

VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



LAB REPORT
on

Artificial Intelligence (23CS5PCAIN)

Submitted by

ABHISHEK PATIL (1BM23CS013)

in partial fulfillment for the award of the degree of
BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING

(Autonomous Institution under VTU)

BENGALURU-560019

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B.M.S. College of Engineering,
Bull Temple Road, Bangalore 560019
(Affiliated To Visvesvaraya Technological University, Belgaum)
Department of Computer Science and Engineering



CERTIFICATE

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **Abhishek patil(1BM23CS013)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

Swathi Sridharan Assistant Professor Department of CSE, BMSCE	Dr. Kavitha Sooda Professor & HOD Department of CSE, BMSCE
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CERTIFICATE OF ACHIEVEMENT

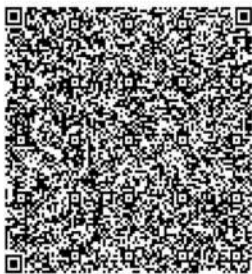
The certificate is awarded to

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for successfully completing

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Name : Abhishek patil Class : D
Section : 5 Roll No. : CS013 Subject : AI LAB

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CIE - 10/10
or
5/5

CLE - 10/10

5/5

Github Link: https://github.com/abhishekipatil-bms/AI_lab

Program 1

Implement Tic –Tac –Toe Game

Implement vacuum cleaner agent

Algorithm:

Week-1

Q) Design a AI playing tic-tac-toe

Algorithm:

checkWinner(board):

if any row/column/diagonal has same symbol:
return that symbol

if no empty cells are left:
return "draw"

return none

minimax(board, depth, is_maximizing):

result = checkWinner(board)

if result is not none;

if result == 'X' return -10

if result == 'O' return +10

if result == Draw return 0

if (is_maximizing)

bestscore = -∞

for each empty cell in board

place "O" in cell

score = minimax(board, depth, false)

undo move

best_score = max(best_score, score)

return best_score

else:

bestScore = $+\infty$

for each empty cell in board

place 'X' in cell

score = minimax(board, d+1, T)

undo move

bestScore = min(bestScore, score)

return bestScore

For

bestMove (board)

bestScore = $-\infty$

bestMove = null

For each empty cell in board

place 'O' in cell

score = minimax(board, 0, false)

undo move

if score > bestScore;

bestScore = score

bestMove = cell

return bestMove

Output:

Your move

Vacuum cleaner

```
room = {  
    'A': 'Dirty'  
    'B': 'Dirty'  
}
```

```
}
```

```
vac_loc = 'A'
```

```
def suck():
```

```
    print(f"Sucking dirt! {vac_loc}")
```

```
    room[vac_loc] = 'clean'
```

```
def move():
```

```
    global vac_loc
```

```
    if (vac_loc == 'A'):
```

```
        print("move to B")
```

```
        vac_loc = 'B'
```

```
    else if (vac_loc == 'B'):
```

```
        print("move to C")
```

```
        vac_loc = 'C'
```

```
    else if (vac_loc == 'C'):
```

```
        print("move to D")
```

```
        vac_loc = 'D'
```

```
    else:
```

```
        print("move to A")
```

```
        vac_loc = 'A'
```

```
}
```

```
while 'Dirty' in room.values():
```

```
    if room[vac_loc] == 'Dirty':
```

```
        suck()
```

```
    else
```

```
        move()
```

Code:

Tic tac toe:

```
def print_board(board):
    for row in board:
        print(" ".join(row))
    print()

def check_winner(board, player):
    for i in range(3):
        if all(board[i][j] == player for j in range(3)):
            return True
        if all(board[j][i] == player for j in range(3)):
            return True
    if all(board[i][i] == player for i in range(3)):
        return True
    if all(board[i][2 - i] == player for i in range(3)):
        return True
    return False

def is_draw(board):
    return all(board[i][j] != '-' for i in range(3) for j in range(3))

def minimax(board, is_ai_turn):
    if check_winner(board, 'O'):
        return 1
    if check_winner(board, 'X'):
        return -1
    if is_draw(board):
        return 0

    if is_ai_turn:
        best_score = -float('inf')
        for i in range(3):
            for j in range(3):
                if board[i][j] == '-':
                    board[i][j] = 'O'
                    score = minimax(board, False)
                    board[i][j] = '-'
                    best_score = max(score, best_score)
            return best_score
    else:
        best_score = float('inf')
        for i in range(3):
            for j in range(3):
                if board[i][j] == '-':
                    board[i][j] = 'X'
                    score = minimax(board, True)
```

```

        board[i][j] = '-'
        best_score = min(score, best_score)
    return best_score

def manual_game():
    board = [['-' for _ in range(3)] for _ in range(3)]
    print("Initial Board:")
    print_board(board)

    while True:
        while True:
            try:
                x_row = int(input("Enter X row (1-3): ")) - 1
                x_col = int(input("Enter X col (1-3): ")) - 1
                if board[x_row][x_col] == '-':
                    board[x_row][x_col] = 'X'
                    break
            except:
                print("Invalid input!")

        print("Board after X move:")
        print_board(board)

        if check_winner(board, 'X'):
            print("X wins!")
            break
        if is_draw(board):
            print("Draw!")
            break

        while True:
            try:
                o_row = int(input("Enter O row (1-3): ")) - 1
                o_col = int(input("Enter O col (1-3): ")) - 1
                if board[o_row][o_col] == '-':
                    board[o_row][o_col] = 'O'
                    break
            except:
                print("Invalid input!")

        print("Board after O move:")
        print_board(board)

```

```

if check_winner(board, 'O'):
    print("O wins!")
    break
if is_draw(board):
    print("Draw!")
    break

cost = minimax(board, True)
print(f"AI evaluation cost from this position: {cost}")

```

```

manual_game()
print("Name: Sanchit Mehta and USN : 1BM23CS299")

```

```

vacuum cleaner:
rooms = int(input("Enter Number of rooms: "))
Rooms = "ABCDEFGHIJKLMNOPQRSTUVWXYZ"
cost = 0
Roomval = {}

```

```

for i in range(rooms):
    print(f"Enter Room {Rooms[i]} state (0 for clean, 1 for dirty): ")
    n = int(input())
    Roomval[Rooms[i]] = n

```

```

loc = input(f"Enter Location of vacuum ( {Rooms[:rooms]} ): ").upper()

```

```

while 1 in Roomval.values():
    if Roomval[loc] == 1:
        print(f"Room {loc} is dirty. Cleaning...")
        Roomval[loc] = 0
        cost += 1
    else:
        print(f"Room {loc} is already clean.")

```

```

move = input("Enter L or R to move left or right (or Q to quit): ").upper()

```

```

if move == "L":
    if loc != Rooms[0]:
        loc = Rooms[Rooms.index(loc) - 1]
    else:
        print("No room to move left.")
elif move == "R":
    if loc != Rooms[rooms - 1]:
        loc = Rooms[Rooms.index(loc) + 1]
    else:
        print("No room to move right.")

