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PRACTICA - 1

Aim:-
Basic of R software

- 1) R is a software for statistical analysis and data computing.
- 2) It is an effective data handling software and outcome storage is possible.
- 3) It is capable of graphical display.

y) It is an free software.

Solve the following.

$$\begin{aligned} & 4+6+8 \div 2 - 5 \\ & 24+6+8 \div 2 - 5 \\ & [1] 9 \end{aligned}$$

$$\begin{aligned} & 0^2 + |-3| + \sqrt{45} \\ & 272 + \sqrt{(-3)} + \sqrt{45} \\ & [1] 13.7082 \end{aligned}$$

$$\begin{aligned} & 5^3 + 7 \times 5 \times 8 + 46 / 5 \\ & 125 + 280 + 7 * 5 * 8 + 46 / 5 \\ & [1] 414.2 \end{aligned}$$

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$$\begin{aligned} & \sqrt{u_2 + 5 * 3 + 7 / 6} \\ & > \text{sqrt}(u_{12} + 5 * 3 + 7 / 6) \\ \text{T13 } & 5.671567 \end{aligned}$$

5

$$\begin{aligned} & \text{round off} \\ & u_6 \div 7 + 9 \times 8 \\ & \text{round } (u_6 \div 7 + 9 \times 8) \\ \text{T13 } & 79 \end{aligned}$$

$$\begin{aligned} & >c(2, 3, 5, 7) * 2 \\ & [17 \quad 4 \quad 6 \quad 10 \quad 14] \end{aligned}$$

$$\begin{aligned} & <(2, 3, 15, 7) * <(2, 3) \\ & [17 \quad 4 \quad 9 \quad 10 \quad 21] \end{aligned}$$

$$\begin{aligned} & >c(2, 3, 5, 7) * c(2, 3, 6, 2) \\ & [17 \quad 4 \quad 9 \quad 3 \quad 0 \quad 14] \end{aligned}$$

$$\begin{aligned} & >c(1, 6, 2, 3) * ^{(-2, -3, -4)} \\ & [17 \quad -2 \quad -18 \quad -8 \quad -3] \end{aligned}$$

$$\begin{aligned} & >c(2, 3, 5, 7) / 12 \\ & [17 \quad 4 \quad 9 \quad 25 \quad 49] \end{aligned}$$

$$\begin{aligned} & >c(1, 6, 8, 9, 4, 5) / 4(2) \\ & [17 \quad 4 \quad 36 \quad 512 \quad 916] \end{aligned}$$

$$\begin{aligned} & >c(6, 2, 7, 5) / c(4, 5) \\ & [17 \quad 1.60, \quad 0.40, \quad 1.75, \quad 1.00] \end{aligned}$$

$$\begin{aligned} & >x = x_0 \quad >y = y_0 \quad >z = z_0 \\ & >x_{12} + y_{13} + z \\ \text{T13 } & 0.7402 \\ & >\text{sqrt}(x_{12} + y) \\ \text{T13 } & 20.73649 \\ & >x_{12} + y_{12} \\ \text{T13 } & 1300 \end{aligned}$$

44

```

44) > x <- matrix (nrow = 4, ncol = 2, data = c(1,2,3,4,
   5,6,7,8))
> x
     [,1]    [,2]
[1,]    1      5
[2,]    2      6
[3,]    3      7
[4,]    4      8

```

5) find $x+y$ and $2x+3y$ where $x = \begin{bmatrix} 4 & 2 \\ 7 & 5 \end{bmatrix}$

```

> y <- matrix (nrow = 3, ncol = 3, data = c(4,7,9,-2,6,5,
   -3,-6,5))
> y
     [,1]    [,2]    [,3]
[1,]    4      7      9
[2,]   -2      6      5
[3,]   -3     -6      5

```

```

> y <- matrix (nrow = 3, ncol = 3, data = c(10,12,15,
   -5,1,-4,-6,7,4,5))
> y
     [,1]    [,2]    [,3]
[1,]    10     -5      7
[2,]    12     -4     -6
[3,]    15      5      4

```

```

> x+y      [1,]    [2,]    [3,]
[1,]    14      -7     13
[2,]    11      -4     16
[3,]    24      -11    18

```

> 2*x + 3*y

	[1,]	[2,]	[3,]
[1,]	88	-19	33
[2,]	50	-12	41
[3,]	63	-28	21

0.6)

marks of statics of cs pattern A

```

x=c(50, 20, 35, 24, 46, 56, 55, 45, 27, 24,
58, 54, 40, 50, 32, 36, 29, 35, 29)
>x=c(data)

```

```

>breqes6=set(20,60,5)
>a=seq(x,breaks=6,right=FALSE)
>b=qrc(a)
>c=transform(c)

```

45:

a	b	area
1	[20, 25]	3
2	[25, 30]	2
3	[30, 35]	1
4	[35, 40]	4
5	[40, 45]	1
6	[45, 50]	3
7	[50, 55]	2
8	[55, 60]	4

PRACTICAL - 02

Topic:- probability distribution.

