Biostatistics 140.653: Applied Linear Regression Third Term, 2016 February 16, 2017 10:35-11:35

Midterm Test

Instructions: This is a closed book test. In answering the questions below, do not consult with any other person or any materials not on the attached pages. Choose the best answer (or answers is more than one are requested) for each question and circle its letter clearly. Good luck.

By signing my name, I agree to abide by the Johns Hopkins University School of Public Health Academic Code:

Name (Print):	 	 	
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Below find results of the NMES data analysis. There are three regressions of $\log_e(\text{total medical expenditures} + 1)$ on the indicator of whether the person has a major smoking caused diease (e.g. lung cancer, cardiovascular disease,...) (mscd=1-yes; 0-no), the persons age in years (lastage), and whether sex is male (male=1) or female (male=0); male:mscd indicates an interaction between these two variables. Log transform was used to make the response variable more nearly Gaussian

```
Estimate Std. Error
                               t value Pr(>|t|)
                   0.02295 247.23 <2e-16 ***
(Intercept) 5.67474
           2.34343
                   0.06689
                             35.03
                                     <2e-16 ***
Residual standard error: 2.519 on 13646 degrees of freedom
Multiple R-squared: 0.08252, Adjusted R-squared: 0.08245
F-statistic: 1227 on 1 and 13646 DF, p-value: < 2.2e-16
Model B: lm(formula = lte ~ ns(lastage, 3) + male + mscd)
          Estimate Std. Error t value
                                         Pr(>|t|)
(Intercept) 5.20666 0.06540 79.62
                                         <2e-16 ***
ns(lastage, 3)1 1.17810 0.09755 12.08 <2e-16 ***
ns(lastage, 3)2 1.89054 0.17374 10.88 <2e-16 ***
ns(lastage, 3)3 1.59383 0.13505 11.80 <2e-16 ***
male
              1.99756 0.06741
                                  29.63 <2e-16 ***
Residual standard error: 2.454 on 13642 degrees of freedom
Multiple R-squared: 0.1291, Adjusted R-squared: 0.1288
F-statistic: 404.6 on 5 and 13642 DF, p-value: < 2.2e-16
Model C: lm(formula = lte ~ ns(lastage, 3) + male + mscd + male:mscd)
          Estimate Std. Error t value
                                        Pr(>|t|)
              5.24695 0.06577 79.774 < 2e-16 ***
(Intercept)
ns(lastage, 3)1 1.16425 0.09749 11.942 < 2e-16 ***
ns(lastage, 3)2 1.89056 0.17357 10.892 < 2e-16 ***
ns(lastage, 3)3 1.61531 0.13497 11.968 < 2e-16 ***
              male
              1.66245 0.09236 18.000 < 2e-16 ***
0.69207 0.13053 5.302 1.16e-07 ***
mscd
male:mscd
Residual standard error: 2.452 on 13641 degrees of freedom
Multiple R-squared: 0.1309, Adjusted R-squared: 0.1305
F-statistic: 342.5 on 6 and 13641 DF, p-value: < 2.2e-16
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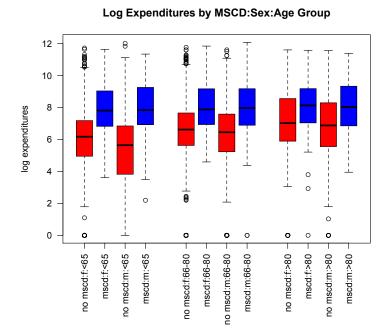
Model A: lm(formula = lte ~ mscd)

- 1. By examining the results of Model A, one can reasonably conclude that (select all correct answers)
- (a) the median expenditure for persons without an mscd is roughly \$5
- (b) the median expenditure for persons without an mscd is roughly \$290
- (c) the median expenditure for persons with an mscd is roughly \$7
- (d) the median expenditure for persons with an mscd is roughly \$10
- (e) the median expenditure for persons with an mscd is roughly \$3,000

2. By examining the results of Model A and assuming the Gaussian assumption for the residuals is a reasonable approximation, make an interval that will include about 95% of the annual medical expenditures for persons without a mscd

- 3. By comparing the results from Models A and B, one can reasonably conclude that (select the single best answer)
- (a) neither *lastage* nor *male* improve the prediction because the R^2 values from the two models are within 0.05 of one another
- (b) neither *lastage* nor *male* improve the prediction because the coefficient for *mscd* changes relatively little
- (c) neither *lastage* nor *male* improve the prediction of the obserbed expenditures because $F_{4.13642}$ = 184.1
- (d) *lastage* and/or *male* improve the prediction of the observed expenditures because $F_{4.13642}$ = 184.1
- (e) none of the above
- 4. By comparing the results from Models A, B and C, one can reasonably conclude that (select the single best answer)
- (a) *male* is neither a confounder nor an effect modifier of the effect of *mscd* on log expenditures because the residual standard deviation changes little across the three models
- (b) male is a confounder of the effect of mscd on log expenditures because the mscd coefficient in Model C changes substantially from its value in Model B
- (c) *male* modifies the effect of *msdc* on log expenditures because the male:mscd coefficient in Model C is statistically significant
- (d) *male* modifies the effect of *msdc* on expenditures because the mscd effect for men is nearly twice as large as for women, a statistically significant finding
- (e) one can not separate the concept of confounding from effect modification with data transformed to the log scale
- 5. Below find box plots of log expenditure orderded by mscd : sex : age category. Viewing this plot and the results of Models A, B and C, one can conclude (select all correct answers)
- (a) median exenditures increase with age for persons without a mscd but are roughly the same at all ages for persons with a mscd
- (b) the effect of mscd on expenditures is modified by age

- (c) median expenditures are higher for females than males of the same age among persons without an mscd but there is little or no sex difference for those with an mscd
- (d) the effect of sex is modified by mscd
- (e) the distribution of log expenditures is roughly symmetric with roughly constant interquartile range across the mscd: sex: age groups making the assumptions of the linear regression model more valid on this scale than on the original expenditure scale



Below find 4 model estimates and a scatterplot of the data with the 4 fitted curves. For model C, the covariance matrix of the estimated regression coefficients is also provided.

