

## What is Merge Sort?

**Merge Sort** is a popular divide-and-conquer sorting algorithm that divides the input array into two halves, recursively sorts them, and then merges the sorted halves into one sorted result.

It is an example of a **stable sort** that guarantees  **$O(n \log n)$**  performance in all cases — best, worst, and average.

## Approach: Divide & Conquer

**Divide:** Split the array into two halves.

**Conquer:** Recursively sort each half using merge sort.

**Combine:** Merge the two sorted halves into one sorted array.

## Key Concept: Merge Step

The key step is merging two sorted arrays efficiently into one sorted array. This is done using a two-pointer approach, comparing elements from both arrays and adding the smaller one into a new result array.

## Time & Space Complexity

**Time Complexity:**  $O(n \log n)$  — Divide takes  $\log n$  steps and merging takes linear time.

**Space Complexity:**  $O(n)$  — Additional space is needed to store the merged arrays.

## Dry Run Example: Merge Sort

**Input:** [5, 2, 4, 1]

Step 1: Divide

[5, 2, 4, 1] →

[5, 2] and [4, 1] →

[5] and [2] | [4] and [1]

Step 2: Merge

Merge [5] and [2] → [2, 5]

Merge [4] and [1] → [1, 4]

Step 3: Final Merge

Merge [2, 5] and [1, 4]:

Compare 2 and 1 → [1]

Compare 2 and 4 → [1, 2]

Compare 5 and 4 → [1, 2, 4]

Remaining elements → [1, 2, 4, 5]

**Output:** [1, 2, 4, 5]

JavaScript

C

C++

Java

Python

C#

```
/**
 * @param {number[]} nums
 * @return {number[]}
 */
var sortArray = function(nums) {
  if (nums.length <= 1) return nums;
  let mid = Math.floor(nums.length / 2);
  let left = sortArray(nums.slice(0, mid));
  let right = sortArray(nums.slice(mid));
  return merge(left, right);
};

function merge(left, right) {
  let res = [], i = 0, j = 0;
  while (i < left.length && j < right.length) {
    if (left[i] < right[j]) {
      res.push(left[i++]);
    } else {
      res.push(right[j++]);
    }
  }
  return [...res, ...left.slice(i), ...right.slice(j)];
}
```