```

```
elif move == "Q":
    break
else:
    print("Invalid input. Please enter L, R, or Q.")
```

```
print("\nAll Rooms Cleaned." if 1 not in Roomval.values() else "Exited before cleaning all rooms.")
print(f"Total cost: {cost}")
print("1BM23CS299")
print("Sanchit Mehta")
```

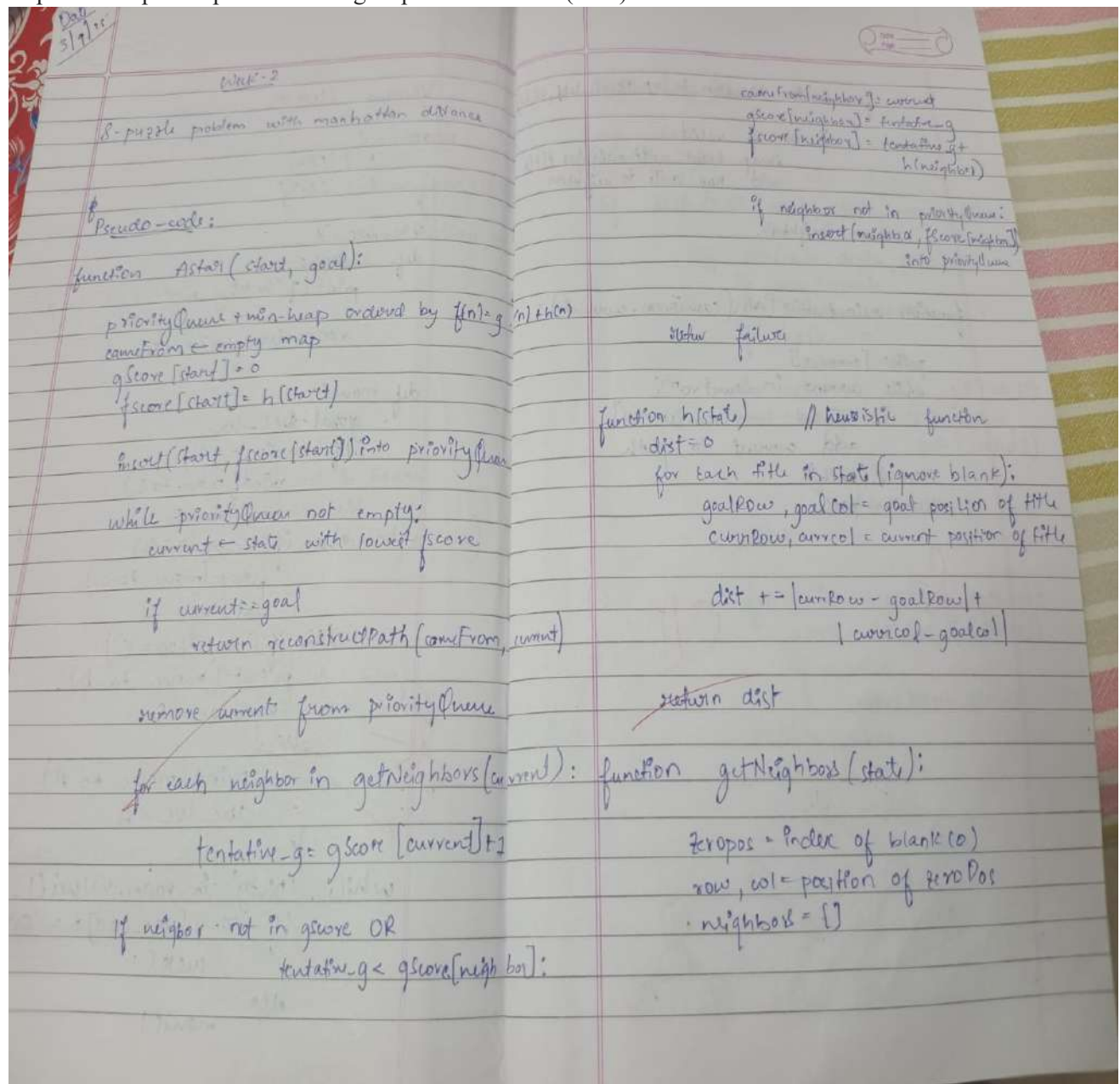
```
Enter Number of rooms: 4
Enter Room A state (0 for clean, 1 for dirty):
0
Enter Room B state (0 for clean, 1 for dirty):
1
Enter Room C state (0 for clean, 1 for dirty):
0
Enter Room D state (0 for clean, 1 for dirty):
1
Enter Location of vacuum (ABCD): A
Room A is already clean.
Enter L or R to move left or right (or Q to quit): L
No room to move left.
Room A is already clean.
Enter L or R to move left or right (or Q to quit): R
Room B is dirty. Cleaning...
Enter L or R to move left or right (or Q to quit): R
Room C is already clean.
Enter L or R to move left or right (or Q to quit): R
Room D is dirty. Cleaning...
Enter L or R to move left or right (or Q to quit): R
No room to move right.

All Rooms Cleaned.
Total cost: 2
1BM23CS299
Sanchit Mehta

=== Code Execution Successful ===
```

Program 2

Implement 8 puzzle problems using Depth First Search (DFS):



for each direction in (up, down, left, right)

if move is valid

swap blank with neighbor tile
add new state to neighbors

return neighbors

function reconstructionPath(cameFrom, current):

path = [current]

while current in cameFrom:

current = cameFrom[current]

add current to path

reverse(path)