1) Check whether the following are p.m.f.

x	p(x)
0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

If the given data is p.m.f then

$$\begin{aligned} \sum p(x) &= 1 \\ \therefore p(0) + (p(1) + p(2) + p(3) + p(4) + p(5)) &= 1 \\ = 0.1 + 0.2 + 0.4 + 0.3 + 0.5 &= 1.0 \end{aligned}$$

$\therefore p(x) \geq 0 \quad \forall x$, it can't be probability function.

$$p(x) \geq 0 \quad \forall x.$$

2)

x	p(x)
1	0.1
2	0.2
3	0.3
4	0.2

The condition for p.m.f is $\sum p(x) = 1$

$$\begin{aligned} \text{So, } \\ \sum p(x) &= p(1) + p(2) + p(3) + p(4) + p(5) \\ &= 0.2 + 0.2 + 0.3 + 0.2 + 0.2 \\ &= 1.1 \end{aligned}$$

∴ The given data is not a p.m.f because sum $p(x) \neq 1$

x	p(x)
10	0.2
20	0.2
30	0.35
40	0.15
50	0.1

The condition for p.m.f is

$$1) \quad p(x) \geq 0 \quad \forall x \text{ satisfy}$$

$$\begin{aligned} 2) \quad \sum p(x) &= 1 \\ \sum p(x) &= p(10) + p(20) + p(30) + p(40) + p(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \\ &= 1 \end{aligned}$$

∴ The given data is p.m.f

Note:

$$\begin{aligned} > \text{Priors} &= \{0.2, 0.3, 0.35, 0.15, 0.1\} \\ > \text{sum (prob)} \end{aligned}$$

717

whether the following is p.d.f
not

$$(i) f(x) = 3-2x; \quad 0 \leq x \leq 1$$

$$(ii) f(x) = 3x^2; \quad 0 < x < 1$$

$$\begin{aligned} i) f(x) &= 3-2x \\ &= \int_0^1 f(x) dx \\ &= \int_0^1 (3-2x) dx \end{aligned}$$

$$= \int_0^1 3dx = \int_0^1 2x dx$$

$$= [3x - 2x^2]_0^1 = 2$$

\therefore the $\int_0^1 f(x) dx = 1$

$$\text{Q) } f(x) = 3x^2 ; \quad x < 2$$

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$$\int_0^1 F(x)$$

$$= \int_0^1 3x^2$$

$$= 3 \int_0^1 x^2$$

$$= \int_0^1 x^2$$

$$= \left[3 \frac{x^3}{3} \right]_0^1 \quad \because x^n = \frac{x^{n+1}}{n+1}$$

$$= x^3$$

$$= 1$$

The $\int_0^1 F(x) = 1$ \therefore It is a p.d.f

$$\frac{1}{2} >x = \text{dbinom}(10, 100, 0.1)$$

```
>x  
[1] 0.1318653
```

$$\stackrel{2}{=} \text{dbinom}(4, 12, 0.2)$$

$$\text{#[1]} \quad 0.1328756$$

$$\text{#[1]} \quad \text{dbinom}(4, 12, 0.2)$$

```
#[1] 0.9274448
```

$$\text{#[1]} \quad 1 - \text{Phi nom}(5, 12, 0.2)$$

$$\text{#[1]} \quad 0.01140528$$

68

3) dbinom(0:5, 5, 0.1)

[1] 0 - 0.69049

[1] 1 - 0.32805

[2] 2 - 0.07290

[3] 3 - 0.00810

[4] 4 - 0.00045

[5] 5 - 0.00001

4) 1) dbinom(5, 12, 0.25)

[1] 0.132414

2) pbinom(5, 12, 0.25)

[1] 0.4455972

3) 1 - pbinom(7, 12, 0.25)

[1] 0.00278151

4) dbinom(6, 12, 0.25)

[1] 0.0491945

PRACTICAL - 3

Topic :- binomial distribution

- # $P(x = x) = \text{binom}(x, n, p)$
- # $P(x \geq x) = \text{binom}(x, n, p)$
- # $P(x > x) = 1 - \text{binom}(x, n, p)$
- # If x is unknown
 $P_1 = P(x \leq x) = \text{binom}(n, n, p)$

Find the probability of exactly 10 success
in hundred trials with $p = 0.1$

Suppose there are 12 mcq, each question has
5 options out of which 1 is correct. Find the
probability of having exactly 4 correct answers

- i) Almost 5 correct answers.
- ii) more than 5 correct answers.

Find the complete distribution when $n = 5$
and $p = 0.1$

$n = 12, P = 0.25$ Find the following problems

- i) $P(x = 5)$
- ii) $P(x \leq 5)$
- iii) $P(x > 7)$
- iv) $P(5 \leq x \leq 7)$

Ex

- 5.) The probability of a salesman making a sale of 0.15. Find the probability of.
- i) No sales out of 10 customer
 - ii) more than 3 ter sales out of 20 customer.

6.) A sales man has 20% probability of making a sale to customer out of 30 customers what minimum number of sales he can make with 80% of probability.

7.) X follows binomial distribution with $n = 10$, $p = 0.1$.

Plot the graph of p.m.f. and c.d.f.

```
5) dbinom(0, 10, 0.15)
```

```
1] 0.1968744
```

```
7) -> binom(3, 20, 0.15)
```

```
1] 0.352248
```

```
b) dbinom(0.88130, 0.2)
```

```
1] 9
```

```
3) >n=10
```

```
>p = 0.3
```

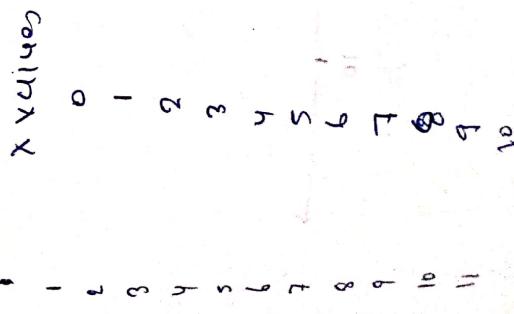
```
>x = 0:10
```

```
>prob = dbinom(x, n, p)
```

```
>cumprob = pbinom(x, n, p)
```

