

**Q1.**

The value of  $\int_0^{\pi/2} \sin^4 x \cos^6 x dx$

- (a)  $3\pi/312$
- (c)  $3\pi/512$

- (b)  $5\pi/512$
- (d)  $5\pi/312$

**Q2.**

If  $I_n = \int_0^{\infty} e^{-x} x^{n-1} dx$ , then  $\int_0^{\infty} e^{-\lambda x} x^{n-1} dx$  is equal to

- (a)  $\lambda I_n$
- (b)  $\frac{1}{\lambda} I_n$
- (c)  $\frac{I_n}{\lambda^n}$
- (d)  $\lambda^n I_n$

**Q3.**

$$\int_0^{\pi/2} \sin^7 x dx$$
 has value

(a)  $\frac{37}{184}$

(b)  $\frac{17}{45}$

(c)  $\frac{16}{35}$

(d)  $\frac{16}{45}$

**Q.4.** Let a,b be positive real numbers such that a < b Given that

$$\lim_{n \rightarrow \infty} \int_0^n e^{-t^2} dt = \frac{\sqrt{\pi}}{2}$$
 Then value of  $\lim_{n \rightarrow \infty} \int_0^n \frac{1}{t^2} (e^{-at^2} - e^{-bt^2}) dt$  is

**IIT JAM 2022**

(a)  $\sqrt{\pi}(\sqrt{b} - \sqrt{a})$

(b)  $\sqrt{\pi}(\sqrt{b} + \sqrt{a})$

(c)  $-\sqrt{\pi}(\sqrt{b} - \sqrt{a})$

(d)  $\sqrt{\pi}(-\sqrt{b} + \sqrt{a})$

**Q.6.** If  $g(x) = \int_{x(x-2)}^{4x-5} f(t)dt$ , where  $f(x) = \sqrt{1+3x^4}$  for  $x \in \mathbb{R}$ , then  $g'(1)$  is   **JAM-2019**

- (a) 6
- (b) 7
- (c) 8
- (d) 10

**Q.7.** Let  $f : [0, 1] \rightarrow [0, \infty)$  be continuous function such

$$\text{that } (f(t))^2 < 1 + 2 \int_0^t f(s)ds, \forall t \in [0, 1]$$

**IIT JAM 2021**

- (a)  $f(t) < 1 + t ; \forall t \in [0, 1]$
- (b)  $f(t) > 1 + t ; \forall t \in [0, 1]$
- (c)  $f(t) = 1 + t ; \forall t \in [0, 1]$
- (d)  $f(t) < 1 + t/2 ; \forall t \in [0, 1]$

**Q.8.** The value of the integral  $\int_{-\pi}^{\pi} |x| \cos nx dx, n \geq 1$  is

**JAM - 2016**

- (a) 0, when n is even      (b) 0, when n is odd
- (c)  $-\frac{4}{n^2}$ , when n is even      (d)  $-\frac{4}{n^2}$ , when n is odd

**Q.9.** Let  $f(x) = \int_{\sin x}^{\cos x} e^{-t^2} dt$ , then  $f\left(\frac{\pi}{4}\right)$  equals

**IIT JAM 2006**

(a)  $\sqrt{\frac{1}{e}}$       (b)  $-\sqrt{\frac{2}{e}}$

(c)  $\sqrt{\frac{2}{e}}$       (d)  $-\sqrt{\frac{1}{e}}$

**Q.10.** Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be continuous function if

$$\int_0^x f(2t)dt = \frac{x}{\pi} \sin(\pi x) \text{ for all } x \in \mathbb{R}, \text{ then } f(2) \text{ is equal}$$

to      **JAM 2007**

- (a) -1
- (b) 0
- (c) 1
- (d) 2

**Q.11.** Let  $f(x) = \int_0^x (x^2 + t^2)g(t)dt$ , where  $g$  is a real valued continuous function on  $\mathbb{R}$ , then  $f'(x)$  is equal to

**JAM – 2008**

- (a) 0
- (b)  $x^3 g(x)$
- (c)  $\int_0^x g(t)dt$
- (d)  $2x \int_0^x g(t)dt$

**Q.12.** Let  $a$  be a non-zero real number, then

$$\lim_{x \rightarrow a} \frac{1}{x^2 - a^2} \int_a^x \sin(t^2) dt \text{ equals JAM - 2009}$$

(a)  $\frac{\sin(a^2)}{2a}$

(b)  $\frac{\cos(a^2)}{2a}$

(c)  $-\frac{\sin(a^2)}{2a}$

(d)  $-\frac{\cos(a^2)}{2a}$

**Q1.** The value of the integral  $\int_{-\pi}^{\pi} |x| \cos nx dx, n \geq 1$  is

**JAM - 2016**

(a) 0, when n is even

(b) 0, when n is odd

(c)  $-\frac{4}{n^2}$ , when n is even

(d)  $-\frac{4}{n^2}$ , when n is odd

**Q.2.** The value of  $\int_0^{\pi/4} \log(1 + \tan \theta) d\theta$  is

(a)  $\frac{\pi}{8}$

(b)  $\log 2$

(c)  $\frac{\pi}{8} \log 2$

(d)  $\frac{\pi}{8} \log 3$

**Q.3.** Evaluate :  $\int_0^{\pi} \frac{x dx}{a^2 \cos^2 x + b^2 \sin^2 x}$

(a)  $\frac{\pi^2}{2a^2b^2}$

(b)  $\frac{\pi^2}{2ab}$

(c)  $\frac{2\pi^2}{a^2b}$

(d)  $\pi^2$

**Q.4.** The limit of sum  $\frac{1}{n} + \frac{1}{n+1} + \frac{1}{n+2} + \dots + \frac{1}{3n}$ , when  $n \rightarrow \infty$  is