return path

O/P - 9

IDDF

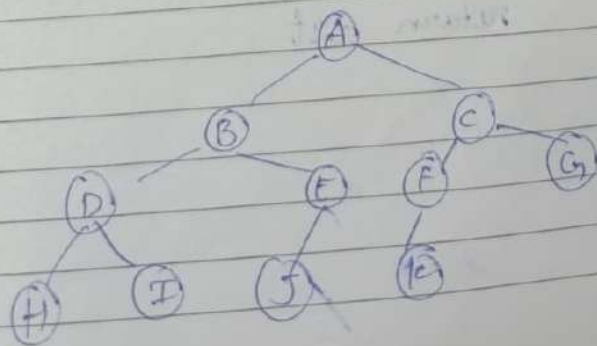
def
Pseu

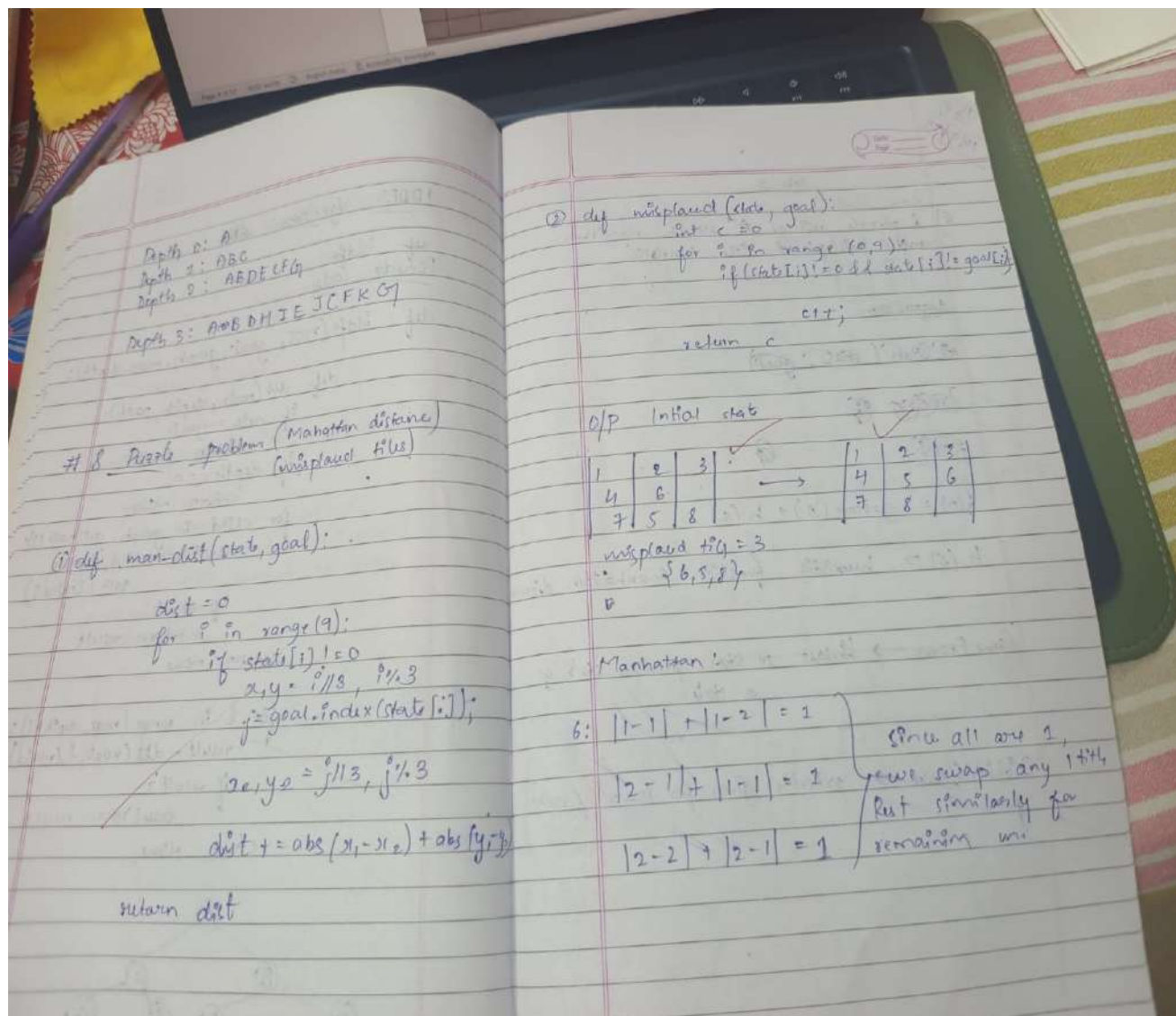
def

IDDFS algorithm with

Pseudo code

```
def iddfs(root, goal, graph, max_depth):  
    def dfs(node, depth, path):  
        if node == goal:  
            return path  
        if depth == 0:  
            return None  
        for child in graph.get(node, []):  
            result = dfs(child, depth-1,  
                          path + [child])  
            if result:  
                return result  
        return None  
    for l in range(max_depth+1):  
        result = dfs(root, l, [root])  
        if result:  
            return result  
    return None
```





goal_state = '123804765'

```

moves = {
    'U': -3,
    'D': 3,
    'L': -1,
    'R': 1
}
count = 0
invalid_moves = {
    0: ['U', 'L'], 1: ['U'], 2: ['U', 'R'],
    3: ['L'], 5: ['R'],
    6: ['D', 'L'], 7: ['D'], 8: ['D', 'R']
}

```

```

def move_tile(state, direction):
    index = state.index('0')
    if direction in invalid_moves.get(index, []):

```

```

    return None

    new_index = index + moves[direction]
    if new_index < 0 or new_index >= 9:
        return None

    state_list = list(state)
    state_list[index], state_list[new_index] = state_list[new_index], state_list[index]
    return ''.join(state_list)

def print_state(state):
    for i in range(0, 9, 3):
        print(' '.join(state[i:i+3]).replace('0', ' '))
    print()

def dfs(start_state, max_depth=50):
    visited = set()
    stack = [(start_state, [])] # Each element: (state, path)

    while stack:
        current_state, path = stack.pop()

        if current_state in visited:
            continue

        # Print every visited state
        print("Visited state:")
        print_state(current_state)

        if current_state == goal_state:
            return path

        visited.add(current_state)
        global count
        count += 1
        if len(path) >= max_depth:
            continue

        for direction in moves:
            new_state = move_tile(current_state, direction)
            if new_state and new_state not in visited:
                stack.append((new_state, path + [direction]))

    return None

start = input("Enter start state (e.g., 724506831): ")

if len(start) == 9 and set(start) == set('012345678'):
    print("Start state:")
    print_state(start)

    result = dfs(start)

```

```

if result is not None:
    print("Solution found!")
    print("Moves:", ' '.join(result))
    print("Number of moves:", len(result))
    print("Number of visited states",count)
    print("IBM23CS299 Sanchit Mehta\n")

    current_state = start
    for i, move in enumerate(result, 1):
        current_state = move_tile(current_state, move)
        print(f'Move {i}: {move}')
        print_state(current_state)
    else:
        print("No solution exists for the given start state or max depth reached.")
else:
    print("Invalid input! Please enter a 9-digit string using digits 0-8 without repetition.")

```

Implement Iterative deepening search algorithm:
goal_state = '123456780'

```

moves = {
    'U': -3,
    'D': 3,
    'L': -1,
    'R': 1
}

invalid_moves = {
    0: ['U', 'L'], 1: ['U'], 2: ['U', 'R'],
    3: ['L'],      5: ['R'],
    6: ['D', 'L'], 7: ['D'], 8: ['D', 'R']
}

def move_tile(state, direction):
    index = state.index('0')
    if direction in invalid_moves.get(index, []):
        return None

    new_index = index + moves[direction]
    if new_index < 0 or new_index >= 9:
        return None

    state_list = list(state)
    state_list[index], state_list[new_index] = state_list[new_index], state_list[index]
    return ''.join(state_list)

def print_state(state):

```

```

    for i in range(0, 9, 3):
        print(' '.join(state[i:i+3]).replace('0', ' '))
    print()

def dls(state, depth, path, visited, visited_count):
    visited_count[0] += 1 # Increment visited states count
    if state == goal_state:
        return path

    if depth == 0:
        return None

    visited.add(state)

    for direction in moves:
        new_state = move_tile(state, direction)
        if new_state and new_state not in visited:
            result = dls(new_state, depth - 1, path + [direction], visited, visited_count)
            if result is not None:
                return result

    visited.remove(state)
    return None

def iddfs(start_state, max_depth=50):
    visited_count = [0] # Using list to pass by reference
    for depth in range(max_depth + 1):
        visited = set()
        result = dls(start_state, depth, [], visited, visited_count)
        if result is not None:
            return result, visited_count[0]
    return None, visited_count[0]

# Main
start = input("Enter start state (e.g., 724506831): ")

if len(start) == 9 and set(start) == set('012345678'):
    print("Start state:")
    print_state(start)

    result, visited_states = iddfs(start, 15)

    print(f"Total states visited: {visited_states}")

    if result is not None:
        print("Solution found!")
        print("Moves:", ' '.join(result))

```

```

print("Number of moves:", len(result))
print("1BM23CS307 Uzair\n")

current_state = start
for i, move in enumerate(result, 1):
    current_state = move_tile(current_state, move)
    print(f'Move {i}: {move}')
    print_state(current_state)
else:
    print("No solution exists for the given start state or max depth reached.")
else:
    print("Invalid input! Please enter a 9-digit string using digits 0-8 without repetition.")