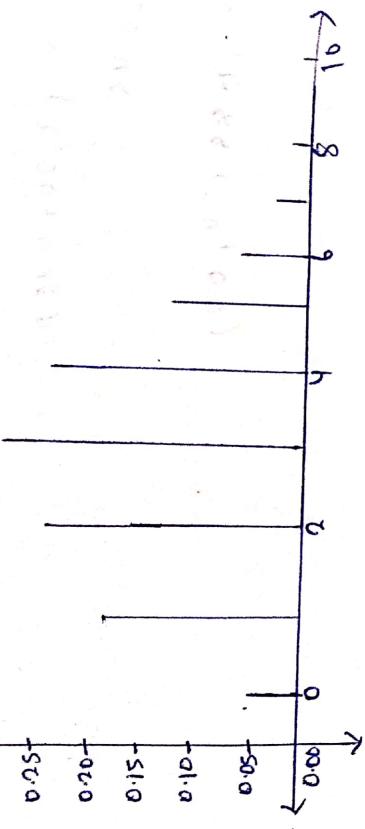
```
>cumprob = pbisom(x, n, p)
```

```
>d = datafram("x values")  
>print(d)
```

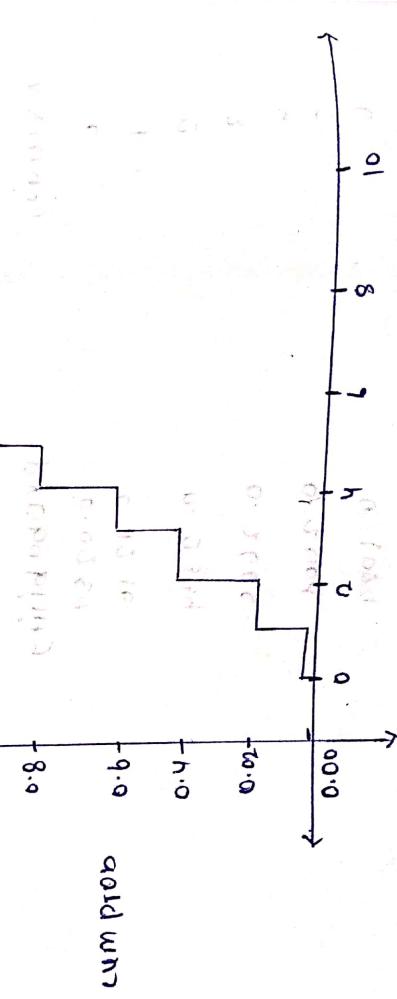


50

> hist(x, prob="in")



> plot(x, cumprob, "s")



PRACTICAL -IIAim:- Normal Distribution

```
# P(x=x) = dnorm(x, mu, sigma)
# P(x≤x) = pnorm(x, mu, sigma)
# P(x>x) = 1 - pnorm(x, mu, sigma)
```

To generate random number from a normal distribution (in random numbers)
The code is rnorm(n, mu, sigma)

- Q1) A random variable X follows normal distribution with mean = $\mu = 12$, $\sigma = \sigma = 6 = 3$. Find
- $P(X \leq 15)$
 - $P(10 \leq X \leq 13)$
 - $P(X > 14)$
 - Generate 5 observations (RANDOM NUMBERS)

Ans

```
R> p1 = rnorm(15, 12, 3)
```

```
[1] 0.8413447
```

```
> cat("p1 = ", p1, "\n", p2)
```

```
> p2 = rnorm(15) = 0.8413447.
```

Q2) $p_1 = pnorm(13, 12, 3) = \text{pnorm}(10, 12, 3)$

```
[1] 0.3780661
```

1.8

$$> p(10 < x < 13) = 0.378066$$

iii) $p_3 = 1 - \text{pnorm}(14, 12, 3)$

> p_3

T1) 0.2524925

> cat("P(x > 14) = ", p3)

$$p(x > 14) = 0.2524925$$

> rnorm(5, 12, 3)

T1) 14.98663 12.51618 13.14904 14.98075

?.) x follows normal distribution with

$$\mu = 10 \quad \sigma = 12 \quad \text{find } ?$$

i) $P(x \leq 7)$

ii) $P(5 < x \leq 12)$

iii) $P(x > 12)$

iv) generate 10 random observation
v) find k such that probability $P(x < k) = 0.4$.

Ans

i) $p_1 = \text{pnorm}(7, 10, 2)$

T1) 0.6668072

> cat("P(x < 7) = ", p1)
 $P(x < 7) = 0.6668072$

ii) $p_2 = \text{pnorm}(12, 10, 2) - \text{pnorm}(5, 10, 2)$

T1) 0.8351351

> cat ("P(X < x < 12) = ", p2)
 $P(15 < X < 12) = 0.8351351$

iii) $p_3 = 1 - \text{pnorm}(12, 10, 2)$

11) 0.1586553

> cat ("P(X > 12) = ", p3)

$P(X > 12) = 0.1586553$

> rnorm(10, 10, 2)

11. 986324	12. 155504	7. 130492
10. 519359	5. 637988	10. 959968
7. 988735	9. 336612	8. 115370
13. 652133		

> qnorm(0.4, 10, 2)
 13.493306

ii) Generate 5 random number from a normal distribution
 with mean = 15 & s.d = 4
 find : sample mean, median, s.d and print (cat)

4) $X \sim N(30, 100)$ ($s^2 = 6 = 10$) Find only
 p_1, p_2 -- (no cat command)

56.

