

## Basic of R Software:-

1. R is a software for statistical analysis and data computing.
2. It is any objective effective data handling software and outcome storage is possible.
3. It is capable of graphical display.
4. It is a free software.

(Q1) Solve the following:

$$\begin{aligned} & 1) 4+6+8 \div 2 - 5 \\ & \rightarrow 4+6+8 / (2-5) \\ & \quad [1] 9 \end{aligned}$$

$$\begin{aligned} & 2) 2^2 + 1 - 31 + \sqrt{45} \\ & \rightarrow 2^2 + \text{abs}(-3) + \text{sqrt}(45) \\ & \quad [1] 13.7082 \end{aligned}$$

$$\begin{aligned} & 3) 5^3 + 7*5*8 + 46/5 \\ & \rightarrow 5^3 + 7*5*5 + 46/5 \\ & \quad [1] 414.2 \end{aligned}$$

problem:  
 $x = 20$   
 $y = 30$   
 $w = 2$

$$\begin{aligned} &\text{find } \\ &x^2 + y^3 + z \\ &\sqrt{x^2 + y} \\ &x^2 + y^2 \end{aligned}$$

$$\begin{aligned} &x^2 + y^3 + z \\ &x^2 + y^3 + z \\ &27402 \end{aligned}$$

$$\begin{aligned} &\text{so } x^2 + y \\ &20 \cdot 73644 \end{aligned}$$

$$\begin{aligned} &x^2 + y^2 \\ &1300 \end{aligned}$$

convert into a matrix form

$\rightarrow x = \text{matrix}(nrow=4, ncol=2, \text{data} = c(1, 2, 3, 4, 5, 6, 7, 8))$

	{,1}	{,2}
{1,}	1	5
{2,}	2	6
{3,}	3	7
{4,}	4	8

Q2:

$$1) C(2, 3, 5, 7)^2$$

$$\rightarrow x = C(2, 3, 5, 7)^2$$

~~2)~~

$$\rightarrow [1] 4 \ 6 \ 10 \ 14$$

$$\rightarrow [2] 4 \ 6 \ 10 \ 14$$

$$2) C(2, 3, 5, 7) + C(2, 1, 3)$$

$$\rightarrow [1] 4 \ 6 \ 10 \ 21$$

$$3) C(1, 6, 2, 3) * C(-2, -3, -4, -1)$$

$$\rightarrow [1] -2 \ -18 \ -8 \ -3$$

$$4) C(2, 3, 5, 7)^2$$

$$\rightarrow [1] 4 \ 6 \ 10 \ 14$$

$$5) C(4, 6, 8, 9, 4, 5) - C(1, 2, 3)$$

$$\rightarrow [1] 4 \ 12 \ 24 \ 9 \ 8 \ 15$$

Q5) Find  $x+3y$  and  $2x+3y$  where.

$$x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}, y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 8 \end{bmatrix}$$

```

> x=matrix(nrow=3, ncol=3, data=c(4,7,9,-2,0,3,
>   7,0,7
>   9,-5,3))
> y=matrix(nrow=3, ncol=3, data=c(10,12,15,-5,-4,-6,
>   12,-4,9
>   15,-6,5))
> 2*x + 3*y
     [,1] [,2] [,3]
[1,]    8    1    9
[2,]   21    4    9
[3,]   27    6    7
  
```

Q5)

Marks: 59, 20, 35, 24, 46, 56, 39, 45, 27, 22, 47,  
58, 54, 40, 30, 32, 36, 29, 33, 39.

```

> x=c(data)
> breaks=seq(20, 60, 5)
> a=cut(x=breaks, right=FALSE)
> b=table(a)
> c=transform(b)
> c
  
```

a	freq	Ans
[20, 25)	3	
[25, 30)	2	
[30, 35)	1	
[35, 40)	4	51219
[40, 45)	1	
[45, 50)	3	
[50, 55)	2	
[55, 60)	4	

## PRACTICAL-2

i) Check whether the followings are pmf or not.

$x$	$p(x)$
0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

If the given data is pmf then  $\sum p(x) = 1$  and  $p(x_i) \geq 0$

Hence,

$$\begin{aligned} \sum p(x) &= p(1) + p(2) + p(0) + p(3) + p(4) \\ &\quad + p(5) \\ &= 0.1 + 0.2 + (-0.5) + 0.4 + 0.3 + 0.5 \end{aligned}$$

$\therefore \sum p(x) = 1$   
 $\therefore \sum p(x) \neq 1$  but  $p(2) = -0.5$   
Hence it is not a pmf

Source code:

```
prob = [0.1]
```

$x$	1	2	3	4	5
$p(x)$	0.2	0.2	0.3	0.2	0.2

The condition for pmf is  $\sum p(x) = 1$  and  $p(x) \geq 0$ ,

$$\begin{aligned} \sum p(x) &= p(1) + p(2) + p(3) + p(4) + p(5) \\ &= 0.2 + 0.2 + 0.3 + 0.2 + 0.2 \end{aligned}$$

$$\sum p(x) = 1.1$$

$\therefore \sum p(x) \neq 1$ .

$\therefore$  The given data is not a pmf because the  $\sum p(x) \neq 1$

\* Source code:-

```
#prob=[0.2,0.2,0.3,0.2,0.2]
sum(prob)
[1]
```

$x$	10	20	30	40	50
$p(x)$	0.2	0.2	0.35	0.15	0.1

The condition for pmf is  $\sum p(x) = 1$  and  $p(x) \geq 0$

$$\begin{aligned} \sum p(x) &= p(10) + p(20) + p(30) + p(40) + p(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \end{aligned}$$

$$\sum p(x) = 1$$

$\therefore \sum p(x) = 1$  Hence it is a pmf.

