CH365 Chemical Engineering Thermodynamics

Lesson 7
Enthalpy, Heat Capacity, and Open Systems – Part 2

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Measures of Flow

$$\dot{m} = \text{mass flow rate} \left(\frac{\text{kg}}{\text{s}}, \frac{\text{lb}_{\text{m}}}{\text{hr}}, \text{ etc.} \right)$$

$$\dot{n} = \text{molar flow rate} \left(\frac{\text{mol}}{\text{s}}, \frac{\text{lbmol}}{\text{s}}, \text{ etc.} \right)$$

$$\dot{q} = \text{volumetric flow rate } \left(\frac{m^3}{s}, \frac{ft^3}{min}, \text{ etc.} \right)$$

$$u = velocity \left(\frac{ft}{hr}, \frac{m}{s}, etc. \right)$$

$$\dot{m} = M\dot{n}$$
 $M = molar mass$

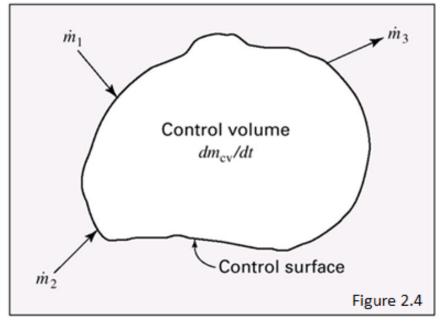
e.g.,
$$\frac{kg}{s} = \frac{kg}{kmol} \cdot \frac{kmol}{s}$$

$$\dot{m} = uA\rho$$
 $A = cross-sectional area = $\frac{\pi D^2}{4}$ $\rho = density = \frac{1}{V}$ [=] $\frac{kg}{m^3}$$

$$\dot{n} = uA\rho \cdot \frac{1}{M} \qquad \qquad e.g., \ \frac{lb_m}{sec} = \frac{ft}{sec} \cdot ft^2 \cdot \frac{lb_m}{ft^3}$$

2.23b – M is missing on p. 47

Equation of Continuity



This diagram changes in Figure 2.5 in a very important way.

$$\left\{ \begin{array}{c} \text{mass in} \\ \text{control volume} \\ \text{at time t} + \Delta t \end{array} \right\} = \left\{ \begin{array}{c} \text{mass in} \\ \text{control volume} \\ \text{at time t} \end{array} \right\} + \left\{ \begin{array}{c} \text{mass entering} \\ \text{control volume} \\ \text{by flow during } \Delta t \end{array} \right\} - \left\{ \begin{array}{c} \text{mass leaving} \\ \text{control volume} \\ \text{by flow during } \Delta t \end{array} \right\}$$

$$\mathbf{m}_{cv} \Big|_{t+\Delta t} = \mathbf{m}_{cv} \Big|_{t} + \dot{\mathbf{m}}_{1} \Delta t + \dot{\mathbf{m}}_{2} \Delta t - \dot{\mathbf{m}}_{3} \Delta t$$

$$m_{cv} \mid_{t+\Delta t} - m_{cv} \mid_{t} = \dot{m}_{1} \Delta t + \dot{m}_{2} \Delta t - \dot{m}_{3} \Delta t$$

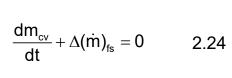
definition of 1st derivative:

$$f'(x) = \frac{df(x)}{dx} = \lim_{\Delta x \to 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

$$\frac{\mathsf{m}_{\mathsf{cv}} \left|_{\mathsf{t}+\Delta \mathsf{t}} - \mathsf{m}_{\mathsf{cv}} \right|_{\mathsf{t}}}{\Delta \mathsf{t}} = \dot{\mathsf{m}}_{\mathsf{1}} + \dot{\mathsf{m}}_{\mathsf{2}} - \dot{\mathsf{m}}_{\mathsf{3}}$$

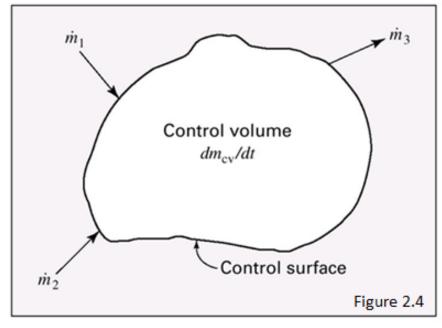
$$\frac{dm_{cv}}{dt} = \dot{m}_1 + \dot{m}_2 - \dot{m}_3$$

