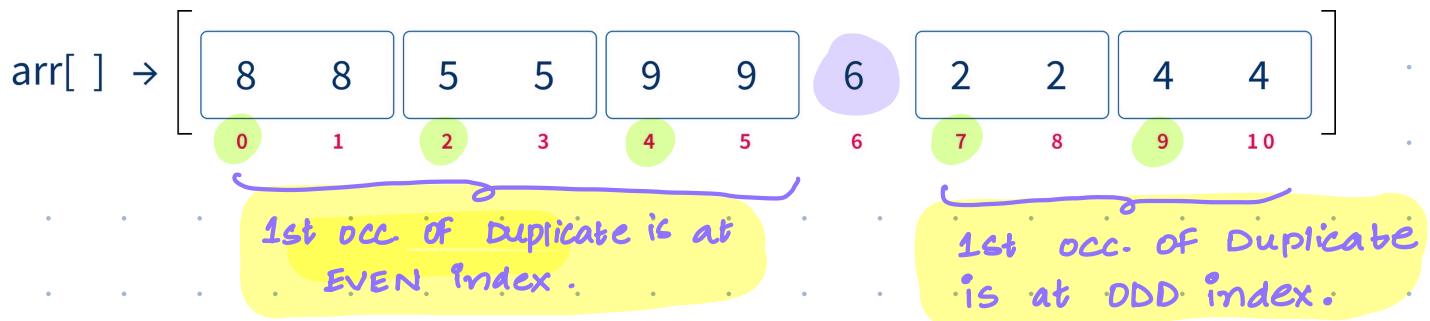
S.C : O(1)



Idea-4 Binary Search.

Target: Unique element

Search Space: Entire Array.



duplicate

 m

duplicate

$A[m] = A[m-1]$

&

$A[m] = A[m+1]$

Unique element
Return $\text{arr}[m]$ 1st occ. of Duplicate
is at EVEN index1st occ. of Duplicate
is at ODD index

Move to RHS.

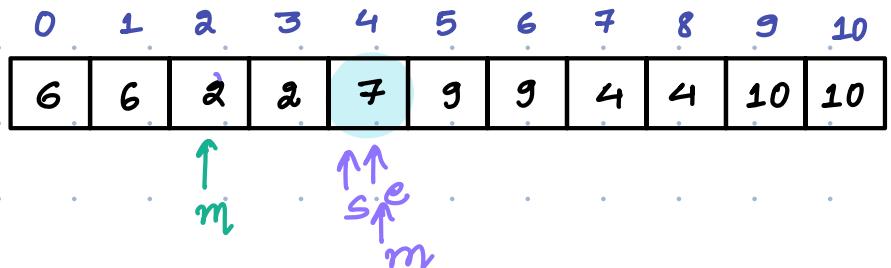
Move to LHS.

Algo :

Find mid & check if it is Unique or Not.

Ans.

check for 1st occ of duplicate & decide which side to move.



s	e	m	$\text{arr}[m]$ Unique?	Is "m" at 2nd occurrence?	$m \bmod 2 = 0$
0	10	5	✗	✗	✗ Go to LHS $e = m - 1$
0	4	2	✗	✗	✓ Go to RHS $S = m + 2$
4	4	4	✓ Return ans.		

</> Code

```
int unique (int arr[]) {  
    n = arr.size();  
  
    if (n == 1) . return arr[0];  
    if (arr[0] != arr[1]) . return arr[0];  
    if (arr[n-1] != arr[n-2]) . return arr[n-1];  
  
    int s = 1, e = n-2;  
  
    while (s <= e) {  
        m = (s+e)/2;  
  
        // Case 1 : Element at m is unique.  
        if (arr[m] != arr[m-1] && arr[m] != arr[m+1])  
            return arr[m];  
  
        // Case 2 : Element at m is Duplicate.  
        if (arr[m] == arr[m-1]) . // If m is at 2nd occ. bring it  
            m = m-1; . to 1st occ.  
  
        if (m%2 == 0)  
            s = m+2;  
        else  
            e = m-1;  
    }  
}
```

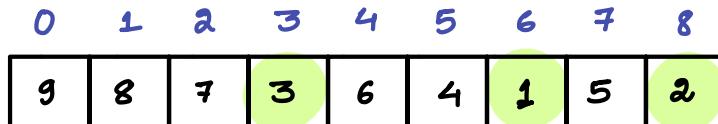
T.C: O(logN)
S.C: O(1)



Local Minima

< Question > : Given an unsorted array of distinct elements. Find any one local minima.

