

Name: **Abhishek Dixit**

Assignment: **Probability Basics**

Batch: **Data Analytics Dec Live Batch**

Question 1: A die is rolled. What is the probability of getting:

(a) An even number

(b) A number greater than 4.

Answer: a) If a die is rolled then the probability of getting an even number is (2,4,6) $\frac{3}{6}$ or we can say that $\frac{1}{2}$.

b) The probability of getting a number greater than 4 will be (5,6) $\frac{2}{6}$ or we can say that $\frac{1}{3}$.

Question 2: In a class of 50 students:

20 like Mathematics (M)

15 like Science (S)

5 like both subjects

What is the probability that a student chosen at random likes Mathematics or Science?

Answer: a) The probability that a student chosen at random likes mathematics science will be:

$$20 + 15 - 5 = 30$$

$$30/50 = \frac{3}{5}$$

The probability of student chosen at random likes mathematics or science is $\frac{3}{5}$.

Question 3: A bag has 3 red and 2 blue balls. If one ball is drawn randomly and is red, what is the probability that the next ball is also red (without replacement)?

Answer: The probability of next ball drawn from bag is red will be $\frac{2}{4}$ which is $\frac{1}{2}$.

Total ball after 1 red ball drawn will be 4(in total) and 2(in red).

Question 4: The population of a school is divided into 60% boys and 40% girls. If you want equal representation of both genders in the sample, which method should you use: Simple Random Sampling or Stratified Sampling? Why?

Answer: **Stratified Sampling** should be used because it ensures equal representation of both boys and girls by sampling separately from each group.

Question 5: The average height of 1000 students = 160 cm. A sample of 100 students shows an average height = 158 cm. Find the sampling error.

Answer: **Sampling Error = Sample Mean – Population Mean**

Sampling error = 158 - 160

Sampling error = **-2 cm**

Question 6: The population mean salary is ₹50,000 with $\sigma = ₹5,000$. If we take a sample of 100 employees, what is the standard error of the mean (SEM)?

Answer: SEM = ₹500

Question 7: In a group of 100 students: 40 like Cricket (C) 30 like Football (F) 10 like both Cricket and Football Find the probability that a student likes at least one sport.

Answer: 40+30-10=60(WHO LIKES AT LEAST ONE SPORT)

So, 60/100 = **0.6 OR 60%**

Question 8: From a deck of 52 cards, two cards are drawn without replacement. What is the probability that both are Aces?

Answer: Probability of first was Ace: **4/52**

Probability of second was Ace: **3/51**

So, $4/52 * 3/51 = 12/2652$
= 1/221

Question 9: A factory produces bulbs with 2% defective rate. If 5 bulbs are chosen at random, what is the probability that all are non-defective?

Answer: Probability a bulb is **non-defective** = $1 - 0.02 = 0.98$ - $0.02 = 0.98$

$P(\text{all non-defective}) = (0.98)^5$

Calculation:

$(0.98)^5 \approx 0.9039$

So, there is about a **90.39%** chance that all 5 bulbs are non-defective.

Question 10: Differentiate between discrete and continuous random variables with examples.

Answer:

Discrete Random Variable	Continuous Random Variable
Takes countable values	Takes uncountable values
Values are usually whole numbers	Values can be any real number within a range
Obtained by counting	Obtained by measuring
Has a probability mass function (PMF)	Has a probability density function (PDF)
Probability of a specific value can be non-zero	Probability of a specific value is zero

Examples

- **Discrete:**
 - Number of students in a class
 - Number of heads when tossing coins
 - Number of defective items
- **Continuous:**
 - Height of students
 - Weight of a person
 - Time taken to complete a task