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Lecture 3

Basic functions for building regression
models: indicator variables; splines;
interactions WITH applications

Review of key concepts from Lecture 2

- ▶ Two main uses / purposes:

- ▶ Etiology: creating useful models to describe how Y is caused or associated with a set of X s
- ▶ Prediction: predicting Y using X

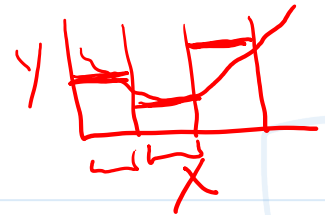
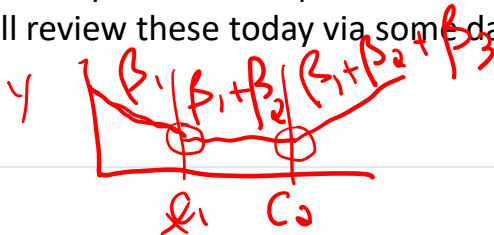


- ▶ Tools for building models to describe how Y changes with X *single variable*
- ▶ Step function: Mean of Y as a function of X changes with abrupt jumps (up and down)

- ▶ Linear spline: Mean of Y as a function of X changes linearly with a slope that changes at specified knot points

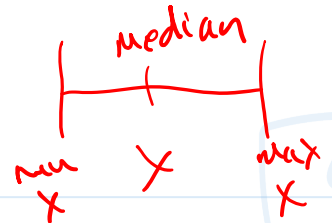
- ▶ Cubic spline: Mean of Y as a function of X is locally cubic with curvature that is changes at specified knot points

- ▶ We will review these today via some data analysis



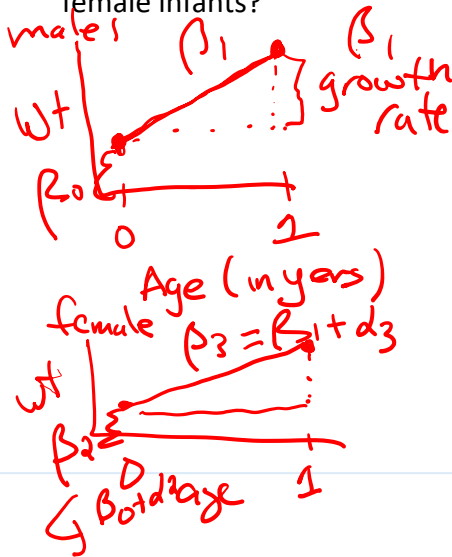
Review of key concepts from Lecture 2

- ▶ Additional smoothers from Lab 1
 - ▶ “loess”: locally estimated scatterplot smoothing
 - ▶ “lowess”: locally weighted estimated scatterplot smoothing
 - Estimates mean Y at a given X using a polynomial function (degree 1 or 2) based on some fraction of the observed data (span, e.g. 0.3 or 30% of the data) using weights: $(1 - |d|)^3$ →
 - ▶ “natural spline” or “natural cubic spline”
 - Cubic splines that assume a linear function beyond the boundary knots
 - You can provide the knots
 - Alternatively, you specify the “degrees of freedom”: defines the number of interior knots ($df - 1 - \text{intercept}$) set at appropriate quantile, where the default boundary knots are the min/max value of X



Interactions of simple functions

- ▶ Interactions allow for $E(Y|X) = \underline{f(x)}$ to vary across subsets of the population of interest
- ▶ Effect modification
- ▶ During the first year of life, is the average “growth rate” in weight for male infants the same as for female infants?



$$E(wt | age) = \beta_0 + \beta_1 age \Rightarrow \text{male}$$

$$E(wt | age) = \beta_2 + \beta_3 age \Rightarrow \text{female}$$

$$E(wt | age) = \beta_0 + \beta_1 age + \alpha_2 F + \alpha_3 F age$$

$$F = \begin{cases} 1 & \text{F} \\ 0 & \text{M} \end{cases}$$

$$\text{male : } \beta_0 + \beta_1 age$$

$$\text{females : } F = 1 \quad (\beta_0 + \alpha_2) + (\beta_1 + \alpha_3) age$$

$$H_0: \alpha_3 = 0$$

$$H_A: \alpha_3 \neq 0$$

Interactions of simple functions

- ▶ During the first year of life, is the average “growth rate” in weight for male infants the same as for female infants?



Interactions of simple functions

- ▶ During the first year of life, is the average “growth curve” for weight for male infants the same as for female infants?

↪

growth is quadratic

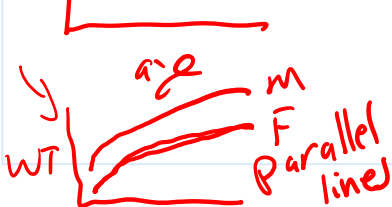


$$m \quad E(wt | age, F) = \beta_0 + \beta_1 age + \beta_2 age^2 + \beta_3 F + \beta_4 F age + \beta_5 F \times age^2$$



model

$$m \quad \beta_0 + \beta_1 age + \beta_2 age^2$$



$F: \text{set } \bar{F} = 1$

$$\boxed{\beta_4, \beta_5 = 0} \quad (\beta_0 + \beta_3) + (\beta_1 + \beta_4) age + (\beta_2 + \beta_5) age^2$$

$\beta_3, \beta_4, \beta_5 = 0$

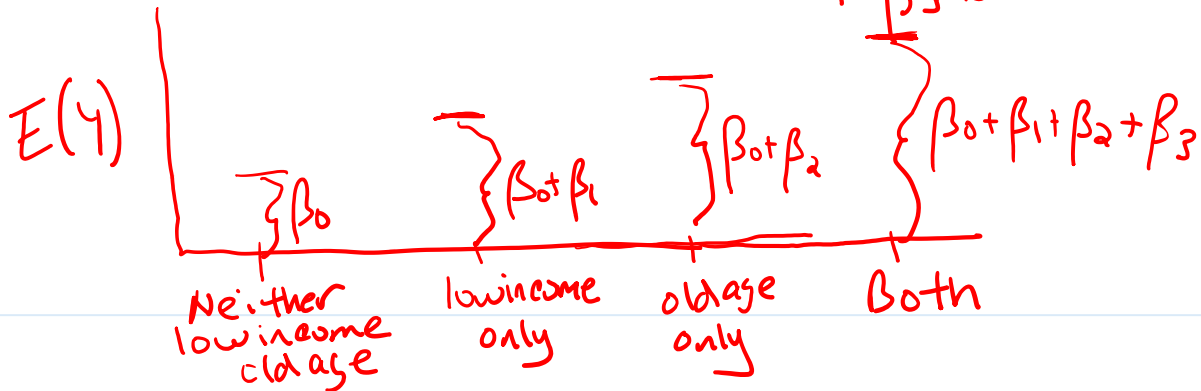
Interactions of simple functions

- Is the effect on average medical expenditures of being both poor and older greater than would be expected given the independent effects of poverty and old age alone

Y = medical expenditures
 $\text{lowincome} = \begin{cases} 1 & \text{low income} \\ 0 & \text{olw} \end{cases}$

$\text{oldage} = \begin{cases} 1 & \text{age} \geq 65 \\ 0 & \text{age} < 65 \end{cases}$

$$E(Y | \text{lowincome}, \text{oldage}) = \beta_0 + \beta_1 \text{lowincome} + \beta_2 \text{oldage} + \beta_3 \text{lowincome} \times \text{oldage}$$



And now some ANALYSIS!

- ▶ For the rest of today, we are going to work through several analyses for the Nepali Anthropometry study.