Mass Balance for Open Systems



$$\Delta(\dot{m})_{fs} = \dot{m}_3 - \dot{m}_1 - \dot{m}_2$$

$$\dot{m} = uA\rho$$
2.23a



This diagram changes in Figure 2.5 in a very important way with the addition of frictionless pistons, but there is no explanation of this in the textbook.

$$\frac{dm_{cv}}{dt} + \Delta(\rho uA)_{fs} = 0 \qquad 2.25$$

$$\Delta(\rho uA)_{fs} = 0$$
 steady state $\frac{dm_{cv}}{dt} = 0$

$$\rho_2 u_2 A_2 - \rho_1 u_1 A_1 = 0$$
 (single entrance and single exit)

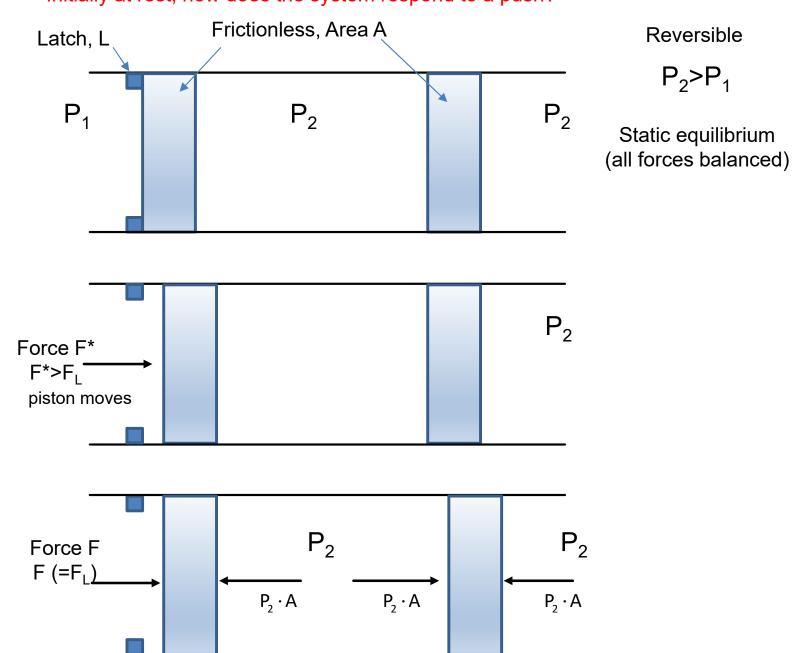
$$\dot{m} = \rho_2 u_2 A_2 = \rho_1 u_1 A_1 = constant$$

$$\dot{m} = \frac{u_1 A_1}{V_1} = \frac{u_2 A_2}{V_2}$$
(specific volume is the re-

(specific volume is the reciprocal of density)

Frictionless "Double Piston" Slide 5

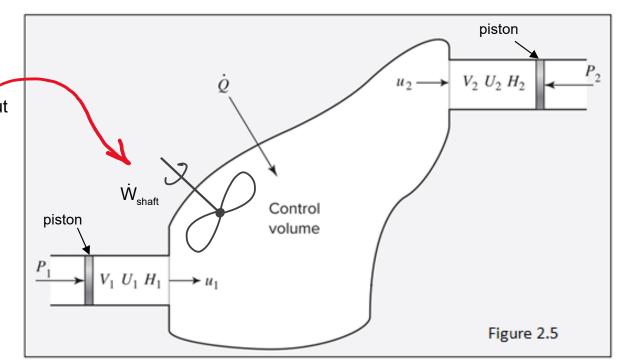
Understanding the "pistons" in figure 2.5 Initially at rest, how does the system respond to a push?



General Energy Balance

Shaft work is not illustrated in Figure 2.5 but is used in the equations.