\* Source code

```
#prob=[0.2,0.2,0.35,0.15,0.1]
sum(prob)
[1]
```

it's x . 32  
prob

Q2) find the c.d.f for the following pmf  
and sketch the graph.

x	10	20	30	40	50
PCX	0.2	0.2	0.35	0.15	0.1

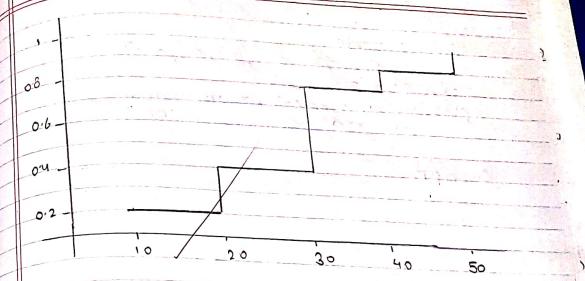
Sol:- Given data is pmf. To find c.d.f from pmf we will use the

$$\begin{aligned} F(x) &= 0 & x < 10 \\ &= 0.2 & 10 \leq x < 20 \\ &= 0.4 & 20 \leq x < 30 \\ &= 0.75 & 30 \leq x < 40 \\ &= 0.90 & 40 \leq x < 50 \\ &= 1.0 & x \geq 50 \end{aligned}$$

x	10	20	30	40	50
PCX	0.2	0.2	0.35	0.15	0.1

CDF  
source code:-  
>prob = [0.2, 0.2, 0.35, 0.15, 0.1];  
>cumsum(prob)  
>x = [10, 20, 30, 40, 50];  
>plot(x, cumsum(prob), "s")

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Q2) find the c.d.f for the following pmf and sketch the graph.

x	1	2	3	4	5	6
PCX	0.15	0.25	0.1	0.2	0.2	0.1

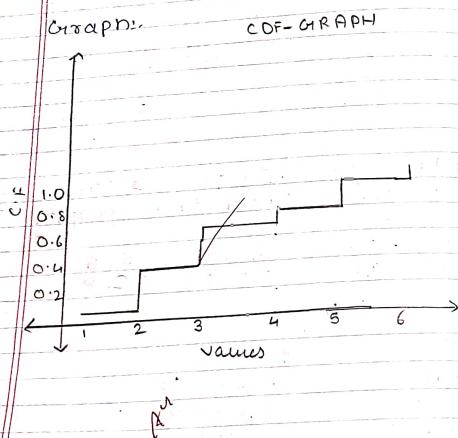
Sol:-  
 $F(x) = 0 \quad x < 1$   
 $= 0.15 \quad 1 \leq x < 2$   
 $= 0.40 \quad 2 \leq x < 3$   
 $= 0.50 \quad 3 \leq x < 4$   
 ~~$= 0.70 \quad 4 \leq x < 5$~~   
 $= 0.90 \quad 5 \leq x < 6$   
 $= 1.00 \quad x \geq 6$

58.

Source code:-

```
>x=c(0.15,0.25,0.1,0.2,0.2,0.1)
>y=c(1,2,3,4,5,6)
>plot(y,cumsum(x),xlab="values",ylab="C",
+col="red","s",main="CDF-GRAPH")
```

Graph:-



58.

Q13 check whether the following is pdf or not

$$\text{if } f(x) = 3 - 2x \quad ; \quad 0 \leq x \leq 1$$

$$\text{ii) } f(x) = 3x^2 \quad ; \quad 0 < x < 1$$

$$\text{iii) } f(x) = 3 - 2x \quad ; \quad 0 \leq x < 1$$

$$\int f(x)$$

$$= \int (3 - 2x) dx$$

$$= \int 3dx - \int 2x dx$$

$$= [3x - x^2]_0^1 = 2''$$

$\therefore \int f(x) = 1 \therefore \text{It is not a pdf}$

$$\text{iv) } f(x) = 3x^2 \quad ; \quad 0 \leq x < 1$$

$$\int f(x)$$

$$= \int 3x^2$$

$$= 3 \int x^2$$

$$= 3 \left[ \frac{x^3}{3} \right]_0^1 \quad \left[ \because x^n = \frac{x^{n+1}}{n+1} \right]$$

$$= x^3$$

$$= 1$$

$\therefore \int f(x) = 1 \therefore \text{It is a pdf}$

### Practical-3

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TOPIC:- To study Binomial Distribution

$$\text{i) } P(X=x) = d\text{ binom}(x, n, p)$$

$$\text{ii) } P(X \leq x) = p\text{ binom}(x, n, p)$$

$$\text{iii) } P(X > x) = 1 - P\text{ binom}(x, n, p)$$

$$\text{iv) If } x \text{ is unknown}$$

$$P_i = P(X \leq i) \dots \text{ (given)}$$

$$q\text{ binom}(P_i, n, p)$$

Q17 Find the probability of exactly 10 successes in 100 trials with  $p = 0.1$

$$> d\text{ binom}(10, 100, 0.1)$$

[1] 0.1318653

Q20 Suppose there are 12 MCQs. Each question has 5 options out of which 1 is correct.