```

```

Enter start state (e.g., 724506831): 724506831
Start state:
7 2 4
5   6
8 3 1

Visited state:
7 2 4
5   6
8 3 1

Visited state:
7 2 4
5 6
8 3 1

Visited state:
7 2 4
5 6 1
8 3

Visited state:
7 2 4
5 6 1
8   3

```

Program 3

Implement A* search algorithm

Date
10/9/25

lab-3

Q1 8 puzzle using A* search algorithm
and mis placed tile heuristic

Algorithm

Q2 Start (start, goal)

Tracing Q

~~Q~~

Q

$$f(n) = g\text{-score}(s) + h(s)$$

$h(s) \rightarrow$ heuristic function manhattan distance

Came From \rightarrow link to store previous state of
a state

Priority Queue \rightarrow priority given for lowest f score
f

initial

1
7

depth	1
	5
	1
	2
	4
	7

$$f(s_1) = 1 +$$

S₄

1	2
4	
7	

$$f = 2 +$$

Initial state S_0

1	2	3
4	5	
7	8	6

Goal state S_f

1	2	3
4	5	6
7	8	

depth = 1

S_1

1	2	3
4		5
7	8	6

$f(S_1) = 1 + 2 = 3$

S_2

	2	3
1	4	5
7	8	6

$f(S_2) = 1 + 4 = 5$

S_3

1	2	3
7	4	5
	8	6

$f(S_3) = 1 + 4 = 5$

path $[S_1, S_2, S_3]$

depth = 2

S_4

1	2	3
4	5	
7	8	6

$f = 2 + 1 = 3$

S_5

1		3
4	2	5
7	8	6

$f = 2 + 3 = 5$

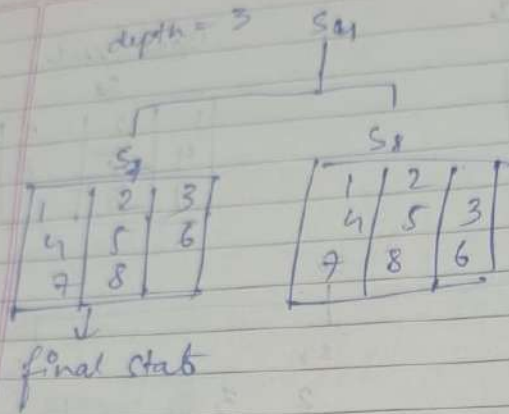
S_6

1	2	3
4	8	5
7		6

$f = 2 + 3 = 5$

path $(S_4, S_2, S_3, S_5, S_6)$

Date 08/10/25



Time Comparison to solve 8 puzzle

Initial state

1	2	3
5	0	6
4	7	8

	steps	time taken
dfs	26	0.001297 seconds
IDDFS	10	0.000372 seconds
A*	4	0.000091 seconds

10/9

```

import heapq

goal_state = '123456780'

moves = {
    'U': -3,
    'D': 3,
    'L': -1,
    'R': 1
}

invalid_moves = {
    0: ['U', 'L'], 1: ['U'], 2: ['U', 'R'],
    3: ['L'],      5: ['R'],
    6: ['D', 'L'], 7: ['D'], 8: ['D', 'R']
}

def move_tile(state, direction):
    index = state.index('0')
    if direction in invalid_moves.get(index, []):
        return None

    new_index = index + moves[direction]
    if new_index < 0 or new_index >= 9:
        return None

    state_list = list(state)
    state_list[index], state_list[new_index] = state_list[new_index], state_list[index]
    return ''.join(state_list)

def print_state(state):
    for i in range(0, 9, 3):
        print(' '.join(state[i:i+3]).replace('0', ' '))
    print()

def manhattan_distance(state):
    distance = 0
    for i, val in enumerate(state):
        if val == '0':
            continue
        goal_pos = int(val) - 1
        current_row, current_col = divmod(i, 3)
        goal_row, goal_col = divmod(goal_pos, 3)
        distance += abs(current_row - goal_row) + abs(current_col - goal_col)
    return distance

def a_star(start_state):

```

```

visited_count = 0
open_set = []
heapq.heappush(open_set, (manhattan_distance(start_state), 0, start_state, []))
visited = set()

while open_set:
    f, g, current_state, path = heapq.heappop(open_set)
    visited_count += 1

    if current_state == goal_state:
        return path, visited_count

    if current_state in visited:
        continue
    visited.add(current_state)

    for direction in moves:
        new_state = move_tile(current_state, direction)
        if new_state and new_state not in visited:
            new_g = g + 1
            new_f = new_g + manhattan_distance(new_state)
            heapq.heappush(open_set, (new_f, new_g, new_state, path + [direction]))

    return None, visited_count

# Main
start = input("Enter start state (e.g., 724506831): ")

if len(start) == 9 and set(start) == set('012345678'):
    print("Start state:")
    print_state(start)

    result, visited_states = a_star(start)

    print(f"Total states visited: {visited_states}")

    if result is not None:
        print("Solution found!")
        print("Moves:", ' '.join(result))
        print("Number of moves:", len(result))
        print("1BM23CS299 sanchit mehta\n")

        current_state = start
        for i, move in enumerate(result, 1):
            current_state = move_tile(current_state, move)
            print(f"Move {i}: {move}")
            print_state(current_state)

```

```
else:
    print("No solution exists for the given start state.")
else:
    print("Invalid input! Please enter a 9-digit string using digits 0-8 without repetition.")
```

```
➡ Enter start state (e.g., 724506831): 283164705
Start state:
2 8 3
1 6 4
7 5

Total states visited: 7
Solution found!
Moves: U U L D R
Number of moves: 5
1BM23CS299 sanchit mehta

Move 1: U
2 8 3
1 4
7 6 5

Move 2: U
2 3
1 8 4
7 6 5

Move 3: L
2 3
1 8 4
7 6 5

Move 4: D
1 2 3
8 4
7 6 5

Move 5: R
1 2 3
8 4
7 6 5
```

Program 4

Implement Hill Climbing search algorithm to solve N-Queens problem

Date
08/10/20

Lab-4 & 5

Hill climbing Algorithm ~~for~~ ~~maximizing~~

function hillclimbing(problem) returns a
state that is local maximum

current \leftarrow MakeNode (problem.initial.state)

loop do

neighbour \leftarrow highest value successor of
current

if neighbour \leq current value
then return current state

current \leftarrow neighbour

~~Hill climbing technique to solve 4-queens~~

~~Simulated Annealing~~

$$P(E) = e^{-\frac{\Delta E}{T}}$$

current \leftarrow initial state

T \leftarrow a large positive value

while T > 0 do

next \leftarrow a random neighbour of current

$\Delta E \leftarrow$ current cost - next cost

if $\Delta E > 0$

current \leftarrow next

else

current \leftarrow next with probability P(E)

end if

decrease T
end while
return current

→ 4 Queens using hill climbing search

Enter the initial state (e.g., 2 0 3 1): 0 1 2

initial state: [0, 1, 2, 3] with cost: 6

Q - - -
- Q - -
- - Q -
- - - Q

step 1:

Best neighbor [1, 0, 2, 3], cost: 6

Q - - -
Q - - -
- - Q -
- - - Q

Step 2:

Best neighbour [2, 0, 1, 3], cost: 1

- Q - -
- - Q -
Q - - -
- - - Q

step 3
Best

- Q - -
- - Q -
Q - - -

Go

→ Sir

Step 3

But neighbours $[2, 0, 3, 1]$ cost = 0

- Q -
- - Q
Q - - -
- - Q -

Goal state reached

7 23

→ Simulated annealing for N Queens

Initial state: $[2, 0, 1, 3]$ cost: 2

- Q - -
- - Q -
Q - - -
- - - Q

Final state: $[1, 3, 0, 2]$

- Q - -
Q - - -
- - - Q
- Q - -

Checking simulated Annealing Threshold

$N=4 \rightarrow$ success rate: 100%

$N=14 \rightarrow$ " : 100%

$N=24 \rightarrow$ " : 90%

$N=34 \rightarrow$ " : 60%

$N=44 \rightarrow$ " : 40%

```

import random
import time

def print_board(state):
    """Prints the chessboard for a given state."""
    n = len(state)
    for row in range(n):
        line = ""
        for col in range(n):
            if state[col] == row:
                line += "Q "
            else:
                line += ". "
        print(line)
    print()

def compute_heuristic(state):
    """Computes the number of attacking pairs of queens."""
    h = 0
    n = len(state)
    for i in range(n):
        for j in range(i + 1, n):
            if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
                h += 1
    return h

def get_neighbors(state):
    """Generates all possible neighbors by moving one queen in its column."""
    neighbors = []
    n = len(state)
    for col in range(n):
        for row in range(n):
            if row != state[col]:
                neighbor = list(state)
                neighbor[col] = row
                neighbors.append(neighbor)
    return neighbors

def hill_climb_verbose(initial_state, step_delay=0.5):
    """Hill climbing algorithm with verbose output at each step."""
    current = initial_state
    current_h = compute_heuristic(current)
    step = 0

    print(f'Initial state (heuristic: {current_h}):')
    print_board(current)
    time.sleep(step_delay)

