

Ex1 Let  $x_{t+1} = x_t + \delta t [x_t \cos \psi_t - y_t \sin \psi_t] + w_t^x$   
 $y_{t+1} = y_t + \delta t [x_t \sin \psi_t + y_t \cos \psi_t] + w_t^y$   
 $\psi_{t+1} = \psi_t + \delta t / v_t + w_t^\psi$

range measure

$$y_{t,j, \text{dist}} = |m_j - p_t| + v_{t,j, \text{dist}}$$

$$y_{t,j, \text{bearing}} = \tan^{-1} \left( \frac{m_j - y_t}{m_x - x_t} \right) - \psi_t + v_{t,j, \text{bearing}}$$

for  $j = 1, 2, \dots, n$

$$x_t = \begin{bmatrix} x_t \\ y_t \\ \psi_t \\ m_x \\ m_y \\ \vdots \\ m_x^n \\ m_y^n \end{bmatrix}$$

$$y_t = \begin{bmatrix} |m - p_t| \\ \vdots \\ |m^n - p_t| \\ \tan^{-1} \left( \frac{m_j - y_t}{m_x - x_t} \right) - \psi \\ \vdots \\ \tan^{-1} \left( \frac{m_y^n - y_t}{m_x^n - x_t} \right) - \psi \end{bmatrix}$$

$$+ \begin{bmatrix} v_{t, \text{dist}} \\ \vdots \\ v_{t, \text{dist}} \\ v_{t, \text{mc}} \\ \vdots \\ v_{t, \text{mc}} \\ v_{t, \text{bc}} \end{bmatrix}$$

$$x_k = f(x_{k-1}, u_k) + w_k$$

$$\begin{bmatrix} x_k \\ y_k \\ \psi_k \\ m_x' \\ m_y' \\ \vdots \\ m_x^n \\ m_y^n \end{bmatrix} = \begin{bmatrix} x_{k-1} + \delta t \left[ \ddot{x}_{k-1} \cos \psi_{k-1} - \ddot{y}_{k-1} \sin \psi_{k-1} \right] \\ y_{k-1} + \delta t \left[ \ddot{x}_{k-1} \sin \psi_{k-1} + \ddot{y}_{k-1} \cos \psi_{k-1} \right] \\ \psi_{k-1} + \delta \theta \psi_{k-1} \\ m_x' \\ m_y' \\ \vdots \\ m_x^n \\ m_y^n \end{bmatrix} + \begin{bmatrix} v_{k-1}^x \\ v_{k-1}^y \\ \psi_{k-1} \\ 0 \\ 0 \\ \vdots \\ 0 \\ 0 \end{bmatrix}$$

$f_k$

$$y_k = \begin{bmatrix} \|m' - p_k\| \\ \|m^n - p_k\| \\ \text{atan2}(m_y' - y_k, m_x' - x_k) - \psi_k \\ \vdots \\ \text{atan2}(m_y^n - y_k, m_x^n - x_k) - \psi_k \end{bmatrix} + \begin{bmatrix} v_k'^x \\ v_k'^y \\ \psi_k' \\ \vdots \\ v_k'^n \\ v_k'^b \end{bmatrix}$$

$$F_k = \frac{\partial f}{\partial x} \Big|_{\hat{x}_{k-1}/k-1, u_k} \rightarrow h_k$$

$$F_K = \begin{bmatrix} 1 & 0 & -8t[x_{K-1}\sin\psi_{K-1}/k_1 + \dot{y}_{K-1}/k_1 \cos\psi_{K-1}] & 0 & \dots & 0 \\ 0 & 1 & 8t[x_{K-1}\cos\psi_{K-1}/k_1 - \dot{y}_{K-1}\sin\psi_{K-1}] & 0 & \dots & 0 \\ 0 & 0 & 1 & 0 & \dots & 0 \\ 0 & 0 & 0 & 1 & \dots & 0 \\ 0 & 0 & \vdots & 0 & \ddots & \vdots \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & \dots & 1 \end{bmatrix}$$