- (a)  $\log 3$
- (b)  $\log 2$
- (c) 0
- (d) 1

**Q5.** The limit when  $n \rightarrow \infty$  of the product

$$\left\{ \left( 1 + \frac{1}{n} \right) \left( 1 + \frac{2}{n} \right) \left( 1 + \frac{3}{n} \right) \dots \left( 1 + \frac{n}{n} \right) \right\}^{1/n}$$

- (a) 2/e
- (b) 4/e
- (c) 5/e
- (d)e

  
**Q6.** The value :  $\lim_{n \rightarrow \infty} \left[ \frac{n!}{n} \right]^{1/n}$  is

- (a) 1/e
- (b) 2/e
- (c) 3/e
- (d) 4/e

**Q.7.** Evaluate  $\int_0^{\infty} x^{1/4} e^{-\sqrt{x}} dx$

(a)  $2\sqrt{\pi}$

(b)  $\frac{3}{2}\pi$

(c)  $\sqrt{\pi}$

(d)  $\frac{3}{2}\sqrt{\pi}$

**Q.8.** Let  $a, b$  be positive real numbers such that  $a < b$ . Given that

$$\lim_{n \rightarrow \infty} \int_0^n e^{-t^2} dt = \frac{\sqrt{\pi}}{2}$$

Then value of  $\lim_{n \rightarrow \infty} \int_0^n \frac{1}{t^2} (e^{-at^2} - e^{-bt^2}) dt$  is

**IIIT JAM 2022**

- (a)  $\sqrt{\pi}(\sqrt{b} - \sqrt{a})$
- (b)  $\sqrt{\pi}(\sqrt{b} + \sqrt{a})$
- (c)  $-\sqrt{\pi}(\sqrt{b} - \sqrt{a})$
- (d)  $\sqrt{\pi}(-\sqrt{b} + \sqrt{a})$

**Q9.**

The value of  $\int_0^{\pi/2} \sin^4 x \cos^6 x dx$

(a)  $3\pi/312$

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**Q10.**

If  $I_n = \int_0^{\infty} e^{-x} x^{n-1} dx$ , then  $\int_0^{\infty} e^{-\lambda x} x^{n-1} dx$  is equal to

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**Q11.**  $\int_0^{\pi/2} \sin^7 x dx$  has value

- (a)  $\frac{37}{184}$
- (b)  $\frac{17}{45}$
- (c)  $\frac{16}{35}$
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**Q.1.** Evaluate  $\int_0^{\infty} x^{1/4} e^{-\sqrt{x}} dx$

(a)  $2\sqrt{\pi}$

(b)  $\frac{3}{2}\pi$

(c)  $\sqrt{\pi}$

(d)  $\frac{3}{2}\sqrt{\pi}$

**Q2.**

If  $I_n = \int_0^{\infty} e^{-x} x^{n-1} dx$ , then  $\int_0^{\infty} e^{-\lambda x} x^{n-1} dx$  is equal to

(a)  $\lambda I_n$

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(c)  $\frac{I_n}{\lambda^n}$

(d)  $\lambda^n I_n$

**Q.3.**

Let  $a, b$  be positive real numbers such that  $a < b$ . Given that

$$\lim_{n \rightarrow \infty} \int_0^n e^{-t^2} dt = \frac{\sqrt{\pi}}{2}$$

Then value of  $\lim_{n \rightarrow \infty} \int_0^n \frac{1}{t^2} (e^{-at^2} - e^{-bt^2}) dt$  is

**IIT JAM 2022**

(a)  $\sqrt{\pi}(\sqrt{b} - \sqrt{a})$

(b)  $\sqrt{\pi}(\sqrt{b} + \sqrt{a})$

(c)  $-\sqrt{\pi}(\sqrt{b} - \sqrt{a})$

(d)  $\sqrt{\pi}(-\sqrt{b} + \sqrt{a})$

**Q4.**

The value of  $\int_0^{\pi/2} \sin^4 x \cos^6 x dx$

- (a)  $3\pi/312$
- (b)  $5\pi/512$
- (c)  $3\pi/512$
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**Q5.**

$$\int_0^{\pi/2} \sin^7 x dx$$
 has value

(a)  $\frac{37}{184}$

(b)  $\frac{17}{45}$

(c)  $\frac{16}{35}$

(d)  $\frac{16}{45}$

**Q.1.** The curve  $ay^2 = x^2(a - x)$  is passing through

- (a) (0, 1)                          (b) (0, 0)
- (c) (1, 0)                          (d) (1, 2)

**Q.2.** The cardioid  $r = a(1 + \cos\theta)$  is symmetric about

- (a)  $\theta = 0$  line
- (b)  $\theta = \pi/4$  line
- (c)  $\theta = \pi/2$  line
- (d) none of these

**Q.3.** The tangent at origin of the curve  $2y^2 = x^2(2 - x)$  is

- (a)  $x = +2y$  and  $x = -2y$
- (b)  $y = 2x$  and  $y = -2x$
- (c)  $x = y$  and  $x = -y$
- (d) none of these

**Q.1.** The curve  $ay^2 = x^2(a - x)$  is passing through

- (a) (0, 1)                                  (b) (0, 0)
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- (b)  $y = 2x$  and  $y = -2x$
- (c)  $x = y$  and  $x = -y$
- (d) none of these

