

College of Engineering Trivandrum

Compiler Design Lab



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Exp 6

1 NFA to DFA

1.1 Aim

Write program to convert NFA to DFA.

1.2 Theory

NFA

- NFA stands for non-deterministic finite automata. It is easy to construct an NFA than DFA for a given regular language.
- The finite automata are called NFA when there exist many paths for specific input from the current state to the next state.
- Every NFA is not DFA, but each NFA can be translated into DFA.
- NFA is defined in the same way as DFA but with the following two exceptions, it contains multiple next states, and it contains ϵ transition.
 - Q : finite set of states
 - Σ : finite set of the input symbol
 - q_0 : initial state
 - F : final state
 - δ : Transition function
 - $\delta : Q \times \Sigma \rightarrow 2^Q$

DFA

- In a DFA, for a particular input character, the machine goes to one state only.
- A transition function is defined on every state for every input symbol.
- Also in DFA null (or ϵ) move is not allowed,
- i.e., DFA cannot change state without any input character.
- DFA consists of 5 tuples Q, Σ, q, F, δ .
 - Q : set of all states.
 - Σ : set of input symbols. (Symbols which machine takes as input)
 - q : Initial state. (Starting state of a machine)
 - F : set of final state.
 - δ : Transition Function, defined as $\delta : Q \times \Sigma \rightarrow Q$.

1.3 Algorithm

Algorithm 1: Algorithm to convert NFA to DFA

```
1 function CONVERTTODFA ( nfa )
2   Initialize an empty object of type DFA with variable name dfa
3   Initialize dfa . num_alphabets = nfa . num_alphabets , i = 0
4   Initialize a set lazySet which stores subsets of Q and store {0} in it Create a new row of
5   size dfa . num_alphabets and insert into dfa .
6   table and initialize all values to -1.
7   While i < lazySet . size ()
8     Iterate through each of the input symbol j in E
9     Initialize an empty set of states reachable and a variable next = -1
10    Iterate i through each element in lazySet [ i ] and push
11    into reachable the set nfa . table [ i ][ j ]
12    Check if reachable is already in lazySet . If yes ,
13    the get the value of next from lazySet . If not , then
14    Insert into lazySet , the set reachable and
15    set next = lazySet . size ()
16    Insert next into dfa . finalStates if any element
17    in reachable is a final state of the original nfa
18    Create a new row of size dfa . num_alphabets and
19    insert into dfa . table and
20    initialize all values to -1.
21    dfa . table [ i ][ j ] = next
22    Increment i
23  Return dfa as the DFA .
24 end function
```

1.4 Code

```
1 //CPP program to convert NFA into DFA
2 #include <bits/stdc++.h>
3 using namespace std;
4 void print_header(int m)
5 {
6     cout << "State";
7     for (int j = 0; j < m; ++j)
8     {
9         char ch = char(int('a') + j);
10        cout << "\t" << ch;
11    }
12    cout << endl;
13 }
14 set<int> split_Add(string s)
15 {
16     int size = s.size();
17     set<int> res;
18     int start = 0;
19     for (int i = 0; i < size; ++i)
20     {
21         if (s[i] == ',')
22         {
23             string sub = s.substr(start, i - start);
24             start = i + 1;
25             int temp = stoi(sub);
26             res.insert(temp);
27         }
28     }
29     string sub = s.substr(start, size - start);
30     int temp = stoi(sub);
31     res.insert(temp);
32     return res;
33 }
34 void print(vector<vector<set<int>>> table)
35 {
36     for (auto x : table)
37     {
38         for (auto y : x)
39         {
40             for (auto z : y)
41             {
42                 cout << z << ",";
43             }
44             cout << "\t";
45         }
46         cout << endl;
47     }
48 }
49 int main()
50 {
51     cout << "Enter the number of states: ";
52     int n, m;
53     cin >> n;
54     cout << "Enter the number of input symbols: ";
55     cin >> m;
56     vector<vector<set<int>>> table(n, vector<set<int>>(m));
57     print_header(m);
58     for (int i = 0; i < n; ++i)
59     {
60         cout << i << "\t";
61         for (int j = 0; j < m; ++j)
62         {
63             string s;
64             cin >> s;
65             set<int> to_states;
66             if (s != "-")
67                 to_states = split_Add(s);
68             table[i][j] = to_states;
69         }
70     }
71     //print(table);
72     int start, last, temp, temp1;
73     set<int> s, f;
74     cout << "Enter the number of start states: ";
```

```

75  cin >> start;
76  cout << "Enter the start states: ";
77  for (int i = 0; i < start; ++i)
78  {
79      cin >> temp;
80      s.insert(temp);
81  }
82  cout << "Enter the number of final states: ";
83  cin >> last;
84  cout << "Enter the final states: ";
85  for (int i = 0; i < last; ++i)
86  {
87      cin >> temp;
88      f.insert(temp);
89  }
90  vector<vector<set<int>>> dfa;
91  set<set<int>>
92      present;
93  map<set<int>, int> state_num;
94  queue<set<int>> elem;
95
96  int dfa_state = 0;
97  elem.push(s);
98  present.insert(s);
99  while (!elem.empty())
100  {
101
102      vector<set<int>> dfa_row;
103
104      set<int> current = elem.front();
105      state_num[current] = dfa_state;
106      dfa_state++;
107      dfa_row.push_back(current);
108      elem.pop();
109      for (int i = 0; i < m; ++i)
110      {
111          set<int> new_state;
112          for (auto x : current)
113          {
114              for (auto y : table[x][i])
115              {
116                  new_state.insert(y);
117              }
118          }
119          dfa_row.push_back(new_state);
120          if (present.find(new_state) == present.end())
121          {
122              present.insert(new_state);
123              elem.push(new_state);
124          }
125      }
126      dfa.push_back(dfa_row);
127  }
128  print_header(m);
129  for (int i = 0; i < dfa_state; ++i)
130  {
131      for (int j = 0; j < m + 1; ++j)
132      {
133          cout << state_num[dfa[i][j]] << "\t";
134      }
135      cout << endl;
136  }
137  cout << "Final states are: ";
138  for (auto x : present)
139  {
140      for (auto y : x)
141      {
142          if (f.find(y) != f.end())
143          {
144              cout << state_num[x] << " ";
145              break;
146          }
147      }
148  }
149  cout << endl;
150  return 0;

```

1.5 Output

```

abhishek@hephaestus:~/Desktop/S7/CD LAB$ g++ nfa-dfa.cpp
abhishek@hephaestus:~/Desktop/S7/CD LAB$ ./a.out
Enter the number of states: 3
Enter the number of input symbols: 2
State   a       b
0       0,2     1
1       1,2     2
2       0,2     1
Enter the number of start states: 1
Enter the start states: 0
Enter the number of final states: 2
Enter the final states: 0 2
State   a       b
0       1       2
1       1       2
2       3       4
3       5       3
4       1       2
5       5       3
Final states are: 0 5 1 3 4

```

```

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Enter the number of states: 3
Enter the number of input symbols: 2
State   a       b
0       0,2     1
1       1,2     2
2       0,2     1
Enter the number of start states: 1
Enter the start states: 0
Enter the number of final states: 2
Enter the final states: 0 2
State   a       b
0       1       2
1       1       2
2       3       4
3       5       3
4       1       2
5       5       3
Final states are: 0 5 1 3 4

```

1.6 Result

Implemented the program to convert ϵ -NFA to a NFA in CPP. It was compiled using g++ version 9.3.0, and executed in Ubuntu 20.04 and the above output was obtained.