$$H = \frac{\partial h}{\partial n} \Big|_{x=n_K/k-1}$$

$$H_K = \begin{bmatrix} \frac{(x_k - m'_x)}{\|m' - p_k\|} & \frac{y_k - m'_y}{\|m' - p_k\|} & 0 & \frac{m'_x - x_k}{\|m' - p_k\|} & \frac{m'_y - y_k}{\|m' - p_k\|} & \dots & 0 & 0 \\ \vdots & \vdots \\ \frac{(x_k - m''_x)}{\|m'' - p_k\|} & \frac{y_k - m''_y}{\|m'' - p_k\|} & 0 & \dots & \dots & \frac{m''_x - x_k}{\|m'' - p_k\|} & \frac{m''_y - y_k}{\|m'' - p_k\|} & \dots & \dots \\ \frac{m'_y - y_k}{\|m' - p_k\|^2} \frac{x_k - m'_x}{\|m' - p_k\|^2} & -1 & \frac{y_k - m'_y}{\|m' - p_k\|^2} \frac{m'_x - x_k}{\|m' - p_k\|^2} & 0 & \dots & 0 & 0 & \dots & \dots \\ \vdots & \vdots \\ \frac{m''_y - y_k}{\|m'' - p_k\|^2} \frac{x_k - m''_x}{\|m'' - p_k\|^2} & -1 & 0 & \dots & \dots & \frac{y_k - m''_y}{\|m'' - p_k\|^2} \frac{x_k - m''_x}{\|m'' - p_k\|^2} & 0 & 0 & \dots \end{bmatrix}$$

Figure 2 (on 1125836cf4b5)

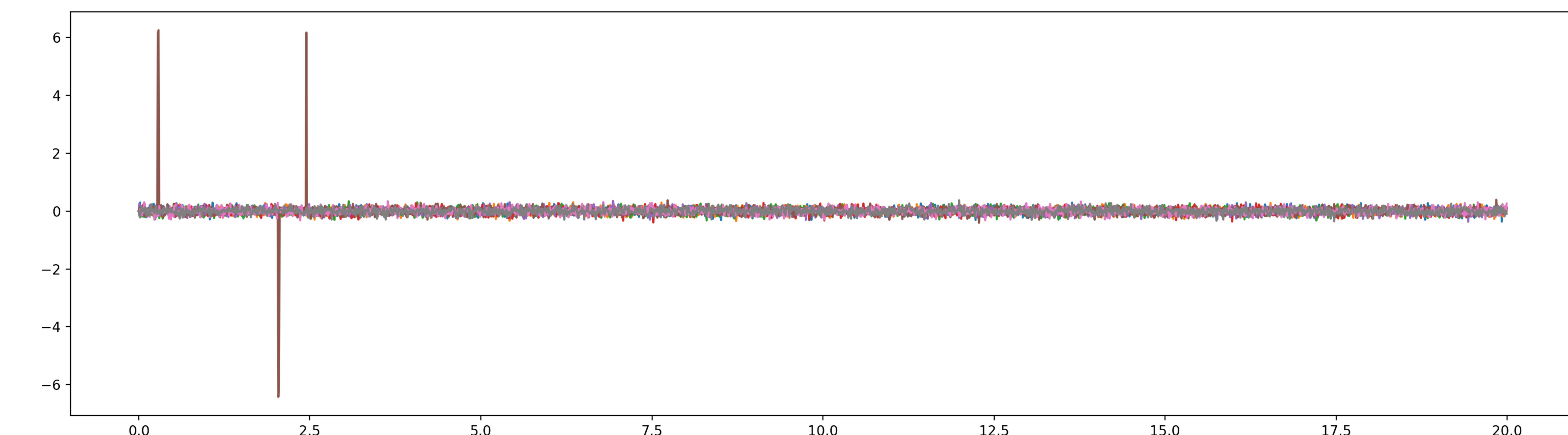
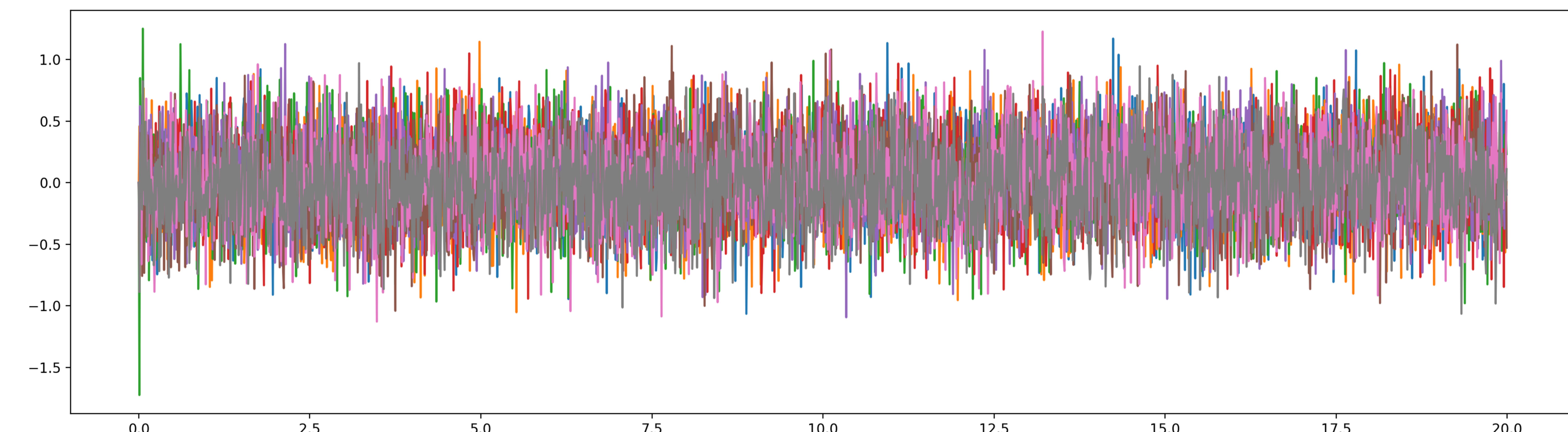


