Kernel Methods for Pattern Analysis Assignment 2

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Contents

| Ι | \mathbf{Cl} | assific | cation Tasks | 3 | | | | | | | |
|---|---------------|---------|---|----|--|--|--|--|--|--|--|
| 1 | Data-sets | | | | | | | | | | |
| | | 1.0.1 | Data-set 1: 2-dimensional input data: | | | | | | | | |
| | | 1.0.2 | Data-set 2 : Image data | | | | | | | | |
| 2 | Exp | erime | nt No.1: Bayes classifier | 9 | | | | | | | |
| | 2.1 | Linear | $\text{Ply Separable classes}(\text{Data-set }1(a)) \ldots $ | | | | | | | | |
| | | 2.1.1 | Decision Region Plots | | | | | | | | |
| | | 2.1.2 | Confusion Matrix and Average Classification Accuracy | 4 | | | | | | | |
| | 2.2 | Non-li | nearly Separable classes(Data-set 1(b)) | 4 | | | | | | | |
| | | 2.2.1 | Decision Region Plots | 4 | | | | | | | |
| | | 2.2.2 | Confusion Matrix and Average Classification Accuracy | Ę | | | | | | | |
| | 2.3 | Overla | apping classes(Data-set 1(c)) | Ę | | | | | | | |
| | | 2.3.1 | Decision Region Plots | į | | | | | | | |
| | | 2.3.2 | Confusion Matrix and Average Classification Accuracy | į | | | | | | | |
| | 2.4 | Image | Data(Data-set 2) | 6 | | | | | | | |
| | | 2.4.1 | Confusion Matrix and Average Classification Accuracy | 6 | | | | | | | |
| | 2.5 | | vations | (| | | | | | | |
| | 2.6 | Exper | iment No. 2: Perceptron Model for Data-set 1(a) | 6 | | | | | | | |
| | | 2.6.1 | Decision Region Plots | 7 | | | | | | | |
| | | 2.6.2 | Confusion Matrix and Average Classification Accuracy | - | | | | | | | |
| | | 2.6.3 | Observation | - | | | | | | | |
| 3 | Ext | erime | nt No.3: MLFFNN Models | 7 | | | | | | | |
| | 3.1 | | $ \text{cly Separable classes}(\text{Data-set }1(\mathbf{a})) \ . \ . \ . \ . \ . \ . \ . \ . \ . \$ | 7 | | | | | | | |
| | | 3.1.1 | Decision Region Plots | 8 | | | | | | | |
| | | 3.1.2 | Confusion Matrix and Average Classification Accuracy | 8 | | | | | | | |
| | | 3.1.3 | Average misclassification vs No of Hidden Nodes | ç | | | | | | | |
| | 3.2 | | nearly Separable classes(Data-set 1(b)) | ç | | | | | | | |
| | _ | 3.2.1 | Decision Region Plots | ç | | | | | | | |
| | | 3.2.2 | Confusion Matrix and Average Classification Accuracy | ç | | | | | | | |
| | | 3.2.3 | Plots of outputs each of the hidden nodes and output nodes in MLFFNN after the model is | | | | | | | | |
| | | 0.2.0 | <u>.</u> | 10 | | | | | | | |
| | | 3.2.4 | | 11 | | | | | | | |
| | 3.3 | J | <u> </u> | 11 | | | | | | | |
| | 5.5 | 3.3.1 | | 12 | | | | | | | |
| | | 3.3.2 | | 12 | | | | | | | |
| | | 3.3.3 | · · · · · · · · · · · · · · · · · · · | 1: | | | | | | | |

