

## Appendix 4: Generic model code

Here we provide generic model code that closely follows the model description described in the main text, without the extra data structures to account for data heterogeneity (as found in Appendix 3).

### Generic model code

```
model_code <- NimbleCode({

#####
#####
# Process model #
#####
#####

#####
# Integral projection model #
#####

# intra-annual change
for (y in 1:n_year) {
  for (t in 1:(Tmax-1)) {

    # Equation 1
    ## project
    N[t + 1, y, 1:n_size] <- kernel[1:n_size, 1:n_size, t] %*%
      (N[t, y, 1:n_size] - C_T[t, y, 1:n_size]) +
      recruit_intro[t, y] * R[y, 1:n_size] # introduce recruits, t = 6

    # Equation 2
    ## kernel
    kernel[1:n_size, 1:n_size, t] <- seasonal_growth(
      xinf, gk, sigma_G, A, ds, D[t, 1:2], n_size, pi, x[1:n_size],
      lower[1:n_size], upper[1:n_size]) * S[t, y, 1:n_size]

    # Equation 7
    ## natural survival
    S[t, y, 1:n_size] <- survival(alpha, beta[y], D[t, 1:2], x[1:n_size])
  }
}

# Equation 8
## year-specific natural mortality (process error, includes mark-recapture)
for (y in 1:(n_year + 1)) {
  beta[y] ~ dgamma(beta_alpha, beta_theta)
}
```

```

## inter-annual change
for (y in 1:(n_year - 1)) {
  for (k in 1:n_size) {

    # Equation 9, 12
    ## overwinter survival and seasonal growth
    ## (use stochastic N node)
    N_stoch[y, k] ~ dbinom(size = seasonal_growth(xinf, gk, sigma_G, A, ds,
                                                    D[Tmax, 1:2], k, pi, y[k],
                                                    lower[k], upper[k]) %*%
                                                    (N[Tmax, y, k] - C_T[Tmax, y, k]),
                           prob = S_o[y, k])

  }

  # fill deterministic N node with stochastic N node
  N[1, y + 1, 1:n_size] <- N_stoch[y, 1:n_size]

  # Equation 10
  ## size- and density-dependent overwinter survival
  S_o[y, 1:n_size] <- overwinter_survival(alpha_o[y],
                                           sum(N[Tmax, y, 1:n_size]),
                                           x[1:n_size])

  # Equation 11
  ## year-specific intensity of overwinter mortality
  alpha_o[y] ~ dgamma(alpha_o_alpha, alpha_o_theta)
}

#####
# Initial population density and annual recruitment #
#####

# Equation 13
## get initial size-structured abundance of adults - year 1
N[1, 1, 1:n_size] <- get_init_adult(mu_A, sigma_A, lower[1:n_size],
                                     upper[1:n_size], lambda_A)

# Equation 14
## annual abundance of recruits
for (m in 1:n_year) {
  lambda_R[m] ~ T(dnorm(mu_lambda, sd = sigma_lambda), 0, Inf)
}

# Equation 15
## annual size distribution of recruits
R[1:n_year, 1:n_size] <- get_init_recruits(mu_R, sigma_R, lower[1:n_size],
                                           upper[1:n_size],
                                           lambda_R[1:n_year], n_year,
                                           n_size)

#####
#####

```

```

# Observation model #
#####
#####

for (y in 1:n_year) {
  for (t in 1:Tmax) {
    for (k in 1:n_size) {

      # Equation 16
      ## binomial distribution with total crabs removed, n_R
      C_T[t, y, k] ~ dbinom(size = round(N[t, y, k]), prob = p[t, y, k])

      # Equation 17
      ## dirichlet-multinomial mixture, conditional probability of capture
      alpha_D[t, 1:totalo, y, k] <- p_C[t, 1:totalo, y, k] * n_p_dir
      C[t, 1:totalo, y, k] ~ ddirchmulti(alpha = alpha_D[t, 1:totalo, y, k],
                                          size = C_T[t, y, k])
    }

    # Equations 18 - 20
    ## calculate hazard rate
    hazard[t, 1:totalo, y, 1:n_size] <- calc_hazard(
      totalo, n_size, h_F_max, h_F_k, h_F_0, h_S_max, h_S_k, h_S_0, h_M_max,
      h_M_A, h_M_sigma, f_index[t, 1:totalo, y], s_index[t, 1:totalo, y],
      m_index[t, 1:totalo, y], soak_days[t, 1:totalo, y], x[1:n_size]
    )

    # Equation 21
    ## total capture probability
    p[t, y, 1:n_size] <- calc_prob(totalo, n_size,
                                   hazard[t, 1:totalo, y, 1:n_size])

    # mean conditional probability of capture
    p_C[t, 1:totalo, y, 1:n_size] <- calc_cond_prob(totalo, n_size,
                                                    hazard[t, 1:totalo,
                                                    y, 1:n_size])
  }
}

#####
#####
# Integrated population model #
#####
#####

#####
# Mark-recapture data #
#####

# Equation 24
## draw recaptured samples, m2, from projected marked samples, n1_project