Find probability of:

i) exactly 4 correct answers.

ii) almost 4 correct answers.

iii) More than 5 correct answers.

$$\text{i) } > d\text{ binom}(4, 12, 1/5)$$

[1] 0.1328756

$$\text{ii) } > p\text{ binom}(4, 12, 1/5)$$

[1] 0.927445

$$\text{iii) } > 1 - p\text{ binom}(4, 12, 1/5)$$

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Q3) Find the complete distribution when  
 $n=5, p=0.1$

```
> d binom(0:5, 0.5, 0.1)
[1] 0.50049
0.32805
0.7290
0.00810
0.00045
0.00001.
```

Q4)  $n=12, p=0.25$ . Find:  
i)  $P(X=5)$     ii)  $P(X \leq 5)$     iii)  $P(X > 7)$   
iv)  $P(6 < X < 7)$

```
i) d binom(5/12, 0.25)
[1] 0.1032414
```

```
ii) p binom(5/12, 0.25)
[1] 0.4555978
```

```
iii) > 1 - p binom(7, 12, 0.25)
[1] 0.00278151
```

```
iv) > dbinom(6, 12, 0.25)
[1] 0.04014945
```

Q5) Find the complete distribution when  
 $n=5, p=0.1$

d binom(0:5, 0.5, 0.1)

Probability of salesman making a sell to  
customer 0.15. Find the probability of:  
i) no sell out of 10 customers

```
> d binom(0, 10, 0.15)
[1] 0.1908744
```

ii) [1] 0.3622748

Q6) A salesman has 20% probability of making  
a sell to a customer out of 30.

```
> d binom(0.88, 30, 0.2)
[1] 9
```

Q7) X followed binomial distribution with  $n=10$ ,  
 $p=0.3$ .

> n = 10

> p = 0.3

> x = 0:n

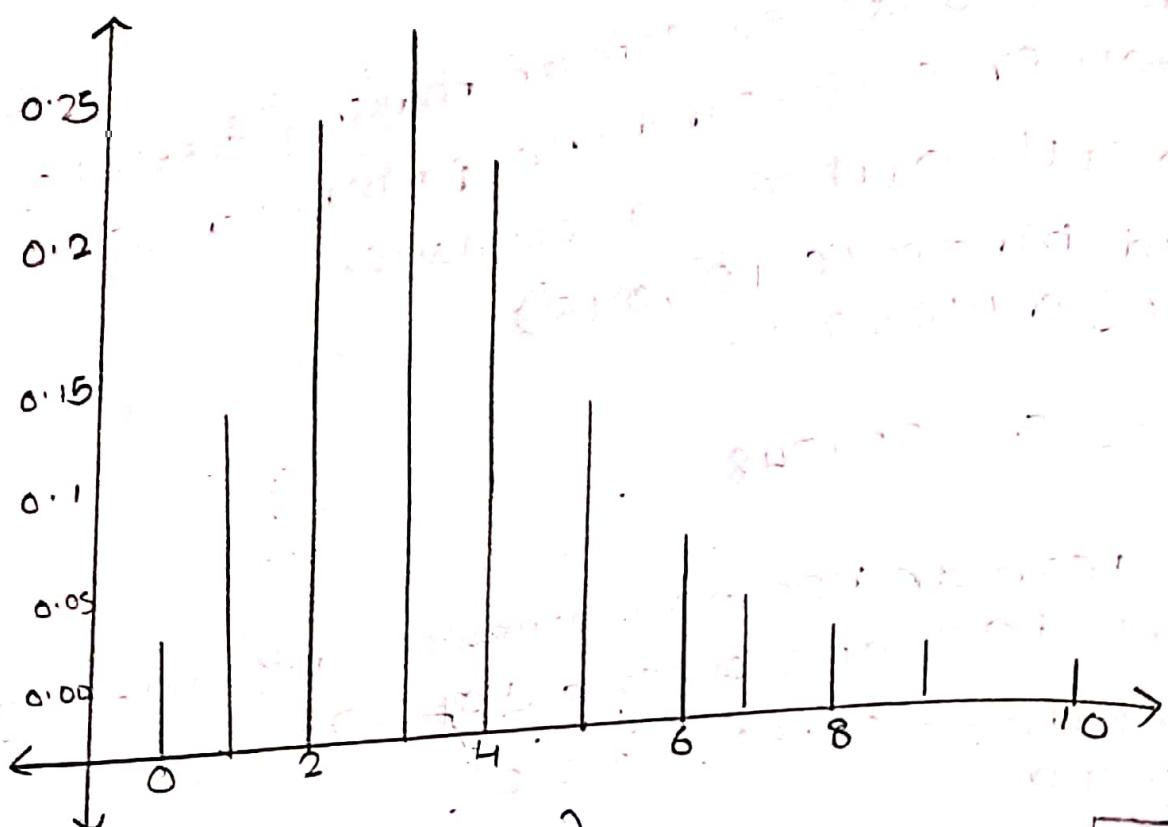
> prob = d binom(x, n, p)

> d = data.frame("xvalues" = x, "probability" = prob)