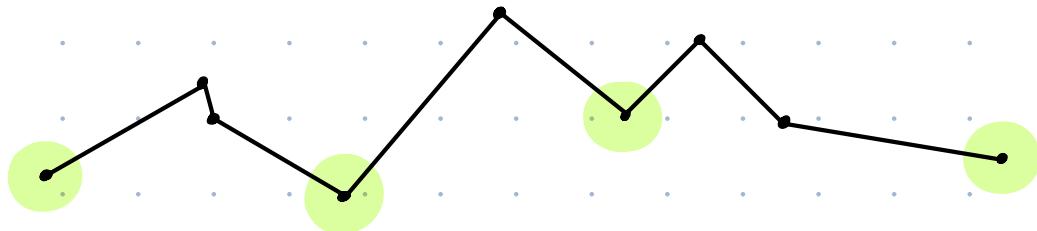
Local Minima : An element which is less than its adjacent neighbours.



Local Minima \rightarrow $\text{arr}[i-1] > \text{arr}[i] < \text{arr}[i+1]$

$\text{arr}[0] < \text{arr}[1]$

$\text{arr}[n-2] > \text{arr}[n-1]$



BF Approach

Iterate & compare each element with its adjacent neighbors.

T.C : $O(N)$

S.C : $O(1)$



Idea

Target : local Minima

Search Space : Entire array

Case: 1



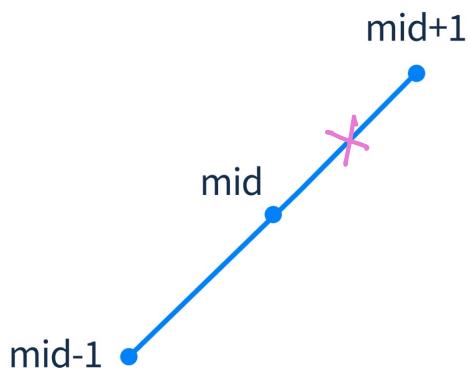
Return arr[mid]

case: 2



Move to RHS.

Case: 3



case: 4



Move to LHS.



Analysing Case 2:

2 options for $(mid-2)$:

① $(mid-2)$

$(mid-2 > mid-1)$

$(mid-1)$ can't be LOCAL MINIMA.



② $(mid-2)$

$(mid-2 < mid-1)$

$(mid-1)$ can't be LOCAL MINIMA.



2 options for $(mid+2)$:

① $mid+2$

$(mid+2 > mid+1)$

$(mid+1)$ is LOCAL MINIMA

② $mid+2$

$(mid+2 < mid+1)$

$(mid+2)$ is LOCAL MINIMA

Observation for LHS :

LHS may or mayn't have
Local Minima.

Observations for RHS :

Definitely 1 Local Minima
on RHS.

Conclusion : LHS may or mayn't have a LOCAL MINIMA but
we are sure definitely there exists a MINIMA on
RHS. so move to RHS.



</> Code

```
int LocalMinima(int [] A) {
```

```
    if (A.size() == 1) return A[0];
```

```
    if (A[0] < A[1]) return A[0];
```

```
    if (A[n-1] < A[n-2]) return A[n-1];
```

```
    s = 1, e = n-2;
```

T.C : O(log N)

S.C : O(1)

```
    while (s <= e) {
```

```
        m = (s+e)/2;
```

|| Case 1 :

```
        if (A[m] < A[m-1] && A[m] < A[m+1])
```

```
            return A[m];
```

|| Case 2 :

```
        else if (A[m] < A[m-1] && A[m] > A[m+1])
```

```
            s = m+1;
```

|| Case 3 :

```
        else if (A[m] > A[m-1] && A[m] < A[m+1])
```

```
            e = m-1;
```

|| Case 4 :

```
        else
```

```
            e = m-1;
```

0	1	2	3	4	5	6	7	8
9	8	7	3	6	4	1	5	10

s	e	m	
0.	8	4	Case 4 : $e = m - 1$
0.	3	1	Case 2 : $s = m + 1$
2.	3	2	Case 2 : $s = m + 1$
3.	3	3	→ Ans. Case 1.

