



Gajendra Purohit ✓

Legend in CSIR-UGC NET & IIT-JAM

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Power series : A series of the form $\sum_{n=0}^{\infty} a_n (x - x_0)^n$ is known as real infinite power series where a_n are constant.

i.e. $\sum_{n=0}^{\infty} a_n (x - x_0)^n = a_0 + a_1(x - \underline{x_0}) + a_2(x - x_0)^2 + \dots$

$n \neq 0$

Some important facts of power series when $x_0 = 0$:

- (1) Every power series converges for $x = 0$, for all value of coefficient a_n . i.e. if power series is not convergent other than $x = 0$, then this series is called nowhere convergent.

$$\sum_{n=0}^{\infty} a_n x^n$$

$$u_n = a_n x^n$$

$$\lim_{n \rightarrow \infty} (u_n) = \lim_{n \rightarrow \infty} a_n x^n = \infty$$

- (2) If a given series converge for all value of x , then we say that the given power series every where convergent.

Region of convergence :

- (3) If the given power series converges for some value of x and diverge for other value of x then the set of all value of x for which it is convergent is known as region of convergence.

$$|x| < r$$

Radius of convergence :

Let $\sum a_n x^n$ is a power series and $|x| < R$ is region of convergence then R is called radius of convergence.

Formula for finding radius of convergence

$$\frac{1}{R} = \lim_{n \rightarrow \infty} \left| \frac{a_{n+1}}{a_n} \right| = \lim_{n \rightarrow \infty} |a_n|^{1/n}$$

$$a_n = \frac{n+1}{(n+2)(n+3)}$$

$$\frac{1}{R} = \lim_{n \rightarrow \infty} \frac{a_{n+1}}{a_n} = \lim_{n \rightarrow \infty} \frac{(n+2)(n+3)(n+1)}{(n+3)(n+4)(n+1)} = 1$$

$$E.I.I)$$

$$E.I.I)$$

$$R = 1$$

$$(-1, 1)$$

Some useful results :

(1) The radius of convergence of $\sum a_n x^n$ is equal to $\sum n a_n x^{n-1}$.

(2) The radius of convergence of $\sum a_n x^n$ is equal to $\sum \frac{a_n}{(n+1)} x^{n+1}$.

(3) If R is the radius of convergence of $\sum a_n x^n$ then radius of convergence of $\sum a_n x^{pm}$ and $\sum a_n x^{pm+k}$; $k \in \mathbb{N}$ is $(R)^{1/p}$; $p > 0$.

(4) If R and R_1 are the radius of convergence of $\sum a_n x^n$ and $\sum b_n x^n$ then radius of convergence of $\sum (a_n x^n + b_n x^n)$ is $\min\{R, R_1\}$

$$\sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^n n^n \rightarrow R=2$$

$$\sum_{n=0}^{\infty} \left(\frac{1}{3}\right)^n n^n \rightarrow R=3$$

$$\sum_{n=0}^{\infty} \left(\left(\frac{1}{2}\right)^n + \left(\frac{1}{3}\right)^n\right) x^n$$

$$R=2$$

$$\min(2, 3) = 2$$

Q1. The radius of convergence of the power series

$$\sum_{n=0}^{\infty} \left(\frac{n^2}{4^n} \right) x^{5n} \text{ is IIT JAM 2022}$$

(a) 4

(b) $\sqrt[5]{4}$

(c) $\frac{1}{4}$

(d) $\frac{1}{\sqrt[5]{4}}$

$$\sum_{n=0}^{\infty} \frac{n^2}{4^n} (x-1)^{5n}$$

$$\begin{aligned} |x-1| &< 4^{1/5} \\ -4^{1/5} &< (x-1) < 4^{1/5} \\ 1-4^{1/5} &< x < 1+4^{1/5} \end{aligned}$$

$$|x| < (4)^{1/5}$$

$$\begin{aligned} \frac{1}{R^5} &= \lim_{n \rightarrow \infty} \frac{a_{n+1}}{a_n} \\ &= \lim_{n \rightarrow \infty} \frac{(n+1)^2 4^n}{4^{n+1} n^2} \\ &= \lim_{n \rightarrow \infty} \frac{1}{4} \cdot \frac{(1+\frac{1}{n})^2}{1} \\ &= \frac{1}{4} \end{aligned}$$

$$R^5 = 4$$

$$R = (4)^{1/5}$$

Q2. Let r be the radius of convergence of the power series

$\frac{1}{3} + \frac{x}{5} + \frac{x^2}{3^2} + \frac{x^3}{5^2} + \frac{x^4}{3^3} + \frac{x^5}{5^3} + \dots$ then the value of r^2 is **IIT JAM 2022**