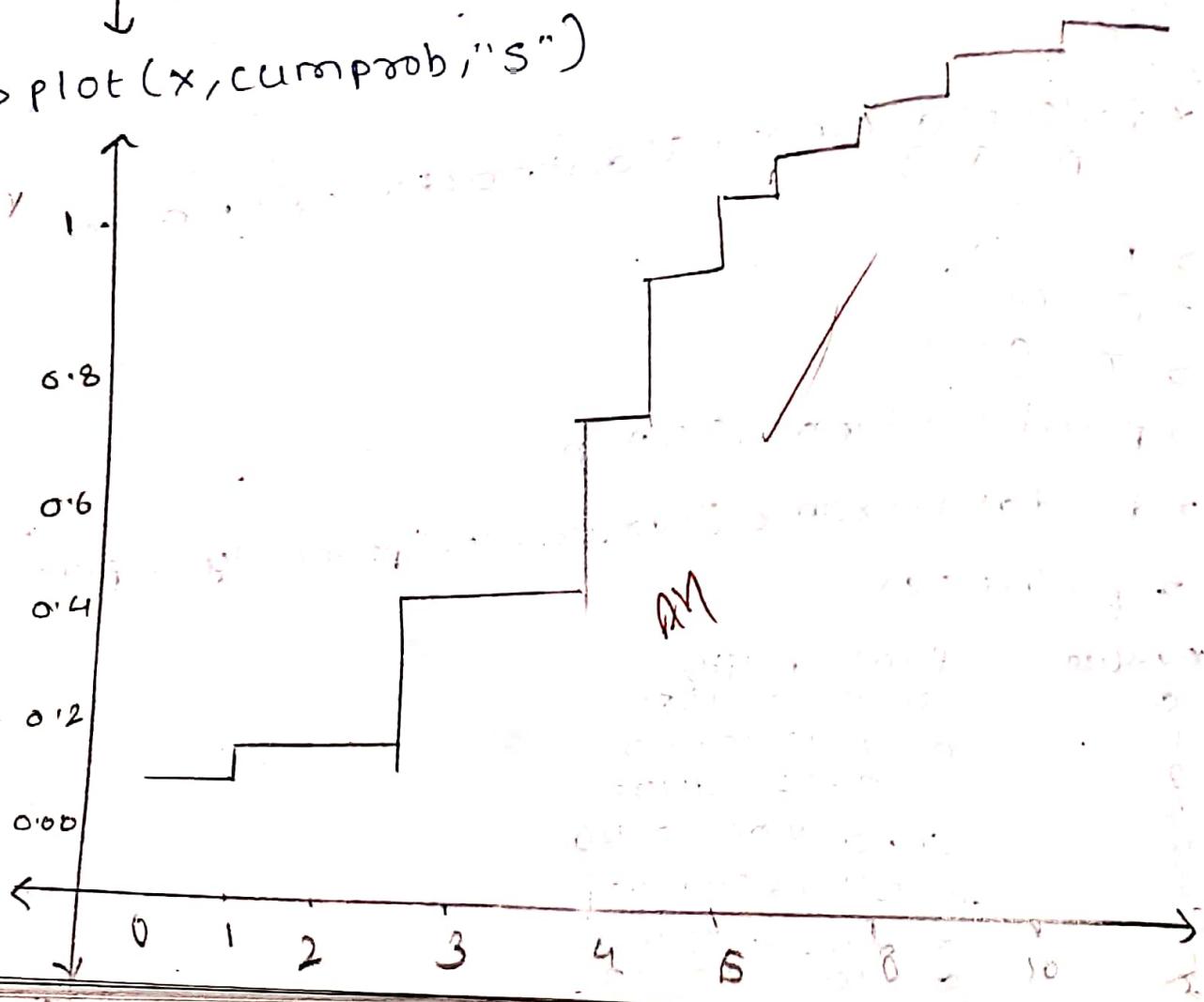
> print(d)

xvalues	probability
0	0.02824752
1	0.1215689210
2	0.233474405
3	0.209120940
4	0.167569090
5	0.1029193452
6	0.05193452
7	0.0193452
8	0.006452
9	0.00193452
10	0.000452

$\rightarrow \text{plot}(x, p \approx 0.6)$



$\rightarrow \text{plot}(x, \text{cumprob}, "S")$



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i)  $\geq p_1 = \text{pnorm}(15, 12, 3)$

?  $p_1$   
> cat ("P(X ≤ 15) = ", p1)

[1] 0.8413447  
 $P(X \leq 15) = 0.8413447$

ii)  $p_2 = \text{pnorm}(13, 12, 3) - \text{pnorm}(10, 12, 3)$

?  $p_2$   
[1] 0.3780661

? cat ("P(10 ≤ X < 13) = ", p2)  
 $P(10 \leq X < 13) = 0.3780661$

iii)  $\text{rnorm}(5, 12, 3)$

? [1] 16.380316 13539877 13050514  
4.181289

Q2)  $X$  follows normal distribution with  
 $\mu = 10$ ,  $\sigma = 2$ , Find:

i)  $\geq p_1 = \text{pnorm}(7, 10, 2)$

?  $p_1$   
[1] 0.0668072

ii)  $\geq p_2 = \text{pnorm}(12, 10, 2)$

?  $p_2$   
[1] 0.8351351

iii)  $\geq p_3 = 1 - \text{pnorm}(12, 10, 2)$

?  $p_3$

Q3) Answers:-

```
> x = rnorm(5, 15, 4)  
> x  
[1] 14.35444 11.8206 12.44472 15.79432  
    16.68769  
  
> am = mean(x)  
> cat("Sample mean is = ", am)  
Sample mean is = 14.2208  
  
> me = median(x)  
> cat("sample median is ", me)  
sample median is = 14.35444  
  
> n = 5  
> variance = (n-1) * var(x)/n  
> sd = sqrt(variance)  
> cat("sample sd is ", sd)  
sample is = 1.870638
```

Q5) Plot the Standard Normal graph.

```
> x = seq(-3, 3, by=0.1)  
> y = dnorm(x)  
> plot(x, y, xlab = "xvalues", ylab = "probabil",  
      main = "standard normal Graph")
```

