

Q.1) Explain Diffie-Hellman Key-exchange algorithm?

Ans. The Diffie-Hellman algorithm provides a way of generating a shared secret between the sender & the receiver in such a way that the secret need not be exchanged or transferred over the communication medium.

- i) Alex chooses 2 prime nos. g & p and also a secret number a . He calculates value of A such that $A = g^a \text{ mod } p$. He then sends g , p and A to Bobby.
- ii) Similarly, Bobby chooses a secret no. b & computes the value of B such that $B = g^b \text{ mod } p$.
- iii) Alex computes shared key at his end as shared key, $S = A \text{ mod } p$.
- iv) Bobby ~~computes~~ computes shared key S , derived in Step 3 & 4 are equal due to mod operation.

$$(g^a \text{ mod } p)^b \text{ mod } p = g^b \text{ mod } p$$

$$(g^b \text{ mod } p)^a \text{ mod } p = g^a \text{ mod } p$$

Q.2) Define:

- 1) Public Key: Public Key is the key which is publicly known to the people & organization.
- 2) Private Key: Private Key is the key which is only known to the organization itself and kept as secret outside the organization.

Q.3) Suppose that 2 parties A & B agree on 7 as modulus, 3 as the primitive root. A chooses 2 & B chooses 5 as their respective secrets. Find Diffie Hellman Key.

Ans. $a=2, b=5, g=3, p=7$

$$\begin{aligned} A &= g^a \bmod p & B &= g^b \bmod p \\ A &= 3^2 \bmod 7 & B &= 3^5 \bmod 7 \\ &= 9 \bmod 7 & &= 243 \bmod 7 \\ &= 2 & &= 5 \end{aligned}$$

A and B exchange A' and B'

A calculates S as

$$\begin{aligned} S &= B^a \bmod p \\ &= 5^2 \bmod 7 \\ &= 25 \bmod 7 = 4 \end{aligned}$$

B calculates S as,

$$\begin{aligned} S &= A^b \bmod p \\ &= 2^5 \bmod 7 = 32 \bmod 7 = 4. \end{aligned}$$

So the shared key between organization A & B is 4.