| | 3.4 | Image Data(Data-set 2) | |
|----|--------------|---|----|
| | 3.5 | Observations | 14 |
| ΙΙ | \mathbf{R} | Regression Tasks | 14 |
| 4 | Dat | ta-sets | 14 |
| | | 4.0.1 Data-set 1: 1-dimensional (Uni-variate) input data | 14 |
| | | 4.0.2 Data-set 2: 2-dimensional (Bi-variate) input data | 14 |
| | | 4.0.3 Data-set 3: Multivariate input data | 14 |
| 5 | Exp | periment No.1: MLFFNN model | 14 |
| | 5.1 | Uni-variate Data (Data-set 1) | 14 |
| | | 5.1.1 Plots of model output and target output | 14 |
| | | 5.1.2 Scatter Plot of Target versus Model Output | 16 |
| | | 5.1.3 Plot of Number of Hidden Layers versus Mean Squared Error | 16 |
| | | 5.1.4 Results | 17 |
| | 5.2 | Bi-variate Data (Data-set 2) | 17 |
| | | 5.2.1 Plots of model output and target output | 17 |
| | | 5.2.2 Scatter Plot of Target versus Model Output | 18 |
| | | 5.2.3 Plot of Number of Hidden Layers versus Mean Squared Error | 19 |
| | | 5.2.4 Plots of outputs each of the hidden nodes in MLFFNN after different number of epochs during | |
| | | training | 19 |
| | | 5.2.5 Plots of outputs of the output nodes in MLFFNN after different number of epochs during | |
| | | ${ m training.}$ | 22 |
| | | 5.2.6 Plots of Mean Squared Error versus Number of Epochs | 23 |
| | | 5.2.7 Table showing weight change with epochs for a hidden layer | 23 |
| | | 5.2.8 Results | 24 |
| | 5.3 | Multivariate Data (Data-set 3) | 24 |
| | | 5.3.1 Scatter Plot of Target versus Model Output | 24 |
| | | 5.3.2 Results | 24 |
| | 5.4 | Observations | 24 |
| 6 | Exp | periment No.2: Generalized RBF model | 24 |
| | 6.1 | Uni-variate Data (Data-set 1) | 25 |
| | | 6.1.1 Plots of MSE Error on Training data, Validation data and Test data. | |
| | | 6.1.2 Plots of model output and target output | 25 |
| | | 6.1.3 Scatter Plot of Target versus Model Output | 26 |
| | 6.2 | Bi-variate Data (Data-set 2) | 26 |
| | | 6.2.1 Results | 26 |
| | | 6.2.2 Plots of MSE Error on Training data, Validation data and Test data. | 26 |
| | | 6.2.3 Plots of model output and target output | 27 |
| | | 6.2.4 Scatter Plot of Target versus Model Output | 28 |
| | 6.3 | Multivariate Data (Data-set 3) | 29 |
| | | 6.3.1 Results | 29 |
| | | 6.3.2 Plots of MSE Error on Training data, Validation data and Test data. | 29 |
| | | 6.3.3 Scatter Plot of Target versus Model Output | 30 |
| | 6.4 | Observations | 30 |

Part I

Classification Tasks

1 Data-sets

1.0.1 Data-set 1: 2-dimensional input data:

(a) Linearly separable classes, (b) Non-linearly separable classes, (c) Overlapping class

1.0.2 Data-set 2: Image data

Models

2 Experiment No.1: Bayes classifier

In this experiment, we were suppose to build Bayes classifier (Gaussian Model or Gaussian Mixture Model) for the various types of data-sets given.

2.1 Linearly Separable classes(Data-set 1(a))

Aim was to build classifier for the given data-set of Linearly Separable classes. Data is bi-variate and the classification task was a three class problem. A simple Gaussian Model is built for the given data-set using the training data-set and examples in test data-set are classified using the trained model. Function is written to train a system to classify a given element to 3 classes using BAYES and NAIVE-BAYES Classifier and to find the Classification Accuracy, Confusion Matrix and Decision Region Plot of data-sets of different classes .

2.1.1 Decision Region Plots

Below shown are decision region plots for the Naive Bayes Classifier and Bayes Classifier respectively.

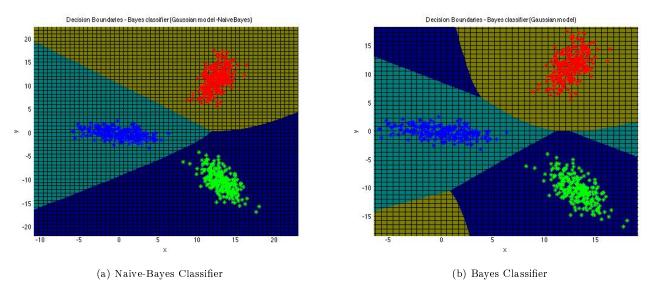


Figure 1: Decision Region Plots for Linearly Separable classes

2.1.2 Confusion Matrix and Average Classification Accuracy

Confusion Matrix for Naive Bayes classifier

| Class Label/Output Label | class1 | class2 | class3 |
|--------------------------|--------|--------|--------|
| class1 | 100 | 0 | 0 |
| ${ m class2}$ | 0 | 100 | 0 |
| class3 | 0 | 0 | 100 |

