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## Eigen value & eigen vector

**Characteristic polynomial :** Let  $A$  be square matrix of order  $n$  then  $C_A(x) = \det(xI - A) = \det(A - xI)$  is a polynomial of degree  $n$  called the characteristic polynomial of  $A$  and the equation  $C_A(x) = \det(A - xI) = 0$  is called characteristic equation.

**Eigen value and Eigen vector :** Let  $A$  be any matrix of order  $n$  then roots of characteristic equation is called eigen value.

i.e. If  $A$  is matrix and  $[A - \lambda I]X = 0$  then  $\lambda$  is eigen value and  $X$  is eigen vector corresponding to  $\lambda$



**Note :** Eigen vector corresponding to distinct eigen value are LI

**Result :** If  $\lambda$  is eigen value of  $A$  then

- (1) Eigen value of  $\alpha A$  is  $\alpha\lambda$
- (2) Eigen value of  $A^n$  is  $\lambda^n$ .
- (3) Sum of all eigen value = Trace ( $A$ )
- (4) Product of all eigen value =  $\det(A)$
- (5) Eigen value of  $A^{-1}$  is  $\lambda^{-1}$ .
- (6) Eigen value of  $\text{Adj}(A)$  is  $\frac{|A|}{\lambda}$
- (7) If sum of each row in  $A$  is equal to  $k$  then  $k$  must be eigen value and it is largest eigen value.

**Q.1.** Let  $A$  be a  $3 \times 3$  matrix with eigen value 1, -1, 0. Then the determinant of  $I + A^{100}$  is

(a) 6

(b) 4

(c) 9

(d) 100

**Q.2.** Let  $A = \begin{pmatrix} 2 & -1 & 3 \\ 2 & -1 & 3 \\ 3 & 2 & -1 \end{pmatrix}$ . Then the largest eigenvalue of A