**Q.1.** The value of  $\iint_R xe^{y^2} dx dy$ , where R is the region bounded by the line  $x = 0$ ,  $y = 1$  and the parabola  $y = x^2$ .**IIT JAM-2006**

- (a)  $-\frac{1}{4}[e - 1]$
- (b)  $\frac{1}{4}[e - 1]$
- (c)  $\frac{1}{4}[e + 1]$
- (d) None

**Q.2.** The value of  $\iint xy(x+y)dx dy$  over the area between  $y^2 = x$  and  $y = x$

- (a)  $\frac{1}{56}$
- (b)  $\frac{3}{56}$
- (c)  $\frac{5}{56}$
- (d)  $\frac{3}{55}$

**Q.3.** The value of  $\iint_R xy dxdy$ , where R is the quadrant of the circle  $x^2 + y^2 = a^2$

- (a)  $a^4/8$
- (b)  $a^2/8$
- (c)  $a/8$
- (d)  $3a/2$

**Q.1.** The value of  $\iint_R xe^{y^2} dx dy$ , where R is the region bounded by the line  $x = 0$ ,  $y = 1$  and the parabola  $y = x^2$ .**IIT JAM-2006**

- (a)  $-\frac{1}{4}[e - 1]$
- (b)  $\frac{1}{4}[e - 1]$
- (c)  $\frac{1}{4}[e + 1]$
- (d) None

**Q.2.** The value of  $\iint xy(x+y)dx dy$  over the area between  $y^2 = x$  and  $y = x$

- (a)  $\frac{1}{56}$
- (b)  $\frac{3}{56}$
- (c)  $\frac{5}{56}$
- (d)  $\frac{3}{55}$

**Q.3.** The value of  $\iint_R xy dxdy$ , where R is the quadrant of the circle  $x^2 + y^2 = a^2$

- (a)  $a^4/8$
- (b)  $a^2/8$
- (c)  $a/8$
- (d)  $3a/2$

**Q.4.** The value of  $\iint_A xy \, dy \, dx$  where A is domain bounded by x-axis ordinate  $x = 2a$  and the curve  $x^2 = 4ay$ .

- (a)  $a/7$
- (b)  $a^4/3$
- (c)  $a^4/5$
- (d)  $a/5$

**Q.5**

The value of integral  $\int_0^3 \int_0^{\sqrt{3x}} \frac{dydx}{\sqrt{x^2 + y^2}}$ . **JAM-2008**

- (a)  $3\log(\sqrt{3} - 2)$  (b)  $\log(\sqrt{3} + 2)$
- (c)  $3\log(\sqrt{3} + 2)$  (d)  $-3\log(\sqrt{3} + 2)$

**Q.6.** The value of the integral  $\iint_D \frac{\sin(2x)}{x} dx dy$  where D denotes the region bounded by the x – axis and the lines  $y = x$  and  $x = 1$ . **IIT JAM 2007**

(a)  $-\frac{\cos 2}{2} + \frac{1}{2}$

(b)  $\frac{\cos 2}{2}$

(c)  $\cos 2$

(d)  $\sin 2$

Q.1. The value of  $\iint_A (x^2 + y^2) dA$ , where A is rectangle

$$2 \leq x \leq 4 \text{ & } 0 \leq y \leq 1$$

- (a)  $57/6$
- (b)  $58/3$
- (c)  $58/7$
- (d) None of these

**Q.2.** The value of integral  $\iint_{-1-1}^{1\ 1} |x + y| \, dx \, dy$  is IIT JAM – 2019

- (a) 1.79
- (b) 1
- (c) 4.39
- (d) 2.66

**Q.3.** The value of  $\iint_R \cos(\max\{x^3, y^{3/2}\}) dx dy$ , where

$R = [0, 1] \times [0, 1]$ . **JAM – 2009**

- (a)  $\sin 2$
- (b)  $\sin 3$
- (c)  $\sin 1$
- (d) None

Q.4. Evaluate  $\int_{\pi/2}^{\pi} \int_0^x \frac{\sin x}{x} dy dx$

- (a) 0      (b) 1
- (c) 2      (d) -1

**Q.5.** The value of the integral  $\int_0^1 \int_0^1 (x^2 + y^2) dx dy$     BHU 2012

- (a) 1
- (b) 0
- (c)  $\frac{1}{2}$
- (d)  $\frac{2}{3}$

Q.6. Evaluate  $\int_0^1 \int_0^1 (2x^3 e^{x^2 y}) dy dx$  JNU 2021

- (a)  $e^2 - e - 2$
- (b)  $e^2 - 2$
- (c)  $e - 2$
- (d) 0

Q.7 The value of integral  $\int_0^{3\sqrt{3x}} \int_0^y \frac{dy dx}{\sqrt{x^2 + y^2}}$ . JAM-2008

- (a)  $3\log(\sqrt{3} - 2)$
- (b)  $\log(\sqrt{3} + 2)$
- (c)  $3\log(\sqrt{3} + 2)$
- (d)  $-3\log(\sqrt{3} + 2)$

**Q.8.** The value of the integral  $\iint_D \frac{\sin(2x)}{x} dx dy$  .where D denotes the region bounded by the x – axis and the lines y = x and x = 1.**IIT JAM 2007**

- (a)  $-\frac{\cos 2}{2} + \frac{1}{2}$       (b)  $\frac{\cos 2}{2}$   
(c)  $\cos 2$       (d)  $\sin 2$

**Q.1.** The value of  $\iint_G \frac{\log(x^2 + y^2)}{x^2 + y^2} dx dy$  where  $G = \{(x, y) \in \mathbb{R}^2; 1 \leq x^2 + y^2 \leq e^2\}$  is **IIT JAM 2010**