Classification Accuracy

1 1 1

Average Accuracy=1

Confusion Matrix for Bayes classifier

| Class Label/Output Label | class1 | class2 | ${\it class3}$ |
|--------------------------|--------|--------|----------------|
| class1 | 100 | 0 | 0 |
| ${ m class2}$ | 0 | 100 | 0 |
| class3 | 0 | 0 | 100 |

Classification Accuracy

1 1 1

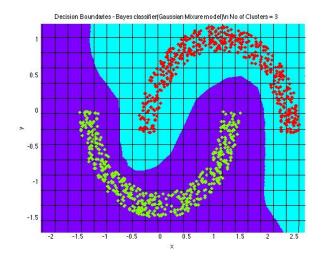
Average Accuracy=1

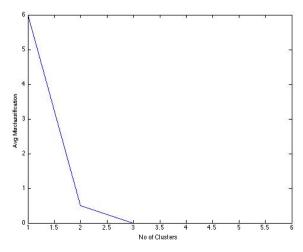
2.2 Non-linearly Separable classes(Data-set 1(b))

Aim was to build classifier for the given data-set of Non-linearly Separable Classes. Data is bi-variate and the classification task was a two class problem. Model is built to classify a given element to any of the three classes using GMM Classifier and to find the Classification Accuracy, Confusion Matrix and Decision Region Plot. Minimum number of mixtures needed per class for best performance is 3.

2.2.1 Decision Region Plots

Below shown are (a) decision region plot for the Bayes Classifier using Gaussian Mixture Model and (b)Average Misclassification vs Number of clusters plot.





- (a) Decision Region Plots of Bayes Classifier (GMM). No. of Clusters=3 $\,$
- (b) Average misclassification vs No. of Clusters

Figure 2: Performance plots for Non-linearly Separable classes

2.2.2 Confusion Matrix and Average Classification Accuracy

Confusion Matrix for Bayes classifier (GMM)

| Class Label/Output Label | class1 | class2 |
|--------------------------|--------|--------|
| class1 | 100 | 0 |
| class2 | 0 | 100 |

Classification Accuracy

1 1

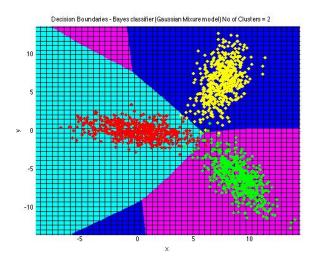
Average Accuracy=1

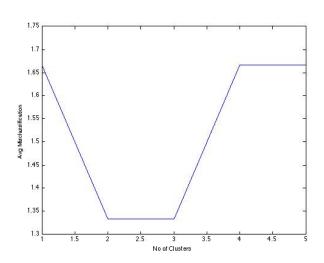
2.3 Overlapping classes(Data-set 1(c))

Aim was to build classifier for the given data-set of Overlapping Classes. Data is bi-variate and the classification task was a three class problem. Model is built to classify a given element to any of the three classes using GMM Classifier and to find the Classification Accuracy, Confusion Matrix and Decision Region Plot.

2.3.1 Decision Region Plots

Below shown are (a) decision region plot for the Bayes Classifier using Gaussian Mixture Model and (b)Plot of Average Misclassification vs Number of clusters.





- (a) Decision Region Plots of Bayes Classifier (GMM). No. of Clusters =2 $\,$
- (b) Average misclassification vs No. of Clusters

Figure 3: Performance plots for Overlapping classes

2.3.2 Confusion Matrix and Average Classification Accuracy

Confusion Matrix for Bayes classifier (GMM)

| Class Label/Output Label | class1 | class2 | class3 |
|--------------------------|--------|--------|--------|
| class1 | 100 | 0 | 0 |
| class2 | 0 | 100 | 0 |
| class3 | 0 | 1 | 99 |

Classification Accuracy

1 | 1 | 0.99

Average Accuracy=0.9967

2.4 Image Data(Data-set 2)

Aim was to build classifier for the given data-set of Classes. Data is multivariate with 48 dimensions and the classification task was a five class problem. Image data-set is splitted in ratio 70:10:20 for Train:Validation:Test . Model is built to classify a given element to any of the five classes using GMM Classifier and to find the Classification Accuracy, Confusion Matrix.