## Practical - 5

## Normal and T-Test.

$$Q1] H_0: \mu = 15$$

$$H_1: \mu \neq 15$$

Random sample of size = 400 is drawn and it is calculated that the sample mean is 14.5. D is 3. Test the hypothesis at 5% level of significance.

$$> m_0 = 15$$

$$> m_x = 14$$

$$> n = 400$$

$$> z_{cal} = (m_x - m_0) / (D / \sqrt{n})$$

$$> z_{cal}$$

$$[1] -6.666667$$

> cat ("calculated value of z is.", z\_{cal})

calculated value of z is = -6.666667

$$> p_value = 2 * (1 - pnorm(z_{cal}))$$

$$> p_value = 2 * (1 - pnorm(abs(z_{cal})))$$

$$> p_value$$

$$[1] 2.61679e-11$$

$\therefore$  The p-value is less than 0.05 then the null hypothesis is rejected.

4) Last year the farmers lost 20% of their crops and sample of 60 fields are collected and found that a per 100 crops are insect polluted. Test the hypothesis at 1% level of significance.

$\geq p = 0.2$   
 $\geq p = 9/60$   
 $\geq n = 60$   
 $\geq \alpha = 1 - P$   
 $\geq z_{\text{cal}} = (p - \bar{p}) / \sqrt{p(1-p)/n}$   
 $\geq z_{\text{cal}} = 0.9682$   
 $\geq p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$   
 $\geq p_{\text{value}} = 0.8329216$   
 $\therefore \text{the value of } p \text{ is greater than } 0.05 \text{ or } 0.01$   
 $\therefore \text{the value is accepted}$

5) Test the hypothesis from the following sample at 5% level of significance.

$\text{H}_0: \mu = 12.5$   
 $\text{x} = c(12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.94, 11.89, 12.11)$   
 $\geq n = \text{length}(x)$   
 $\geq n = 9$   
 $\geq \text{mx} = \text{mean}(x)$   
 $\geq \text{var} = (n-1) * \text{var}(x) / n$   
 $\geq s.d = \text{sqrt}(\text{var})$   
 $\geq s.d = 0.495$   
 $\geq m_0 = 12.5$   
 $\geq t = (\text{mx} - m_0) / (s.d / (\sqrt{n}))$   
 $\geq t = -0.894904$

$\geq p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(t)))$   
 $\geq p_{\text{value}} \leq 0$

$\therefore \text{The pvalue is less than } 0.05$   
 $\therefore H_0 \text{ is rejected.}$

$\geq 16.170$

19/1/2019

## Practical - 6

P8 Topic: Large sample Test.

- i) Let the population mean (the exp amount spent by customer in a hotel) is 250. A sample of 100 customers selected. The sample mean is calculated as 275 and S.D is 30. Test the hypothesis that the population is 250 or not at 5% level of significance.
- ii) In a random sample of 1000 students, it is found that 750 use blue pen. Test the hypothesis the population proportion is 0.8 at 1% level of significance.

(a)  $H_0: \mu = 250$  against  $H_1: \mu \neq 275$   
 $\sigma_x = 275$   
 $S.D = 30$   
 $n = 100$   
 $z_{\text{cal}} = (\bar{x} - \mu_0) / (\sigma_x / \sqrt{n})$   
 $z_{\text{cal}}$   
 $p_{\text{value}}$   
 $[1] 8.3333$   
 $p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$   
 $p_{\text{value}}$   
 $[1] 0$   
 $\therefore p_{\text{value}} \text{ is less than } 0.05$   
 $\therefore \text{It is rejected at } 5\% \text{ level of significance.}$

Q2)  $H_0: p = 0.8$  against  $H_1: p \neq 0.8$

$p = 0.8$   
 $\alpha = 1 - p$   
 $\alpha = 750 / 1000$   
 $n = 1000$   
 $z_{\text{cal}} = (p - p_0) / (\sqrt{p_0(1-p_0)/n})$   
 $[1] -3.952847$   
 $p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$   
 $p_{\text{value}}$   
 $[1] 7.72268 e^{-5}$

$\therefore p_{\text{value}} \text{ is less than } 0.01$   
 $\therefore H_0 \text{ is rejected at } 1\% \text{ level of significance.}$

iii) Two random samples of size 1000 and 2000 are drawn from two populations with the same S.D = 2.5. The sample means are 67.5 and 68 respectively. Test the Hypothesis  $H_0: \mu_1 = \mu_2$  against  $H_1: \mu_1 \neq \mu_2$  at 5% level of significance.

H0

A study of noise level in two hospitals is given below. Test the claim that the two Hospitals have the same level of noise at 1% level of significance.

	HOS A	HOS B
size	84	84
mean	61.2	59.4
S.D	7.9	7.5

v) In a sample of 600 students in a college 400 use blue ink, in another college from sample of 900 students 450 use blue ink. Test the Hypothesis that the proportion of students using blue ink in two colleges are equal or not at 1% level of significance.

iii)  $H_0: \mu_1 = \mu_2$  ag.  $H_1: \mu_1 \neq \mu_2$

33.

