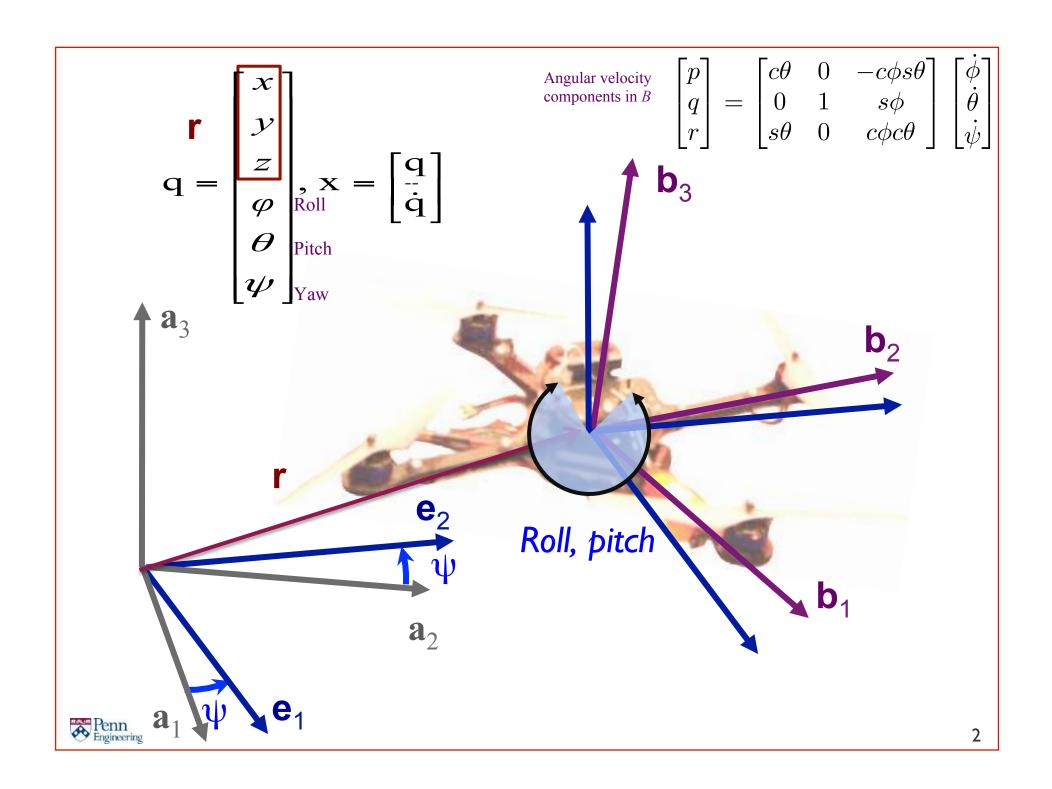
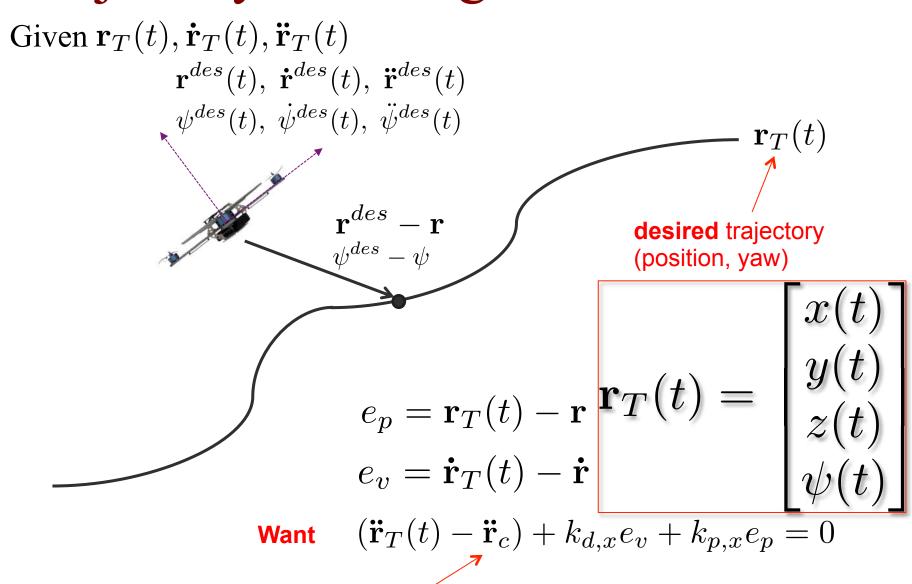
3-D Quadrotor