```

```

for (k in 1:n_size) {
  m2[k] ~ dbinom(size = round(n1_project[k]), prob = p_mc[k])
}

# Equation 25
## total capture probability with mark-recapture data
p_mc[1:n_size] <- calc_prob(totalo_mc, n_size,
                             hazard_mc[1:totalo_mc, 1:n_size])

# size-dependent hazard rates with mark-recapture data
hazard_mc[1:totalo_mc, 1:n_size] <- calc_hazard(
  totalo_mc, n_size, h_F_max, h_F_k, h_F_0, h_S_max, h_S_k, h_S_0, h_M_max,
  h_M_A, h_M_sigma, f_index_mc[1:totalo_mc], s_index_mc[1:totalo_mc,],
  m_index_mc[1:totalo_mc], soak_days[1:totalo_mc], x[1:n_size]
)

# Equation 26
## apply kernel from time of marking to time of recapture
n1_project[1:n_size] <- kernel_mc[1:n_size, 1:n_size] %*% n1[1:n_size]

kernel_mc[1:n_size, 1:n_size] <- seasonal_growth(xinf, gk, sigma_G, A, ds,
                                                  D_mc[1:2], n_size, pi,
                                                  x[1:n_size], lower[1:n_size],
                                                  upper[1:n_size]) *
  survival(alpha, beta[5], D_mc[1:2], x[1:n_size])

#####
# Growth model #
#####

# incorporated hierarchically as informative priors in the unified model
# asymptotic size
xinf ~ dnorm(inf_prior[1, 1], sd = inf_prior[1, 2])
# growth rate
gk ~ dnorm(inf_prior[2, 1], sd = inf_prior[2, 2])
# amplitude of growth oscillations
A ~ dnorm(inf_prior[3, 1], sd = inf_prior[3, 2])
# inflection point of growth oscillations
ds ~ dnorm(inf_prior[4, 1], sd = inf_prior[4, 2])

#####
#####
# Vague priors #
#####
#####

##
# size selectivity parameters
##

```

```

# minnow max. hazard rate
h_M_max ~ dunif(priors[1, 1], priors[1, 2])
# minnow max. size of capture
h_M_A ~ dunif(priors[2, 1], priors[2, 2])
# minnow sigma of gaussian size selectivity curve
h_M_sigma ~ dunif(priors[3, 1], priors[3, 2])
# fukui max. hazard rate
h_F_max ~ dunif(priors[4, 1], priors[4, 2])
# fukui k of logistic size selectivity curve
h_F_k ~ dunif(priors[5, 1], priors[5, 2])
# fukui midpoint of logistic size selectivity curve
h_F_0 ~ dunif(priors[6, 1], priors[6, 2])
# shrimp max. hazard rate
h_S_max ~ dunif(priors[7, 1], priors[7, 2])
# shrimp k of logistic size selectivity curve
h_S_k ~ dunif(priors[8, 1], priors[8, 2])
# shrimp midpoint of logistic size selectivity curve
h_S_0 ~ dunif(priors[9, 1], priors[9, 2])

##
# IPM - natural mortality
##

# gamma distributions shape for instantaneous intensity of mortality
beta_alpha ~ dunif(priors[10, 1], priors[10, 2])
# gamma distributions rate for instantaneous intensity of mortality
beta_theta ~ dunif(priors[11, 1], priors[11, 2])
# size-dependent natural mortality, shared across all sites
alpha ~ dunif(priors[12, 1], priors[12, 2])
# gamma distribution shape - instantaneous intensity of overwinter mortality
alpha_o_alpha ~ dunif(priors[13, 1], priors[13, 2])
# gamma distribution rate - instantaneous intensity of overwinter mortality
alpha_o_theta ~ dunif(priors[14, 1], priors[14, 2])

##
# IPM - growth
##

# growth error
sigma_G ~ dunif(priors[15, 1], priors[15, 2])

##
# observation process
##
# dirichlet multinomial (overdispersion in count data)
ro_dir ~ dbeta(priors[16, 1], priors[16, 2])
n_p_dir <- (1 - ro_dir) / ro_dir

##
# initial population density and annual recruitment
##

# initial adult size (mean and sd)