A) Ans

```
> p1 = rnorm(40, 30, 10)
> p1
[1] 0.8413447
p2 = 1 - pnorm(35, 30, 10)
> p2
[1] 0.3085375
> p3 = pnorm(35, 30, 10) - pnorm(25, 30, 10)
[1] 0.3829244
> qnorm(0.6, 30, 10)
[1] 32.53347
```

B) Ans

```
> x = rnorm(5115, 4)
> x
[1] 16.03602 12.58878 16.91096 17.37383
> am = mean(x)
> am
[1] 15.01140
> med = median(x)
> med
[1] 16.43602
```

> variance = (n-1) * var(x) / n
> variance
[1] 2.9636

```

sd = sqrt(varience)
sd
[1] 1.72771
> cat ("Sample mean is = ", meo)
[1] "Sample mean is = 15.67034"
> sample
sample median is = "me"
> cat ("Sample mean is = 15.67024"
sample mean is median is = "me")
> cat ("Sample median is = 16.43602"
sample sd is = "sd")
> cat ("Sample sd is = 1.72771"
sample

```

plot the standard normal graph.

```

ans x = seq (-3, 3, by = 0.1)
y = dnorm (x)
plot (x, y, xlab = "x values", ylab = "probability",
main = "standard normal graph")

```

PRACTIC AL - 05

Aim: Normal & T-test.

- (Q1.) Test the Hypothesis $H_0: \mu = 15$, $H_1: \mu \neq 15$.
Random sample of size 400 is drawn and it is calculated the sample mean is 14. And the standard deviation is 3. Test the hypothesis at 5% level of significance.

$m \rightarrow$ mean \rightarrow population
 $s \rightarrow$ std $n \rightarrow$ sample size.

```
sd  
> m0 = 15  
> mx = 14  
> sd = 3  
> n = 400  
> zw = (mx - m0) / (sd / (sqrt(n)))  
> zw  
[1] -6.666667
```

```
> cat("calculated value at z is = ,")  
calculated value at z is = ,  
> cat("calculated value at z is = -6.666667  
> pvalue = 2 * (1 - pnorm(abs(z(w))))  
> pvalue  
[1] 2.616798e-11  
Since p value is less than 0.05 we reject  
H0.  $\mu = 15$ .
```

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e) Test the hypothesis $H_0: \mu = 10, \mu \neq 10$
Random sample of size 400 is drawn with sample
mean 10.2 and standard deviation 2.25. Test the
hypothesis at 5% level of significance.

$$\text{Soln: } H_0: \mu_0 = 10$$

$$H_1: \mu \neq 10$$

$$H_0: \sigma_0 = 2.25$$

$$H_1: \sigma \neq 2.25$$

$$H_0: n = 400$$

$$H_1: n \neq 400$$

$$Z_{\text{cal}} = \frac{(m_x - m_0)}{\left(\sigma_0 / \sqrt{n} \right)}$$

$$Z_{\text{cal}}$$

$$1.7777778$$

$$\begin{aligned} &> \text{cat}(\text{"calculate value of z is"} = 1, 2, \text{cal}) \\ &\text{calculate} = 2 * (1 - pnorm(qbs(zcal))) \\ &\rightarrow pValue \\ &0.07544036. \end{aligned}$$

3) Test the hypothesis No proportion of smokers in a college is 0.2 a sample is collected and sample proportion is calculated as 0.125. Test the hypothesis at 5% Level of significance (sample size $n = 400$)
 $P \rightarrow \text{population}$
 $p \rightarrow \text{sample}$.

Solution : $\geq p = 0.2$

$$\geq p = 0.125$$

$$\geq n = 400$$

$$\geq \varnothing = 1 - p$$

$$\geq z_{\text{cal}} = (p - \varnothing) / (\sqrt{\varnothing(1-\varnothing)/n})$$

$\geq z_{\text{cal}}$

$$[1] - 3.75$$

(Q.4.)

Last year farmers lost 20% of their crops. A random sample of 60 fields are collected with found that of field crops are insect damaged. Test the hypothesis at 1% level of significance.

$$\begin{aligned} p &= 0.2 && \text{(capital)} \\ P &= 9/60 && \end{aligned}$$

Solution :

$$\geq p = 0.2$$

$$\geq p = 9/60$$

$$\geq n = 60$$

$$\begin{aligned} \geq z_{\text{cal}} &= (p - \varnothing) / (\sqrt{\varnothing(1-\varnothing)/n}) \\ \geq z_{\text{cal}} & \end{aligned}$$

$$[1] 0.9682458$$

$$\begin{aligned} \geq p \text{ value} &= 2 * (1 - \text{norm}(\text{abs}(z_{\text{cal}}))) \\ \geq p \text{ value} & \end{aligned}$$

$$[1] 0.3329216$$

\therefore The value is 0.1 so value is accepted.

The Hypothesis $H_0: \mu = 12.5$ from the following sample at 5% level of significance.

```
> x = c(12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.94,
      11.89, 12.16, 12.04)
```

```
> n = length(x)
```

```
> n
```

```
[1] 10
```

```
> mx = mean(x)
```

```
> mx
```

```
[1] 12.167
```

```
> var = (n-1) * var(x)/n
```

```
> variance
```

```
[1] 0.019521
```

```
> sd = sqrt(variance)
```

```
> sd
```

```
[1] 0.1397176
```

```
> m0 = 12.3
```

```
> t = (mx - m0) / (sd / sqrt(n))
```

```
> t
```

```
[1] -8.894909
```

```
> pvalue = 2 * (1 - pnorm(abs(t)))
```

```
> pvalue
```

```
[1] 0
```

∴ The value is less than 0.05 the value is accepted.