- (a)  $\pi$
- (b)  $2\pi$
- (c)  $3\pi$
- (d)  $4\pi$

**Q.2.** The value of  $\iint \sqrt{x^2 + y^2} dx dy$  over the region lying in xy-plane and bounded by  $x^2 + y^2 = 4$ ,  $x^2 + y^2 = 9$

(a)  $\frac{37\pi}{3}$

(b)  $\frac{38}{3}\pi$

(c)  $\frac{19}{2}\pi$

(d)  $\frac{19}{3}\pi$

**Q.3.** Let D be the region in the first quadrant lying between  $x^2 + y^2 = 1$  &  $x^2 + y^2 = 4$ , value of integral  
 $\iint_D \sin(x^2 + y^2) dx dy$ . IIT JAM - 2007

(a)  $\frac{\pi}{4}(\cos 1 - \cos 2)$       (b)  $\frac{\pi}{4}(\cos 1 - \cos 4)$

(c)  $\frac{\pi}{2}(\cos 1 - \cos 2)$       (d)  $\frac{\pi}{2}(\cos 1 - \cos 4)$

**Q.4** If  $G$  is the region in  $\mathbb{R}^2$  given by

$$G = \left\{ (x, y) \in \mathbb{R}^2 : x^2 + y^2 < 1, \frac{x}{\sqrt{3}} < y < \sqrt{3}x, x > 0, y > 0 \right\}$$

then the value of  $\frac{200}{\pi} \iint_G x^2 dx dy$  is **IIT JAM 2022**

- (a) 2.5
- (b) 4.16
- (c) 3
- (d) 5.5

**Q.8.** The integral  $\iint_R e^{x^2+y^2} dy dx$ , where R is the semicircle region bounded by the x – axis and the curve  $y = \sqrt{1-x^2}$  equals

**SAU 2017**

(a)  $\frac{\pi}{2}(e+1)$

(b)  $\frac{\pi}{2}(e-1)$

(c)  $\frac{\pi}{2}(e^2)$

(d)  $\frac{\pi}{2}e$

Q.1. The integral  $\iint_R e^{x^2+y^2} dy dx$ , where R is the semicircle region bounded by the x – axis and the curve  $y = \sqrt{1-x^2}$  equals

SAU 2017

(a)  $\frac{\pi}{2}(e+1)$

(b)  $\frac{\pi}{2}(e-1)$

(c)  $\frac{\pi}{2}(e^2)$

(d)  $\frac{\pi}{2}e$

**Q.2.** Let  $p$  and  $t$  be positive real numbers. Let  $D_t$  be the closed disc of radius  $t$  center  $(0,0)$  i.e.  $D_t = \{(x,y) : x^2 + y^2 \leq t^2\}$ .

$$\text{Define } I(p,t) = \iint_{D_t} \frac{dxdy}{(p^2 + x^2 + y^2)^p}$$

Then  $\lim_{t \rightarrow \infty} I(p,t)$  is finite      **IIT JAM 2021**

- (a) only if  $p > 1$
- (b) only if  $p < 1$
- (c) only if  $p = 1$
- (d) for no value of  $p$

Q.3. The value of the real number m in the following equation

$$\int_0^1 \int_{-\sqrt{2-x^2}}^{\sqrt{2-x^2}} (x^2 + y^2) dy dx = \int_{m\pi}^{\pi/2} \int_0^{\sqrt{2}} r^3 dr d\theta \text{ is IIT JAM 2016}$$

- (a) 0
- (b) 1
- (c) 2
- (d) 1/4

Q.4. Let  $I = \int_0^{2\sqrt{9-y^2}} \int_{\sqrt{4-y^2}}^{2\sqrt{9-y^2}} 2xy dx dy + \int_2^{3\sqrt{9-y^2}} \int_2^{3\sqrt{9-y^2}} 2xy dx dy$ . IIT-JAM 2010

Then using the transformation  $x = r \cos\theta$ ,  $y = r \sin\theta$ ,  
integral I is equal to

(a)  $\int_0^{\pi/2} \int_0^3 r^2 \sin 2\theta dr d\theta$

(b)  $\int_0^{\pi/2} \int_0^2 r^3 \sin 2\theta dr d\theta$

(c)  $\int_0^{\pi/2} \int_0^3 r^3 \sin 2\theta dr d\theta$

(d)  $\int_0^{\pi/2} \int_0^{-3} r^2 \sin 2\theta dr d\theta$



Q.5. The value of  $\iint_D (x + 2y) dx dy$ , where D is region in the xy-plane bounded by the straight line  $y = x + 3$ ,  $y = x - 3$ ,  $y = -2x + 4$  and  $y = -2x + 2$ . IIT JAM – 2007

- (a) 10
- (b) 11
- (c) 12
- (d) 13

**Q.1.** The value of  $\int_0^1 \int_x^1 \sin(y^2) dy dx$ . JAM – 2017

- (a)  $\frac{1 + \cos 1}{2}$
- (b)  $1 - \cos 1$
- (c)  $1 + \cos 1$
- (d)  $\frac{1 - \cos 1}{2}$

