

# CH365 Chemical Engineering Thermodynamics

## Lesson 29 Residual Properties II

Agenda  
Review  
Finish PS10  
Start Capstone Calcs.

# Block 6 Look-Ahead (CDP)

## Real Gas Properties

- Residual Properties
- $M = V, U, H, S, \text{ or } G$

$$M^R \equiv M - M^{\text{ig}} \quad (\text{Eq. 6.41})$$

$$M \equiv M^{\text{ig}} + M^R$$

Ideal gas (ig) follows ideal gas law

## Real Solution Properties (Liquids)

- Excess Properties
- $M^E = V^E, U^E, H^E, S^E, \text{ or } G^E$

$$M^E \equiv M - M^{\text{id}} \quad (\text{Eq. 6.41})$$

$$M \equiv M^{\text{id}} + M^E$$

$$G^E \equiv G - G^{\text{id}}$$

$$H^E \equiv H - H^{\text{id}}$$

$$S^E \equiv S - S^{\text{id}}$$

Ideal solution (id) follows Raoult's law ( $y_i P = x_i P_i^{\text{sat}}$ ).

## $G^E$ is related to the activity coefficients

From Gibbs-Duhem:

$$\frac{G^E}{RT} = \sum_i x_i \ln \gamma_i \quad (\text{Eq. 13.10})$$

Margules  
(1-constant)

$$\log \gamma_1 = A x_2^2 \quad \log \gamma_2 = A x_1^2$$

- The constant  $A$  is known from fitting experimental data.
- These are the so-called “binary interaction parameters” in CHEMCAD and in the *capstone design problem*.

# Residual Properties from Cubic EOS

Generic cubic equation of state (in Z-Form)

(WPR3)

$$q = q(x) = \frac{\Psi \alpha(x)}{\Omega \cdot x} \quad (\text{Eq. 3.51})$$

$$\alpha = \alpha(x)$$

( $\alpha$  is found in Table 3.1)

These are the red equations from L28 slide 8 (cleanup).

**Important:**  $\alpha$  is written as a function of  $x$  where  $x$  replaces  $T_r$ .

$q$  derivatives must be evaluated before process conditions ( $T_R$ ,  $P_r$ ) are entered.

$$\beta = \Omega \frac{P_r}{T_r} \quad (3.50)$$

$$Z = 1 + \beta - q\beta \frac{Z - \beta}{(Z + \varepsilon\beta)(Z + \sigma\beta)} \quad (3.48)$$

$$\frac{H^R}{RT} = Z - 1 + T_r \left( \frac{dq}{dT_r} \right) \cdot I$$

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$$\frac{S^R}{R} = \ln(Z - \beta) + \left( q + T_r \frac{dq}{dT_r} \right) \cdot I$$

$$I = \frac{1}{\sigma - \varepsilon} \ln \left( \frac{Z + \sigma\beta}{Z + \varepsilon\beta} \right) \quad (13.72)$$

$$\varepsilon \neq \sigma$$

# Questions?