```

```

mu_A ~ dunif(priors[17, 1], priors[17, 2])
sigma_A ~ dunif(priors[18, 1], priors[18, 2])

# initial recruit size (mean and sd)
mu_R ~ dunif(priors[19, 1], priors[19, 2])
sigma_R ~ dunif(priors[20, 1], priors[20, 2])

# abundance of recruits (mean and sd)
mu_lambda ~ dunif(priors[21, 1], priors[21, 2])
sigma_lambda ~ dunif(priors[22, 1], priors[22, 2])

# abundance of adults in year 1
lambda_A ~ dunif(priors[23, 1], priors[23, 2])

})

```

## Nimble functions

### Process model functions

#### Initial population density of adults

This function corresponds to equation 1 in main text.

```

# initial size distribution of adults - year 1
get_init_adult <- nimbleFunction (

  run = function(mu_A = double(0), sigma_A = double(0),
                 lower = double(1), upper = double(1),
                 lambda_A = double(0))
  {
    returnType(double(1))

    # moment match from normal to gamma
    var <- sigma_A ^ 2
    shape <- mu_A ^ 2 / var
    rate <- mu_A / var
    prop_adult <- pgamma(q = upper, shape = shape, rate = rate) -
      pgamma(q = lower, shape = shape, rate = rate)

    # get initial size-structured abundance of adults
    out <- prop_adult * lambda_A

    return(out)
  }
)

```

#### Size-structured recruitment

This function corresponds to equation 15 in main text.

```

# annual size distributions of recruit
get_init_recruits <- nimbleFunction (

  run = function(mu_R = double(0), sigma_R = double(0),
                 lower = double(1), upper = double(1),
                 lambda_R = double(1), n_year = double(0),
                 n_size = double(0))

  {
    returnType(double(2))

    # create empty array
    out <- matrix(NA, ncol = n_size, nrow = n_year)

    var <- sigma_R ^ 2
    shape <- mu_R ^ 2 / var
    rate <- mu_R / var
    prop_recruit <- pgamma(q = upper, shape = shape, rate = rate) -
      pgamma(q = lower, shape = shape, rate = rate)

    # get initial size-structured abundance of recruits
    for (i in 1:n_year) {
      out[i, ] <- prop_recruit[1:n_size] * lambda_R[i]
    }

    return(out)
  }
)

```

## Seasonal growth

This function corresponds to equations 4-5 in main text.

```

# function for seasonal growth kernel
seasonal_growth <- nimbleFunction (
  run = function(xinf = double(0), k = double(0),
                 sigma_G = double(0), A = double(0),
                 ds = double(0), D = double(1),
                 n_size = double(0), pi = double(0), x = double(1),
                 lower = double(1), upper = double(1))

  {
    returnType(double(2))

    # create empty array
    array <- matrix(NA, ncol = n_size, nrow = n_size)

    # season adjusted params
    S_t <- (A * k / (2 * pi)) * sin(2 * pi * (D[2] - (1 + ds)))
    S_t0 <- (A * k / (2 * pi)) * sin(2 * pi * (D[1] - (1 + ds)))

    # p(y|y)
    for (i in 1:n_size) {
      increment <- (xinf - x[i]) *
        (1 - exp(-k * (D[2] - D[1]) - S_t + S_t0))
    }
  }
)

```

```

    mean <- x[i] + increment
    array[1:n_size, i] <- (pnorm(upper, mean, sd = sigma_G) -
                          pnorm(lower, mean, sd = sigma_G))
  }

  # normalize
  for (i in 1:n_size) {
    array[, i] <- array[, i] / sum(array[, i])
  }
  return(array)
}
)

```

## Natural survival

This function corresponds to equation 7 in main text.

```

# natural (non-winter) survival
survival <- nimbleFunction (

  run = function(alpha = double(0), beta = double(0), D = double(1),
                 x = double(1))
  {
    returnType(double(1))

    # get survival rate
    out <- exp(-(D[2] - D[1]) * (beta + alpha / x ^ 2))

    return(out)
  }
)