**Q2.** The value of the integral  $\int_{y=0}^1 \int_{x=0}^{1-y^2} y \sin(\pi(1-x)^2) dx dy$  is

**JAM-2019**

- (a)  $\frac{1}{2\pi}$
- (b)  $2\pi$
- (c)  $\pi/2$
- (d)  $2/\pi$

**Q.3.** The value of integral  $\int_0^1 \int_x^1 y^4 e^{xy^2} dy dx$  is **JAM – 2018**

(a)  $\frac{e+1}{2}$

(b)  $\frac{e-1}{2}$

(c)  $\frac{e-2}{3}$

(d)  $\frac{e+2}{3}$

**Q.4.** The value of double integral  $\iint\limits_0^{\pi} \frac{\sin y}{\pi - y} dy dx$ . **JAM-2016**

- (a) 0
- (b) 1
- (c) 2
- (d)  $2\pi$

**Q.5.** The value of  $\int_0^4 \int_{\sqrt{4-x}}^2 e^{y^3} dy dx$ . **JAM-2012**

(a)  $e^8 + 1$       (b)  $e^8 - 1$

(c)  $\frac{e^8 - 1}{2}$       (d)  $\frac{e^8 - 1}{3}$

**Q.6.** After the change of order of integration ,the double

integral  $\int_0^8 \int_{x^{1/3}}^2 dy dx$  becomes      **CUCET 2021**

(a)  $\int_{x^{1/3}}^2 \int_0^8 dx dy$

(b)  $\int_0^2 \int_0^{y^3} dx dy$

(c)  $\int_8^0 \int_{x^{1/3}}^2 dx dy$

(d)  $\int_0^2 \int_0^{y^3} dx dy$

**Q.7.** Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be continuous function and  $a > 0$  then the

integral  $\int_0^a \int_0^x f(y) dy dx$  equals

(a)  $\int_0^a yf(y) dy$

(b)  $\int_0^a (a-y)f(y) dy$

(c)  $\int_0^a (y-a)f(y) dy$

(d)  $\int_a^0 yf(y) dy$

**Q1.** Change the order of integration  $\int_0^1 \int_{x-1}^{\sqrt{1-x^2}} f(x, y) dy dx$ .

**IIT-JAM-2010**

(a)  $\int_0^1 \int_0^{\sqrt{1-y^2}} f(x, y) dx dy + \int_{-1}^0 \int_0^{1+y} f(x, y) dx dy$

(b)  $\int_0^1 \int_0^{\sqrt{1-y^2}} f(x, y) dx dy - \int_{-1}^0 \int_0^{1+y} f(x, y) dx dy$

(c)  $\int_0^1 \int_0^{1+y} f(x, y) dx dy - \int_{-1}^0 \int_0^{1+y} f(x, y) dx dy$

(d) None of these

**Q2.** The value of  $\int_0^{\pi/2} \int_{\pi/2}^{\pi} \frac{\sin x}{x} dx dy + \int_{\pi/2}^{\pi} \int_y^{\pi} \frac{\sin x}{x} dx dy$

**IIT-JAM-2007**

- (a) 0                           (b) 1  
(c) 2                           (d) 3

**Q3.** Change the order of integration in  $\int_{-1}^2 \int_{-x}^{2-x^2} f(x, y) dy dx$ .

**IIT-JAM – 2010**

(a)  $\int_{-1-\sqrt{2-y}}^{2-\sqrt{2-y}} \int f(x, y) dx dy - \int_{-2}^{1-\sqrt{2-y}} \int f(x, y) dx dy$

(b)  $\int_{1-\sqrt{2-y}}^{2-\sqrt{2-y}} \int f(x, y) dx dy + \int_0^{1-\sqrt{2-y}} \int f(x, y) dx dy$

(c)  $\int_{-1-\sqrt{2-y}}^{2-\sqrt{2-y}} \int f(x, y) dx dy + \int_{-2}^{1-\sqrt{2-y}} \int f(x, y) dx dy$

(d) None of these

**Q4.** Change the order of  $\int_0^1 \int_0^{1/x} \frac{y}{(1+xy)^2(1+y^2)} dy dx$

(a)  $\int_0^1 \int_0^\infty \frac{y}{(1+xy)^2(1+y^2)} dx dy + \int_1^\infty \int_0^{1/y} \frac{-y}{(1+xy)^2(1+y^2)} dx dy$

(b)  $\int_0^1 \int_0^1 \frac{y}{(1+xy)^2(1+y^2)} dx dy + \int_1^\infty \int_0^{1/y} \frac{y}{(1+xy)^2(1+y^2)} dx dy$

(c)  $\int_0^1 \int_0^1 \frac{y}{(1+xy)^2(1+y^2)} dx dy - \int_1^\infty \int_0^{1/y} \frac{y}{(1+xy)^2(1+y^2)} dx dy$

(d) None of these

**Q5.** Change the order of integration in  $\int_0^{2a} \int_{x^2/4a}^{3a-x} f(x, y) dy dx$ .

$$(a) I = \int_0^a \int_0^{\sqrt{4ay}} f(x, y) dx dy + \int_a^{3a} \int_0^{3a-y} f(x, y) dx dy$$

$$(b) I = \int_0^a \int_0^{\sqrt{4ay}} f(x, y) dx dy - \int_a^{3a} \int_0^{3a-y} f(x, y) dx dy$$

$$(c) I = \int_0^a \int_0^{a-y} f(x, y) dx dy + \int_a^{3a} \int_0^{3a-y} f(x, y) dx dy$$

(d) None of these

**Q6** Change the order of double integration  $I = \int_0^1 \int_{\sqrt{y}}^{2-y} f dx dy$

(a)  $I = \int_0^1 \int_0^{x^2} f dy dx - \int_1^2 \int_0^{2-x} f dy dx$

(b)  $I = \int_0^1 \int_0^{x^2} f dy dx + \int_1^2 \int_0^{2-x} f dy dx$

(c)  $I = \int_0^1 \int_0^{x^2} f dy dx + \int_0^{x^2} \int_0^{2-x} f dy dx$

(d) None of these

**Q7.** Change the order of integration in the double integral

$$\int_{-1}^2 \left( \int_{-x}^{2-x^2} f(x, y) dy \right) dx \quad \text{IIT-JAM - 2011}$$

