

CH365 Chemical Engineering Thermodynamics

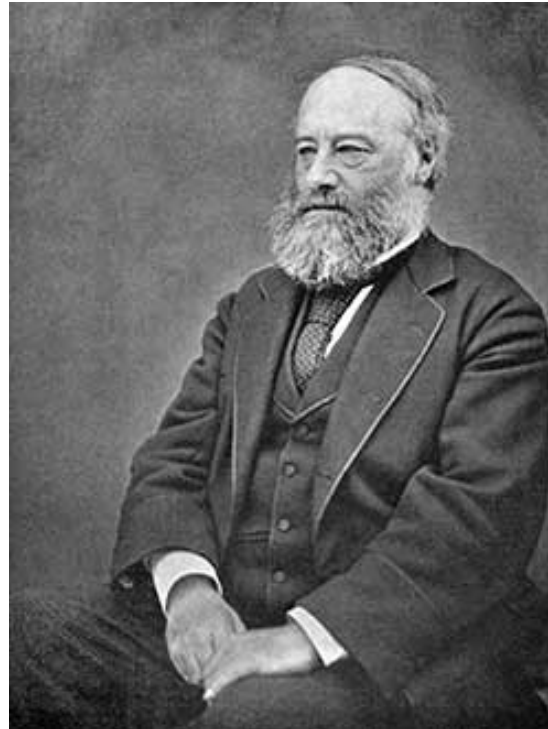
Lesson 4

Internal Energy, Energy Balances, and State Functions

Professor Andrew Biaglow

James P. Joule

24 December 1818 to 11 October 1889



Resistive Heating:
a.k.a. Joule's Law
 $P = I^2 R$

Joule-Thompson:
Joule's 2nd Law
Gas throttling

William Thomson
a.k.a. Baron Kelvin

Obscure home-schooled brewer's son. Tutored by John Dalton. Ran the brewery by day and conducted experiments at night as a hobby.

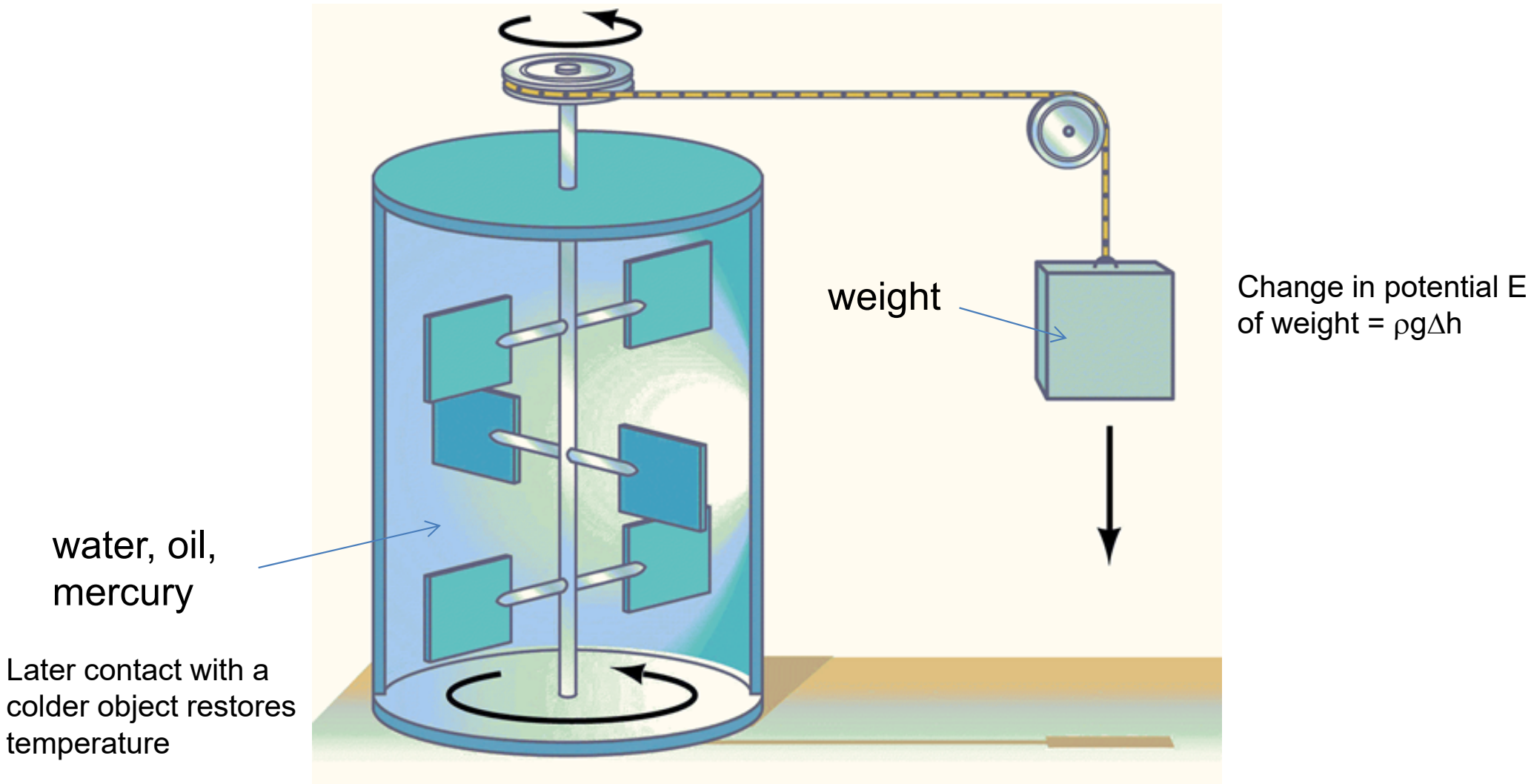
Impressed by the famous cannon-boring experiments of Count Rumford, in which heat is created continuously by the mechanical work of boring a cannon, and which violated the caloric theory of heat.