```

```

while True:
    neighbors = get_neighbors(current)
    next_state = None
    next_h = current_h

    for neighbor in neighbors:
        h = compute_heuristic(neighbor)
        if h < next_h:
            next_state = neighbor
            next_h = h

    if next_h >= current_h:
        print(f'Reached local minimum at step {step}, heuristic: {current_h}')
        return current, current_h

    current = next_state
    current_h = next_h
    step += 1
    print(f'Step {step}: (heuristic: {current_h})')
    print_board(current)
    time.sleep(step_delay)

def solve_n_queens_verbose(n, max_restarts=1000):
    """Solves N-Queens problem using hill climbing with restarts and verbose output."""
    for attempt in range(max_restarts):
        print(f'\n=== Restart {attempt + 1} ===\n')
        initial_state = [random.randint(0, n - 1) for _ in range(n)]
        solution, h = hill_climb_verbose(initial_state)
        if h == 0:
            print(f'Solution found after {attempt + 1} restart(s):')
            print_board(solution)
            return solution
        else:
            print(f'No solution in this attempt (local minimum).\n')
    print("Failed to find a solution after max restarts.")
    return None

# --- Run the algorithm ---
if __name__ == "__main__":
    N = int(input("Enter the number of queens (N): "))
    solve_n_queens_verbose(N)
    print("1BM23CS299 Sanchit Mehta")

```

Output:

Enter the number of queens (N): 4

=== Restart 1 ===

Initial state (heuristic: 3):

Q . Q .
. Q . .
... Q
....

Step 1: (heuristic: 1)

.. Q .
. Q . .
... Q
Q . . .

Reached local minimum at step 1, heuristic: 1

✗ No solution in this attempt (local minimum).

=== Restart 2 ===

Initial state (heuristic: 3):

. Q . .
.. Q .
....
Q . . Q

Step 1: (heuristic: 1)

. Q . .
.. Q .
Q . . .
... Q

Reached local minimum at step 1, heuristic: 1

✗ No solution in this attempt (local minimum).

=== Restart 3 ===

Initial state (heuristic: 2):

....
. Q . Q
....
Q . Q .

Step 1: (heuristic: 1)

. Q . .
... Q
....

Q . Q .

Step 2: (heuristic: 0)

. Q . .

. . . Q

Q . . .

. . Q .

Reached local minimum at step 2, heuristic: 0

✅ Solution found after 3 restart(s):

. Q . .

. . . Q

Q . . .

. . Q .

1BM23CS299 sanchit

Program 5

Simulated Annealing to Solve 8-Queens problem

Q Write a program to implement Simulated Annealing Algorithm.

Step-1 : State = [1, 3, 2, 0], Cost = 1

. . . ϕ
 ϕ - -
- - ϕ -
- ϕ - -

Step 2 : State = [1, 3, 0, 2], Cost = 0

- - ϕ -
 ϕ - - -
- - - ϕ
- ϕ - -

Solution found at step 2

final state : [1, 3, 0, 2]

final cost (no of attacking pairs) : 0

- - ϕ -
 ϕ - - -
- - - ϕ
- ϕ - -

Algo: -

Current \leftarrow initial state
T \leftarrow a large positive value
while T > 0 do
 next \leftarrow a random neighbor of current
 $\Delta E \leftarrow$ Current cost - next cost
 if $\Delta E > 0$ then
 Current \leftarrow next
 else
 Current \leftarrow next with probability
 $P = e^{\frac{\Delta E}{T}}$
 end if
 decrease T
end while
return Current

Output \Rightarrow Initial state: [1, 0, 2, 3]

0 - 0 - -

0 - - -

1 - - 0 -

- - - 0

Step 0 : state: [1, 0, 2, 3] cost =

- 0 - -

0 - - -

- - 0 -

- - - 0

```

import random
import math

def compute_heuristic(state):
    """Number of attacking pairs."""
    h = 0
    n = len(state)
    for i in range(n):
        for j in range(i + 1, n):
            if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
                h += 1
    return h

def random_neighbor(state):
    """Returns a neighbor by randomly changing one queen's row."""
    n = len(state)
    neighbor = state[:]
    col = random.randint(0, n - 1)
    old_row = neighbor[col]
    new_row = random.choice([r for r in range(n) if r != old_row])
    neighbor[col] = new_row
    return neighbor

def dual_simulated_annealing(n, max_iter=10000, initial_temp=100.0, cooling_rate=0.99):
    """Simulated Annealing with dual acceptance strategy."""
    current = [random.randint(0, n - 1) for _ in range(n)]
    current_h = compute_heuristic(current)
    temperature = initial_temp

    for step in range(max_iter):
        if current_h == 0:
            print(f"🟢 Solution found at step {step}")
            return current

        neighbor = random_neighbor(current)
        neighbor_h = compute_heuristic(neighbor)
        delta = neighbor_h - current_h

        if delta < 0:
            current = neighbor
            current_h = neighbor_h
        else:
            # Dual acceptance: standard + small chance of higher uphill move
            probability = math.exp(-delta / temperature)
            if random.random() < probability:
                current = neighbor
                current_h = neighbor_h

```

```

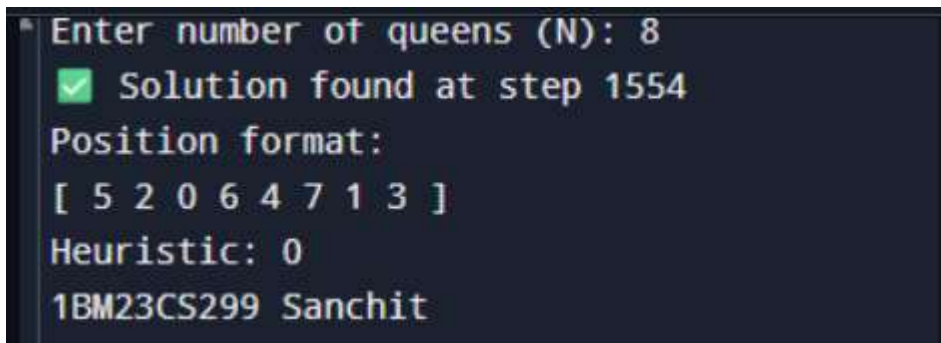
    temperature *= cooling_rate
    if temperature < 1e-5: # Restart if stuck
        temperature = initial_temp
        current = [random.randint(0, n - 1) for _ in range(n)]
        current_h = compute_heuristic(current)

    print("❌ Failed to find solution within max iterations.")
    return None

# --- Run the algorithm ---
if __name__ == "__main__":
    N = int(input("Enter number of queens (N): "))
    solution = dual_simulated_annealing(N)

    if solution:
        print("Position format:")
        print("[", " ".join(str(x) for x in solution), "]")
        print("Heuristic:", compute_heuristic(solution))
        print("1BM23CS299 Sanchit")