(a)  $I = \int_{-2}^1 \left( \int_{-y}^{\sqrt{2-y}} f(x, y) dx \right) dy - \int_1^2 \left( \int_{-\sqrt{2-y}}^{\sqrt{2-y}} f(x, y) dx \right) dy$

(b)  $I = \int_{-2}^1 \left( \int_{-y}^{\sqrt{2-y}} f(x, y) dx \right) dy + \int_1^2 \left( \int_{-\sqrt{2-y}}^{\sqrt{2-y}} f(x, y) dx \right) dy$

(c)  $I = \int_0^1 \left( \int_{-y}^{\sqrt{2+y}} f(x, y) dx \right) dy + \int_0^2 \left( \int_{-\sqrt{2-y}}^{\sqrt{2+y}} f(x, y) dx \right) dy$

(d) None of these

**Q.1.** After the change of order of integration ,the double integral  $\int_0^8 \int_{x^{1/3}}^2 dy dx$  becomes

**CUCET 2021**

(a)  $\int_{x^{1/3}}^2 \int_0^8 dx dy$

(b)  $\int_0^2 \int_0^{y^3} dx dy$

(c)  $\int_8^0 \int_{x^{1/3}}^2 dx dy$

(d)  $\int_0^2 \int_0^{y^3} dx dy$

**Q.2.** Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be continuous function and  $a > 0$  then the

integral  $\int_0^a \int_0^x f(y) dy dx$  equals **JAM – 2009**

(a)  $\int_0^a yf(y) dy$       (b)  $\int_0^a (a-y)f(y) dy$

(c)  $\int_0^a (y-a)f(y) dy$       (d)  $\int_a^0 yf(y) dy$

Q3. The value of  $I = \iint_{0,0}^{1,x} x^2 e^{xy} dx dy$  is

(a)  $\frac{e+2}{2}$

(b)  $\frac{e-2}{2}$

(c)  $\frac{e-1}{2}$

(d)  $\frac{e+1}{2}$

Q4.  $\int_0^{\pi/2} \int_x^{\pi/2} \frac{\sin y}{y} dy dx$  is equal to

- (a) 1
- (b) 2
- (c) 3
- (d) 4

- Q5. The value of the double integral  $\iint\limits_{0 \leq y \leq a}^{\alpha \alpha} \frac{x}{x^2 + y^2} dx dy$  is
- (a)  $\frac{\pi a}{4}$
  - (b)  $\frac{3\pi a}{4}$
  - (c)  $-\frac{\pi a}{3}$
  - (d)  $\frac{2\pi a}{3}$

**Q6,** If  $\int_{y=0}^1 \int_{x=0}^{y+4} dx dy = \int_{x=0}^4 \int_{y=0}^1 dy dx + \int_{x=4}^5 \int_{y=g(x)}^{h(x)} dy dx$ , then the

function g(x) and h(x) are, respectively **JAM – 2009**

- (a) (x - 4) and 1
- (b) (x + 4) and 1
- (c) 1 and (x - 4)
- (d) 1 and (x + 4)

Q7. Evaluate  $\iint \sqrt{4x^2 - y^2} dx dy$  over region bounded by  
 $y = 0, y = x, x = 1$  is

(a)  $\frac{\sqrt{3}}{6} + \frac{\pi}{9}$

(b)  $\frac{\sqrt{3}}{5} + \frac{\pi}{9}$

(c)  $\frac{\sqrt{2}}{3}$

(d)  $\frac{\sqrt{7}}{9}$

Q.1. The area of the planer region bounded by the curve  $x = 6y^2 - 2$  and  $x = 2y^2$ . IIT-JAM 2015

(a)  $\frac{\sqrt{2}}{3}$

(b)  $\frac{2\sqrt{2}}{3}$

(c)  $\frac{4\sqrt{2}}{3}$

(d)  $\sqrt{2}$

Q.2. The area of  $\{ (x,y) \in \mathbb{R}^2 ; |x| + |y| \leq 2 \}$  is **HCU 2021**

- (a) 4
- (b) 8
- (c) 10
- (d) 5

Q.3. The area of the region in the first quadrant that is bounded by  
 $y = \sqrt{x}$ ,  $y = x - 2$  and the x-axis

- (a)  $1/3$
- (b)  $10$
- (c)  $10/3$
- (d)  $4$

**Q4.** Area enclosed by the curve  $y^2 = x$  and  $y^2 = 2x - 1$  lying in the first quadrant is IIT JAM – 2005

- (a) 1/6
- (b) 1/4
- (c) 1/2
- (d) 1/3

**Q.5.** Consider the open rectangle  $G = \{(s,t) \in \mathbb{R}^2 : 0 < s < 1 \text{ and } 0 < t < 1\}$  and the map  $T : G \rightarrow \mathbb{R}^2$  given by

$$T(s,t) = \left( \frac{\pi s(1-t)}{2}, \frac{\pi(1-s)}{2} \right) \text{ for } (s,t) \in G \text{ Then the area of}$$

the image  $T(G)$  of the map  $T$  is equal to **IIT JAM 2022**

- (a)  $\pi/4$
- (b)  $\pi^2/4$
- (c)  $\pi^2/8$
- (d) 1

**Q.1.** Evaluate  $\iiint_W z \, dx \, dy \, dz$  where  $W$  is the region bounded by the plane

$x = 0, y = 0, z = 0, z = 1$  and the cylinder  $x^2 + y^2 = 1$  with  
 $x \geq 0, y \geq 0$  **IT JAM 2006**

