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**Legend** in CSIR-UGC NET & IIT-JAM

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**Subsequence :** Let  $\langle a_n \rangle$  be a given sequence. If  $\langle n_k \rangle$  is strictly increasing sequence of natural numbers, then  $\langle a_{n_k} \rangle$  is called a subsequence of  $\langle a_n \rangle$ .



**Complementary Subsequence :** If all the terms of two subsequence are distinct then these subsequences are called complementary subsequences.

### Important result :

- (1) If a sequence  $\langle a_n \rangle$  converges to  $l$ , then every subsequence of  $\langle a_n \rangle$  converges to  $l$ . Converse may not be true
- (2) If two complementary subsequences of a sequence  $\langle a_n \rangle$  are converges to same limit  $l$ , then  $\langle a_n \rangle$  converge to  $l$ . This is best process for show that sequence is not converge.

### Important result :

- (1) If a sequence  $\langle a_n \rangle$  converges to  $l$ , then every subsequence of  $\langle a_n \rangle$  converges to  $l$ .

i.e. all subsequences of a convergent sequence converge to same limit but converse need not be true.



- (2) If two complementary subsequence of a sequence  $\langle a_n \rangle$  are converges to same limit  $l$ , then  $\langle a_n \rangle$  converges to  $l$ .
- (3) Every subsequence of divergent sequence is divergent but converse need not true.
- (4) Every subsequence of a monotonic sequence are monotonic.
- (5) A non-monotonic sequence can have monotonic subsequence.
- (6) Every subsequence of bounded sequence is bounded but converse need not be true.



- (7) Every sequence have atleast one monotonic subsequence.
- (8) A bounded sequence have atleast one convergent subsequence.
- (9) If two subsequence are convergent then sequence need not be convergent.

**Cauchy Sequence :** A sequence is called a cauchy sequence iff it is convergent sequence.



**Q1.** Let  $\langle a_n \rangle$ ,  $\langle b_n \rangle$  and  $\langle c_n \rangle$  be sequences of real numbers such that  $b_n = a_{2n}$  and  $c_n = a_{2n+1}$ . Then  $\langle a_n \rangle$  is convergent.

- (a) Implies  $\langle b_n \rangle$  is convergent but  $\langle c_n \rangle$  need not be convergent.
- (b) Implies  $\langle c_n \rangle$  is convergent but  $\langle b_n \rangle$  need not be convergent.
- (c) Implies both  $\langle b_n \rangle$  and  $\langle c_n \rangle$  are convergent.
- (d) If both  $\langle b_n \rangle$  and  $\langle c_n \rangle$  are convergent.



▲ 1 • Asked by Megha

Dekhiye sir





**Q2.** If  $\langle x_n \rangle$  is a convergent sequence in  $\mathbb{R}$  and  $\langle y_n \rangle$  is a bounded sequence in  $\mathbb{R}$ , then we can conclude that

- (a)  $\langle x_n + y_n \rangle$  is convergent
- (b)  $\langle x_n + y_n \rangle$  is bounded
- (c)  $\langle x_n + y_n \rangle$  has no convergent subsequence
- (d)  $\langle x_n + y_n \rangle$  has no bounded subsequence.



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**Q3.** Which of the following is true?

(a) Every sequence that has convergent subsequence is a Cauchy sequence.

(b) Every sequence that has convergent subsequence is bounded sequence

(c) The sequence  $\langle \sin n \rangle$  has convergent subsequence.

(d) The sequence  $\left\langle n \cos \frac{1}{n} \right\rangle$  has a convergent subsequence.

**Q.4.** Which of the following is false?

- (a) Every bounded sequence has a convergent subsequence.
- (b) Every sequence has a monotonic sub-sequence.
- (c) Every sequence has a limit point.
- (d) Limit points of a sequence is always limit of sequence.



**Q.5.** Which of the following statements about a sequence of real numbers are true

- (a) Every bounded sequence has a convergent subsequence
- (b) Every sequence has monotonic subsequence
- (c) Every sequence has a limit point
- (d) Every sequence has countable number of terms

- Q.6.** Let  $\langle a_n \rangle$  be a bounded sequence of real numbers. then
- (a) There is a subsequence of  $\langle a_n \rangle$  which is convergent
  - (b) Every subsequence of  $\langle a_n \rangle$  is convergent
  - (c) There is exactly one subsequence of  $\langle a_n \rangle$  which is convergent
  - (d) None of these



**Q.7.** If a sequence  $\langle a_n \rangle$  is bounded, then the sequence

(a) has no convergent subsequence

(b) has a convergent subsequence

(c) must be converge

(d) is monotonic

Q.8. Consider the statement :

$S_1$  : Every Cauchy sequence of  $\mathbb{R}$  is convergent.

$S_2$  : Every convergent sequence is a Cauchy sequence.

$S_3$  : Every Cauchy sequence is bounded.

Which of the following is true?

(a) Only  $S_1$                       (b) Only  $S_1$  and  $S_3$

(c) Only  $S_2$  and  $S_3$

(d) All the statements





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# Educator Profile



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## Educator highlights

- Works at Pacific Science College
- Studied at M.Sc., NET, PhD(Algebra), MBA(Finance), BEd
- PhD, NET | Plus Educator For CSIR NET | Youtuber (260K+Subs.) | Director Pacific Science College |
- Lives in Udaipur, Rajasthan, India
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