2.4.1 Confusion Matrix and Average Classification Accuracy

Confusion Matrix for Bayes classifier (GMM)

| Class Label/Output Label | class1 | class2 | class3 | class4 | class5 |
|--------------------------|--------|--------|--------|--------|--------|
| class1 | 29 | 9 | 0 | 1 | 3 |
| class2 | 7 | 15 | 2 | 4 | 2 |
| class3 | 6 | 7 | 27 | 3 | 1 |
| class4 | 5 | 10 | 3 | 22 | 1 |
| class5 | 1 | 7 | 0 | 3 | 76 |

Classification Accuracy

| 0.6579 0.5000 | 0.6136 | 0.5366 | 0.8736 |
|-----------------|--------|--------|--------|
|-----------------|--------|--------|--------|

Average Accuracy=0.6363

2.5 Observations

- For linearly Separable classes, Naive Bayes and Bayes Classifier performances are similar. This is because there are not much dependancy between the two features of the feature vector and only diagonals contributes to covariance matrix.
- For the Non-linearly Separable classes, GMM using 3 clusters found to be sufficient to get zero miscalssification. Hence the shape of the decision region is not too complex.
- For overlapping classes, if the number of clusters increases beyond 3, misclassification also increases, this is because when overlapped datapoints tend to form a different cluster in the other class, classifier learns wrongly.
- GMM using 10 clusters found to be suitable for given image data-set.

2.6 Experiment No. 2: Perceptron Model for Data-set 1(a)

The aim was to build a perceptron model for the Linearly Separable Data-set. Data is bi-variate and the classification task was a three class problem. One against one(1V1) method is used for classification of the examples to any of the three classes using Perceptron Model Based Classifier and to find the Classification Accuracy, Confusion Matrix and Decision Region Plot.

2.6.1 Decision Region Plots

Below shown are decision region plots for the Perceptron Model based Classifier.

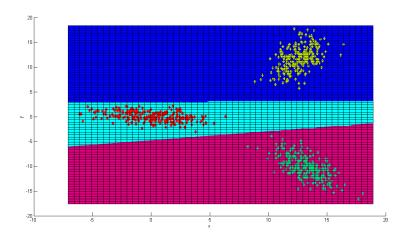


Figure 4: Decision Region Plot for Linearly Separable classes-Perceptron

2.6.2 Confusion Matrix and Average Classification Accuracy

Confusion Matrix

| Class Label/Output Label | class1 | class2 | class3 |
|--------------------------|--------|--------|--------|
| class1 | 100 | 0 | 0 |
| class2 | 0 | 100 | 0 |
| class3 | 0 | 0 | 100 |

Classification Accuracy

1 1 1

Average Accuracy=1

2.6.3 Observation

- Decision region decided by 1-Vs-1 method is different from that obtained by Bayes Classifier.
- Batch mode is observed to be faster than the pattern mode (online mode) even though the accuracies are same

3 Experiment No.3: MLFFNN Models

Multi Layer Feed Forward Neural Network Model is built to classify various types of data. Given data is split into Training, Validation and Test data-sets based on their index. Training function, Performance function, Transfer function are chosen appropriately.

3.1 Linearly Separable classes(Data-set 1(a))

Aim was to build MLFFNN Model Classifier for the given data-set of Linearly Separable classes. Data is bi-variate and the classification task was a three class problem. MLFFNN Classifier is built classify the given example and to find the Classification Accuracy, Confusion Matrix and Decision Region Plot.

3.1.1 Decision Region Plots

Below is the decision region plot for the Linearly Separable classes with the trained model.

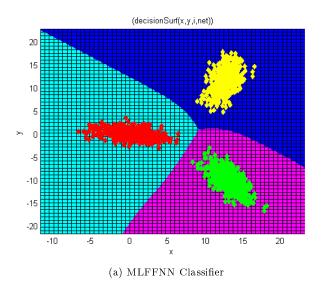


Figure 5: Decision Region Plots for Linearly Separable classes

3.1.2 Confusion Matrix and Average Classification Accuracy

Confusion Matrix for MLFFNN classifier on Linearly Separable Data

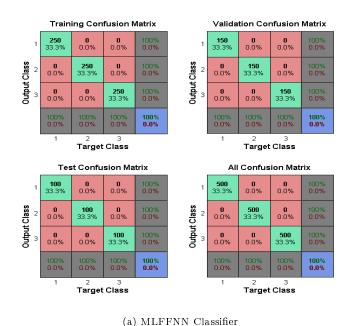


Figure 6: Confusion Matrices for Linearly Separable classes

Classification Accuracy

1 1 1

3.1.3 Average misclassification vs No of Hidden Nodes

Below is the plot of average misclassification with the number of nodes in the hidden layer.