PRACTICAL No-05

Aimee - large sample test.

- (Q.1.) Let the population mean (μ) the amount spent by customer in a restaurant is 250. A sample of 100 customers selected. Sample mean is carrying as 272 and SD as 30. Test the hypothesis that population mean is 250 or not at 5% level of significance.

- (Q.2.) In a random sample of 100 students it is found that 750 use blue pen. Test the hypothesis that population proportion is 0.8 at 1% level of significance.

(Q.1) Solution:

$$\begin{aligned}
 H_0 &= H_0 : \mu = 275 \text{ against } H_1 : \mu \neq 275 \\
 &> \mu_0 = 250 \\
 &> \mu_x = 275 \\
 &> n = 100 \\
 &> \sigma_d = 30 \\
 &> Z_{\text{cal}} = (\mu_x - \mu_0) / (\sigma_d / \sqrt{n}) \\
 &> Z_{\text{cal}} = [1] 8.233333 \\
 &> p\text{-value} = 2 * (1 - \text{norm}(Z_{\text{cal}})) \\
 &> p\text{-value} \\
 &= 0.110
 \end{aligned}$$

?cat ("zcal", "zcal")

?zcal : 8.3333333

?cat ("pvalue", "pvalue")
?cat ("pvalue", "pvalue")

pvalue : 0

i. p value = 0 < 0.05 therefore reject H₀ at 5% level of significance.

ii. H₀: p = 0.8 against H₁: p ≠ 0.8

>p = 0.8

>q = 1-p

>p = 750 / 1000

>n = 1000

>zcal = (p - q) / (sqrt(p * q / n))

>zcal

117 - 3.95 284.7

p value = 2 * (1 - pnorm(zabs(zcal)))

>pvalue

117 7.7268e - 00505

i. The value is less 0.01 we reject H₀

Q)

Two random sample of size 1000 & 2000 are drawn from two population with the same SD = 2.5. The sample means are 67.5 & 68 respectively. Test the hypothesis H₀: μ₁ = μ₂ against H₁: μ₁ ≠ μ₂ at 5% level of significance.

Hospital	Hospital (A)	Hospital (B)
Size	84	34
mean	61.2	59.4
S.D.	7.9	7.5

(Q.4) The study of noise level in two hospitals is given below. Test the claim that the two hospitals have same level of noise at one (1%) level of significance.

(Q.5) In a sample of 600 students in a college who use blue ink. Test the Hypothesis that the proportion of students using blue ink in two colleges are or not. At 1% level of significance,

$$(Q.3) H_0: \mu_1 = \mu_2 \text{ vs } H_1: \mu_1 \neq \mu_2$$

$$\begin{aligned} > n_1 &= 1000 \\ > n_2 &= 2000 \\ > \bar{x}_1 &= 67.5 \\ > \bar{x}_2 &= 68 \\ > S.D. &= 2.5 \\ > Z_{cal} &= (\bar{x}_1 - \bar{x}_2) / \sqrt{\left(\frac{s^2}{n_1} + \frac{s^2}{n_2}\right)} \end{aligned}$$

? zcal = 5.163978

? cut (zcal : "zcal")

? n1 = 5.163978

? pvalue = 2 * (1 - pnorm(qabs(zcal)))

? pvalue

? cut(, pvalue:, , pvalue)

? pvalue: 6.241736e-07

? rejected.

? n1 = 84

? n2 = 34

? mx1 = 61.2

? mx2 = 59.4

? sd1 = 7.9

? sd2 = 7.5

? zcal = (mx1 - mx2) / sqrt((sd1^2/n1) + (sd2^2/n2))

? zcal

? 1.162528

? pvalue = 2 * (1 - pnorm(zcal))

? pvalue

? cat("pvalue:", pvalue)

? pvalue: 6.2450211

? pvalue: 6.2450211

\therefore The value is greater than 0.01 use accept H_0 .

$$\begin{aligned}
 &> n_1 = 600 \\
 &> n_2 = 900 \\
 &> p_1 = 400/600 \\
 &> p_2 = 450/900 \\
 &> z_{\text{cal}} = (p_1 - p_2) / \sqrt{q * (p * q * (1/n_1 + 1/n_2))} \\
 &\quad [1] 6.381534 \\
 &> pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}}))) \\
 &> \text{pvalue} \\
 &[1] 1.753222e-10
 \end{aligned}$$

\therefore Value is less than 0.01 the value is rejected.

Q. 6)

$$\begin{aligned}
 &\text{First Sample size:} \\
 &H_0: p_1 = p_2 \text{ as } H_1: p_1 \neq p_2 \\
 &n_1 = 200 \\
 &n_2 = 200 \\
 &p_1 = 44/200 \\
 &p_2 = 30/200
 \end{aligned}$$

$$\begin{aligned}
 &n_1 = 200 \\
 &n_2 = 200 \\
 &p_1 = 44/200 \\
 &p_2 = 30/200 \\
 &p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2) \\
 &q = 1 - p
 \end{aligned}$$

```
7 val 1.802741  
1] pvalue = 2 * (1 - pnorm(abs(zval)))
```

```
7 pvalue
```

```
1] 0.07142888
```

Albeit: greater than 0.05.

① Topic: small sample Test.

Q.1) The marks of 10 students are given by
 $63, 63, 66, 67, 68, 69, 70, 70, 71, 72$
Test the hypothesis that the sample comes from a population with average marks 66.