```



```

Enter number of queens (N): 8
✅ Solution found at step 1554
Position format:
[ 5 2 0 6 4 7 1 3 ]
Heuristic: 0
1BM23CS299 Sanchit

```

Program 6

Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not:

Lab 6
 8) KB using propositional logic & query entails the knowledge base

→ Algorithm $TI_ENTAILS_USER_INPUTS$

Input:
 $KB_sentences \leftarrow$ list of propositional sentences from user
 $query \leftarrow$ query sentence from user

Process:
 $symbols \leftarrow$ all unique propositional symbols appearing in $KB_sentences$ and $query$
 return $TI_CHECK_ALL(KB_sentences, query, symbols, empty_model)$

→ Function $TI_CHECK_ALL(KB, \alpha, symbols, model)$:

if $symbols$ is empty then
 if $PL_TRUE?(KB, model)$ then
 return $PL_TRUE?(\alpha, model)$
 else
 return True

else

$P \leftarrow first(symbols)$

return $symbols - \{P\}$

$model_true = model \cup \{P = true\}$
 $model_false = model \cup \{P = false\}$

return ($TI_CHECK_ALL(KB, \alpha, rest, model_true)$
 AND
 $TI_CHECK_ALL(KB, \alpha, rest, model_false)$)

→ Function $PL_TRUE?(sentence_set, model)$:

for each sentence S in $sentence_set$:
 if S evaluates to false under $model$:
 return False

return True

2) KB:

1) $Q \rightarrow P$

2) $P \rightarrow \neg Q$

3) $Q \vee R$

→ Truth table

Queries

1) R

2) ~~$P \rightarrow P$~~ $P \rightarrow P$

3) $Q \rightarrow R$

α_2	α_3
$P \rightarrow P$	$Q \rightarrow R$
T	T
F	(T)
T	F
F	T
T	T
F	(T)
F	F
(T)	T

entails
KB

Ex 1: KB = $(A \vee C) \wedge (B)$

Output:

Enter KB sentences:

$(A \vee C) \wedge (B \vee \neg C)$

$(a \vee c) \wedge (b \vee \neg c)$

Enter query sentence:

$a \vee b$

KB entails Query (KB \models Query)

Ex 2: Enter KB sentences:

$q \rightarrow P$

$P \rightarrow \neg q$

$q \vee r$

Enter Query sentence:

R

KB entails Query (KB \models R)

Enter Query sentence:

$r \rightarrow P$

KB does NOT entail Query (KB $\not\models$ Query)

Enter Query sentence:

$q \rightarrow r$

KB entails Query (KB \models Query)

P	Q	R	Q → P	P → Q	Q ∨ R	KB
T	T	T	T	T	T	T
T	T	F	T	F	T	F
T	F	T	F	T	T	F
T	F	F	F	F	F	F
F	T	T	T	T	T	T
F	T	F	T	F	F	F
F	F	T	F	T	T	F
F	F	F	F	F	F	F

KB is true:
 $(P, Q, R) = (F, F, T)$
 $(P, Q, R) = (T, F, T)$

α
 KB entails $R \ \& \ Q \rightarrow R$
 not entails $R \rightarrow P$

α_1
 α_2
 α_3
 α_4
 α_5
 α_6
 α_7
 α_8
 α_9
 α_{10}
 α_{11}
 α_{12}
 α_{13}
 α_{14}
 α_{15}
 α_{16}
 α_{17}
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 α_{90}
 α_{91}
 α_{92}
 α_{93}
 α_{94}
 α_{95}
 α_{96}
 α_{97}
 α_{98}
 α_{99}
 α_{100}

Query entails

doesn't entail

KB entails

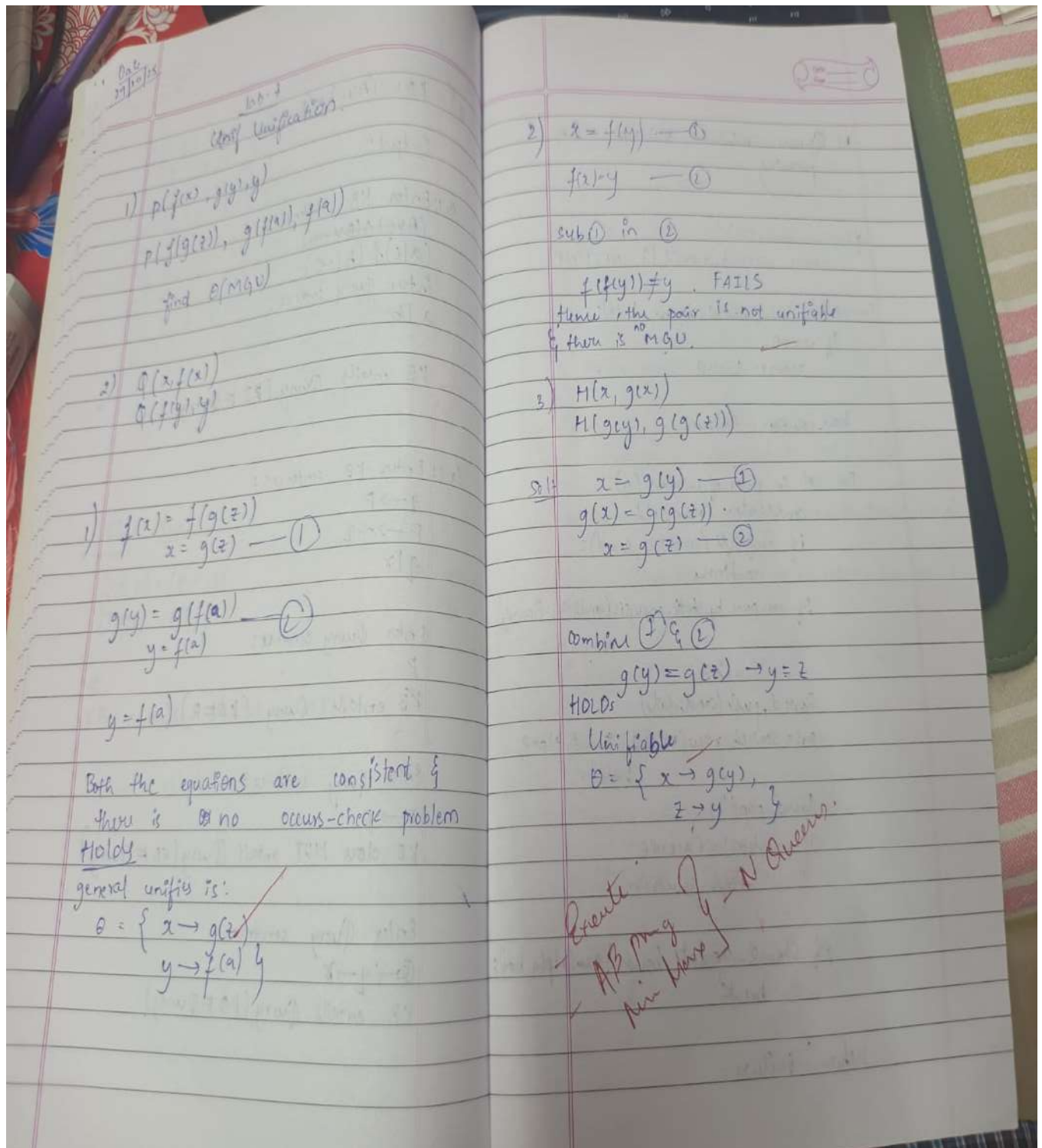
```
▲ Enter knowledge base (e.g. (and A (or B C))): A
Enter query (e.g. A): A
Symbols: ['A']
A   KB  α
True   True   True
False  False  False

Does KB entail α? : True

=== Code Execution Successful ===
```