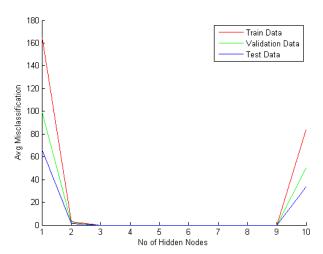


Figure 7: Average misclassification vs No. of Hidden Nodes

3.2 Non-linearly Separable classes(Data-set 1(b))

Aim was to build classifier for the given data-set of Non-linearly Separable Classes. Data is bi-variate and the classification task was a two class problem. Model is built to classify a given element to any of the three classes using MLFFNN Classifier and to find the Classification Accuracy, Confusion Matrix and Decision Region Plot. Minimum number of mixtures needed per class for best performance was 3.

3.2.1 Decision Region Plots

Below shown is the decision region plot for the MLFFNN Classifier.

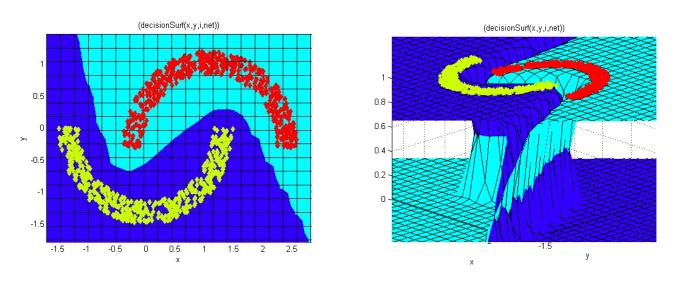


Figure 8: Decision Region Plot for Non- linearly Separable classes

3.2.2 Confusion Matrix and Average Classification Accuracy

Confusion Matrix for classifier



(a) MLFFNN Classifier

Figure 9: Confusion Matrices for Linearly Separable classes

Classification Accuracy

 $\mid 1 \mid 1$

Average Accuracy=1

3.2.3 Plots of outputs each of the hidden nodes and output nodes in MLFFNN after the model is trained

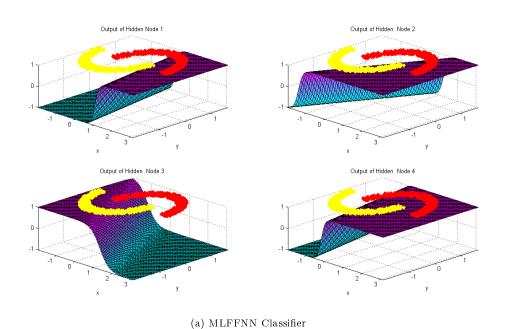


Figure 10: Output of individual nodes in Hidden Layer

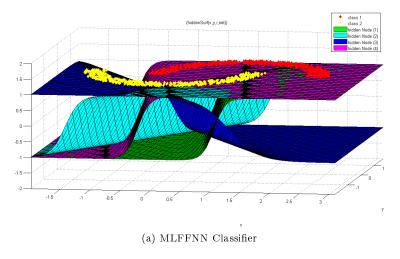


Figure 11: Output of Hidden Layer for Non-linearly Separable Classes

3.2.4 Average misclassification vs No of Hidden Nodes

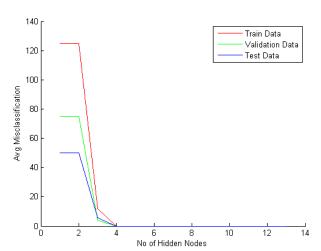


Figure 12: Average misclassification vs No. of Hidden Nodes

3.3 Overlapping classes (Data-set 1(c))

Aim was to build MLFFNN classifier for the given data-set of Overlapping Classes. Data is bi-variate and the classification task was a three class problem. Model is built to classify a given element to any of the three classes using the Classifier and to find the Classification Accuracy, Confusion Matrix and Decision Region Plot.

