

#### Gajendra Purohit



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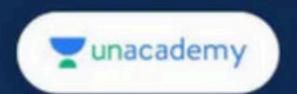
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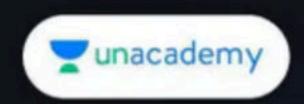
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#### Permutation Group

Lecture Index:-i) Construction of S<sub>n</sub>

- ii) Properties of S<sub>n</sub>
- iii) Even/odd permutation

<u>Symmetric Set/Permutation Set</u> -: Set of all one-one onto mapping from set containing n elements to itself. It's denoted by  $S_n$ . The number of elements in  $S_n$  is n!  $[o(S_n) = n!]$ 

### Properties of S<sub>n</sub>

Cyclic/cycles Permutation-: Let S be a finite set. Let  $a \in S$  and  $\sigma$  be a permutation on S.

Length of cycle-: An element  $\sigma \in S_n$  is called cycle of length r if there exist r symbols such that  $(i_1, i_2, i_3, ... i_r)$ .

If length of cycle is r then it is called r - cycle

Disjoint cycle-:letc<sub>1</sub> =  $(a_1, a_2, a_3, \dots a_r)$  and  $c_2 = (b_1, b_2, b_3, \dots b_s)$  be two cycles,  $c_1$ ,  $c_2$  are called disjoint if there is no common symbol in these two cycles i.e.,  $(a_1, a_2, a_3, \dots a_r) \cap (b_1, b_2, b_3, \dots b_s) = \phi$ 

Transposition -: Every cycle of length 2 is a transposition.

Note-: i) every permutation  $\sigma \in S_n$  can be expressed as a product of disjoint cycles.

ii) Every r-cycle can be expressed as a product of (r-1) transposition.

**Product of permutation**: let  $\sigma_1 \in S_n \& \sigma_2 \in S_n$  be two permutation of  $S_n$ , then product of permutation is  $\sigma_1 \sigma_2 \in S_n$ .

### Even & Odd permutation

The number of transposition in decomposition of any permutation  $\sigma$  is either always odd or always even according to  $\sigma$  is odd or even permutation.

Odd permutation: If  $\sigma \in S_n$  be r-cycle, then  $\sigma$  is odd permutation if r is even or  $\sigma$  has odd transposition.

Even permutation: If  $\sigma \in S_n$  be r-cycle, then  $\sigma$  is even permutation if r is odd or  $\sigma$  has even transposition.

NOTE-: The permutation groups S<sub>n</sub> exactly half are even and half are odd.

Alternating group, $(A_n)$ : The set of all even permutation of  $S_n$  forms w.r.t composition of mappings. It's denoted by  $A_n$  and called alternating group of even permutation.

Order of alternating group,  $A_n$  is  $\frac{n!}{2}$ .

Q.1.: Let  $\sigma$  be the 100 cycle (1 2 3 .... 100) and let  $\tau$  be the transposition (49 50) in the permutation of  $\sigma\tau$  is IIT JAM 2019

(a) 100

(b) 99

(c)98

(d) 2

Q.2 Let 
$$\alpha = \binom{123456}{213546}$$
 &  $\beta = \binom{123456}{612435}$ .  
a)  $\alpha^{-1} = \alpha$ 

- b)  $\beta^{-1} = \beta$
- c)  $\alpha\beta = \beta\alpha$
- d) None of these

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**Q.3.** Let 
$$\alpha = \binom{12345678}{23451786} \& \beta = \binom{12345678}{13876524}$$
.

- a)  $\alpha$  cannot be written in product of disjoint cycles.
- b)  $\alpha$  is even permutation.
- c)  $\beta$  is even permutation.
- d)  $\beta = (23874)(56)$

#### Q.4. Which of the following statements is/are TRUE?

- a) n be a positive integer, if n is odd then an n-cycle is odd permutation.
- b) n be a positive integer, if n is odd then an n-cycle is even permutation.
- c) If  $\alpha$  is even  $\Longrightarrow \alpha^{-1}$  is odd
- d) If  $\alpha$  is even  $\Rightarrow \alpha^{-1}$  is even

- Q.5. Let  $\alpha$  and  $\beta$  belong to  $S_n$ ;  $\alpha\beta \in A_n$ , then which of the following is True?
  - (a) αis even and β is odd
  - (b) $\alpha$  is odd and  $\beta$  is even
  - (c) Both are even
  - (d) Both are odd

Q.6. Let  $\sigma = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 2 & 1 & 3 & 5 & 4 & 6 \end{pmatrix}$  then which of the following is true?

(a) σis cycle of length 4

(b)  $\sigma$  is product of disjoint cycle.

(c) 
$$\sigma = (1234)$$

(d) None of these

Q.7. Let 
$$\sigma = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 \\ 3 & 2 & 1 & 5 & 4 \end{pmatrix}$$
 then

(a) 
$$\sigma = (1 \ 2 \ 3 \ 4 \ 5)$$

(b) 
$$\sigma = (1 \ 3 \ 2)(4 \ 5)$$

(c) 
$$\sigma = (1 \ 3)(4 \ 5)$$

(d) 
$$\sigma = (1 4 5)(2 3)$$

Q.8. Let  $\sigma = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 6 & 2 & 4 & 5 & 1 & 3 \end{pmatrix}$  then number of transposition in  $\sigma$ 

- (a) 1
- (d)4

(c)3

Q.9. Let 
$$\sigma = \begin{pmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \end{pmatrix}$$
,  $\tau = \begin{pmatrix} 1 & 2 & 3 \\ 2 & 1 & 3 \end{pmatrix}$ ,  $J = \begin{pmatrix} 1 & 2 & 3 \\ 1 & 3 & 2 \end{pmatrix}$  then

$$(a)O(\sigma tJ) = 1$$

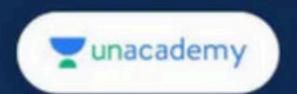
(b) 
$$O(\sigma \tau J) = 2$$

(c) 
$$O(\sigma) = 2$$

(d) 
$$O(\tau) = 3$$

Q.10. Let  $\alpha$  and  $\beta$  are any two elements in  $S_n$ , then  $\alpha^{-1}\beta^{-1}\alpha$   $\beta$  is

- a) Even
- b) Odd
- c) Depend on  $\alpha$  and  $\beta$
- d) None of these



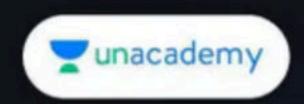
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### **Educator Profile**





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### Works at Pacific Science College

- Studied at M.Sc., NET,
   PhD(Algebra), MBA(Finance),
   BEd
- PhD, NET | Plus Educator For CSIR NET | Youtuber
   (260K+Subs.) | Director Pacific Science College |
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