



**Gajendra Purohit** ✓

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## Detailed Course 2.0 on **Sequence and Series For IIT JAM' 23**

October 26  
9:00 AM

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
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## Detailed Course on Group Theory **For CSIR NET 2023**

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## Series of real numbers

**D'Alembert Ratio test** – Let  $\sum u_n$  be a positive terms series such that

(A)  $\lim_{n \rightarrow \infty} \frac{u_{n+1}}{u_n} = l$  Then the series is

- (i) Convergent if  $l < 1$
- (ii) Divergent if  $l > 1$
- (iii) Test fails for  $l = 1$

(B)  $\lim_{n \rightarrow \infty} \frac{u_{n+1}}{u_n} = \infty$  then  $\sum u_n$  is divergent.

**Q.1.** Suppose

$$a_n = \frac{3^n + 3}{5^n - 5} \text{ and } b_n = \frac{1}{(1+n^2)^{1/4}} \text{ for } n = 2, 3, 4, \dots \text{ Then}$$

which of the following is true

(a) Both  $\sum_{n=2}^{\infty} a_n$  and  $\sum_{n=2}^{\infty} b_n$  are convergent

(b) Both  $\sum_{n=2}^{\infty} a_n$  and  $\sum_{n=2}^{\infty} b_n$  are divergent

(c)  $\sum_{n=2}^{\infty} a_n$  is convergent and  $\sum_{n=2}^{\infty} b_n$  are divergent

(d)  $\sum_{n=2}^{\infty} a_n$  is divergent and  $\sum_{n=2}^{\infty} b_n$  are convergent



**Q2.** Let  $\langle a_n \rangle$  be a sequence of positive real numbers, the

series  $\sum_{n=1}^{\infty} a_n$  converges if the series

(a)  $\sum_{n=1}^{\infty} a_n^2$  converges

(b)  $\sum_{n=1}^{\infty} \frac{a_n}{2^n}$  converges

(c)  $\sum_{n=1}^{\infty} \frac{a_{n+1}}{a_n}$  converges

(d)  $\sum_{n=1}^{\infty} \frac{a_n}{a_{n+1}}$  converges

**Q6.** The series  $x + \frac{2^2 x^2}{2!} + \frac{3^3 x^3}{3!} + \dots$  is convergent if  $x$  belong to the interval

(a)  $\left(0, \frac{1}{e}\right)$

(b)  $\left(\frac{1}{e}, \infty\right)$

(c)  $\left(\frac{2}{e}, \frac{3}{e}\right)$

(d)  $\left(\frac{3}{e}, \frac{4}{e}\right)$

**Q3.** What value of  $x$ , the series  $\sum_{n=1}^{\infty} \frac{x^n}{n^2 + 1}$  is divergent?

(a)  $(0, 1)$

(b)  $(2, \infty)$

(c)  $(1, \infty)$

(d)  $(0, 2)$



## Cauchy's condensation test :

If  $f(n)$  is a positive monotonically decreasing function of  $n$ , then the two infinite series  $\sum f(n)$  and  $\sum a^n f(a^n)$  converge or diverge together, where  $a > 1$ ,  $a \in \mathbb{Z}$ .

Q4. For which value of 'p' the series  $\sum_{n=2}^{\infty} \frac{1}{n(\log n)^p}$  is convergent?

(a) 1

(b) 2

(c) 1/2

(d) 1/3



**Q5.** Which of the following series is Divergent

(a)  $\sum_{n=1}^{\infty} \frac{1}{n} \sin^2 \frac{1}{n}$

(b)  $\sum_{n=1}^{\infty} \frac{1}{n} \log n$

(c)  $\sum_{n=1}^{\infty} \frac{1}{n^2} \sin \frac{1}{n}$

(d)  $\sum_{n=1}^{\infty} \frac{1}{n} \tan \frac{1}{n}$

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**Cauchy's  $n^{\text{th}}$  root test :** Let  $\sum u_n$  be a positive terms series

and let  $\lim_{n \rightarrow \infty} (u_n)^{1/n} = l$ .

Then the series is

- (a) Convergent if  $l < 1$
- (b) Divergent if  $l > 1$
- (c) Test fails if  $l = 1$

**Note :** If  $n^{\text{th}}$  term of series is in the power of  $n$  then we can use Cauchy's  $n^{\text{th}}$  root test.

**Q1.** Which of the following series is/are convergent?

(a)  $\sum_{n=1}^{\infty} \left( \frac{5n+1}{4n+1} \right)^n$

(b)  $\sum_{n=1}^{\infty} \frac{\sin \frac{1}{n}}{n^{1/n}}$

(c)  $\sum_{n=1}^{\infty} \left( 1 - \frac{1}{n} \right)^n$

(d)  $\sum_{n=1}^{\infty} \sqrt{n} \left( 1 - \cos \left( \frac{1}{n} \right) \right)$



**Q2.** For  $n \geq 1$ , let  $a_n = \begin{cases} n2^{-n} & \text{if } n \text{ is odd} \\ 3^{-n} & \text{if } n \text{ is even} \end{cases}$ . Which of the following statements is/are convergent?

(a) The sequence  $\langle a_n \rangle$  is convergent

(b) The sequence  $\langle a_n \rangle$  is divergent

(c) The series  $\sum_{n=1}^{\infty} a_n$  is convergent

(d) The series  $\sum_{n=1}^{\infty} a_n$  is divergent

## Cauchy's integral test :

If  $u(x)$  is non-negative decreasing integrable function such that  $u(n) = u_n$  then  $\sum_{n=1}^{\infty} u_n$  is convergent iff the value of  $\int_1^{\infty} u(x) dx$  is finite.



Q3 . The convergence for series  $\sum_{n=1}^{\infty} \frac{1}{n(\log n)}$  is

- (a) Convergent
- (b) Oscillatory

- (b) Divergent
- (d) None of these

Q4 . Which of the following series is divergent?

(a)  $\sum_{n=1}^{\infty} \frac{1}{n} \sin^2 \frac{1}{n}$

(b)  $\sum_{n=1}^{\infty} \frac{1}{n} \log n$

(c)  $\sum_{n=1}^{\infty} \frac{1}{n^2} \sin \frac{1}{n}$

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
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# Educator Profile



**Gajendra Purohit** ✓

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## Educator highlights

- Works at Pacific Science College
- Studied at M.Sc., NET, PhD(Algebra), MBA(Finance), BEd
- PhD, NET | Plus Educator For CSIR NET | Youtuber (260K+Subs.) | Director Pacific Science College |
- Lives in Udaipur, Rajasthan, India
- Unacademy Educator since



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