Soln: $H_0: \mu = 66$
 $\bar{x} = ((63, 63, 66, 67, 68, 69, 70, 70, 71, 72))$
> t-test (x)

One sample test.

Data: x .
 $t = 68, 319, df = 9, p\text{-value} = 1.558e - 13$
alternative hypothesis : true mean is not. equal
95 percent confidence interval.
65.68 | 71 70.148 29.

Sample estimated.
mean of x .
67.9

Since p-value is less than 0.05
we reject hypothesis at S.I.
level of significance
 $> 10s = 0.05$
 $> pvalue = 1.558e - 13$

If ($P\text{value} > 0.05$) \Rightarrow Stat ("accept H_0 ")
 else \Rightarrow Stat ("reject H_0 ")
 reject $H_0 \rightarrow$

Two groups of students score the following marks
 Test the hypothesis that there is no significant difference between the two groups.

group 1 = 18, 22, 21, 17, 20, 19, 23, 20, 22,
 group 2 = 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

Soln: H_0 : There is no difference between two groups.

$x = \{18, 22, 21, 17, 20, 19, 23, 20, 22, 21\}$
 $y = \{16, 20, 14, 21, 20, 18, 13, 15, 17, 21\}$
 $t\text{-test } (x, y)$
 Welch Two Sample t-test

data: x and y.
 $t = 2.2512$, $|t| = 16.316$, $P - \text{Value} = 0.03798$
 alternative hypothesis: true difference means is not equal to 0.

95% present confidence interval:
 0.16282055 to 0.0371795
 sample estimates:
 mean of x mean of y:
 20.1 17.5

$p\text{ value} = 0.03798$
 > 0.05 ($P\text{value} > 0.05$) \Rightarrow Stat ("accept H_0 ")
 \Rightarrow if ($P\text{value} > 0.05$) \Rightarrow Stat ("reject H_0 ")
 else \Rightarrow Stat ("accept H_0 ")

else we reject ("reject H_{0"}) {.

reject H₀?

Since p - value is less than 0.05 we reject the null hypothesis at 5% level of significance.

Q.3)

The sales data of 6 shops before and after a special campaign are given below.
Before : 53, 28, 31, 48, 50, 42,
After : 58, 29, 30, 55, 56, 45.
Test the hypothesis that the campaign is effective or not.

H₀: There is no significant difference between before and after the campaign.

> x = c(53, 28, 31, 48, 50, 42)
> y = c(58, 29, 30, 55, 56, 45)
> t.test(x, y, paired = T, alternative = "greater")

Data : x and y

t = -2.3815, df = 5, p-value = 0.9806.
alternative hypothesis: true difference in means is greater than 0

95 percent confidence interval :

-6.035547 1.1
sample estimates:
-3.5

? p-value = 0.9806

60

If ($p\text{-value} > 0.05$) \Rightarrow we ("accept H_0 ") \wedge
else \Rightarrow we ("reject H_0 ") \wedge
accept H_0

since p-value is greater than 0.05 we accept hypothesis at 5% level of significance.

(ii) Two medicines are applied to the two patients respectively.

group 1: 10, 12, 13, 11, 14

group 2: 8, 9, 12, 14, 15, 10, 9

Is there any significant difference between two medicines.

Hypothesis: H_0 : There is no significant difference b/w medicines of two groups

$\rightarrow x = \{10, 12, 13, 11, 14\}$

$\rightarrow y = \{8, 9, 12, 14, 15, 10, 9\}$

$\rightarrow t\text{-test } (x, y)$

With two sample t-test

data: x and y

$$t = 0.80384, dy = 9.7894, p\text{-value} = 0.4406$$

at. alternative hypothesis: true difference in mean is not equal to 0.

95 percent confidence interval:

$$-1.48171, 3.781171$$

sample estimates:

mean of x and y

$P - \text{value} = 0.4406$

> if ($P - \text{value} > 0.05$) \Rightarrow (accept H_0)
 else \Rightarrow (reject H_0)
 accept H_0

Since the p-value is greater than 0.05 we accept the hypothesis at 5% level of significance.

(e) S) The following are the weights before and after the diet program. Is the diet program effective?
 Before: 120, 125, 130, 123, 119,
 After: 100, 110, 95, 90, 115, 99.

Solution: H₀: There is no significant difference.
 $\rightarrow x = (120, 125, 115, 130, 123, 119)$;
 $\rightarrow y = (100, 110, 95, 90, 115, 99)$
 $\rightarrow t - \text{test } (x, y, \text{ paired} \leftarrow T, \text{ alternative} = ("less")$

paired t-test.

data: x and y.

$t = 5$, $P - \text{value} = 0.4962$
 n. 3458

alternative hypothesis: true difference in mean is less than 0
 95 percent confidence interval:
 from 24.0295 to 45.9705

estimated:

sample difference
mean of the difference
 $= 19.8333$

```
? p-value = 0.9963
? if (p-value > 0.05) {
  cat("accept H0")
} else {
  cat("reject H0")
}
accept H0
```

since the p-value is greater than 0.05
we accept the hypothesis at 5% level of significance.

PRACTICAL 8

- Q.1) Topic : Large and small sample test.
- The arithmetic mean of a sample of 100 items from large population is 52. If the standard deviation of the hypothesis that the population mean is against the alternative it is more than 53.4.

```

Ans:  $H_0: \mu = 53$ 
       $H_1: \mu > 53$ 
 $> n = 100$ 
 $> m_x = 52$ 
 $> m_0 = 53$ 
 $> \sigma_d = 7$ 
 $> z_{cal} = (m_x - m_0) / (\sigma_d / \sqrt{n})$ 
 $> z_{cal}$ 
[1] -4.285114.
> cat ("Calculated z value is: ", zcal)
calculated z value is = -4.285714.
> p-value = 1 - pnorm (abs(zcal))
> pvalue
[1] 1.82153e-05

```

Since p-value is less than 0.05 we reject the hypothesis at level of significance.

