

CADET _____ SECTION _____ TIME OF DEPARTURE _____

DEPARTMENT OF CHEMISTRY & LIFE SCIENCE

CH365 2024-2025

Veteran's Day Bonus - Steam Tables

11 November 2024

TEXT: Smith, Van Ness, & Abbott

SCOPE: Lessons 27-32

ANTICIPATED TIME: 60 Minutes

References Permitted: Open notes, book, internet, CHEMCAD, Mathematica, Excel.

INSTRUCTIONS

1. This is a BONUS exercise and is due **2359 11 November 2024**.
2. There are 2 problems on 3 pages (not including the cover or reference pages).
3. A Mathematica file "VDB_Gibbs_Generating_Function.nb" that accompanies this handout is found in Canvas.
4. The reference article "VDB_Reference_Article_IF97.pdf" that accompanies this handout is found in Canvas.
5. A Microsoft Word file "VDB_Deliverables.docx" that accompanies this handout is found in Canvas.
6. Deliverables are your completed tables and Mathematica files in pdf format with cover sheet in a single pdf file, plus working Mathematica and CHEMCAD files (three files total). Save all electronic work in Canvas.

(TOTAL WEIGHT: 30 POINTS)

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PROBLEM	VALUE	ADD
A	15	
B	15	
TOTAL BONUS	30	

Problem: Weight:
A 15

In Lesson 27, we discussed the idea that the Gibbs energy function is a generating function for all other thermodynamic properties. The steam tables are an important application of this principle.[1] The properties in the tables are calculated from the Gibbs energy according to the generating functions in Table 1.

Table 1. Thermodynamic property relations derived from the Gibbs energy function (equation 1) and its derivatives, from Table 3 in Reference 1.

Property	Relation	Reference
Specific Volume	$v = (\partial g / \partial p)_T$	L27, Slide 11
Specific Internal energy	$u = g - T(\partial g / \partial T)_p - P(\partial g / \partial p)_T$	Eq. 6.1 (L27 Slide 6), combined with definitions of specific entropy and volume (s and v).
Specific entropy	$s = -(\partial g / \partial T)_p$	L27, Slide 11
Specific enthalpy	$h = g - T(\partial g / \partial T)_p$	Eq 6.4 (L27 Slide 6), combined with above definition of specific entropy s .

The Gibbs energy generating function for steam is

$$\frac{g(T, p)}{RT} = \sum_{i=1}^{34} n_i (7.1 - \pi)^{I_i} (\tau - 1.222)^{J_i} \quad (1)$$

where $\pi = p/p^*$, $\tau = T^*/T$, $p^* = 16.53$ MPa, $T^* = 1386$ K and $R = 0.461526$ kJ kg⁻¹ K⁻¹. The constants n_i , I_i , and J_i , as well an implementation of equation 1, are included in the Mathematica file that accompanies this exercise. [2]

In this assignment, you will modify the provided Mathematica file to calculate v , u , s , and h using the property relations in Table 1. To receive any credit, you must verify the test values in Table 2 on the following page. Ensure that your calculated answers contain the same precision as shown in Table 2 (nine significant figures), and complete Table 3 using your Mathematica results using the same format as in Table 2.

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Table 2. Thermodynamic property values calculated using equation 1 for selected values of T and p .

Property	$T = 300 \text{ K}$ $p = 3 \text{ MPa}$	$T = 300 \text{ K}$ $p = 80 \text{ MPa}$	$T = 500 \text{ K}$ $p = 3 \text{ MPa}$
$v / (\text{m}^3 \text{ kg}^{-1})$	$0.100\,215\,168 \times 10^{-2}$	$0.971\,180\,894 \times 10^{-3}$	$0.120\,241\,800 \times 10^{-2}$
$h / (\text{kJ kg}^{-1})$	$0.115\,331\,273 \times 10^3$	$0.184\,142\,828 \times 10^3$	$0.975\,542\,239 \times 10^3$
$u / (\text{kJ kg}^{-1})$	$0.112\,324\,818 \times 10^3$	$0.106\,448\,356 \times 10^3$	$0.971\,934\,985 \times 10^3$
$s / (\text{kJ kg}^{-1} \text{ K}^{-1})$	0.392 294 792	0.368 563 852	$0.258\,041\,912 \times 10^1$

The format of the entries in this table follows Table 5 in Reference 1.

Table 3. Cadet MATHEMATICA answers for comparison with Table 2.

Property	$T = 300 \text{ K}$ $p = 3 \text{ MPa}$	$T = 300 \text{ K}$ $p = 80 \text{ MPa}$	$T = 500 \text{ K}$ $p = 3 \text{ MPa}$
$v / (\text{m}^3 \text{ kg}^{-1})$			
$h / (\text{kJ kg}^{-1})$			
$u / (\text{kJ kg}^{-1})$			
$s / (\text{kJ kg}^{-1} \text{ K}^{-1})$			

Note: Cadets must use the same format for numbers used in Table 2.

Cadet: _____

Problem: Weight:
B 15

Design a CHEMCAD flow sheet that allows you to calculate v , s , u , and h and compare your answers to the values in Table 2. Complete Table 4 using your CHEMCAD results. Use nine significant figures and put all results in the same format used in Table 2.

Table 4. Cadet CHEMCAD answers for comparison with Table 2.

Property	T = 300 K p = 3 MPa	T = 300 K p = 80 MPa	T = 500 K p = 3 MPa
$v / (\text{m}^3 \text{ kg}^{-1})$			
$h / (\text{kJ kg}^{-1})$			
$u / (\text{kJ kg}^{-1})$			
$s / (\text{kJ kg}^{-1} \text{ K}^{-1})$			

Note: Cadets must use the same format for numbers as in Table 2.

References

1. The calculations in this exercise are found in IAPWS R7-97(2012), published by the International Association for the Properties of Water and Steam, Lucerne, Switzerland, August 2007. IAPWS R7-97(2012) is widely used in process simulators such as CHEMCAD and has been standardized by international convention.
2. The Gibbs energy function and the constants in this document pertain to Region 1 in Reference 1. Specifically, region 1 is $273.15 < T < 623.15$ K and $p^{\text{sat}}(T) < p < 100$ MPa. Other constants in Reference 1 pertain to other temperature-pressure regions.