```

## Density-dependent overwinter survival

This function corresponds to equation 10-11 in main text.

```

# density- and size-dependent overwinter survival
overwinter_survival <- nimbleFunction (

  run = function(alpha_o = double(0), N = double(1),
                 x = double(1))
  {
    returnType(double(1))

    # get probability of survival
    out <- exp(-(alpha_o * sum(N) / x ^ 2))

    return(out)
  }
)

```



## Observation model functions

### Conditional multinomial observation model

This function corresponds to equations 18-20 in main text.

```
# calculate trap hazard rate of obs j, based on trap type and soak days
calc_hazard <- nimbleFunction (

  run = function(nobs = double(0), n_size = double(0), h_F_max = double(0),
    h_F_k = double(0), h_F_0 = double(0), h_S_max = double(0),
    h_S_k = double(0), h_S_0 = double(0), h_M_max = double(0),
    h_M_A = double(0), h_M_sigma = double(0), f_index = double(1),
    s_index = double(1), m_index = double(1),
    soak_days = double(1), x = double(1))

  {
    returnType(double(2))

    # create empty array
    array <- array(init = FALSE, dim = c(nobs, n_size))

    # loop through observations
    for (j in 1:nobs) {
      # P(capture)
      array[j, 1:n_size] <- size_sel_log(pmax = h_F_max, k = h_F_k,
        midpoint = h_F_0, x = x) *
        f_index[j] * soak_days[j] +
        size_sel_log(pmax = h_S_max, k = h_S_k, midpoint = h_S_0, x = x) *
        s_index[j] * soak_days[j] +
        size_sel_norm(pmax = h_M_max, xmax = h_M_A, sigma = h_M_sigma, x = x) *
        m_index[j] * soak_days[j]
    }
    return(array)
  }
)
```

These functions correspond to equation 21 in main text

```
# calculate conditional probability of capture
calc_cond_prob <- nimbleFunction (
  run = function(nobs = double(0), n_size = double(0), hazard = double(2))
  {
    returnType(double(2))

    # create empty array
    array <- array(init = FALSE, dim = c(nobs, n_size))
    # loop through sizes
    for (k in 1:n_size) {
      #P(capture in trap j / captured at all)
      array[1:nobs, k] <- hazard[1:nobs, k] / sum(hazard[1:nobs, k])
    }
    return(array)
  }
)
```

```

# calculate total capture probability
calc_prob <- nimbleFunction (

  run = function(nobs = double(0), n_size = double(0), hazard = double(2))
  {
    returnType(double(1))

    # create empty array
    p <- rep(NA, n_size)

    # loop through sizes
    for (k in 1:n_size) {
      # 1 - exp(-P(captured at all))
      p[k] <- 1 - exp(-sum(hazard[1:nobs, k]))
    }
    return(p)
  }
)

```

### Size-selective hazard rates

These functions correspond to equations 18-20 in main text.

```

# bell-shaped size selective hazard rate
size_sel_norm <- nimbleFunction (
  # input and output types
  run = function(pmax = double(0), xmax = double(0), sigma = double(0),
    x = double(1))
  {
    returnType(double(1))
    vector <- pmax * exp(-(x - xmax) ^ 2 / (2 * sigma ^ 2))

    return(vector)
  }
)

# logistic size selective hazard rate
size_sel_log <- nimbleFunction (
  run = function(pmax = double(0), k = double(0), midpoint = double(0),
    x = double(1))
  {
    returnType(double(1))

    vector <- pmax / (1 + exp(-k * (x - midpoint)))

    return(vector)
  }
)

```

### Dirichlet-multinomial mixture

These functions correspond to equation 17 in main text.

```

# define dirichlet multinomial mixture
# pdf
ddirchmulti <- nimbleFunction (
  run = function(x = double(1), alpha = double(1), size = double(0),
    log = integer(0, default = 0)) {
    returnType(double(0))
    logProb <- lgamma(size + 1) - sum(lgamma(x + 1)) + lgamma(sum(alpha)) -
      sum(lgamma(alpha)) + sum(lgamma(alpha + x)) -
      lgamma(sum(alpha) + size)
    if (log) return(logProb)
    else return(exp(logProb))
  })

# random number generator
rdirchmulti <- nimbleFunction (
  run = function(n = integer(0), alpha = double(1), size = double(0)) {
    returnType(double(1))
    if (n != 1) print("rdirchmulti only allows n = 1; using n = 1.")
    p <- rdirch(1, alpha)
    return(rmulti(1, size = size, prob = p))
  })

```