



Gajendra Purohit ✓

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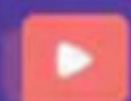
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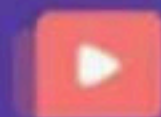
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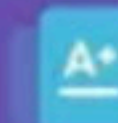


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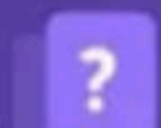
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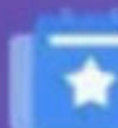
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Result :Let W_1 & W_2 are two subspace of V then
$$\dim(W_1 + W_2) = \dim W_1 + \dim W_2 - \dim(W_1 \cap W_2)$$

Result :Let V be a vector space of dimension n and W be a
subspace of V with m Linearly independent condition
then $\dim V = n - m$

Q.1 Let $W_1 = \{(u, v, w, x) \in \mathbb{R}^4 \mid u + v + w = 0, 2v + x = 0, 2u + 2w - x = 0\}$ & $W_2 = \{(u, v, w, x) \in \mathbb{R}^4 \mid u + w + x = 0, u + w - 2x = 0, v - x = 0\}$. Then which among the following is true.

- (a) $\dim(W_1) = 1$ (b) $\dim(W_2) = 2$
(c) $\dim(W_1 \cap W_2) = 1$ (d) $\dim(W_1 + W_2) = 3$

Q.2. Consider the subspace $W = \{(x_1, x_2, \dots, x_{10}) \in \mathbb{R}^{10}; x_n = x_{n-1} + x_{n-2} \text{ for } 3 \leq n \leq 10\}$ of the vector space \mathbb{R}^{10} .

The dimension of W is

- | | |
|-------|--------|
| (a) 2 | (b) 3 |
| (c) 9 | (d) 10 |

Q.3. Let $W_1 = \{(x, y, z) \in \mathbb{R}^3; 3x + y = 0\}$ & $W_2 = \{(x, y, z) \in \mathbb{R}^3; z = 0\}$. Then $\dim(W_1 \cap W_2)$ is

(a) 0

(b) 1

(c) 2

(d) 3

Q4. Let V be the vector space of all 2×2 matrices over R .

Consider the subspace $W_1 = \left\{ \begin{bmatrix} a & -a \\ c & d \end{bmatrix}; a, c, d \in R \right\}$ &

$$W_2 = \left\{ \begin{bmatrix} a & b \\ -a & d \end{bmatrix}; a, b, d \in R \right\}.$$

If $m = \dim(W_1 \cap W_2)$ & $n = \dim(W_1 + W_2)$ then $m + n$ is

- | | |
|-------|-------|
| (a) 5 | (b) 6 |
| (c) 7 | (d) 8 |

Q.5. Let $A = \begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 3 \\ x & y & z \end{bmatrix}$ and let $V = \{(x, y, z) \in \mathbb{R}^3; \det A = 0\}$.

Then dimension of V equals to

(a) 0

(b) 1

(c) 2

(d) 3

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Linear Transformation

Let V and V' be vector space over F . A mapping $T : V \rightarrow V'$ is a linear transformation if for all $u, v \in V$ & $\alpha, \beta \in F$

$$T(\alpha u + \beta v) = \alpha T(u) + \beta T(v) \text{ \& } T(\alpha u) = \alpha T(u); \text{ for all } \alpha \in F$$

Note : Let V & V' be vector space over F & $T : V \rightarrow V'$ be a linear transformation. Then

(a) $T(0) = 0; 0 \in V$

(b) $T(-v) = -T(v) ; \text{ for all } v \in V$

Q.1. Which of the following is a linear transformation from \mathbb{R}^3 to \mathbb{R}^2 ?

(A) $f \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 4 \\ x+y \end{pmatrix}$

(B) $g \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} xy \\ x+y \end{pmatrix}$

(C) $h \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} z-x \\ x+y \end{pmatrix}$

(a) Only f

(b) Only g

(c) Only h

(d) All of the above

Null space of Linear transformation : Let $T : V(F) \rightarrow V'(F)$ be a linear transformation then null space of T is the set of all vectors of $V(F)$ s.t. $T(u) = 0$; (zero vector of V') and it is denoted by $\ker(T)$ i.e. $\ker(T) = \{u \in V(F) : T(u) = 0\}$

Note : If $V(F)$ & $V'(F)$ be two vector space & $T : V(F) \rightarrow V'(F)$ be linear transformation then $\ker(T)$ is subspace of $V(F)$.

Range of linear transformation : Let $V(F)$ & $V'(F)$ be two vector space and $T : V \rightarrow V'$ be a linear transformation. Then the Range of T written as $R(T)$ is the set of all vectors β in V' such that $\beta = T(\alpha)$ for some α in V .

i.e. $\text{Range}(T) = \{T(\alpha) \in V' \mid \alpha \in V\}$

Note : Let $T : V(F) \rightarrow V'(F)$ be a linear transformation then $\text{Range}(T)$ is subspace of $V'(F)$.

Rank & Nullity of Linear Transformation :

Let $T : V(F) \rightarrow V'(F)$ be a linear transformation & $\text{Range}(T)$ & $\ker(T)$ are range space of T & null space of T then \dim

$$\{\text{Range}(T)\} = \rho(T) = \text{rank of } T$$

$$\& \dim \{\ker(T)\} = \eta(T) = \text{nullity of } T$$

Sylvester's Law : Let $T : V(F) \rightarrow V'(F)$ be linear transformation

$$\text{then } \rho(T) + \eta(T) = \dim V(F)$$

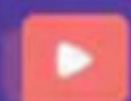
One-One linear transformation : Let $T : V \rightarrow V'$ be a linear transformation with $\eta(T) = 0$ then T is called one-one linear transformation.

Onto linear transformation : Let $T : V \rightarrow V'$ be a linear transformation with $\rho(T) = \dim V'$ Then T is called onto linear transformation.



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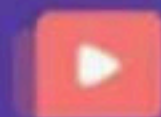
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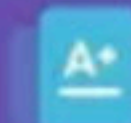


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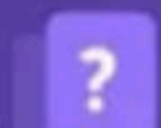
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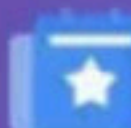
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Educator highlights

- Works at Pacific Science College
- Studied at M.Sc., NET, PhD(Algebra), MBA(Finance), BEd
- PhD, NET | Plus Educator For CSIR NET | Youtuber (260K+Subs.) | Director Pacific Science College |
- Lives in Udaipur, Rajasthan, India
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