- Q.2) In a big city 350 out of 700 males are found to be smokers. Based on information suppose exactly half of the males in the city are smokers at 1% level.

~~H₀~~ $H_0: p = \mu$

$$\geq p = 0.5$$

$$\geq \alpha = 1 - \beta$$

$$\geq p = 350 / 700$$

$$\geq n = 700$$

$$\geq z_{\text{cal}} = (p - \bar{p}) / (\text{sqrt}(p * \alpha(n)))$$

$\geq z_{\text{cal}}$ calculated Z value is $= 0.7200$

Calculated Z value is $= 0$

$$\geq p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$\geq p\text{value}$$

0.1

Since Pvalue is greater than 0.05 we accept hypothesis at 1% level of significance.

3) Thousand article from a factory A are found to have 21 defective, 1500 articles from a and factory B are found to have 14 defective. Test at 5% LOS that the two factory are similar are not.

$H_0: p_1 = p_2$ as $H_1: p_1 \neq p_2$

$$\geq n_1 = 1000$$

$$\geq n_2 = 1500$$

$$\geq p_1 = 0.01$$

$$\geq p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

0.014

23

$$\begin{aligned}> p \\ \text{[1]} & 0.014\end{aligned}$$

$$\begin{aligned}> q = 1 - p \\ > q \\ \text{[1]} & 0.986\end{aligned}$$

$$\begin{aligned}> z_{\text{cal}} = (\rho_1 - \rho_2) / \sqrt{(\rho_1 * (1/\rho_1 + 1/\rho_2))} \\ \text{[1]} & 2.084842\end{aligned}$$

$$\begin{aligned}> \text{cat} \left(\text{"calculated"} \right. \\ & \left. \text{calculated } z\text{ value is } = z_{\text{cal}} \right) \\ > \text{pvalue} = 2 * (1 - \text{pnorm}(z_{\text{cal}})) \\ \text{[1]} & 0.03708364\end{aligned}$$

since pvalue at 5% level of significance is less than 0.05 we reject the hypothesis

e.4) A sample of size 400 was drawn at 5%. Los had the sample with mean 100 and variance 25 from a population

$$\begin{aligned}\text{Ans:} \\ \overline{x} = 100.4 = 100 \\ > m_x = 99 \\ > m_o = 100 \\ > s_d = 5 \\ > n = 400\end{aligned}$$

63

$$\chi^2_{\text{cal}} = (m_1 - m_0) / \text{Cov}(\text{Cov}(n))$$

$$\chi^2_{\text{cal}} = 2.5$$

$$\text{P-value} = 2 * (1 - \text{norm}(\text{abs}(z_{\text{cal}})))$$

$$\text{P-value}$$

$$0.01241933$$

since P-value is less than 0.05 we reject H₀.
hypothesis at 5% level of significance.

1) The flower stems are selected and the heights are found to be (in) 63, 63, 68, 69, 71, 71, 72. Test the hypothesis that the mean height is 66 or not at 1% LOS.

Ans: H₀: $\mu = 66$
 $\chi = (63, 63, 68, 69, 71, 71, 72)$
t-test (χ)
one sample t-test.

data $\equiv \chi$.
 $t = 47.94$, $df = 6$, P-value = 5.522e-09
Alternative hypothesis: true mean is not equal to 66.

b. 95 percent confidence interval
64.66079 71.62092
sample estimate:
mean of χ .
68.14286

83

Since p-value is less than 0.05 we reject hypothesis at 1% level of significance.

Q.6.)

Two random samples were drawn from 2 normal populations and their values are (A) $\rightarrow 66, 67, 75, 76, 88, 90, 92$, (B) $\rightarrow 64, 66, 74, 78, 82, 85, 87, 92, 93, 95$. Test at 5% LOS that the sample comes from whether the population have the same variance at 5% LOS.

$$\begin{aligned}
 \text{Ans} \quad H_0: \sigma_1^2 = \sigma_2^2 & \\
 > x = c(66, 67, 75, 76, 88, 90, 92) \\
 > y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95) \\
 > \text{var. test}(x, y)
 \end{aligned}$$

F-test to compare two variances.

Data of x and y.

$$\begin{aligned}
 F &= 0.70686, \text{ numdf} = 8, \text{ denum df} = 10, \\
 p\text{-value} &= 0.6359. \\
 \text{alternative hypothesis: } &\text{true ratio of 95\% confidence is not equal to } \\
 &0.6833662 \quad 3.0366393
 \end{aligned}$$

Sample estimate. Ratio of variance standard error.

$$\begin{aligned}
 &0.7068567. \\
 &p\text{-value} = 0.6359. \\
 &\text{if } (p\text{-value} > 0.05) \text{ accept } H_0'' \text{ else } (\text{but } c \text{ if rejected } H_0'')?
 \end{aligned}$$

accept H_0

since p-value is greater than 0.05 we accept hypothesis at 5% level of significance.