Figure 1 (on 1125836cf4b5)

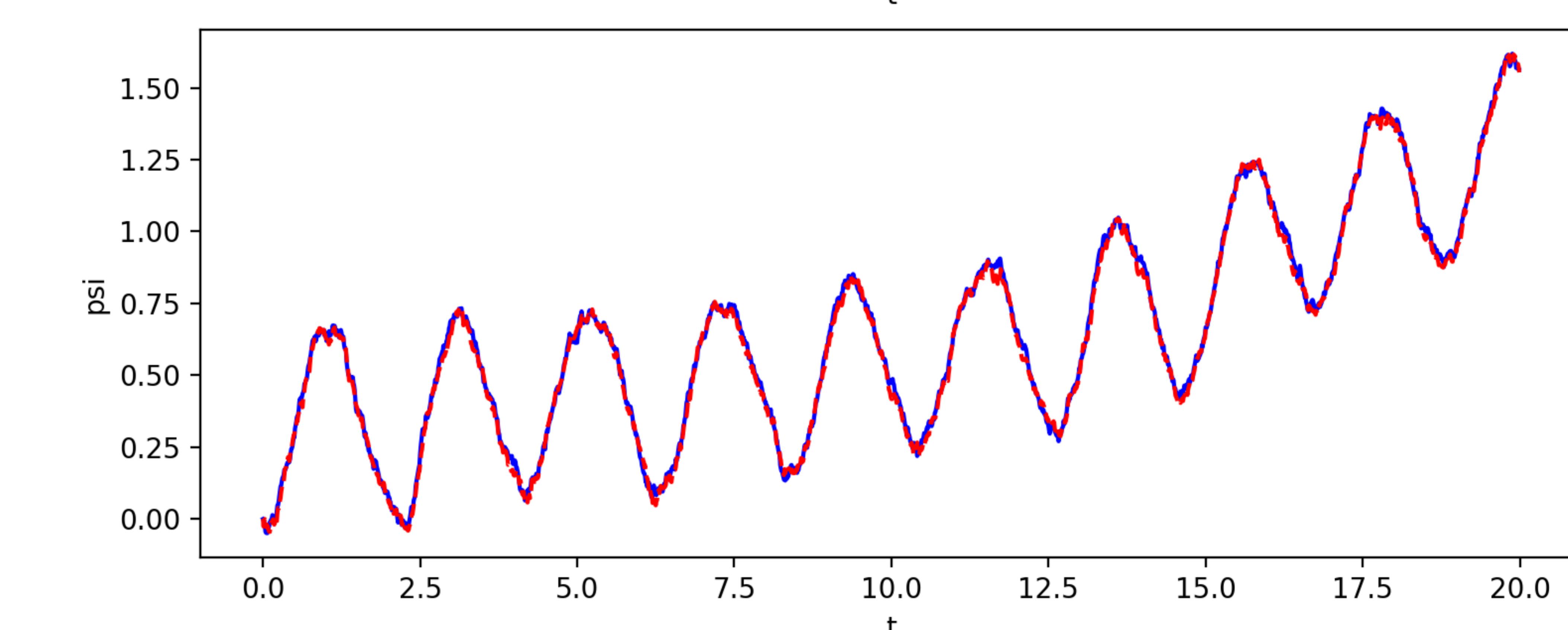
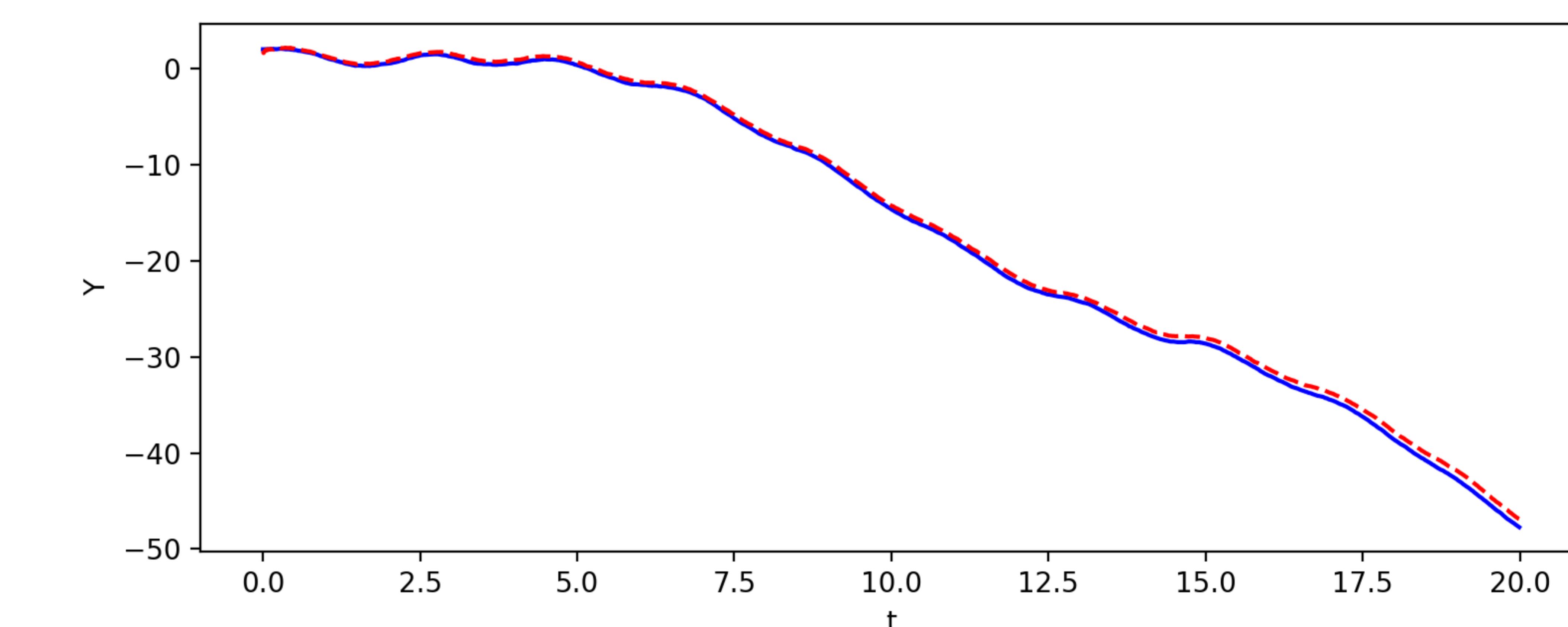
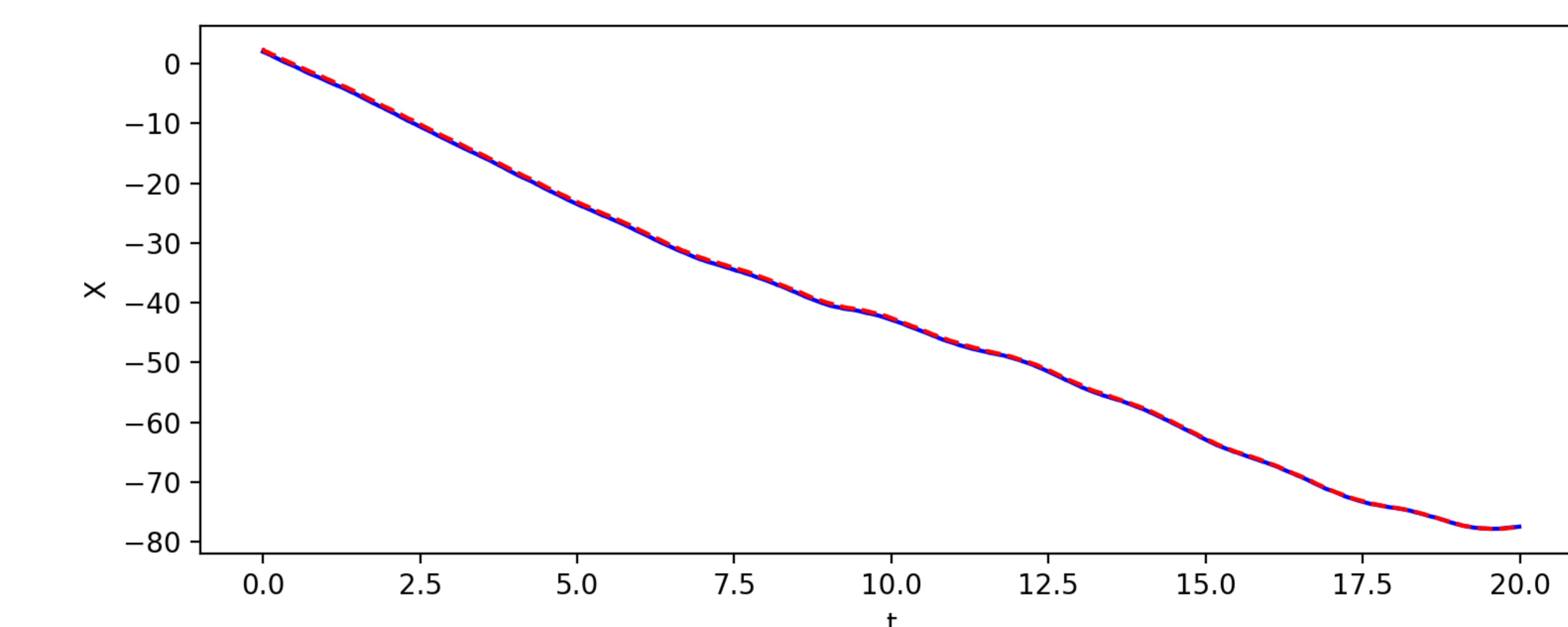
