

Ans to the Q/A no. 4

Given,

Local induced gradient, δ_m

output neuron = δ_f

$$f \text{ layer, } y_f = \phi(v_f)$$

$$h \text{ layer, } y_h = \phi''(v_h)$$

$$p \text{ layer, } y_p = \phi'''(v_p)$$

$$m \text{ layer, } y_m = \phi'(v_m)$$

$$v_j = \sum_i w_{ji} y_i$$

$$e_j = d_j - y_j$$

$$E = \frac{1}{2} \sum_j e_j^2$$

$$\delta_m = \frac{-\delta E}{\delta v_m}$$

$$= \frac{\delta E}{\delta y_m} \cdot \frac{\delta y_m}{\delta v_m}$$

$$= - \frac{\delta E}{\delta y_m} \cdot \frac{\delta y_m}{\delta v_m}$$

$$= \frac{-\delta E}{\delta y_m} \cdot \phi'(v_m)$$

$$\frac{\partial E}{\partial y_m} = \frac{-\partial E}{\partial e_f} \cdot \frac{\partial e_f}{\partial y_f} \cdot \frac{\partial y_f}{\partial v_f} \cdot \frac{\partial v_f}{\partial z_n} \cdot \frac{\partial y_h}{\partial v_n} \cdot \frac{\partial v_n}{\partial y_p} \cdot \frac{\partial y_p}{\partial v_p} \cdot \frac{\partial v_e}{\partial y_m}$$

Now,

$$E = \frac{1}{2} \sum_{f \in E} F^2$$

So,

$$\text{Computation} = - \sum_{f \in E} e_f \cdot -1 \cdot \varphi \cdot w_{f_n} \cdot \varphi'(v_n) \cdot w_{np}$$

$$\varphi''(v_p) \cdot w_{pm}$$

$$= \sum_{f \in E} e_f \cdot \varphi'(v_f) \cdot w_{fn} \cdot \varphi'(v_n) \cdot w_{np}$$

$$\cdot \varphi''(v_p) \cdot w_{pp}$$

$$= \sum_{f \in E} \delta_f \cdot w_{fh} \cdot \varphi''(v_n) \cdot w_{hp} \cdot \varphi''(v_p) \cdot w_{pm}$$