Question: How does the system respond to a "push" on the left-hand piston?



$$\begin{split} \frac{d(mU)_{cv}}{dt} &= -\Delta \Bigg[\Bigg(U + \frac{1}{2}u^2 + zg \Bigg) \dot{m} \Bigg]_{fs} + \dot{Q} + \dot{W}_{tot} \\ \frac{d(mU)_{cv}}{dt} &= -\Delta \Bigg[\Bigg(U + \frac{1}{2}u^2 + zg \Bigg) \dot{m} \Bigg]_{fs} + \dot{Q} - \Delta \Big[\Big(PV \Big) \dot{m} \Big]_{fs} + \dot{W}_{shaft} \\ \frac{d(mU)_{cv}}{dt} &= -\Delta \Bigg[\Bigg(U + PV + \frac{1}{2}u^2 + zg \Bigg) \dot{m} \Bigg]_{fs} + \dot{Q} + \dot{W}_{shaft} \\ \frac{d(mU)_{cv}}{dt} + \Delta \Bigg[\Bigg(H + \frac{1}{2}u^2 + zg \Bigg) \dot{m} \Bigg]_{fs} &= \dot{Q} + \dot{W}_{shaft} \\ 2.27 \end{split}$$

There are two mechanisms to add or remove work:

$$\dot{W}_{tot} = \dot{W}_{expansion} + \dot{W}_{shaft}$$

$$\dot{W}_{expansion} = -P\Delta V \dot{m}$$

$$bar \cdot \frac{10^5 \frac{kg}{m \cdot s^2}}{bar} \cdot \frac{m^3}{kg} \cdot \frac{kg}{s}$$

$$= \frac{kg \cdot m^2}{s^3} = \frac{J}{s} = Watts$$

$$\frac{d(mU)_{cv}}{dt} + \Delta [H\dot{m}]_{fs} = \dot{Q} + \dot{W}_{shaft}$$
 2.28 (ignores changes in PE and KE)

Steady-State Systems

$$\Delta \Bigg[\Bigg(H + \frac{u^2}{2} + gz \Bigg) \dot{m} \Bigg]_{fs} = \dot{Q} + \dot{W}_{S}$$

general open system steady-state energy balance

$$\Delta\!\left(H\!+\!\frac{u^2}{2}\!+\!gz\right)\!\dot{m}=\dot{Q}+\dot{W}_{S}$$

2.30

constant flow open system energy balance (constant density) with one inlet and one outlet.

SI units:
$$\Delta H + \frac{\Delta (u^2)}{2} + g\Delta z = Q + W_S$$

2.31

First law of thermodynamics for steady-state, steady flow, constant density process with one inlet and one outlet

English units:
$$\Delta H + \frac{\Delta \left(u^2\right)}{2g_c} + \frac{g}{g_c} \Delta z = Q + W_S$$

all properties are energy per mass

$$\frac{\dot{Q}}{\dot{m}} = Q$$
 $\frac{\dot{W}_S}{\dot{m}} = W_S$

$$\Delta H = Q + W_S$$

Ignoring kinetic and potential energy changes

Problem 2.38

Carbon dioxide gas enters a water-cooled compressor at conditions $P_1 = 15$ (psia) and $T_1 = 50$ (degF), and is discharged at conditions $P_2 = 520$ (psia) and $T_2 = 200$ (degF). The entering CO_2 flows through a 4-inch-diameter pipe with a velocity of 20 (ft) (s)⁻¹, and is discharged through a 1-inch-diameter pipe. The shaft work supplied to the compressor is 5,360 (Btu) (lb mol)⁻¹. What is the heat-transfer rate from the compressor in (Btu) (hr)⁻¹?

Additional Information:

$$H_1 = 307 (Btu) (lb_m)^{-1}$$
 and $V_1 = 9.25 (ft)^3 (lb_m)^{-1}$

$$H_2 = 330 \, (Btu) \, (lb_m)^{-1} \text{ and } V_2 = 0.28 \, (ft)^3 \, (lb_m)^{-1}$$

Problem 2.28

Nitrogen flows at steady state through a horizontal, insulated pipe with inside diameter of 1.5 (in). A pressure drop results from flow through a partially opened valve. Just upstream from the valve the pressure is 100 (psia), the temperature is 120 (degF), and the average velocity is 20 (ft)(s). If the pressure just downstream from the valve is 20 (psia), what is the temperature? Assume for nitrogen that PV/T is constant, Cv=(5/2)R, and Cp=(7/2)R. (Values of R are given in App. A.)