Program 7

Implement unification in first order logic:



```
import json
```

```
# --- Helper Functions for Term Manipulation ---
```

```
def is_variable(term):
```

```
    """Checks if a term is a variable (a single capital letter string)."""
```

```
    return isinstance(term, str) and len(term) == 1 and 'A' <= term[0] <= 'Z'
```



```

def occurs_check(variable, term, sigma):
    """
    Checks if 'variable' occurs anywhere in 'term' under the current substitution 'sigma'.
    This prevents infinite recursion (e.g., unifying X with f(X)).
    """
    term = apply_substitution(term, sigma) # Check the substituted term

    if term == variable:
        return True

    # If the term is a list (function/predicate), check its arguments recursively
    if isinstance(term, list):
        for arg in term[1:]:
            if occurs_check(variable, arg, sigma):
                return True

    return False

def apply_substitution(term, sigma):
    """
    Applies the current substitution 'sigma' to a 'term' recursively.
    """
    if is_variable(term):
        # If the variable is bound in sigma, apply the binding
        if term in sigma:
            # Recursively apply the rest of the substitutions to the binding's value
            # This is critical for chains like X/f(Y), Y/a -> X/f(a)
            return apply_substitution(sigma[term], sigma)
        return term

    if isinstance(term, list):
        # Apply substitution to the arguments of the function/predicate
        new_term = [term[0]] # Keep the function/predicate symbol
        for arg in term[1:]:
            new_term.append(apply_substitution(arg, sigma))
        return new_term

    # Term is a constant or an unhandled type, return as is
    return term

def term_to_string(term):
    """
    Converts the internal list representation of a term into standard logic notation string.
    e.g., [f, 'Y'] -> "f(Y)"
    """
    if isinstance(term, str):

```

```

    return term

if isinstance(term, list):
    # Term is a function or predicate
    symbol = term[0]
    args = [term_to_string(arg) for arg in term[1:]]
    return f'{symbol}({','.join(args)})'

return str(term)

# --- Main Unification Function ---

def unify(term1, term2):
    """
    Implements the Unification Algorithm to find the MGU for term1 and term2.
    Returns the MGU as a dictionary or None if unification fails.
    """
    # Initialize the substitution set (MGU)
    sigma = {}

    # Initialize the list of pairs to resolve (the difference set)
    diff_set = [[term1, term2]]

    print(f'--- Unification Process Started ---')
    print(f'Initial Terms:')
    print(f'L1: {term_to_string(term1)}')
    print(f'L2: {term_to_string(term2)}')
    print("-" * 35)

    while diff_set:
        # Pop the current pair of terms to unify
        t1, t2 = diff_set.pop(0)

        # 1. Apply the current MGU to the terms before comparison
        t1_prime = apply_substitution(t1, sigma)
        t2_prime = apply_substitution(t2, sigma)

        print(f'Attempting to unify: {term_to_string(t1_prime)} vs {term_to_string(t2_prime)}')

        # 2. Check if terms are identical
        if t1_prime == t2_prime:
            print(f' -> Identical. Current MGU: {term_to_string(sigma)}')
            continue

        # 3. Handle Variable-Term unification

```

```

if is_variable(t1_prime):
    var, term = t1_prime, t2_prime
elif is_variable(t2_prime):
    var, term = t2_prime, t1_prime
else:
    var, term = None, None

if var:
    # Check if term is a variable, and if so, don't bind V/V
    if is_variable(term):
        print(f" -> Both are variables. Skipping {var} / {term}")
        # Ensure they are added back if not identical (which is caught by step 2).
        # If V1 != V2, we add V1/V2 or V2/V1 to sigma. Since step 2 handles V/V, this means V1
        != V2 here.
        if var != term:
            sigma[var] = term
            print(f" -> Variable binding added: {var} / {term_to_string(term)}. New MGU:
{term_to_string(sigma)}")
            # Occurs Check: Fail if the variable occurs in the term it's being bound to
            elif occurs_check(var, term, sigma):
                print(f" -> OCCURS CHECK FAILURE: Variable {var} occurs in
{term_to_string(term)}")
                return None

            # Create a new substitution {var / term}
        else:
            sigma[var] = term
            print(f" -> Variable binding added: {var} / {term_to_string(term)}. New MGU:
{term_to_string(sigma)}")

    # 4. Handle Complex Term (Function/Predicate) unification
    elif isinstance(t1_prime, list) and isinstance(t2_prime, list):
        # Check functor/predicate symbol and arity (number of arguments)
        if t1_prime[0] != t2_prime[0] or len(t1_prime) != len(t2_prime):
            print(f" -> FUNCTOR/ARITY MISMATCH: {t1_prime[0]} != {t2_prime[0]} or arity
mismatch.")
            return None

        # Add corresponding arguments to the difference set
        # Start from index 1 (after the symbol)
        for arg1, arg2 in zip(t1_prime[1:], t2_prime[1:]):
            diff_set.append([arg1, arg2])
        print(f" -> Complex terms matched. Adding arguments to difference set.")

    # 5. Handle Constant-Constant or other mismatches (Fail)
    else:
        print(f" -> TYPE/CONSTANT MISMATCH: {term_to_string(t1_prime)} and

```

```

{term_to_string(t2_prime)} cannot be unified.")
    return None

print("-" * 35)
print("--- Unification Successful ---")

# Final cleanup to ensure all bindings are fully resolved
final_mgu = {k: apply_substitution(v, sigma) for k, v in sigma.items()}
return final_mgu

# --- Define the Input Terms ---

# L1 = Q(a, g(X, a), f(Y))
literal1 = ['Q', 'a', ['g', 'X', 'a'], ['f', 'Y']]

# L2 = Q(a, g(f(b), a), X)
literal2 = ['Q', 'a', ['g', ['f', 'b'], 'a'], 'X']

# --- Run the Unification ---

mgu_result = unify(literal1, literal2)

if mgu_result is not None:
    print("\n[ Final MGU Result ]")

    # Format the final MGU for display using the new helper function
    clean_mgu = {k: term_to_string(v) for k, v in mgu_result.items()}
    final_output = ', '.join([f'{k} / {v}' for k, v in clean_mgu.items()])
    print(f'Final MGU: {{ {final_output} }}')

    # --- Verification ---
    print("\n[ Verification ]")
    unified_l1 = apply_substitution(literal1, mgu_result)
    unified_l2 = apply_substitution(literal2, mgu_result)

    print(f'L1 after MGU: {term_to_string(unified_l1)}')
    print(f'L2 after MGU: {term_to_string(unified_l2)}')

    if unified_l1 == unified_l2:
        print("-> SUCCESS: L1 and L2 are identical after applying the MGU.")
    else:
        print("-> ERROR: Unification failed verification.")
else:
    print("\nUnification FAILED.")

print("Sanchit Mehta 1BM23CS299")

```

Output

```
--- Unification Process Started ---
Initial Terms:
L1: Q(a, g(X, a), f(Y))
L2: Q(a, g(f(b), a), X)
-----
Attempting to unify: Q(a, g(X, a), f(Y)) vs Q(a, g(f(b), a), X)
  -> Complex terms matched. Adding arguments to difference set.
Attempting to unify: a vs a
  -> Identical. Current MGU: {}
Attempting to unify: g(X, a) vs g(f(b), a)
  -> Complex terms matched. Adding arguments to difference set.
Attempting to unify: f(Y) vs X
  -> Variable binding added: X / f(Y). New MGU: {'X': ['f', 'Y']}
Attempting to unify: f(Y) vs f(b)
  -> Complex terms matched. Adding arguments to difference set.
Attempting to unify: a vs a
  -> Identical. Current MGU: {'X': ['f', 'Y']}
Attempting to unify: Y vs b
  -> Variable binding added: Y / b. New MGU: {'X': ['f', 'Y'], 'Y': 'b'}
-----
--- Unification Successful ---

[ Final MGU Result ]
Final MGU: { X / f(b), Y / b }

[ Verification ]
L1 after MGU: Q(a, g(f(b), a), f(b))
L2 after MGU: Q(a, g(f(b), a), f(b))
-> SUCCESS: L1 and L2 are identical after applying the MGU.
Sanchit Mehta 1BM23CS299

=== Code Execution Successful ===
```