$n_1 = 1000$   
 $n_2 = 2000$   
 $\bar{m}_{x1} = 67.5$   
 $\bar{m}_{x2} = 68$   
 $s_{d1} = 2.5$   
 $s_{d2} = 2.5$   
 $z_{cal} = (\bar{m}_{x1} - \bar{m}_{x2}) / \sqrt{s_{d1}^2/n_1 + s_{d2}^2/n_2}$   
 $\approx -5.163978$   
 $p_{value} = 2 * (1 - pnorm(|z_{cal}|))$   
 $\approx 2.417564e-07$   
 $\therefore p_{value}$  is less than 0.05  
 $\therefore H_0$  is rejected at 5% level of significance.  
 $\therefore$  It is rejected at 1% level of significance.

iv)  $H_0: \mu_1 \neq \mu_2$  ag.  $H_1: \mu_1 = \mu_2$

34.

$n_1 = 84$   
 $n_2 = 34$   
 $\bar{m}_{x1} = 61.2$   
 $\bar{m}_{x2} = 59.4$   
 $s_{d1} = 7.9$   
 $s_{d2} = 7.5$   
 $z_{cal} = (\bar{m}_{x1} - \bar{m}_{x2}) / \sqrt{s_{d1}^2/n_1 + s_{d2}^2/n_2}$   
 $\approx -1.162528$   
 $p_{value} = 2 * (1 - pnorm(|z_{cal}|))$   
 $\approx 0.2450211$   
 $\therefore p_{value}$  is greater than 0.01  
 $\therefore H_0$  is accepted at 1% level of significance.

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$H_0: P_1 = P_2$  against  $H_1: P_1 \neq P_2$

$n_1 = 600$   
 $n_2 = 900$   
 $P_1 = 400/600$   
 $P_2 = 450/900$   
 $P = ((n_1 * P_1) + (n_2 * P_2)) / (n_1 + n_2)$   
 $q = 1 - P$   
 $z_{cal} = (P_1 - P_2) / \sqrt{P * q * (1/n_1 + 1/n_2)}$   
 $\approx 6.381534$   
 $p_{value} = 2 * (1 - pnorm(|z_{cal}|))$   
 $\approx 1.735222e-10$   
 $\therefore p_{value}$  is less than 0.01  
 $\therefore H_0$  is rejected at 1% level of significance.

v)  $H_0: P_1 = P_2$  against  $H_1: P_1 \neq P_2$

$n_1 = 200$   
 $n_2 = 200$   
 $P_1 = 44/200$   
 $P_2 = 30/200$   
 $P = ((n_1 * P_1) + (n_2 * P_2)) / (n_1 + n_2)$   
 $q = 1 - P$   
 $z_{cal} = (P_1 - P_2) / \sqrt{P * q * (1/n_1 + 1/n_2)}$   
 $\approx 1.802741$

53  
i  
 $pvalue = 2 * [1 - pnorm (abs(zcal))]$   
 $pvalue$   
 $\{1\} 0.07142888$

$\therefore$  pvalue is greater than 0.05  
 $\therefore$  pvalue is accepted at 5% level of significance.

$\cancel{AM}$   
 $\cancel{21}$   $\cancel{x}$  70

TOPIC:- Small Sample Test:-

Q1) The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 71, 70, 72. Test the hypothesis that the sample comes from a population with avg marks 66.

Soln:-  
 $H_0: \mu = 66$   
 $\Rightarrow x = (63, 63, 66, 67, 68, 69, 70, 70, 71, 72)$   
 $\Rightarrow t\text{-test}(x)$

data:  $x$   
 $t = 68.319$ ;  $df = 9$ ,  $p\text{-value} = 1.558 \times 10^{-13}$   
 alternative hypothesis: true mean is not equal to a 95% confidence interval 65.65171, 70.14829.

Sample estimates:

Mean of  $x$ : 67.9

Since  $p$  value is less than 0.05  
 " we reject hypothesis at 5% level of significance.

mean of  $x$  mean of  $y$ :

17.5

70

pvalue = 0.03798

absolut &

if (pvalue > 0.05) { cat("Accept") }

else { cat("Reject") }

reject.

since pvalue is less than 0.05

$H_0$  is rejected.

Q3) The sales data of six shops before and after a special campaign is effective or not.

before: 53, 28, 31, 48, 50, 42

After: 58, 29, 30, 55, 56, 45

Test the hypothesis that campaign is effective or not.

$x = c(53, 28, 31, 48, 50, 42)$

$y = c(58, 29, 30, 55, 56, 45)$

t-test(x, y, paired = T, alternative = "greater")

Paired t-test

data:  $x$  and  $y$

t = 2.7818, df = 5, pvalue = 0.0806

Alternative hypothesis: true difference in means greater than 0.

as percent confidence interval:

-6.035547 to 7

Sample estimates:

Mean of differences  
-3.5

```
> pvalue = 0.9806  
> if(pvalue > 0.05) {cat("Accept")}  
else {cat("Reject")}  
Accept.  
> since p value is greater than 0.05 we  
accept hypothesis at 5% level of significance.
```

Q4) H<sub>0</sub>: there is no significant difference

```
> x = c(120, 125, 115, 130, 123, 119)  
> y = c(100, 114, 95, 90, 115, 99)  
> t.test(x, y, paired = T, alternative = "less")
```

Paired t-test

data: x and y  
t = 4.3458, df = 5, pvalue = 0.9963

Alternative hypothesis: true difference in  
mean is less than 0

as percent confidence interval: 7.0295 ± 29.0295

Sample estimates:

Mean of differences

19.8333

```
> pvalue
```

71

```
?if(pvalue > 0.05) {cat("Accept")}  
else {cat("Reject")}
```

Accept >

since the pvalue is greater  
than 0.05 we accept the  
hypothesis at 5% level of significance.