```
Estimate Std. Error t value Pr(>|t|)
            1.64743
                        0.15021 10.968 < 2e-16 ***
(Intercept)
             0.22489
                        0.03938
                                  5.711 2.72e-08 ***
Residual standard error: 1.584 on 298 degrees of freedom
Multiple R-squared: 0.09865, Adjusted R-squared: 0.09563
F-statistic: 32.62 on 1 and 298 DF, p-value: 2.717e-08
Model B. lm(formula = y \sim x + x_sp3)
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.18324
                        0.10861
                                  10.89
                                          <2e-16
                                          <2e-16 ***
             0.52622
                        0.03251
                                  16.19
            -6.67539
                        0.37987
                                 -17.57
                                          <2e-16 ***
x sp3
Residual standard error: 1.111 on 297 degrees of freedom
Multiple R-squared: 0.5581, Adjusted R-squared: 0.5551
F-statistic: 187.6 on 2 and 297 DF, p-value: < 2.2e-16
Model C. lm(formula = y \sim x + x sp1 + x sp2 + x sp3)
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Model A. $lm(formula = y \sim x)$

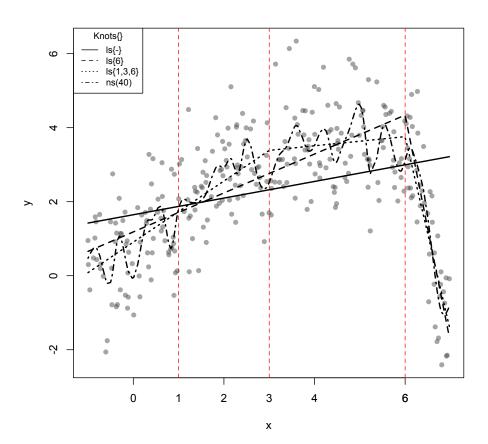
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Estimate Std. Error t value Pr(>|t|)
(Intercept) 0.906853
                       0.115777 7.833 8.68e-14 ***
            0.823758
                       0.166998 4.933 1.36e-06 ***
                                0.016 0.986879
x_sp1
            0.004347
                       0.264084
                      0.191942 -3.670 0.000287 ***
x_sp2
           -0.704500
           -5.384054  0.438489  -12.279  < 2e-16 ***
x sp3
Residual standard error: 1.061 on 295 degrees of freedomMultiple R-squared:
           Adjusted R-squared: 0.5941
F-statistic: 110.4 on 4 and 295 DF, p-value: < 2.2e-16
```

> summary(fit3)\$cov.unscaled

	(Intercept)	X	x_sp1	x_sp2	x_sp3
(Intercept)	0.011905115	-0.006249419	0.002723164	0.004168002	-0.001447362
X	-0.006249419	0.024769184	-0.036316021	0.013648263	-0.004739435
x_sp1	0.002723164	-0.036316021	0.061940475	-0.033736304	0.018295008
x sp2	0.004168002	0.013648263	-0.033736304	0.032721142	-0.036323644
_ x_sp3	-0.001447362	-0.004739435	0.018295008	-0.036323644	0.170768596

Model D. $lm(formula = y \sim ns(x, 40))$

Residual standard error: 1.021 on 259 degrees of freedom Multiple R-squared: 0.6748, Adjusted R-squared: 0.6245 F-statistic: 13.43 on 40 and 259 DF, p-value: < 2.2e-16



- 6. By examining the results of Model A and the figure above, one can reasonably conclude about the dependence of y on x that (select the single best answer)