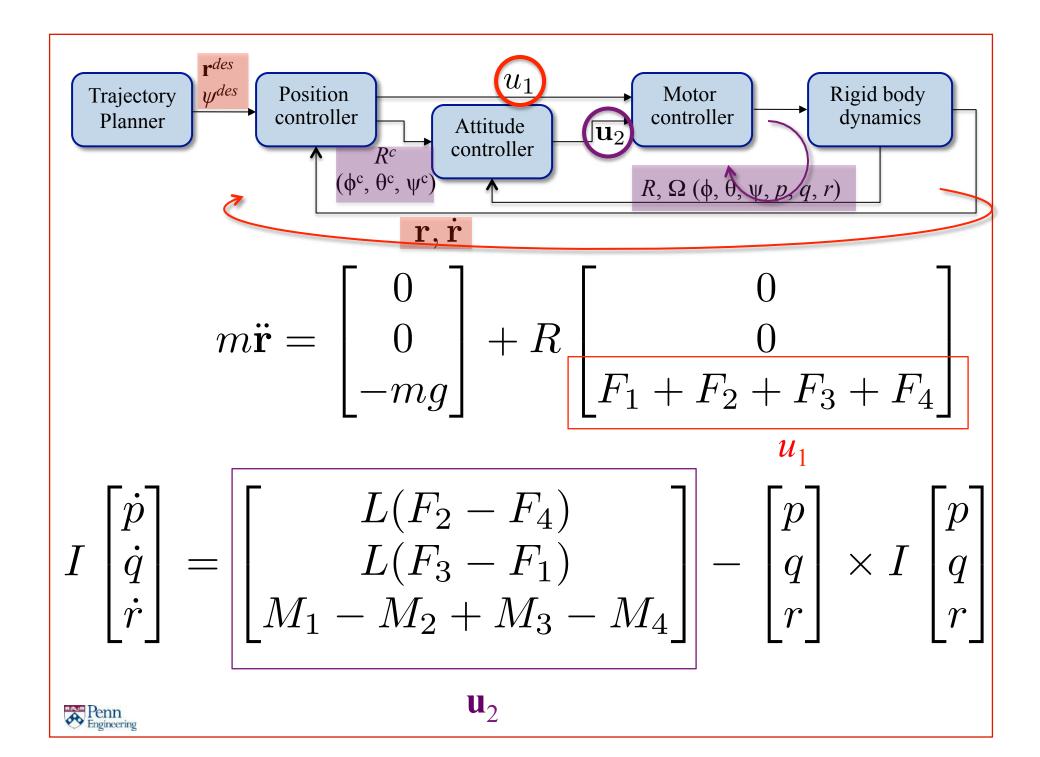


Trajectory Tracking in 3 Dimensions

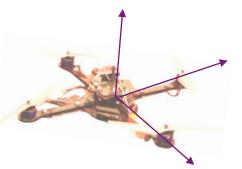




Commanded acceleration, calculated by the controller



Control for Hovering



Linearize the dynamics at the hover configuration

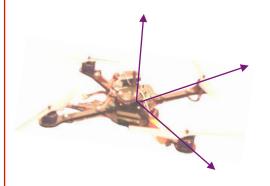
$$(u_1 \sim mg, \theta \sim 0, \phi \sim 0, \psi \sim \psi_0)$$
$$(u_2 \sim 0, p \sim 0, q \sim 0, r \sim 0)$$

$$m\ddot{\mathbf{r}} = \begin{bmatrix} 0\\0\\-mg \end{bmatrix} + R \begin{bmatrix} 0\\0\\F_1 + F_2 + F_3 + F_4 \end{bmatrix}$$

$$I\begin{bmatrix} \dot{p} \\ \dot{q} \\ \dot{r} \end{bmatrix} = \begin{bmatrix} L(F_2 - F_4) \\ L(F_3 - F_1) \\ M_1 - M_2 + M_3 - M_4 \end{bmatrix} - \begin{bmatrix} p \\ q \\ r \end{bmatrix} \times I\begin{bmatrix} p \\ q \\ r \end{bmatrix}$$