Ak

Answers:

$$H_0: \mu = 55$$

$$H_1: \mu \neq 55$$

$$n = 100$$

$$\bar{m}_x = 52$$

$$m_0 = 65$$

$$s_d = 7$$

$$z_{\text{cal}} = (\bar{m}_x - m_0) / (s_d / \sqrt{n})$$

$$z_{\text{cal}} = -4.285714$$

{1}

$\text{cat}("calculated z value is:", z_{\text{cal}})$

calculated z value is = -4.285714

$$p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$p_{\text{value}}$

$${1} 1.82153e-05$$

since,  $p_{\text{value}}$  is less than 0.05  
 $\therefore$  we Reject the Hypothesis at 5% level  
of significance.

$$H_0: \mu \leq 350$$

$$p = 0.5$$

$$Q = 1 - p$$

$$p = 350 / 700$$

$$n = 700$$

$$z_{\text{cal}} = (p - P) / (\sqrt{P * Q / n})$$

$z_{\text{cal}}$

$${1} 0$$

$$p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$${1},$$

Since pvalue is greater than 0.05  
 $\therefore$  we accept hypothesis at 5% level of significance.

$H_0: P_1 = P_2$  as  $H_1: P_1 \neq P_2$

```

> n1 = 1000
> n2 = 1500
> p1 = 0.02
> p2 = 0.01
> p = (n1 * p1 + n2 * p2) / (n1 + n2)
> P = p - (p1 + p2) / 2
> q = 1 - p
> zcal = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))
> zcal
[1] 2.084842
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.03708364

```

Since pvalue is less than 0.05

$\therefore$  It is rejected at 5% level of significance.

$H_0: \mu = 100$

$M_x = 99$

$M_0 = 100$

$S_d = 8$

$n = 400$

$z_{\text{cal}} = (M_x - M_0) / (S_d / (\sqrt{n}))$

$z_{\text{cal}}$

[1] -2.5

$p\text{value} = 2 * (1 - pnorm(\text{abs}(z_{\text{cal}})))$

$p\text{value}$

[1] 0.01241933

Since pvalue is less than 0.05  
 $\therefore$  we reject at 5% level of significance

$x = c(63, 63, 68, 69, 71, 71, 72)$

$t\text{-test}(>i)$

One sample t-test

data: x  
 $t = 4.5$ ,  $df = 5$ ,  $p\text{value} = 1.023e-07$   
 alternative hypothesis: true mean is not equal to 0

as 95% confidence interval:

63.64413 71.35587

Sample estimates:

Mean of x  
 67.5

85

$$\Rightarrow \bar{x} = 1200$$

6)  $H_0: \text{Population have the same variance}$   
 $H_0: \sigma_1^2 = \sigma_2^2$

$$\begin{aligned} &x = [66, 67, 75, 76, 82, 84, 88, 90, 92] \\ &y = [64, 66, 67, 74, 78, 82, 85, 87, 92, 93, 95] \\ &\text{var.test}(x, y) \end{aligned}$$

F test to compare two variances

data: x and y

$$F = 0.70686, \text{num df} = 8, \text{denom df} = 10, \text{p value} = 0.6359$$

alternative hypothesis: true ratio of variance is not equal to 1 93.1

confidence interval:

$$0.1833662 - 3.0360393$$

Sample estimated:

Ratios of variable

$$0.7068567$$

$$H_0: \mu = 1200$$

$$m_x = 1160$$

$$m_o = 1200$$

$$s_d = 125$$

$$n = 100$$

$$z_{\text{cal}} = (m_x - m_o) / (s_d / \sqrt{n})$$

$$z_{\text{cal}} = -4$$

$$p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$p_{\text{value}} = 6.33424 \times 10^{-5}$$

since p value is less than 0.05

∴ it is rejected at 5% level of significance.

$$H_0: P_1 = P_2$$

$$n_1 = 200$$

$$n_2 = 300$$

$$P_1 = 44/1200$$

$$P_2 = 56/300$$

$$P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$$

$$P$$

$$= 0.2$$

$$q = 1 - P$$

$$z_{\text{cal}} = (P_1 - P_2) / \sqrt{P * q * (1/n_1 + 1/n_2)}$$

$$z_{\text{cal}}$$

$$= 0.9128709$$

$$p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$= 0.3613104$$

since p value is less than 0.05 ∴ it is rejected at 5% level of significance.

use the following data to test whether the condition of Home and condition of child are independent or not.

condition of Home

	Clean	Dirty	
cond. of child	clean	70	50
	fair	80	20
	dirty	35	45

SOL:-

$H_0$ : condition of Home & child are independent

$x \in \{70, 80, 35, 50, 20, 45\}$

$x = c(70, 80, 35, 50, 20, 45)$

$> m = 3$

$> n = 2$

$> y = \text{matrix}(x, nrow=m, ncol=n)$

$> y$

	{,1}	{,2}
[1,]	70	50
[2,]	80	20
[3,]	35	45

$> p_value = \text{chisq.test}(y)$

$> p_value$

$\chi^2_{\text{square}} = 25.646, \text{df} = 2, \text{p-value} = 2.698e^{-6}$

since p value is less than 0.05  
 $\therefore$  It is rejected.  
 $\therefore$  They are not independent

- 2) Test the Hypothesis that the vaccination and the disease are independant or not:-

		Vaccine	
		Aff.	No
Disease	Aff.	70	46
	No	35	37

So ? :-

$H_0$ : vaccination and disease are independent.

```

> x = c(70, 35, 46, 47)
> m = 2
> n = 2
> y = matrix(x, nrow = m, ncol = n)
> y
> p_value = chisq.test(y)
> p_value

```

Pearson Chi-Square test

```

data: y
X-squared = 2.0275, df = 1, p-value = 0.1545

```

, oneway.test(values ~ ind, data = d, var.equal = T)

data: values and ind

F = 11.735, num df = 3, denom df = 9, p-value = 0.00183

, anova = aov(values ~ ind, data = d)

, summary(anova)

	DF	Sum Sq	Mean Sq	Fvalue	F > F'
ind	3	71.06	23.688	11.73	6.00183
Residuals	9	18.17	2.019		

∴ pvalue is less than 0.05

∴ It is accepted.

