



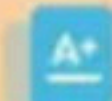
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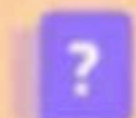
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Transpose of a matrix :

If $A = [a_{ij}]_{m \times n}$ then transpose of A is denoted by A^T is defined as $A^T = [b_{ij}]_{n \times m}$.

Example : Let $A = \begin{bmatrix} 1 & 2 & 3 \\ 1 & 3 & 1 \end{bmatrix}$ then $A^T = \begin{bmatrix} 1 & 1 \\ 2 & 3 \\ 3 & 1 \end{bmatrix}$.

Properties of transpose of matrix :

If A & B are two matrices and k is any number then

(1) $(kA)^T = kA^T$



$$(2) \quad (A + B)^T = A^T + B^T$$

$$(3) \quad (AB)^T = B^T A^T$$

$$(4) \quad \text{If } A \text{ is square matrix then } (A^n)^T = (A^T)^n.$$

Conjugate of a matrix :

If $A = [a_{ij}]_{m \times n}$ then conjugate of A denoted by \bar{A} .

Conjugate transpose of a matrix :

If $A = [a_{ij}]_{m \times n}$ then conjugate transpose of A denoted by A^θ as $A^\theta = (\bar{A})^T$.

$$(2) \quad (A + B)^\theta = A^\theta + B^\theta$$

$$(3) \quad (AB)^\theta = B^\theta A^\theta$$

Trace of a square matrix : Sum of all diagonal elements of a square matrix A is known as Trace of A .

Q.1 Let $A = \begin{bmatrix} a & 0 & 1 \\ 0 & 1 & 2 \\ 1 & 2 & 3 \end{bmatrix}$ be a matrix of order 3 whose Trace is 5, then value of a is

(a) 0

(b) 1

(c) 2

(d) -1

Properties of Trace of matrix (A) :

- (1) If A be a square matrix of order n and k is any number then $\text{Tr}(kA) = k\text{Tr}(A)$
- (2) If A & B are square matrix of same order n, then $\text{Tr}(A + B) = \text{Tr}(A) + \text{Tr}(B)$
- (3) $\text{Tr}(AB) = \text{Tr}(BA)$
- (4) If $A = [a_{ij}]_{m \times n}$ is any matrix then $\text{Trace}(AA^T) = \text{Sum of squares of every element of A.}$
- (5) $\text{Tr}(AA^{\theta}) = \text{sum of the squares of modulus of each element of A.}$

Q2. A real $n \times n$ matrix $A = [a_{ij}]$ is defined as

$$\begin{cases} a_{ij} - i & \forall i = j \\ 0 & \text{Otherwise} \end{cases}, \text{ then Trace}(A) \text{ is}$$

(a) $\frac{n(n+1)}{2}$

(b) $\frac{n(n-1)}{2}$

(c) $\frac{n(n+1)(2n+1)}{2}$

(d) n^2

Q.3 If A, B & C are square matrix of same order then which of the following is/are equal to $\text{Tr}(ABC)$ is

(a) $\text{Tr}(ACB)$ (b) $\text{Tr}(BCA)$

(c) $\text{Tr}(BAC)$ (d) $\text{Tr}(CAB)$

Q.4. If $S = \left\{ A = [a_{ij}]_{3 \times 3} \mid AA^T = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{bmatrix} \& a_{ij} \in R \right\}$. Then :

is

- | | |
|----------------------------|---------------------|
| (a) Empty set | (b) Singleton set |
| (c) Countably infinite set | (d) Uncountable set |

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Definition of Determinant :Let $A = [a_{ij}]_{n \times n}$ be a matrix, then $|A|$ is called a determinant of order n .

(1) Determinant of order 2 :

$$\text{Let } A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}$$

$$|A| = a_{11}.a_{22} - a_{21}.a_{12}$$

(2) Determinant of order 3 :

$$\text{Let } A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$$

$$\text{Then } |A| = a_{11} \begin{vmatrix} a_{22} & a_{23} \\ a_{32} & a_{33} \end{vmatrix} - a_{12} \begin{vmatrix} a_{21} & a_{23} \\ a_{31} & a_{33} \end{vmatrix} + a_{13} \begin{vmatrix} a_{21} & a_{22} \\ a_{31} & a_{32} \end{vmatrix}$$

Singular matrix : If $|A| = 0$ then this matrix is called Singular matrix

Non – Singular matrix : If $|A| \neq 0$,then this matrix is called non – singular matrix

Q .5. The number of distinct real values of x for which the

matrix $\begin{pmatrix} x & 1 & 1 \\ 1 & x & 1 \\ 1 & 1 & x \end{pmatrix}$ is singular is

(a) 1

(b) 2

(c) 3

(d) infinite

Property of determinant :

- (1) Determinant of diagonal matrix is product of all diagonal element
- (2) Determinant of Identity matrix is always one
- (3) Determinant of upper or lower triangular matrix is always product of diagonal elements
- (4) The value of determinant doesnot change when rows and columns are interchanged
- (5) If any two rows or columns are identically then value of determinant is zero

(6) $|A^T| = |A|$

(7) $|A+B|$ and $|A| + |B|$ may not be equal

(8) Let $A = [a_{ij}]_{n \times n}$ & then $|kA| = k^n |A|$

(9) Let A & B are two matrix then $|AB| = |A|.|B|$

Q.6. Let P be 4×4 matrix whose determinant is 10. The determinant of the matrix $-3P$ is

(a) -810

(b) -30

(c) 30

(d) 810

Q7.

Let $A = \begin{bmatrix} 2 & 3 & 1 \\ 5 & 1 & 2 \\ 1 & 0 & 0 \end{bmatrix}$ then

- (a) A is invertible
- (b) $|A|$ is odd
- (c) $|A|$ is divisible by 2
- (d) $|A|$ is prime number

Q.8. It is known that $X = X_0 \in M_2(\mathbb{Z})$ is a solution of $AX - XA = A$ for some $A \in \left\{ \begin{pmatrix} 1 & 1 \\ -1 & -1 \end{pmatrix}, \begin{pmatrix} -1 & 1 \\ 1 & -1 \end{pmatrix}, \begin{pmatrix} 1 & -1 \\ -1 & 1 \end{pmatrix} \right\}$. Which of the following values are not possible for the determinant of X_0 ?

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- (a) $\det(X_0) = 0$ (b) $\det(X_0) = 2$
(c) $\det(X_0) = 6$ (d) $\det(X_0) = 10$

Q.9. Let M & N be any two 4×4 matrices with integer entries.

Satisfying $MN = 2 \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$. Then the maximum value of

$\det(M) + \det(N)$ is

(a) 16

(b) 17

(c) 18

(d) 19



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