Joule's Experiment

relationship between work and heat

determined “the mechanical equivalent of heat with exactness”

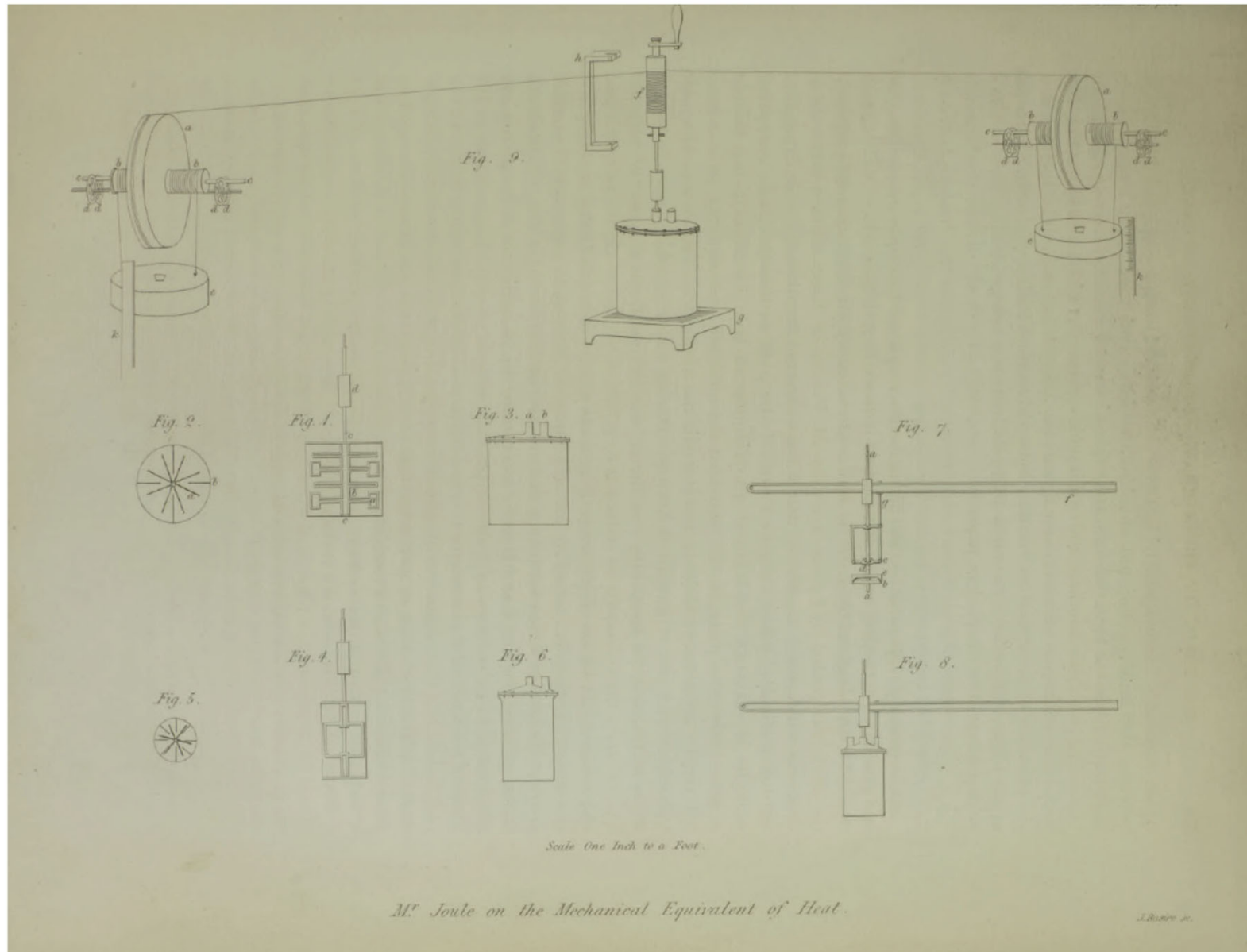
J.P. Joule, On the Mechanical Equivalent of Heat, *Philosophical Transactions of the Royal Society of London* 140 (1850): 61-82