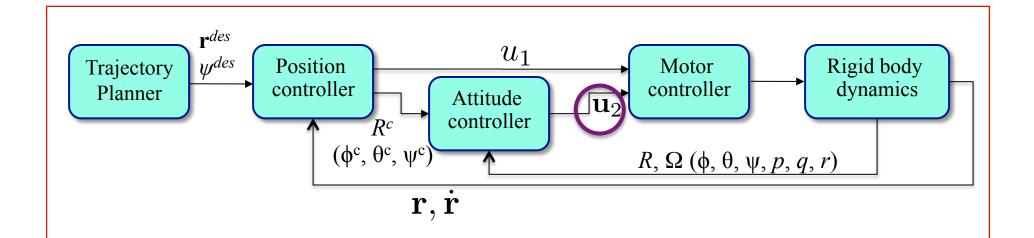
Control for Hovering



$$(u_2 \sim 0, p \sim 0, q \sim 0, r \sim 0)$$

$$I\begin{bmatrix} \dot{p} \\ \dot{q} \\ \dot{r} \end{bmatrix} = \begin{bmatrix} L(F_2 - F_4) \\ L(F_3 - F_1) \\ M_1 - M_2 + M_3 - M_4 \end{bmatrix} - \begin{bmatrix} p \\ q \\ r \end{bmatrix} \times I\begin{bmatrix} p \\ q \\ r \end{bmatrix}$$

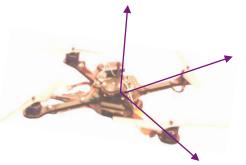




$$\mathbf{u}_{2} = \begin{bmatrix} k_{p,\phi}(\phi_{c} - \phi) + k_{d,\phi}(p_{c} - p) \\ k_{p,\theta}(\theta_{c} - \theta) + k_{d,\theta}(q_{c} - q) \\ k_{p,\psi}(\psi_{c} - \psi) + k_{d,\psi}(r_{c} - r) \end{bmatrix}$$



Control for Hovering



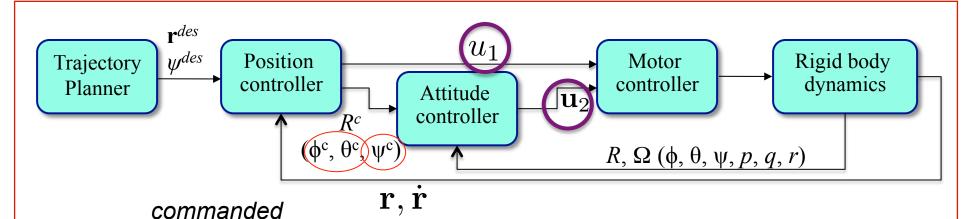
$$m\ddot{\mathbf{r}} = \begin{bmatrix} 0\\0\\-mg \end{bmatrix} + R \begin{bmatrix} 0\\0\\F_1 + F_2 + F_3 + F_4 \end{bmatrix}$$
 ation
$$u_1$$

Linearization

$$(u_1 \sim mg, \theta \sim 0, \phi \sim 0, \psi \sim \psi_0)$$

 $\ddot{r}_1 = \ddot{x} = g(\theta \cos \psi + \phi \sin \psi)$
 $\ddot{r}_2 = \ddot{y} = g(\theta \sin \psi - \phi \cos \psi)$





$$(\ddot{r}_{i,des} - \ddot{r}_{i,c}) + k_{d,i}(\dot{r}_{i,des} - \dot{r}_i) + k_{p,i}(r_{i,des} - \ddot{r}_i) = 0$$

$$u_1 = m(g + \ddot{r}_{3,c})$$

$$\phi_c = \frac{1}{g} (\ddot{r}_{1,c} \sin \psi_{des} - \ddot{r}_{2,c} \cos \psi_{des})$$

$$\theta_c = \frac{1}{g} (\ddot{r}_{1,c} \cos \psi_{des} + \ddot{r}_{2,c} \sin \psi_{des})$$

$$\psi_c = \psi^{des}$$

specified

$$\mathbf{u}_{2} = \begin{bmatrix} k_{p,\phi}(\phi_{c} - \phi) + k_{d,\phi}(p_{c} - p) \\ k_{p,\theta}(\theta_{c} - \theta) + k_{d,\theta}(q_{c} - q) \\ k_{p,\psi}(\psi_{c} - \psi) + k_{d,\psi}(r_{c} - r) \end{bmatrix}$$

