

#### Gajendra Purohit



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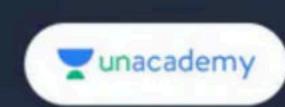
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Subsequence: Let <an> be a given sequence. If <nk> is strictly

increasing sequence of natural numbers, then  $\langle a_{n_k} \rangle$  is called a

subsequence of  $< a_n >$ .

Complementry Subsequence: If all the terms of two subsequence are

distinct then these subsequences are called complementary subsequences.

#### Important result:

- (1) If a sequence <an> converges to l, then every subsequence of <an> converges to l. Converse may not be true
- (2) If two complementry subsequences of a sequence <a<sub>n</sub>> are converges to same limit l, then <a<sub>n</sub>> converge to l. This is best process for show that sequence is not converge.

#### Important result:

(1) If a sequence  $\langle a_n \rangle$  converges to l, then every subsequence of  $\langle a_n \rangle$  converges to l.

i.e. all subsequences of a convergent sequence converge to same limit but converse need not be true.

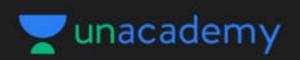
- (2) If two complementary subsequence of a sequence <a<sub>n</sub>> are converges to same limit l, then <a<sub>n</sub>> converges to l.
- (3) Every subsequence of divergent sequence is divergent but converse need not true.
- (4) Every subsequence of a monotonic sequence are monotonic.
- (5) A non-monotonic sequence can have monotonic subsequence.
- (6) Every subsequence of bounded sequence is bounded but converse need not be true.

- (7) Every sequence have atleast one monotonic subsequence.
- (8) A bounded sequence have atleast one convergent subsequence.
- (9) If two subsequence are convergent then sequence need not be convergent.

Cauchy Sequence: A sequence is called a cauchy sequence iff it is convergent sequence.

Q1. Let  $\langle a_n \rangle$ ,  $\langle b_n \rangle$  and  $\langle c_n \rangle$  be sequences of real numbers such that  $b_n = a_{2n}$  and  $c_n = a_{2n+1}$ . Then  $\langle a_n \rangle$  is convergent.

- (a) Implies <br/> is convergent but <cn> need not be convergent.
- (b) Implies  $\langle c_n \rangle$  is convergent but  $\langle b_n \rangle$  need not be convergent.
- (c) Implies both  $\langle b_n \rangle$  and  $\langle c_n \rangle$  are convergent.
- (d) If both  $\langle b_n \rangle$  and  $\langle c_n \rangle$  are convergent.



▲ 1 • Asked by Megha

Dekhiye sir



- Q2. If  $\langle x_n \rangle$  is a convergent sequence in R and  $\langle y_n \rangle$  is a bounded sequence in R, then we can conclude that
  - (a)  $\langle x_n + y_n \rangle$  is convergent
  - (b)  $\langle x_n + y_n \rangle$  is bounded
  - (c)  $\langle x_n + y_n \rangle$  has no convergent subsequence
  - (d)  $\langle x_n + y_n \rangle$  has no bounded subsequence.

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## FOUNDATION COURSE OF MATHEMATICS FOR CSIR-NET

- Q3. Which of the following is true?
  - (a) Every sequence that has convergent subsequence is a Cauchy sequence.
  - (b) Every sequence that has convergent subsequence is bounded sequence
  - (c) The sequence <sin n> has convergent subsequence.
  - (d) The sequence  $\left\langle n\cos\frac{1}{n}\right\rangle$  has a convergent subsequence.

### Q.4. Which of the following is false?

- (a) Every bounded sequence has a convergent subsequence.
- (b) Every sequence has a monotonic sub-sequence.
- (c) Every sequence has a limit point.
- (d) Limit points of a sequence is always limit of sequence.

- Q.5. Which of the following statements about a sequence of real numbers are true
  - (a) Every bounded sequence has a convergent subsequence
  - (b) Every sequence has monotonic subsequence
  - (c) Every sequence has a limit point
  - (d) Every sequence has countable number of terms

- Q.6. Let  $< a_n >$  be a bounded sequence of real numbers. then
  - (a) There is a subsequence of  $< a_n >$  which is convergent
  - (b) Every subsequence of < an is convergent
  - (c) There is exactly one subsequence of  $< a_n >$  which is convergent
  - (d) None of these

Q.7. If a sequence  $\langle a_n \rangle$  is bounded, then the sequence

(a) has no convergent subsequence

(b) has a convergent subsequence

(c) must be converge

(d) is monotonic

Q.8. Consider the statement:

S1 Every Cauchy sequence of R is convergent.

S<sub>2</sub>: Every convergent sequence is a Cauchy sequence.

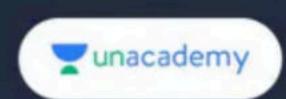
S<sub>3</sub>: Every Cauchy sequence is bounded.

Which of the following is true?

(a) Only S<sub>1</sub> (b) Only S<sub>1</sub> and S<sub>3</sub>

(c) Only S2 and S3

(d) All the statements



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### **Educator Profile**





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### Works at Pacific Science College

- Studied at M.Sc., NET,
  PhD(Algebra), MBA(Finance),
  BEd
- PhD, NET | Plus Educator For CSIR NET | Youtuber
   (260K+Subs.) | Director Pacific Science College |
- Lives in Udaipur, Rajasthan,
  India
- Unacademy Educator since

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