For each fluid, a fixed amount of work is required per unit mass for every degree of temperature rise.

Joule's Apparatus

J.P. Joule, On the Mechanical Equivalent of Heat, *Philosophical Transactions of the Royal Society of London* 140 (1850): 61-82



Joule's Data

J.P. Joule, On the Mechanical Equivalent of Heat, *Philosophical Transactions of the Royal Society of London* 140 (1850): 61-82

TABLE I.

No. of experiment and cause of change of temperature.	Total fall of weights in inches.	Mean temperature of air.	Difference be- tween mean of columns 5 and 6 and column 3.	Temperature of apparatus.		Gain or loss of heat during experiment.
				Commencement of experiment.	Termination of experiment.	
1 Friction	1256.96	57.698	2.252—	55.118	55.774	0.656 gain
1 Radiation ...	0	57.868	2.040—	55.774	55.882	0.108 gain
2 Friction	1255.16	58.085	1.875—	55.882	56.539	0.657 gain
2 Radiation ...	0	58.370	1.789—	56.539	56.624	0.085 gain
3 Friction	1253.66	60.788	1.596—	58.870	59.515	0.645 gain
3 Radiation ...	0	60.926	1.373—	59.515	59.592	0.077 gain
4 Friction	1252.74	61.001	1.110—	59.592	60.191	0.599 gain
4 Radiation ...	0	60.890	0.684—	60.191	60.222	0.031 gain
1	2	3	4	5	6	7

Internal Energy

Energy added as work can be removed later as heat. Where is this energy between its addition and transfer out?

First Law of Thermodynamics

Although energy assumes many forms, the total quantity of energy is constant, and when energy disappears in one form, it appears simultaneously in other forms.

$$\Delta(\text{Energy of System}) + \Delta(\text{Energy of Surroundings}) = 0$$

System: Region of space in which the process occurs

- a system can be any size
- boundaries may be real or imaginary
- can be a single substance or a component of a mixture

Surroundings: Everything with which the system interacts

Energy Balance for Closed Systems

Closed System vs. Open Systems (described later)

System boundary does not permit the transfer of matter between the system and surroundings

Q and W are positive for transfer into the system from surroundings, pages 26-27. Heat or work added to system increase internal energy.

$$\Delta(\text{Energy of System}) = Q + W$$

Internal energy changes only:

Intensive U vs
extensive U^t
(L1 Silde 16)

$$\Delta U^t = Q + W$$

Differential form:

$$dU^t = dQ + dW$$

$$n\Delta U = Q + W \quad \text{eq 2.5}$$

$$n\Delta U = \Delta U^t \text{ if } n = 1 \text{ mol}$$

$$ndU = dQ + dW \quad \text{eq 2.6}$$

$$ndU = dU^t \text{ if } n=1 \text{ mol}$$

Units:
J, ft·lb_f, or Btu

Axiom to First Law:

There exists a form of energy, known as the internal energy U, which is an intrinsic property of a system, functionally related to the “measureable coordinates” which characterize the system. For a closed system not in motion, changes in this property are given by equations 2.5 and 2.6.