- (a)  $\pi$
- (b)  $\pi/2$
- (c)  $\pi/4$
- (d)  $\pi/8$

**Q.2.** The value of  $\int_{x=0}^1 \int_{y=0}^{x^2} \int_{z=0}^y (y+2z) dz dy dx$  is **IT JAM 2014**

- (a) 1/53
- (b) 2/21
- (c) 1/6
- (d) 5/3

**Q.3.** The value of  $\int_{z=0}^1 \int_{y=0}^z \int_{x=0}^y xy^2 z^3 dx dy dz$  is **IIT JAM – 2012**

- (a) 1/90
- (b) 1/50
- (c) 1/45
- (d) 1/10

**Q.4.** If the triple integral over the region bounded by the plane  $2x + y + z = 4$ ,  $x = 0$ ,  $y = 0$ ,  $z = 0$  is given by  $\int_0^2 \int_0^{\lambda(x)} \int_0^{\mu(x,y)} dz dy dx$ . Then the function  $\lambda(x) - \mu(x, y)$  is

**HT JAM – 2016**

- (a)  $x + y$
- (b)  $x - y$
- (c)  $x$
- (d)  $y$

**Q.5.** Let  $V$  be the region bounded by the plane  $x = 0$ ,  $x = 2$ ,  $y = 0$ ,  $z = 0$  and  $y + z = 1$ , then the value of the integral

$$\iiint_V y \, dx \, dy \, dz \text{ is IIT JAM - 2011}$$

- (a)  $1/2$
- (b)  $4/3$
- (c)  $1$
- (d)  $1/3$

**Q.6.** The value of the integral  $\iiint_V (x^2y + 1) dx dy dz$ , where V is  
region given by  $x^2 + y^2 \leq 1$ ,  $0 \leq z \leq 2$  is **IIT JAM 2020**

- (a)  $\pi$
- (b)  $2\pi$
- (c)  $3\pi$
- (d)  $4\pi$

**Q.7.** The value of  $\iiint_V \frac{dxdydz}{\sqrt{1-x^2-y^2-z^2}}$ , where V is volume of  $x^2 + y^2 + z^2 = 1$ .

- (a)  $\pi$
- (b)  $\pi^2$
- (c)  $\pi/2$
- (d)  $8\pi$

**Q.1.** Evaluate  $\iiint xyz \, dx \, dy \, dz$  taking throughout the ellipsoid  $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} \leq 1$  in which variable are positive.

(a)  $\frac{abc}{8}$

(b)  $\left(\frac{abc}{2}\right)^2$

(c)  $\frac{abc}{4}$

(d)  $\frac{a^2 b^2 c^2}{48}$

**Q.2.** Consider the region  $G = \{(x,y,z) \in \mathbb{R}^3 : 0 < z < x^2 - y^2, x^2 + y^2 < 1\}$ . Then the volume of G is equal to **IIT JAM 2022**

- (a) 1
- (b) 0
- (c) 2
- (d) 1.4

Q.3. Volume of the solid is

$$\left\{ (x, y, z) \in R^3 \mid 1 \leq x \leq 2, 0 \leq y \leq \frac{2}{x}, 0 \leq z \leq x \right\}$$

expressible as **IIT – JAM 2017**

$$(a) \int_1^2 \int_0^{2/x} \int_0^x dz dy dx$$

$$(b) \int_1^2 \int_0^x \int_0^{2/x} dy dz dx$$

$$(c) \int_0^2 \int_1^z \int_0^{2/x} dy dx dz$$

$$(d) \int_0^2 \int_{\max(z,1)}^2 \int_0^{2/x} dy dx dz$$

**Q.4.** If the volume of the solid in  $\mathbb{R}^3$  bounded by the surface by the surface  $x = -1, x = 1, y = -1, y = 1, z = 2, y^2 + z^2 = 2$  is  $\alpha - \pi$ , then  $\alpha$  equal to **IIT JAM 2018**

- (a) 4                                      (b) 5
  
- (c) 6                                      (d) 7

**Q.5.** The volume of the closed region bounded by the planes  $x = 0$ ,  $y = 0$ ,  $z = 0$  and  $2x + 5y + 10z = 10$  is [JAM CA-  
**2008]**

- (a)  $20/3$
- (b)  $5$
- (c)  $10/3$
- (d)  $5/3$

**Q.6.** The volume of the solid bounded by the planes  $x + 2y + z = 2$ ,  $x = 2y$ ,  $x = 0$  and  $z = 0$  is [JAM CA 2010]

$$(a) \int_0^1 \int_0^{2-2y} \int_0^{2-x-2y} dz dx dy$$

$$(b) \int_{x/2}^1 \int_0^{1-\frac{x}{2}} \int_0^{2-x-2y} dz dy dx$$

$$(c) \int_0^{1/2} \int_0^{2y} \int_0^{2-x-2y} dz dx dy$$

$$(d) \int_0^1 \int_0^{1/2} \int_0^{2-x-2y} dz dx dy$$

Q.7. The volume of the region in  $\mathbb{R}^3$  given by

$$3|x| + 4|y| + 3|z| \leq 12 \text{ is } [\text{JAM CA-2011}]$$

- (a) 64
- (b) 48
- (c) 32
- (d) 24

Q.8. Find the volume of the region bounded by the plane

$$x = 0, y = 0, z = 0 \text{ and } 6x + 4y + 3z = 12.$$

[JAM MS-2008]