is

(a) 1

(b) 2

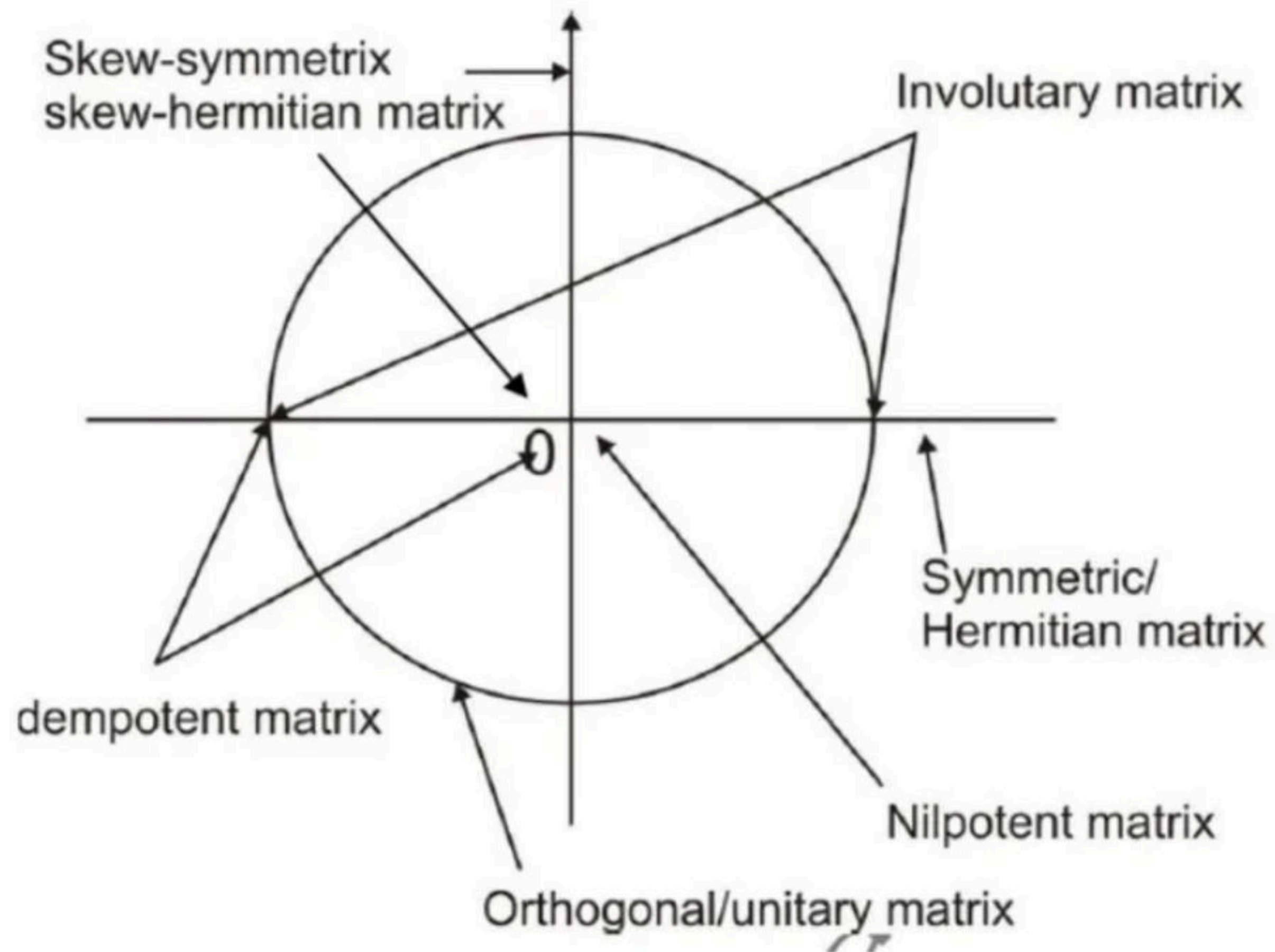
(c) 3

(d) 4



## Eigen value for different type of matrix

- (1) Eigen values of symmetric matrix and hermitian matrix are real.
- (2) Eigen value of skew-symmetric and skew-hermitian matrix are either zero or purely imaginary.
- (3) Eigen values of involutory matrix are either 1 or -1 or both.
- (4) Eigen values of idempotent matrix are either 0 or 1 or both.
- (5) Eigen values of nilpotent matrix are 0.
- (6) Eigen values of orthogonal matrix and unitary matrix are unit modulus.





(7) Eigen value of permutation matrix.

Let  $\sigma = c_1.c_2. .... c_k$  product of disjoint cycles such that  $l(c_i) = r_i$  where  $l(c_i) = \text{length of } c_i$ .

Then characteristic of A is  $e(x) = \prod_{r_i} (x^{r_i} - 1)$

i.e.  $\sigma = (12)(3) \in S_3$

$c_1 = (12)$  and  $l(c_1) = 2 = r_1$

$c_2 = (3)$  and  $l(c_2) = 1 = r_2$  then  $c(x) = (x^2 - 1)(x - 1)$

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- **REAL ANALYSIS**
- **FUNCTION OF ONE & TWO VARIABLE**
- **LINEAR ALGEBRA**
- **MODERN ALGEBRA**

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- SEQUENCE & SERIES
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Q.3. Which of the following properties are true?

- (a) If  $\lambda$  is an eigen value of  $A$  then  $2\lambda$  is an eigen value of  $A^{-1}$ .
- (b) If  $\lambda$  is an eigen value of  $A$  then  $1/\lambda$  is an eigen value of  $A^{-1}$ .
- (c) If  $\lambda$  is an eigen value of an orthogonal matrix, then  $1/\lambda$  is also its eigen value.
- (d) All of the above.

**Q.4.** The square matrix  $A$  is said to be an idempotent if  $A^2 = A$ .

An idempotent matrix is non-singular iff

- (a) All E.V. are real
- (b) All E.V. are real non-negative
- (c) All E.V. are either 0 or 1
- (d) All E.V. are 1



**Q.5** The trace of the matrix  $A = \begin{bmatrix} 3 & 2 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}^{15}$  is

(a)  $1 + 3^{15}$

(b)  $2 + 3^{15}$

(c)  $3^{15}$

(d) 0

**Q.6.** Let  $A$  be  $3 \times 3$  matrix with real entries such that 1, -1, 2 are its eigenvalues if  $B = A^3 + 2A^2 + I$ , then

(a)  $\det(B) = 50$                       (b)  $\det(B) = 136$

(c)  $\det(B) = 23$                       (d)  $\det(B) = 17$



**Q.7..** Let  $A$  and  $B$  be  $n \times n$  real matrices and let  $C = \begin{pmatrix} A & B \\ B & A \end{pmatrix}$

.Which of the following statements are true?

- (a) If  $\lambda$  is an eigenvalue of  $A + B$  then  $\lambda$  is an eigen value of  $C$
- (b) If  $\lambda$  is an eigenvalue of  $A - B$  then  $\lambda$  is an eigen value of  $C$
- (c) If  $\lambda$  is an eigen value of  $A$  or  $B$  then  $\lambda$  is an eigen value of  $C$
- (d) All eigen values of  $C$  are real



Q.8. Which of the following eigen values of the matrix.

$$\begin{bmatrix} 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \end{bmatrix}$$

(a) 1

(b) -1

(c) i

(d) -i



**Q.1.** Let  $M_n(\mathbb{R})$  be the set of  $n \times n$  matrices with real entries.  
Which of the following is true?

- (a) Any matrix  $A \in M_4(\mathbb{R})$  has a real eigen value.
- (b) Any matrix  $A \in M_5(\mathbb{R})$  has a real eigen value.
- (c) Any matrix  $A \in M_2(\mathbb{R})$  has a real eigen value
- (d) None of these



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# Educator Profile



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## Educator highlights

- Works at Pacific Science College
- Studied at M.Sc., NET, PhD(Algebra), MBA(Finance), BEd
- PhD, NET | Plus Educator For CSIR NET | Youtuber (260K+Subs.) | Director Pacific Science College |
- Lives in Udaipur, Rajasthan, India
- Unacademy Educator since



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