Example 2.3(a)

A gas is contained in a cylinder by a piston. The initial pressure of the gas is 7 bar, and the volume is 0.10 m^3 . The piston is held in place by latches in the cylinder wall. The whole apparatus is placed in a total vacuum. What is the energy change of the apparatus if the restraining latches are removed so that the gas suddenly expands to double its initial volume, the piston striking other latches at the end of the process? (System: gas, piston, and cylinder)

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Thermodynamic State and State Functions

State Functions

Depend only on present conditions, however reached.
Calculated as a function of *intensive* variables, e.g.,

$$U = f(T, P) \quad \text{Postulate: fixing any two intensive properties fixes all others}$$

f is a function of “measurable coordinates” T and P

Is pressure a state function?

$$PV = RT \Rightarrow P = \frac{RT}{V} = f(T, V)$$

Yes, pressure can be written as a state function.

(As long as we use intensive V and not extensive V^t)

$$\int_{P_1}^{P_2} dP = P_2 - P_1 = \Delta P \quad \int_{V_1}^{V_2} dV = V_2 - V_1 = \Delta V$$

Q and W are not state functions and depend on path.

$$\int dQ = Q \quad \int dW = W$$

(These are path integrals – mathematically different.)

Example 2.4

Refer to the figure below. When a system is taken from state a to state b along path acb , 100 J of heat flows into the system and the system does 40 J of work.

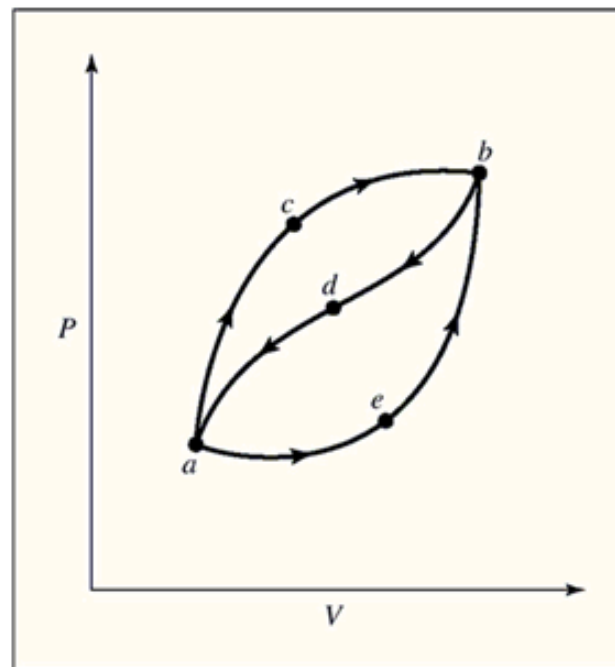


Diagram for Ex. 2.4.

Problem 2.6

One mole of a gas in a closed system undergoes a four-step thermodynamic cycle. Use the data given in the following table to determine the numerical values for the missing quantities, i.e., determine a-h.

Step	$\Delta U^t/\text{J}$	Q/J	W/J
12	-200	a	-6000
23	b	-3800	c
34	d	-800	300
41	4700	e	f
12341	g	h	-1400

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23	b	-3800	c
34	-500	-800	300
41	4700	e	f
12341	0	1400	-1400