(a) 1

(b) 3

(c) 5

(d) 7

$\sum_{n=0}^{\infty} \frac{x^{2n}}{3^{n+1}} + \frac{x^{2n+1}}{5^{n+1}}$

$R_1 = \sqrt{3}$

$R_2 = \sqrt{5}$

Q $x + \frac{2^2 x^2}{2!} + \frac{3^3 x^3}{3!} + \dots$

belong to the interval

~~(a) $(0, 1/e)$~~

~~(b) $(-1/e, \infty)$~~

~~(c) $(\frac{2}{e}, \frac{3}{e})$~~

~~(d) $(\frac{3}{e}, \frac{4}{e})$~~

$|x| < \frac{1}{e}$

$(-\frac{1}{e}, \frac{1}{e})$

is convergent if

$$\sum_{n=1}^{\infty} \frac{x^n n^n}{n!}$$

$$\frac{1}{R} = \lim_{n \rightarrow \infty} \frac{n^n}{n!} = \lim_{n \rightarrow \infty} \frac{n^n}{(n+1)!} \cdot \frac{(n+1)!}{n!}$$

$$= \lim_{n \rightarrow \infty} \frac{n^n}{(n+1)!} \cdot \frac{(n+1)!}{n!} = \lim_{n \rightarrow \infty} \frac{n^n}{(n+1)!} \cdot \frac{(n+1)!}{n!}$$

$$\frac{1}{R} = \lim_{n \rightarrow \infty} (1 + \frac{1}{n})^n = e$$

$R = 1/e$



Q3. The radius of convergence of the power series

$$\sum_{n=1}^{\infty} \left(\frac{n+2}{n} \right)^{n^2} x^n \text{ is IIT-JAM 2020}$$

(a) e^2

(b) $\frac{1}{\sqrt{e}}$

(c) $\frac{1}{e}$

(d) $\frac{1}{e^2}$

$$\frac{1}{R} = \lim_{n \rightarrow \infty} (a_n)^{1/n}$$

$$\frac{1}{R} = \lim_{n \rightarrow \infty} \left(\left(1 + \frac{2}{n} \right)^{n^2} \right)^{1/n}$$

$$\frac{1}{R} = e^2$$
$$R = \frac{1}{e^2}$$

Interval of convergence of series

$$(x+1) - \frac{(x+1)^2}{4} + \frac{(x+1)^3}{9} - \frac{(x+1)^4}{16} + \dots$$

$$|x+1| < 1$$

$$-1 < (x+1) < 1$$

$$-2 \leq x \leq 0$$

$$\left(-\frac{2}{4}, \frac{0}{4} \right)$$

$$[-2, 0]$$

$$u_n = \frac{(x+1)^{n-1}}{n^2}$$

$$\frac{1}{R} = \lim_{n \rightarrow \infty} \frac{u_{n+1}}{u_n}$$

$$\frac{1}{R} = \lim_{n \rightarrow \infty} \frac{1}{(n+1)^2} n^2$$

$$\frac{1}{R} = 1$$

$$R = 1$$

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$$\sum_{h=0}^{\infty} a_n x^n$$

$$a_n = \begin{cases} \frac{1}{3^n} \\ \frac{1}{5^n} \end{cases}$$

n -even

n -odd

Radius of Convergence is

(a) 0

~~(b) 3~~

(c) 5

(d) 15

$R_1 = 3$

$R_2 = 5$

①

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Q4.

Let $a_n = \frac{(1+(-1)^n)}{2^n} + \frac{(1+(-1)^{n-1})}{3^n}$ then the radius of

convergence of the power series $\sum a_n x^n$ about $x = 0$

IIT JAM 2018

- (a) 1

- ~~(b) 2~~

- (c) 3

- (d) 4

$$-\sum \frac{1}{2n} + \left(\sum \frac{1}{2n} + \sum \frac{1}{3n} \right)$$

2, 1, 3, 1, 3

Q5. Let k be a positive integer. The radius of convergence of the series $\sum_{n=0}^{\infty} \frac{(n!)^k}{(kn)!} z^n$ is **[CSIR NET 2014]**

(a) k

(b) k^{-k}

(c) k^k

(d) ∞

Q6. The sum of the finite series

$$S = \frac{1}{2} - \frac{1}{3 \times 1!} + \frac{1}{4 \times 2!} - \frac{1}{5 \times 3!} + \dots \text{is equal to}$$

[CSIR-NET Nov. 2020]

(A) $2 - \frac{1}{e}$

(B) $1 - \frac{2}{e}$

(C) $\frac{2}{e} - 1$

(D) $\frac{1}{e} - 2$

Q7. Let $S_1 = \frac{1}{3} - \frac{1}{2} \times \frac{1}{3^2} + \frac{1}{3} \times \frac{1}{3^3} - \frac{1}{4} \times \frac{1}{3^4} + \dots$ and

$$S_2 = \frac{1}{4} + \frac{1}{2} \times \frac{1}{4^2} + \frac{1}{3} \times \frac{1}{4^3} + \frac{1}{4} \times \frac{1}{4^4} + \dots$$

Which of the following identities is true?

[CSIR-NET Feb. 2022]

(A) $3S_1 = 4S_2$

(B) $4S_1 = 3S_2$

(C) $S_1 + S_2 = 0$

(D) $S_1 = S_2$



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Educator highlights

- Works at Pacific Science College
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