- (a) the mean y has a statistically significant positive linear dependence on x
- (b) the mean y is estimated to increase 0.22 ± 0.078 per unit increase in x
- (c) the mean y is a non-linear function of x and a single slope is not an adequate summary of the relationship
- (d) the mean y when x=0 is close to 0, then increases with x
- (e) the residuals are not Gaussian making inferences about the mean incorrect
- 7. In the space below, calculate the estimated rate of change in mean y per unit x above x=6 from Models B and C. Which slope is steeper?

8. In the space below, calculate a 95% confidence interval for the slope above 6 for Model C.

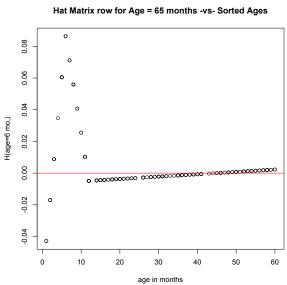
9. Test the null hypothesis that Model B does not improve the prediction of y relative to Model A. Calculate the test statistic and decide whether or not to reject the null that Models B does not improve upon A.

The mean squared errors (MSE) without cross-validation (equal to the squares of the residual standard deviations above) and the 10-fold cross-validated mean squared errors (CV-MSE) for the four models are as follows:

Model	Α	В	С	D
MSE	2.51	1.23	1.13	1.04
CV-MSE	2.51	1.25	1.15	1.21

- 10. Which model will predict a new observation with the smallest mean squared error? (select the single best answer)
- (a) A (b) B (c) C (d) D (e) no model has the smallest mean squared error
- 11. The difference between the MSE and the CV-MSE above increases across the 4 models A->D. This is because: (select the single best answer)
- (a) the flexibility of the models increases from A to D providing more opportunity for optimization to capitalize on chance
- (b) the MSE values are decreasing
- (c) the CV-MSE is 10-fold, not n-fold
- (d) the 10% left out observations make it more difficult to estimate the bigger models
- (e) CV-MSE is a biased estimator

From a regression of Nepal childrens' weight on {age, (age-6)+, and (age-12)+}, below find a plot of a row of the hat matrix H for which the corresponding age is 6 months.



- 12. The shape of the row in the plot tells us that: (select the single best answer)
- (a) the predicted weight for a child of age 6 months largely depends on the weights of children in the sample with ages between 2 and 10 months of age
- (b) the residual weight is smaller for ages near age 0 and again beyond age 12
- (c) the predicted weight is more precise for ages beyond age 12
- (d) the mean squared error is smaller for ages beyond age 12
- (e) (a) and (b)
- 13. The correlation of predicted values at times 0 and 6 is: (select the single best answer)
- (a) positive (b) negative (c) zero (d) positive, then negative (e) (a) and (b)