Program 8

Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning:

Date
15/11/20

lab-8 first Order logic

function $FOI_FC_ASK(KB, \alpha)$ returning
a substitution or false

inputs: KB , the knowledge base, a set of
first order definite clauses α ,
the query, or atomic sentence,

local variable: new , the new sentences
inferred on each iteration

repeat until new is empty

$new \leftarrow \{\}$

for each rule r in KB do

$Cp, r, \dots, p_n \Rightarrow q$ standardize

variables (rule)

for each θ such that $subset(\theta, p_1, \dots, p_n) =$
 $subset(\theta, p_1, \dots, p_n)$

for some p'_1, \dots, p'_n in KB

$q' \leftarrow subset(\theta, q)$

if q' does not unify with some
sentence already in KB or new then

add q' to new

$\theta \leftarrow unify(q', \alpha)$

if θ is not fail then return θ

add new to KB

return
false

```

from typing import List, Tuple, Dict, Set, Union

Predicate = Tuple[str, Tuple[str, ...]]

class Rule:
    def __init__(self, head: Predicate, body: List[Predicate]):
        self.head = head
        self.body = body

    def __repr__(self):
        body_str = ', '.join(f'{p[0]} {p[1]}' for p in self.body)
        return f'{body_str} => {self.head[0]} {self.head[1]}'

# Knowledge base
class KnowledgeBase:
    def __init__(self):
        self.facts: Set[Predicate] = set()
        self.rules: List[Rule] = []

    def add_fact(self, fact: Predicate):
        self.facts.add(fact)

    def add_rule(self, rule: Rule):
        self.rules.append(rule)

    def forward_chain(self, query: Predicate) -> bool:
        inferred = set(self.facts)
        added = True

        while added:
            added = False
            for rule in self.rules:
                if all(self._match_fact(body_pred, inferred) for body_pred in rule.body):
                    if not self._match_fact(rule.head, inferred):
                        inferred.add(rule.head)
                        added = True
                        print(f'Inferred: {rule.head}')

                if self._match_fact(query, inferred):
                    return True
            return self._match_fact(query, inferred)

    def _match_fact(self, self, pred: Predicate, fact_set: Set[Predicate]) -> bool:
        return pred in fact_set

# --- Example usage ---
if __name__ == "__main__":

```



```

kb = KnowledgeBase()

kb.add_fact(("Parent", ("John", "Mary")))
kb.add_fact(("Parent", ("Mary", "Sue")))

facts_list = list(kb.facts)
for f1 in facts_list:
    for f2 in facts_list:
        if f1[0] == "Parent" and f2[0] == "Parent":
            if f1[1][1] == f2[1][0]:
                head = ("Grandparent", (f1[1][0], f2[1][1]))
                body = [f1, f2]
                kb.add_rule(Rule(head, body))

query = ("Grandparent", ("John", "Sue"))
result = kb.forward_chain(query)

print(f'Query {query} is', "True" if result else "False")
print("sanchit 1bm23cs299")

```

Output

```

Inferred: ('Grandparent', ('John', 'Sue'))
Query ('Grandparent', ('John', 'Sue')) is True
sanchit 1bm23cs299

```

```

=== Code Execution Successful ===

```

Program 9

Create a knowledge base consisting of first order logic statements and prove the given query using Resolution

Resolution

- 1) convert all to CNF
- 2) negate conclusions & convert result to CNF
- 3) Add negated conclusions to the premise clauses
- 4) Repeat while contradictory or no progress is made:
 - a. select 2 clauses
 - b. Resolve them together, performing all required unifications
 - c. if resolvent is the empty clause, a contradiction has been found
 - d. If not, add resolvent to the premise

If we succeed on step 4 we have proved the conclusion

FOL \rightarrow CNF

- 1) Eliminate biconditional & implication
- 2) move \neg inwards
- 3) standard variables apart by renaming them: each quantifier should use diff variable
- 4) skolemize: each existential variable is replaced by a skolem constant or skolem functions of the universally quantified variables
- 5) Drop Universal quantifier
- 6) Distribute \wedge over \vee

Output

Knowledge Base CNF Clauses:

Parent(John,Mary)

\sim Parent(x,y) | Ancestor(x,y)

Parent(Mary,Sam)

\sim Parent(x,y) | \sim Ancestor(y,z) | Ancestor(x,z)

Query: Ancestor(John, Sam) => TRUE

Program 10

Implement Alpha-Beta Pruning

```

all-conflict(r1, c1, r2, c2):
    return (r1 == r2) or (c1 == c2) or
           (abs(r1 - r2) == abs(c1 - c2))

```

```

conflicts(r, c, Board):
    for q in Board:
        if all-conflict((r, c), q):
            return True
    return False

```

```

Order-of-columns(n):
    return heuristic-column-order-list

```

```

Can-prune-by-static-analyser(candidates, Board, row, n):
    return 'cand-anal-pies = (n - row)'

```

Output:

```

Board = [ ]
row = 1
column order tried = [1, 2, 3, 4]
[(1, 2), (2, 3), (3, 4), (4, 2)]

```

```

. Q . .
. . . Q
Q . . .
. . Q .

```

N Queens minimax w/ alpha-beta pruning

if solve n-queens(n):
return search_row(1, [], -INF, +INF)

search_row(row, board, alpha, beta):

if row > n:
return board

best_solution = FAILURE

for col in order_of_columns(n):

candidate = (row, col)

if conflicts(candidate, board):
continue

if can-prune-by-static-analysis(candidate, board,
row, n):

continue

board.push(candidate)

sol = search_row(row+1, board, alpha,
beta)

board.pop()

if solution != FAILURE:

return solution

if should-update-bounds & prune(alpha, beta):
break

return Failure

```

Code:
import math

def alpha_beta_search(state):
    return max_value(state, -math.inf, math.inf)

def max_value(state, alpha, beta):
    if terminal_test(state):
        return utility(state)
    v = -math.inf
    for a in actions(state):
        v = max(v, min_value(result(state, a), alpha, beta))
        if v >= beta:
            return v
    alpha = max(alpha, v)
    return v

def min_value(state, alpha, beta):
    if terminal_test(state):
        return utility(state)
    v = math.inf
    for a in actions(state):
        v = min(v, max_value(result(state, a), alpha, beta))
        if v <= alpha:
            return v
    beta = min(beta, v)
    return v

values = [3, 5, 6, 9, 1, 2, 0, -1]
max_depth = 3

def terminal_test(state):
    return state >= len(values) // 2**(max_depth - depth[state])

def utility(state):
    return values[state]

def actions(state):
    if depth[state] == max_depth:
        return []
    return [0, 1]

def result(state, action):
    child = state * 2 + 1 + action
    depth[child] = depth[state] + 1
    return child

```

```
depth = {0: 0}  
print("Optimal value:", alpha_beta_search(0))  
print("Sanchit Mehta")
```

```
Best value for maximizer: 3  
Sanchit Mehta 1bm23cs299
```