



University of Engineering & Management, Kolkata

Term - II Examination, October - November, 2021

Programme Name: B.Tech in Computer Science

Semester: 5th

Paper Name: Signals & Systems

Paper Code: ESC501

Full Marks: 100

Time: 3 hours

GROUP A (20 Marks)

Answer the following questions. Each question is of 2 marks.

1.

- (i) State the convolution property of z-transform.
- (ii) Define Final value theorem of Laplace transform
- (iii) Explain the convolution property of z-transform.
- (iv) What is meant by impulse response of any system?
- (v) Give synthesis and analysis equations of CT Fourier Transform
- (vi) What is an anti-aliasing filter?
- (vii) Explain sampling frequency.
- (viii) What is over sampling?
- (ix) What is the role of zero padding in DFT based signal analysis?
- (x) What is zero order hold?

GROUP B (30 Marks)

Answer the following questions. Each question is of 5 marks.

- 2. Find the z-transform of the causal sequence. $X(n) = \{1, 0, 3, -1, 2\}$.
- 3. Prove the linearity property of Laplace Transform.

4. Find the Laplace transform of the function $x(t) = e^{-5t}[u(t) - u(t-5)]$

5. A. Explain the problems with related to ideal Low Pass Filter.

OR

B. Write the complex form of a Fourier Series $f(x)$ defined in the interval $(c, c+2l)$.

6. A. Explain the complete process of reconstruction of a Band-limited signal using ideal low pass filter.

OR

B. Explain the Frequency Domain representation of a sampled signal.

7. A. Explain Dirichelt's conditions for a function to be expanded as a Fourier Series.

OR

B. Given a continuous-time signal $x(t)$ with Nyquist rate ω_0 . Determine the Nyquist rate for the continuous time signal $x^2(t)$.

GROUP C (50 Marks)

Answer the following questions. Each question is of 10 marks.

8. A. Find the initial value of the z transform

$$X(z) = \frac{3z + 4}{(z - 1)(z + 1)}$$

OR

B. Consider the signal $x(t) = [\cos t + \sin t + \cos t \sin t]$. Find the even and odd component of the signal $x(t)$.

9. Explain the following operations on signals with suitable example.

- i) Time shifting
- ii) Time scaling
- iii) Time reversal
- iv) Signal addition

10. A. From the given impulse response $h(n)$ of the system, find whether the systems are causal and stable i)

$$h(n) = 2^n u(-n)$$

ii)

$$h(n) = 5^n u(3 - n)$$

OR

10. B. Describe the relation between DFT to Fourier Series

OR

ii) Find the DTFT of the discrete sequence $x(n) = \{1, 1, 1, 1, 1, 1, 0, 0\}$

11. A. Write the complex form of a Fourier Series $f(x)$ defined in the interval $(c, c + 2l)$

OR

B. Find the z transform of the signal $x(n) = u(n) - u(n - 4)$

12. A. Demonstrate the sampling theorem and the sinc interpolation formula for the signal

$$f(t) = \text{sinc}^2(5\pi t) = \text{sinc}^2\left(\frac{10\pi t}{2}\right).$$

OR

B. Explain Nyquist rate. Then explain and prove the condition of oversampling