3.3.1 Decision Region Plots

Below shown is the decision region plot for the MLFFNN Classifier.

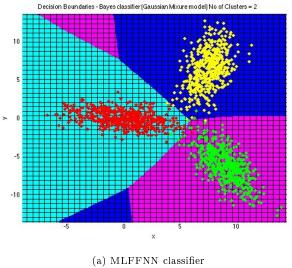


Figure 13: Decision Region Plot for Overlapping classes

3.3.2 Confusion Matrix and Average Classification Accuracy

Confusion Matrix for classifier



(a) MLFFNN Classifier

Figure 14: Confusion Matrices for Overlapping classes

Classification Accuracy

1 | 1 | 0.97

Average Accuracy=0.99

3.3.3 Average misclassification vs No of Hidden Nodes

Figure 15: Average misclassification vs No. of Hidden Nodes

3.4 Image Data(Data-set 2)

Aim was to build classifier for the given data-set of Classes. Data is multivariate with 48 dimensions and the classification task was a five class problem. Image data-set is splitted in ratio 70:10:20 for Train:Validation:Test . Model is built to classify a given element to any of the five classes using MLFFNN Classifier and to find the Classification Accuracy, Confusion Matrix.

3.4.1 Confusion Matrix and Average Classification Accuracy

Confusion Matrix for classifier

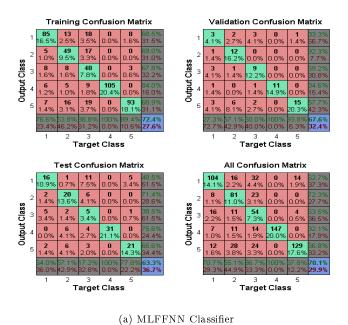


Figure 16: Confusion Matrices for Classifier- Image Data-set

Classification Accuracy

| 0.64 | 0.571 | 0.172 | 0.100 | 0.778 |
|------|-------|-------|-------|-------|
| 0.01 | 0.011 | 0.112 | 0.100 | 0.110 |

Average Accuracy=0.633

3.5 Observations

- For linearly Separable classes, decision surface is almost similar to what we got from Naive Bayes Classifier. Number of hidden nodes of the is 3 for classifier (MLFFNN) which gives 100% accuracy.
- Average miscals sification is decreasing w.r.to the number of hidden layers until a certain number of nodes and then increases.
- For Non-linearly Separable classes, MLFFNN with 4 hidden nodes gave 100% accuracy.
- Decision region is a weighted sum of hidden layer outputs. We can see from the hidden layer outputs plot that, how each node contribute to decision region.
- For overlapping classes, highest accuracy is obtained when number of hidden nodes is 4.
- For image data-set single hidden layer did not give good accuracy (~20%). But, two hidden layers with 100 and 30 nodes respectively gave highest accuracy (63%) which is same as that given by Bayes Classifier.

Part II

Regression Tasks

4 Data-sets

- 4.0.1 Data-set 1: 1-dimensional (Uni-variate) input data
- 4.0.2 Data-set 2: 2-dimensional (Bi-variate) input data
- 4.0.3 Data-set 3: Multivariate input data

Models

5 Experiment No.1: MLFFNN model

Multi Layer Feed Forward Neural Network Model is built to approximate various types of functions. Given data is split into Training, Validation and Test data-sets based on their index. Training function, Performance function, Transfer function are chosen appropriately.

5.1 Uni-variate Data (Data-set 1)

Aim was to build MLFFNN regression model for the given data-set. Data is uni-variate and the regression task was to approximate the underlying function for the test data-set using the trained model

5.1.1 Plots of model output and target output

Below are the plots of model output and target output for training data, validation data and test data using MLFFNN Model.

