

#### Gajendra Purohit



Legend in CSIR-UGC NET & IIT-JAM

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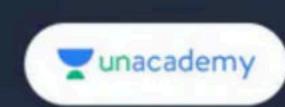
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### Limit point / Cluster point :

(i) Terms of Sequence: Let  $<a_n>$  be a sequence then  $a_1, a_2, ...., a_n$  are called term of sequence.

**Definition :** A number p is said to be a limit point of a sequence  $\langle a_n \rangle$ , if every neighbourhood of p contain infinite terms of  $\langle a_n \rangle$ .

Another Definition: A number 'p' repeated infinitely times, then p is said to be limit points of  $< a_n >$ .

Note: Let <a<sub>n</sub>> be a sequence of real number and let p be a real number, if there exist a neighbourhood of p which contain only finite terms of sequence, then p is not limit point.

#### Result:

- (1) Bolzano Weierstrass Theorem : Every bounded sequence has a limit point.
- (2) Unbounded sequence may have limit point.

Limit of a sequence: Let <an> be a sequence, limit of the sequence is

denoted by  $\lim_{n\to\infty} a_n$ .

#### Result:

- (1) A sequence can have atmost one limit.
- (2) Unbounded sequence cannot have limit

Example: 
$$a_n = \begin{cases} 2 & if & n \text{ is prime} \\ n & if & n \text{ is not prime} \end{cases}$$

It has no limit because it is unbounded but it has a limit point.

(3) A non-monotonic sequence can have limit.

- (4) A bounded sequence may not have limit
- (5) If limit point of a sequence is unique, then it is limit of sequence.
- (6) If limit points of a sequence are more than one then sequence cannot have limit.
- (7) Limit of a sequence is also a limit point of a sequence but conversely need not be true.

### Q1. Which of the following is true

- (a) Every sequence has a limit point
- (b) A limit point is a limit of sequence
- (c) Unbounded sequence may have a limit
- (d) Unbounded sequence may have limit point

- Q2. Consider the interval (-1, 1) and a sequence  $\{a_n\}_{n=1}^{\infty}$  of elements in (-1, 1). Then
  - (a) Every limit point of  $\{a_n\}$  is in (-1, 1)
  - (b) Every limit point of {a<sub>n</sub>} is in [-1, 1]
  - (c) The limit points of  $\{a_n\}$  can only be in  $\{-1, 0, 1\}$
  - (d) The limit points of {a<sub>n</sub>} cannot be in {-1, 0, 1}

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## FOUNDATION COURSE OF MATHEMATICS FOR CSIR-NET

### Q3. Which of the following statement is true?

- (a) A number 'p' is said to be limit point of sequence <an> if every neighbourhood of 'p' contain infinite number of terms of <an>
- (b) A number 'q' is said to be limit point of sequence <br/>
  every neighbourhood of 'q' contain finite number of terms of <br/>
  of <br/>
  of.
- (c) Any point of a sequence is said to be limit point of a sequence if every neighbourhood of this point contain atmost two point of given sequence.
- (d) None of these

Q.4. Define 
$$S = \lim_{n \to \infty} \left( 1 - \frac{1}{2^2} \right) \left( 1 - \frac{1}{3^2} \right) ... \left( 1 - \frac{1}{n^2} \right)$$
 IIT JAM 2021

(a) 3/4

(b) 1

(c) 1/2

(d) 1/4

Q.5. Let  $< a_n > b$  the sequence of the real numbers such that  $a_1 = 1$  and  $a_{n+1} = a_n + a_n^2$  for all  $n \ge 1$  Then IIT JAM 2019

(a) 
$$a_4 = a_1(1 + a_1)(1 + a_2)(1 + a_3)$$

(b) 
$$\lim_{n\to\infty}\frac{1}{a_n}=0$$

(c) 
$$\lim_{n\to\infty}\frac{1}{a_n}=1$$

(d) 
$$\lim_{n\to\infty} a_n = 0$$

Q6. Let  $a_n = \frac{b_{n+1}}{b_n}$ , where  $b_1 = 1$ ,  $b_2 = 1$  and  $b_{n+2} = b_n + b_{n+1}$ ,  $n \in \mathbb{N}$ .

Then  $\lim_{n\to\infty} a_n$  is IIT-JAM – 2018

(a) 
$$\frac{1-\sqrt{5}}{2}$$

(b) 
$$\frac{1-\sqrt{3}}{3}$$

(c) 
$$\frac{1+\sqrt{3}}{2}$$

(d) 
$$\frac{1+\sqrt{5}}{2}$$

Q7. Let  $\langle S_n \rangle$  be a sequence of positive real numbers satisfying  $2S_{n+1} = S_n^2 + \frac{3}{4}$ ,  $n \ge 1$ , if  $\alpha$  and  $\beta$  are the roots of the equation

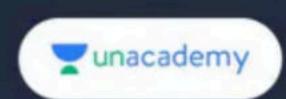
 $x^2 - 2x + \frac{3}{4} = 0$  and  $\alpha < S_1 < \beta$ , then which of the following is

true? IIT-JAM 2016

- (a) <S<sub>n</sub>> is monotonically decreasing
- (b) <S<sub>n</sub>> is monotonically increasing

(c) 
$$\lim_{n\to\infty} S_n = \alpha$$

(d) 
$$\lim_{n\to\infty} S_n = \beta$$



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### **Educator Profile**





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#### Educator highlights

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### Works at Pacific Science College

- Studied at M.Sc., NET,
   PhD(Algebra), MBA(Finance),
   BEd
- PhD, NET | Plus Educator For CSIR NET | Youtuber
   (260K+Subs.) | Director Pacific Science College |
- Lives in Udaipur, Rajasthan,
   India
- Unacademy Educator since

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