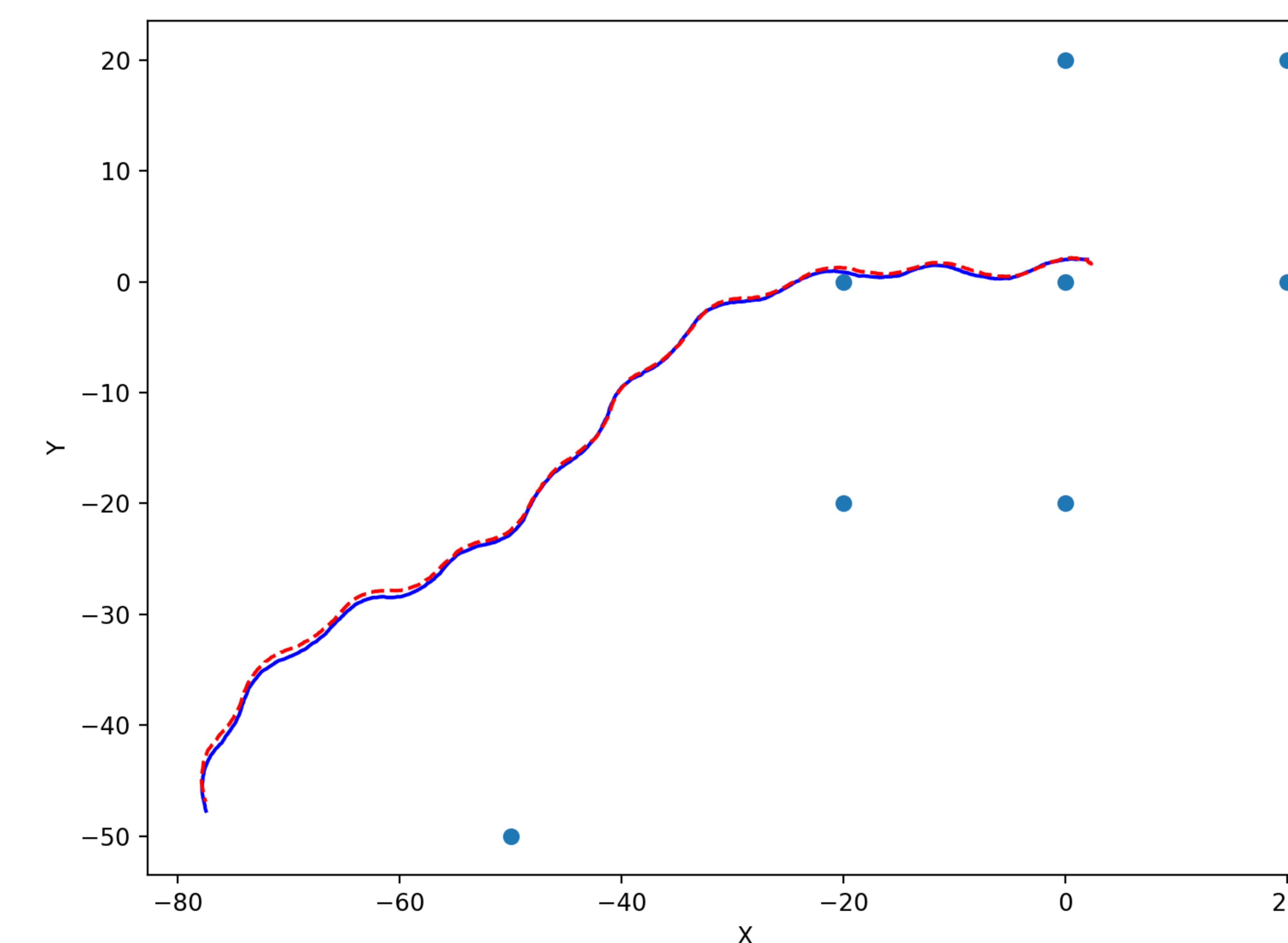



Figure 1 (on 1125836cf4b5)



below.

 $a * (lf - lr) / (m * xdot)$ , [0, 0, 0, 1], [0, -(2 \* Ca \* (lf - lr))] $y[node, 1], trajectory[node + forwardIndex, 0] - trajectory[node, 0]$  $(X - trajectory[node + forwardIndex, 0]) * np.sin(psiDesired)$  $trajectory[-1, 0] - trajectory[node, 0]) * np.sin(psiDesired)$