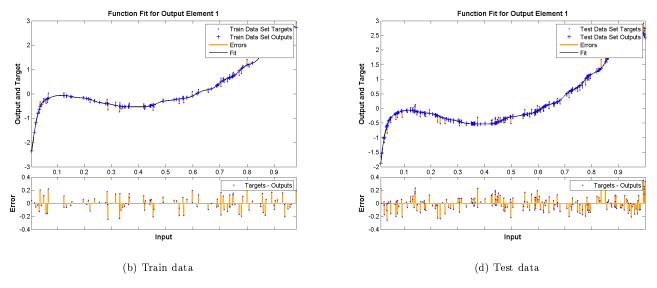


Figure 17: Realization of model output and target output

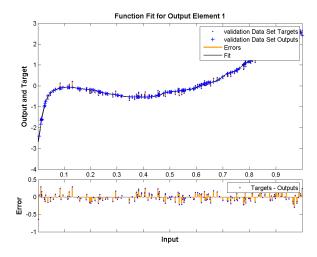


Figure 18: Validation data-Realization of model and target output

5.1.2 Scatter Plot of Target versus Model Output

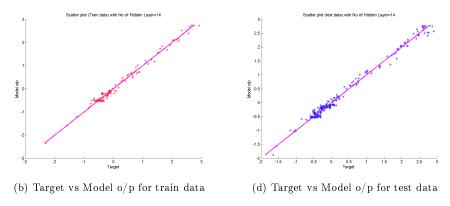


Figure 19: Scatter Plot of Target vs Model output

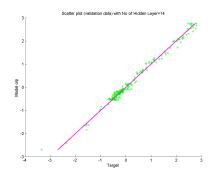
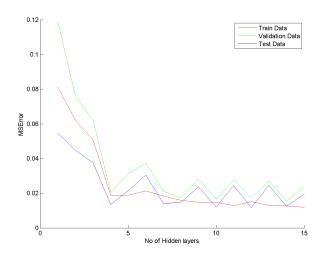


Figure 20: Scatter Plot of Target vs Model $\mathrm{o/p}$ for validation data

5.1.3 Plot of Number of Hidden Layers versus Mean Squared Error



(a) Number of Hidden Layers versus Mean Squared Error

Figure 21: MLFFNN Regression model for uni-variate data

5.1.4 Results

| No. of Hidden Nodes | 10 |
|------------------------|--------|
| MSE on Validation Data | 0.0165 |
| MSE on Test Data | 0.0119 |

5.2 Bi-variate Data (Data-set 2)

Aim was to build MLFFNN regression model for the given data-set. Data is bi-variate and the regression task was to approximate the underlying function for the test data-set using the trained model

5.2.1 Plots of model output and target output

Below are the plots of model output and target output for training data, validation data and test data using MLFFNN Model.

