

Q1: Three coins are tossed. What is the probability of getting (i) all heads, (ii) two heads, (iii) at least one head, (iv) at least two heads?

Sol.: Let 'S' be the sample – space. Then $S = \{ HHH, HHT, HTH, THH, HTT, THT, TTH, TTT \}$

(i) Let 'E1' = Event of getting all heads, Then $E1 = \{ HHH \}$

$$|E1| = 1$$

$$P(E1) = |E1| / |S| = 1 / 8$$

(ii) Let $E2 =$ Event of getting '2' heads. Then:

$$E2 = \{ HHT, HTH, THH \}$$

$$|E2| = 3$$

$$P(E2) = 3 / 8$$

(iii) Let $E3 =$ Event of getting at least one head. Then:

$$E3 = \{ HHH, HHT, HTH, THH, HTT, THT, TTH \}$$

$$|E3| = 7$$

$$P(E3) = 7 / 8$$

(iv) Let $E4 =$ Event of getting at least one head, Then:

$$E4 = \{ HHH, HHT, HTH, THH, \}$$

$$|E4| = 4$$

$$P(E4) = 4/8 = 1/2$$

Q2: What is the probability, that a number selected from 1, 2, 3, ..., 25, is a prime number, when each of the numbers is equally likely to be selected.

Sol.: $S = \{ 1, 2, 3, \dots, 25 \}$ $|S| = 25$

And $E = \{ 2, 3, 5, 7, 11, 13, 17, 19, 23 \}$ $|E| = 9$

Hence $P(E) = |E| / |S| = 9 / 25$

Q3: Two dice are thrown simultaneously. Find the probability of getting :

- (i) The same number on both dice,
- (ii) An even number as the sum,
- (iii) A prime number as the sum,
- (iv) A multiple of '3' as the sum,
- (v) A total of at least 0,
- (vi) A doublet of even numbers,
- (vii) A multiple of '2' on one dice and a multiple of '3' on the other dice.

Sol.: Here:

$$S = \{ (1,1), (1,2), \dots, (1,6), (2,1), (2,2), \dots (2,6), (3,1), (3,2), \dots (3,6), \dots, (5,1), (5,2), \dots (5,6), (6,1), (6,2), \dots (6,6) \}$$
$$|S| = 6 \times 6 = 36$$

(i) Let $E1 =$ Event of getting same number on both side:

$$E1 = \{ (1,1), (2,2), (3,3), (4,4), (5,5), (6,6) \}; \quad |E1| = 6$$

$$P(E1) = |E1| / |S| = 6/36 = 1/6$$

(ii) Let $E2 =$ Event of getting an even number as the sum.

$$E2 = \{ (1,1), (1,3), (1,5), (2,2), (2,4), (2,6), (3,1), (3,3), (3,5), (4,2), (4,4), (4,6), (5,1), (5,5), (6,2), (6,4), (6,6) \}$$

$$|E2| = 18 \text{ hence } P(E2) = |E2| / |S| = 18/36 = 1/2$$

(iii) Let $E3 =$ Event of getting a prime number as the sum..

$$E3 = \{ (1,1), (1,2), (1,4), (1,6), (2,1), (2,3), (2,5), (3,2), (3,4), (4,1), (4,3), (5,2), (5,6), (6,1), (6,5), \}$$

$$|E_3| = 15$$

$$P(E_3) = |E_3| / |S| = 15/36 = 5/12$$

(iv) Let E_4 = Event of getting a multiple of '3' as the sum.

$$E_4 = \{ (1,2), (1,5), (2,1), (2,4), (3,3), (3,6), (4,2), (4,5), (5,1), (5,4), (6,3), (6,6) \}$$

$$|E_4| = 12$$

$$P(E_4) = |E_4| / |S| = 12/36 = 1/3$$

(v) Let E_5 = Event of getting a total of at least 10.

$$E_5 = \{ (4,6), (5,5), (5,6), (6,4), (6,5), (6,6) \}$$

$$|E_5| = 6$$

$$P(E_5) = |E_5| / |S| = 6/36 = 1/6$$

(vi) Let E_6 = Event of getting a doublet of even numbers.

$$E_6 = \{ (2,2), (4,4), (6,6) \}$$

$$|E_6| = 3$$

$$P(E_6) = |E_6| / |S| = 3/36 = 1/12$$

(vii) Let E_7 = Event of getting a multiple of '2' on one dice and a multiple of '3' on the other dice.

$$E_7 = \{ (2,3), (2,6), (4,3), (4,6), (6,3), (3,2), (3,4), (3,6), (6,2), (6,4) \}$$

$$|E_7| = 11$$

$$P(E_7) = |E_7| / |S| = 11/36$$

Q4.: What is the probability, that a leap year selected at random will contain 53 Sundays?

Sol.: A leap year has 366 days, therefore 52 weeks i.e. 52 Sunday and 2 days.

The remaining 2 days may be any of the following :

- (i) Sunday and Monday
- (ii) Monday and Tuesday
- (iii) Tuesday and Wednesday
- (iv) Wednesday and Thursday
- (v) Thursday and Friday
- (vi) Friday and Saturday
- (vii) Saturday and Sunday

For having 53 Sundays in a year, one of the remaining 2 days must be a Sunday.

$$|S| = 7; \quad |E| = 2$$

$$P(E) = |E| / |S| = 2 / 7$$

Q5.: Two cards are drawn at random. Find the probability that both the cards are of red colour or they are queen.

Sol.: Let S = Sample – space.

A = The event that the two cards drawn are red.

B = The event that the two cards drawn are queen.

$A \cap B$ = The event that the two cards drawn are queen of red colour.

$$|S| = C(52, 2), \quad |A| = C(26, 2), \quad |B| = C(4, 2)$$

$$n(A \cap B) = C(2, 2)$$

$$P(A) = |A| / |S| = C(26, 2) / C(52, 2), \quad P(B) = |B| / |S| = C(4, 2) / C(52, 2)$$

$$P(A \cap B) = |A \cap B| / |S| = C(2, 2) / C(52, 2)$$

$$P(A \cup B) = ?$$

$$\text{We have } P(A \cup B) = P(A) + P(B) - P(A \cap B) = C(26, 2) / C(52, 2) + C(4, 2) / C(52, 2) - C(2, 2) / C(52, 2) = 55/221$$