Given the following data the life of types  
of 4 brands

Type	Observation
A	(20, 23, 18, 17, 18, 22, 24)
B	(19, 15, 17, 20, 16, 17)
C	(21, 19, 22, 17, 20)
D	(15, 14, 16, 18, 14, 16)

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```

> x1 = c(20, 23, 18, 17, 18, 22, 24)
> x2 = c(19, 15, 17, 20, 16, 17)
> x3 = c(21, 19, 22, 17, 20)
> x4 = c(15, 14, 16, 18, 14, 16)
> d = stack(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4))
> names(d)
[1] "values" "ind"
> one way . test(values ~ ind, data = d, var . equal = T)
F = 6.84445, num df = 3, denom df = 20, pvalue: 0.0022
> anova = aov(values ~ ind, data = d)
> summary(anova)
```
p value is less than 0.05
∴ It is rejected.

```

#### Q5) COPY DATA FROM Excel file

```

>
> x = read.csv("C:/Users/admin/Desktop/marks.csv")
> x

```

→

```

> Sd = sqrt((n-1) * var(x$Maths)/n)
> Sd
[1] 12.64911
> n = length(x$Maths)
> Sd = sqrt((n-1) * var(x$Maths)/n)
> Sd
[1] 15.2
> cor(x$Stats, x$Maths)
[1] 0.530618

```

$A_1^{202}$

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| Stats | Maths |
|-------|-------|
| 40    | 60    |
| 45    | 48    |
| 42    | 47    |
| 35    | 20    |
| 37    | 25    |
| 36    | 27    |
| 49    | 37    |
| 59    | 58    |
| 20    | 25    |
| 27    | 27    |

```

> am = mean(x$Stats)
> am
[1] 37

```

```

> am = mean(x$Maths)
> am
[1] 34.4

```

```

> m1 = median(x$Stats)
> m1
[1] 38.5

```

```

> m2 = median(x$Maths)
> m2
[1] 37

```

```

> n = length(x$Stats)
> n
[1] 10

```

```

> Sd = sqrt((n-1) * var(x$Stats)/n)
> Sd

```

```

[1] 12.64911

```

```

> n = length(x$Maths)

```

```

> Sd = sqrt((n-1) * var(x$Maths)/n)
> Sd

```

```

[1] 15.2

```

```

> cor(x$Stats, x$Maths)

```

```

[1] 0.530618

```

## topic: Non-Parametric Test

Q1) Following are the amount of sulphur oxide emitted by industry in 20 days. Apply sign test to test the hypothesis that median is 21.5 at 5% level of significance.

17, 15, 20, 20, 18, 22, 25, 27, 0, 24, 20, 17, 6,  
24, 14, 15, 23, 24, 26.

$H_0$ : population median is 21.5

$$\rightarrow x = c(17, \dots, 26)$$

$$\rightarrow \text{length}(n)$$

$$\{1\} 20$$

$$\rightarrow m_e = 21.5$$

$$\rightarrow s_p = \text{length}(n[\{x > m_e\}])$$

$$\rightarrow s_n = \text{length}(n[x \leq m_e])$$

$$\rightarrow n = s_p + s_n$$

$$\rightarrow p_v = \text{pbinum}(s_p, n, 0.5)$$

$$\rightarrow p_v$$

$$\{1\} 0.4719015$$

$\therefore$  p value is more than 0.05  
 $\therefore$  we accept the hypothesis.

Ex

(Q2) Following is the data often observation apply sign test to test the hypothesis that the population median is 625. being the alternative it is more than 625.

612, 619, 631, 628, 643, 640, 655, 649,  
670, 663

H<sub>0</sub>: population median is 625

```
R> x = c(622, 619, 631, 628, 643, 640, 655, 649, 670, 663)
R> length(x)
[1] 10
R> me = 625
R> sp = length(c(x > me))
R> sn = length(x[x < me])
R> pu = pbinom(sn, n, 0.5)
R> pu
[1] 0.0546875
```

∴ P-value is more than 0.05 Hence we accept the hypothesis.

Q53

The weight of students before and after they stop smoking below, using Wilcoxon test that there is no significant change.

Before(x)      (y) After.

|    |    |
|----|----|
| 65 | 72 |
| 75 | 74 |
| 75 | 72 |
| 62 | 66 |
| 72 | 73 |

$H_0$ : There is no change

$H_1$ : There is change

---

$$x = \{65, 75, 75, 62, 72\}$$

$$y = \{72, 74, 72, 66, 73\}$$

$$d = x - y$$

---

$$d =$$

$$\{1, 3, -4, -1, 1\}$$

$$> wilcox.test(x, after, "two.sided", m.u = 0)$$

data: x

$$v = 15, p\text{ value} = 0.05791$$

$\therefore$  p-value is greater than 0.05  
∴ we accept the Hypothesis.

A.Y  
9.7.20

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