- (a) 1
- (b) 2
- (c) 3
- (d) 4

Q.9. Find the finite volume enclosed by the paraboloids  
 $z = 2 - x^2 - y^2$  and  $z = x^2 + y^2$ . IIT JAM - 2007

(a)  $\pi$

(b)  $-\pi$

(c)  $2\pi$

(d) None

**Q.1.** The volume of the solid of revolution of the loop of the curve  $y^2 = x^4(x + 2)$  about the x-axis (round off to 2 decimal places) is **IIT-JAM 2019**

- (a) 6.69
- (b) 6.75
- (c) 6.80
- (d) 6.93

**Q.2** Find the volume of the solid formed by revolving the cycloid about its base.

- (a)  $3\pi^2 a^3$
- (b)  $5\pi^2 a^3$
- (c)  $6\pi^2 a^3$
- (d) None of these

**Q.3** Find the volume formed by the revolution of the loop of the curve  $y^2(a+x) = x^2(a-x)$  about x-axis.

(a)  $\pi a^2 \left[ 2 \log 2 - \frac{4}{3} \right]$

(b)  $\pi a^2 \left[ 2 \log 2 + \frac{4}{3} \right]$

(c)  $\pi a^2 \left[ 2 \log 3 - \frac{4}{3} \right]$

(d) None of these

**Q.4.** The volume of the solid of revolution of

$$y = \frac{a}{2}(e^{x/a} + e^{-x/a})$$
 about x-axis between  $x = 0$  and

$x = b$  is **IIT JAM – 2009**

(a)  $\frac{\pi a^3}{8}(e^{2b/a} - e^{-2b/a}) - \frac{\pi a^2 b}{2}$

(b)  $-\frac{\pi a^3}{8}(e^{2b/a} - e^{-2b/a}) + \frac{\pi a^2 b}{2}$

(c)  $-\frac{\pi a^3}{8}(e^{2b/a} - e^{-2b/a}) - \frac{\pi a^2 b}{2}$

(d)  $\frac{\pi a^3}{8}(e^{2b/a} - e^{-2b/a}) + \frac{\pi a^2 b}{2}$

**Q.5.** Volume of the solid generated by revolving the region bounded by the lines  $x = 0$ ,  $y = 1$  and the curve  $y = \sqrt{x}$  about the line  $y = 1$  is equal to **IIT JAM – 2007**

- (a)  $\pi/6$
- (b)  $\pi/2$
- (c)  $5\pi/2$
- (d)  $3\pi/2$

**Q.1** The surface area obtained by revolving  $y = 2x$ , for  $x \in [0, 2]$ , about y-axis is **IIT JAM 2009**

- (a)  $2\pi\sqrt{5}$
- (b)  $4\pi\sqrt{5}$
- (c)  $2\sqrt{5}\pi$
- (d)  $4\sqrt{5}\pi$

**Q.2.** The surface area of the portion of the plane  $y + 2z = 2$  within the circle  $x^2 + y^2 = 3$  is **IIT JAM – 2016**

(a)  $\frac{3\sqrt{5}}{2}\pi$

(b)  $\frac{5\sqrt{5}}{2}\pi$

(c)  $\frac{7\sqrt{5}}{2}\pi$

(d)  $\frac{9\sqrt{5}}{2}\pi$

**Q.3.** The area of the surface  $z = \frac{xy}{3}$  intercepted by the cylinder  $x^2 + y^2 \leq 16$  lies in the interval **IIT JAM 2017**

- (a)  $(20\pi, 22\pi]$
- (b)  $(22\pi, 24\pi]$
- (c)  $(24\pi, 26\pi]$
- (d)  $(26\pi, 28\pi]$

**Q.4.** The area of the part of the surface of the paraboloid  $x^2 + y^2 + z = 8$  lying inside the cylinder  $x^2 + y^2 = 4$  is

**IIT JAM – 2019**

- (a)  $\frac{\pi}{2}(17^{3/2} - 1)$       (b)  $\pi(17^{3/2} - 1)$   
(c)  $\frac{\pi}{6}(17^{3/2} - 1)$       (d)  $\frac{\pi}{3}(17^{3/2} - 1)$

**Q.5.** Find the area of the portion of the surface  $z = x^2 - y^2$  in  $\mathbb{R}^3$  which lies inside the solid cylinder  $x^2 + y^2 \leq 1$ .

**IIT JAM – 2012**

(a)  $\frac{\pi}{6}[5^{3/2} - 1]$       (b)  $\frac{\pi}{6}[13^{3/2} - 1]$

(c)  $\frac{\pi}{3}[5^{3/2} - 1]$       (d)  $\frac{\pi}{2}[5^{3/2} - 1]$

**Q.6.** Find the surface area generated by the revolution of the cardioid  $r = a(1 + \cos\theta)$  about the initial line.

- (a)  $\frac{72}{5}\pi a^2$
- (b)  $\frac{64}{5}\pi a^2$
- (c)  $\frac{32}{5}\pi a^2$
- (d) None

**Q.7.** Find the surface area of the portion of the cone  
$$z^2 = x^2 + y^2$$
 that is inside the cylinder  
$$z^2 = 2y.$$

**IIT JAM – 2008**

- (a)  $2\sqrt{2}\pi$
- (b)  $4\sqrt{2}\pi$
- (c)  $6\sqrt{2}\pi$
- (d)  $8\sqrt{2}\pi$