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Survival Analysis
Biostatistics 140.641
Spring, 2001

FINAL EXAM

1. (a) Characterize survival analysis. (no more than 100 words for your answer).
(b) Define the proportional hazards model in two cases: (i) time-independent covariates, and (ii) time-dependent covariates.
(c) Define 'independent censoring' in a one sample setting. Define 'independent censoring' in the the proportional hazards model with time-independent covariates.
(d) What is "informative censoring"? Discuss the possible occurrence of informative censoring in a clinical treatment-control study.
2. Let $(y_1, \delta_1), \dots, (y_n, \delta_n)$ represent the observed data and let $y_{(1)} < y_{(2)} < \dots < y_{(k)}$, $k \leq n$, be the distinct, uncensored and ordered failure times. Under which situation will the Kaplan-Meier estimate $\hat{S}(y_{(k)}^+)$ equal 0? Give a detailed discussion and interpret the result (Hint: Think of the practical applications where $\hat{S}(y_{(k)}^+) > 0$ or $= 0$).
3. Use the two-sample proportional hazards model to analyze the treatment/control data:

Treatment: 7, 9⁺, 11, 12

Control: 0, 6⁺, 7⁺

- (a) Write out the partial likelihood function and describe the estimation procedures (Note: You don't need to calculate the partial likelihood estimate here).
- (b) Are you concerned about the small sample size in (a)? Explain.
- (c) Suppose the censoring mechanism is independent. Calculate the Kaplan-Meier estimate for the treatment data.

4. Assume the failure time T has the exponential density $f(t) = \theta e^{-\theta t}$, $t, \theta > 0$.

(a) Identify the hazard function of T .

(b) Denote the hazard function of T by $\lambda(t)$. Verify that for a positive constant b , the random variable bT has the hazard function $\lambda(t)/b$. Interpret the result.

5. Consider a parameterized proportional hazards model

$$\text{model I: } \lambda(t|x) = \theta e^{\beta x}, \quad \theta > 0,$$

where $\lambda(t)$ denotes a hazard function, x is the covariate and β is a real-valued parameter. Consider an alternative model (parameterized accelerated failure time model)

$$\text{model II: } T = T_0 e^{\alpha x},$$

where T_0 is the 'baseline failure time', x is the covariate, and α is a real-valued parameter.

(a) Interpret Model I.

(b) Interpret Model II.

(c) Identify the situation when Models I and II are equivalent to each other. (Note: Two models are said to be equivalent if they include the same class of failure time distributions.)