Lesson 4 Problems

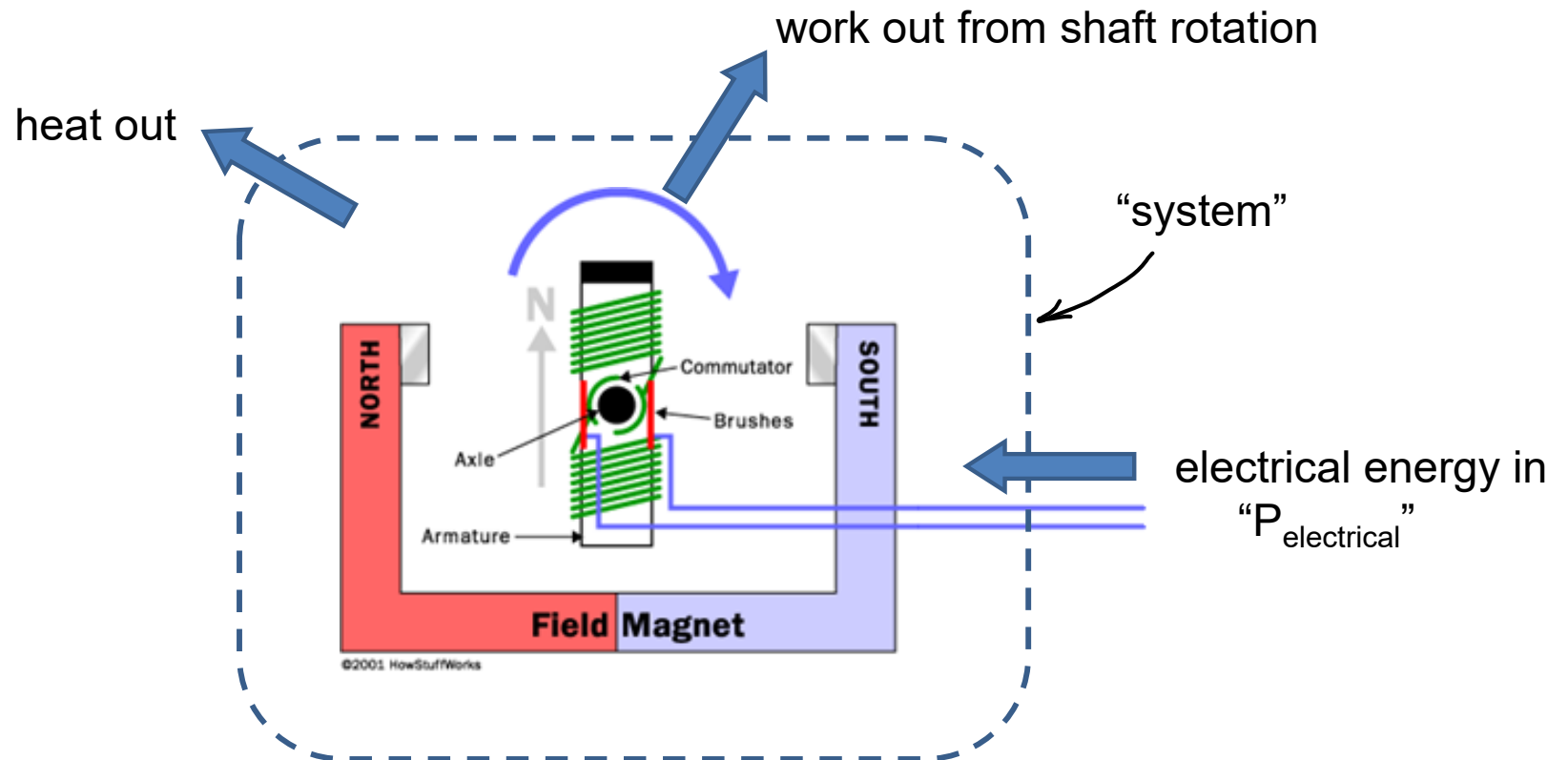
Problem 2.1

A nonconducting container filled with 25 kg of water at 20 deg C is fitted with a stirrer which is made to turn by gravity acting on a weight of mass 35 kg. The weight falls slowly through a distance of 5 m in driving the stirrer. Assuming that all work done on the weight is transferred to the water and that the local acceleration of gravity is $9.8 \frac{m}{s^2}$, determine:

- (a) The amount of work done on the water.
- (b) The internal energy change of the water.
- (c) The final temperature of the water, for which $C_p = 4.18 \frac{kJ}{kg \cdot degC}$.
- (d) The amount of heat that must be removed from the water to return it to its initial temperature.
- (e) The total energy change of the universe because of (1) the process of lowering the weight, (2) the process of cooling the water back to its initial temperature, and (3) both processes together.

Problem 2.4

An electric motor under steady load draws 9.7 amperes at 110 volts, delivering 1.25 hp of mechanical energy. What is the rate of heat transfer from the motor, in kW?



First Law:

$$\Delta U = Q + P_{\text{electrical}} + W$$

At steady state, $\Delta U = 0$:

$$0 = Q + P_{\text{electrical}} + W$$