- Q) A company producing light bulbs finds that mean life span of the population of bulbs is 1200 hours with s.d 125. A sample of 100 bulbs have mean 1150 hours. Test whether the difference b/w population and sample mean is significantly different?

```
#  
H0 = H0: μ = 1200  
#  
> m0 = 1200  
> mx = 1150  
> n = 100  
> sd = 125  
> zcut = (mx - m0) / (sd / (sqrt(n)))  
> cut_l "calculated z value is -4  
> pvalue = 2 * (1 - pnorm (abs (zcut)))  
## 6.34334248e-05  
pvalue is less than 0.05 we reject hypothesis
```

since pvalue is less than 0.05 we reject hypothesis

Q) From each of two consignment of apples, a sample of size 200 is drawn and number of bad apples are counted. Test whether the proportion of rotten apples in two assignments are significantly different at 1% LOS?

No. of bad apples
Sample size 200
56 49

Q3

Solution $H_0: \mu = p_1 \neq p_2$

```
> n1 = 200
> n2 = 300
> p1 = 44/200
> p2 = 56/300
> p = (n1 * p1 + n2 * p2) / (n1 + n2)
> p
[1] 0.2
> q = 1 - p
> zcal = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))
> zcal
[1] 0.9128709
> cat("calculated z values is =", zcal)
calculated = value is 0.9128709
> pvalue = 2 * (1 - pnorm(zabs(zcal)))
> pvalue
[1] 0.3613104
```

Since pvalue is greater than 0.05 we accept the hypothesis.

PRACTICAL NO-9

hi - square tests and ANOVA (Analysis Variance)

use the following data test whether the condition of home and the condition of child are independent or not.

→ condition of Home.

	Clean	Fairly Clean	Dirty
Clean	70	50	20
Fairly Clean	80	20	45
Dirty	35	45	45

→ H_0 : Condition of Home and child are independent

$$\chi^2 = \sum (O - E)^2 / E$$

$$m = 3$$

$$n = 2$$

$$y = \begin{bmatrix} 70 & 50 & 20 \\ 80 & 20 & 45 \\ 35 & 45 & 45 \end{bmatrix}$$

$$\begin{bmatrix} 70 & 50 & 20 \\ 80 & 20 & 45 \\ 35 & 45 & 45 \end{bmatrix}$$

$$PV = \chi^2 \text{ - test } (x).$$

$$PV \text{ Pearson's chi Squared data.}$$

23

χ^2 - squared = 25. 646 df = 2 , pvalue = 2.69%

H_0 is rejected, since pvalue is less than 0.05

Q: Test the hypothesis that vaccination and disease are independent or not

vaccine.

Disease	Affected	Not Affected
Affected	70	46
Not Affected	35	37

H_0 : Condition of disease and vaccination are independent
 $X = [70, 46, 35, 37]$.

$m=2$

$n=2$
 $y = \text{matrix}(x, nrow = m, ncol (=n))$

y
 $[1,] [2,]$
70 46
 $[2,] [3,]$
35 37
 $PV = \text{chisq.test}(y)$
 PV

χ^2 - squared = 2.0275 df = 1 , pvalue = 0.1545
 H_0 is Accepted since pvalue is more than 0.05

66

(3) Perform ANOVA for the following data.

Type	Observation
B	50, 52.
C	53, 55, 53
D	52, 54, 54, 55.

> H0: The means are equal For A, B, C, D

```
x1 = c(50, 52)
x2 = c(53, 55, 53)
x3 = c(60, 68, 57, 56)
x4 = c(52, 54, 54, 55)
```

```
d = stack(list(b) = x1, b2 = x2, b3 = x3, b4 = x4))
names(d)
```

```
[1] "value" "ind"
```

> oneway.ttest(value ~ ind, data = d, var.equal =

one-way analysis of means
data: value ind

```
f = 11.735, num df = 3, denom df = 9, p-value
```

> anova = anova(values ~ ind, data = d)

Summary (anova)

DF	num sl	mean sq	F - value	p > F
Ind	3	71.06	23.688	11.73
Residuals	17	18.17	2.019	0.00153 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '' 3.

33

(Q-4) The following data gives the life of the life of the four brands.

Type	Life
A	20, 23, 18, 17, 18, 22, 24.
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20.
D	16, 14, 16, 18, 14, 16.

→ H₀: The average life of A, B, C, D are equal.
 $x_1 = c(20, 23, 18, 17, 18, 22, 24)$
 $x_2 = c(19, 15, 17, 20, 16, 17)$
 $x_3 = c(21, 19, 22, 17, 20)$
 $x_4 = c(16, 14, 16, 18, 14, 16)$
d = stack (list (b1, b2 = x_2 , b3 = x_3 , b4 = x_4))
names (d)

> oneway.ttest (value and incl, data = d, var.equal = T)
One-way analysis of means
data:
 $F = 6.8445$, num df = 3, denom df = 20,
P-value = 0.002349,
> anova = anova (value ~ incl, data = d)
summary (anova).
Scanned with CamScanner

6.7

```
df      sumsq    meansq   f.value    p.value
DF
3       91.94     30.479    6.845    0.00235
3       89.06     4.453
```

Q5) How to import a . csv file in R software.
x = read.csv("c:/users/admin/Desktop/STATS.csv")
> print(x)

1	40	60
2	45	48
3	42	47
4	45	40
5	37	25
6	36	27
7	49	57
8	59	58
9	20	25
10	29	27.

> qm = mean(x\$stats)

> qm

[1] 37

n = length(x\$stats)
> qm

sd = sqrt((n-1)*var(x\$stats)) / n
[+→] 37 sd

qm = mean(x\$stats)

qm

[1] 39.4
sd = sqrt((n-1)*var(x\$stats)) / n
sd

5.8

117 15.2

Conv. X & Starts; X & matns

FEB 0. 830613

117 0. 830618