



Gajendra Purohit ✓

Legend in CSIR-UGC NET & IIT-JAM

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Function of several variable:

Definition of n-tuples: The Euclidean n-space R^n is the set of all n-tuples (x_1, x_2, \dots, x_n) of real numbers on which the two operation of vector addition and scalar multiplication are defined as follow :

(i) Vector addition of two n-tuples:

Let (x_1, x_2, \dots, x_n) & (y_1, y_2, \dots, y_n) are two vectors then

$$(x_1, x_2, \dots, x_n) + (y_1, y_2, \dots, y_n) = (x_1 + y_1, x_2 + y_2, \dots, x_n + y_n)$$

(ii) Scalar multiplication:

Let $(x_1, x_2, \dots, x_n) \in R^n$ & $\alpha \in R$, then

$$\alpha(x_1, x_2, \dots, x_n) = (\alpha x_1, \alpha x_2, \dots, \alpha x_n)$$

Real valued function on n-variables:

Let $S \subseteq \mathbb{R}^n$, then a map $f : S \rightarrow \mathbb{R}$ is called real valued function on n variables.

Limit of function of two variable:

Let $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ be a function & $(a, b) \in \mathbb{R}^2$, $l \in \mathbb{R}$, then we usually denote limit by $\lim_{(x,y) \rightarrow (a,b)} f(x, y) = l$.

Important method :

Path method :

If $f(x, y)$ gives same values ' l ' along all paths $y = \phi(x)$ passing through (a, b) ,

Then $\lim_{(x,y) \rightarrow (a,b)} f(x, y) = l$.

Convert function from cartesian form to polar form :

Let $f(x, y)$ is a function of two variable in cartesian form, then
put $x = r \cos \theta$ & $y = r \sin \theta$

Then $f(x, y)$ convert into $f(r, \theta)$ which is called in polar form.

Bounded function:

A function of two variables $f(x, y)$ is said to be bounded iff \exists $M > 0$ s.t. $|f(x, y)| \leq M$; for all (x, y)

Results : If a function $f(x, y)$ is bounded then limit of this function need not be exist.

Results : If limit of function exist then function need not be bounded.

Function from \mathbb{R}^n to \mathbb{R}^m :

Let $f : \mathbb{R}^n \rightarrow \mathbb{R}^m$

s.t. $f(x_1, x_2, \dots, x_n) = (\phi_1, \phi_2, \dots, \phi_m)$, where $\phi_i : \mathbb{R}^n \rightarrow \mathbb{R}$

Limit of a function from $\mathbb{R}^n \rightarrow \mathbb{R}^m$:

Let $f : \mathbb{R}^n \rightarrow \mathbb{R}^m$

s.t. $f(x_1, \dots, x_n) = (\phi_1, \dots, \phi_m)$

f has a limit at point (a, b) iff all ϕ_i have limit at (a, b) .

Q.1. Let $L = \lim_{(x,y) \rightarrow (2,-2)} \frac{\sqrt{x-y}-2}{(x-y)-4}$, then L is

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(a) $1/2$

(b) $1/4$

(c) $1/8$

(d) 1

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Q.3. Let $l = \lim_{(x,y) \rightarrow (0,0)} \frac{x^2 y^2}{x^2 + y^2}$ and consider the set

$A = \{x \in \mathbb{R} \mid e^x = l\}$. Then

- (a) $A = \phi$
- (b) A is singleton
- (c) A is countably infinite
- (d) A is uncountable

Q.3. Let $L = \lim_{(x,y) \rightarrow (0,0)} \frac{x^2 y}{x^4 + y^2}$, then L is

(a) 0

(b) 1

(c) 1/2

(d) does not exist

Q.4. For $t \in \mathbb{R}$, let $[t]$ denote the greatest integer less than or equal to t . Define function

$h : \mathbb{R}^2 \rightarrow \mathbb{R}$ and $g : \mathbb{R} \rightarrow \mathbb{R}$ by

$$h(x, y) = \begin{cases} \frac{-1}{x^2 - y} & \text{if } x^2 \neq y \\ 0 & \text{if } x^2 = y \end{cases}$$

and $g(x, y) = \begin{cases} \frac{\sin x}{x} & \text{if } x \neq 0 \\ 0 & \text{if } x = 0 \end{cases}$ then which of the

following is false **IIT JAM 2022**

(a) $\lim_{(x,y) \rightarrow (\sqrt{2}, \pi)} \cos\left(\frac{x^2 y}{x^2 + 1}\right) = \frac{-1}{2}$

(b) $\lim_{(x,y) \rightarrow (\sqrt{2}, 2)} e^{h(x,y)} = 0$

(c) $\lim_{(x,y) \rightarrow (e, e)} \log(x^{y-[y]}) = e - 2$

(d) $\lim_{(x,y) \rightarrow (0,0)} e^{2y} g(x) = 1$

Q.5. Let S be the set of $(\alpha, \beta) \in \mathbb{R}^2$ s.t. $\frac{x^\alpha y^\beta}{\sqrt{x^2 + y^2}} \rightarrow 0$ as

$(x, y) \rightarrow (0, 0)$, then S is

(a) $\{(\alpha, \beta) ; \alpha > 0, \beta > 0\}$

(b) $\{(\alpha, \beta) ; \alpha > 2, \beta > 2\}$

(c) $\{(\alpha, \beta); \alpha + \beta > 1\}$

(d) $\{(\alpha, \beta) ; \alpha + 4\beta > 1\}$

Q.6. Statement – 1 : $\lim_{(x,y) \rightarrow (0,0)} \frac{x^2 y^2}{(x^2 + y^2)^2}$ exists.

Statement – 2 : $\lim_{(x,y) \rightarrow (0,0)} \frac{x^3 y^3}{(x^2 + y^2)^{3/2}}$ exists.

Then

- (a) Statement – 1 is true but statement – 2 is not
- (b) Statement – 2 is true but statement – 1 is not
- (c) Both statements are true
- (d) Both statements are false

Q.7. For what value of α & β , $f(x, y) \rightarrow 0$ as $(x, y) \rightarrow (0, 0)$.

Where $f(x, y) = \frac{x^3 + y^3}{x^\alpha + y^\beta}$.

(a) for $\alpha = 1, \beta = 1$

(b) for $\alpha = 2, \beta = 2$

(c) for $\alpha = 3, \beta = 3$

(d) None of these

Q.8. Let $f(x, y) = \frac{x \cdot y^2}{x^2 + y^4}$. Then $\lim_{(x, y) \rightarrow (0, 0)} f(x, y)$.

(a) is equal to $1/2$

(b) is equal to $2/5$

(c) is equal to $3/5$

(d) none of the above

Q.9. Let $\mathbb{R}^2 \rightarrow \mathbb{R}$ be defined by

$$f(x, y) = \begin{cases} \frac{x^2 - y^2}{x^2 + y^2}, & (x, y) \neq (0, 0) \\ 0, & (x, y) = (0, 0) \end{cases} . \text{ Then is equal to}$$

(a) $1/3$

(b) $2/3$

(c) $4/3$

(d) None of the above



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Educator highlights

- Works at Pacific Science College
- Studied at M.Sc., NET, PhD(Algebra), MBA(Finance), BEd
- PhD, NET | Plus Educator For CSIR NET | Youtuber (260K+Subs.) | Director Pacific Science College |
- Lives in Udaipur, Rajasthan, India
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