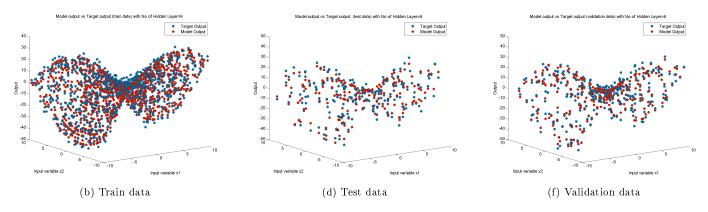


Figure 22: Realization model output and target output, N=1000

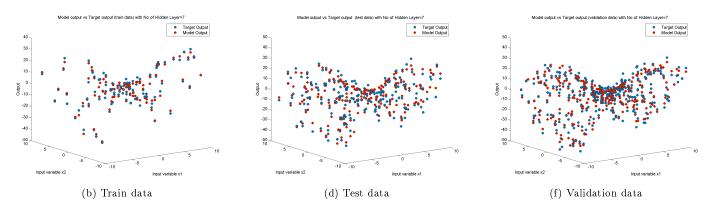


Figure 23: Realization model output and target output, N=100

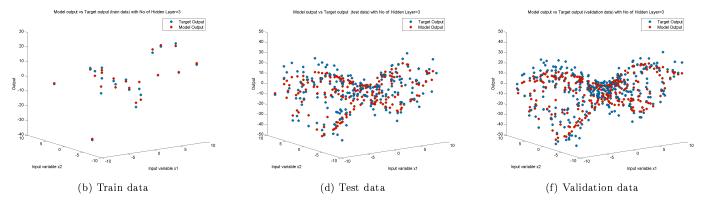


Figure 24: Realization model output and target output, N=20

5.2.2 Scatter Plot of Target versus Model Output.

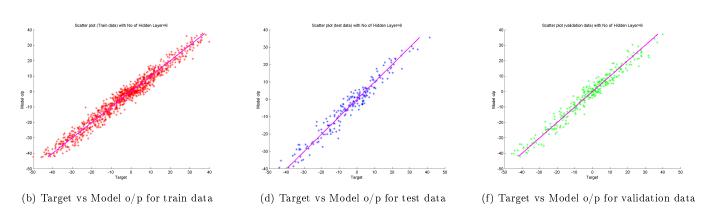


Figure 25: Target vs Model output, N=1000

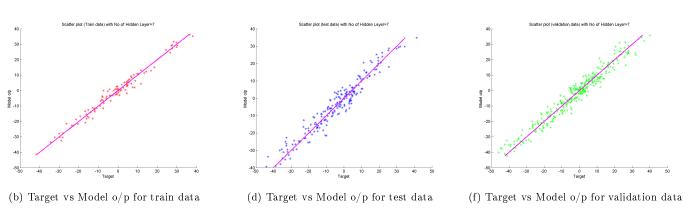


Figure 26: Target vs Model output, N=100

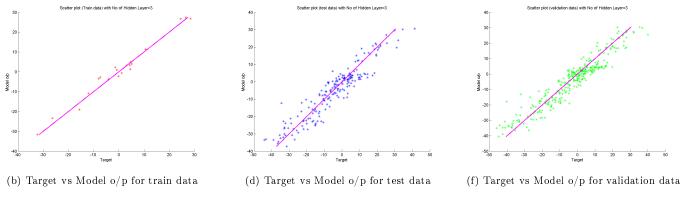


Figure 27: Target vs Model output

5.2.3 Plot of Number of Hidden Layers versus Mean Squared Error.

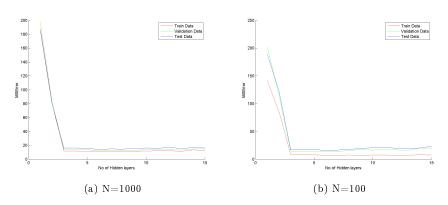
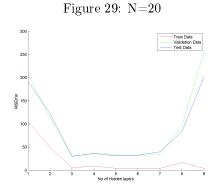


Figure 28: Number of Hidden Layers versus Mean Squared Error



5.2.4 Plots of outputs each of the hidden nodes in MLFFNN after different number of epochs during training.

Below are the plots of hidden layer outputs for different number of epochs. For this we considered Hidden nodes 1 and 4 outputs.

Figure 30: Outputs of Hidden Node (1)

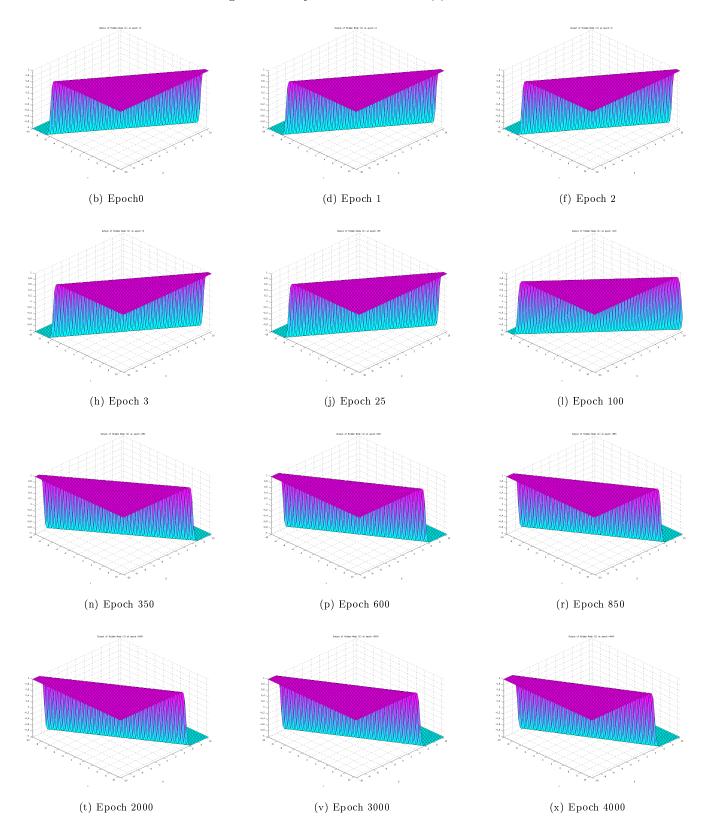
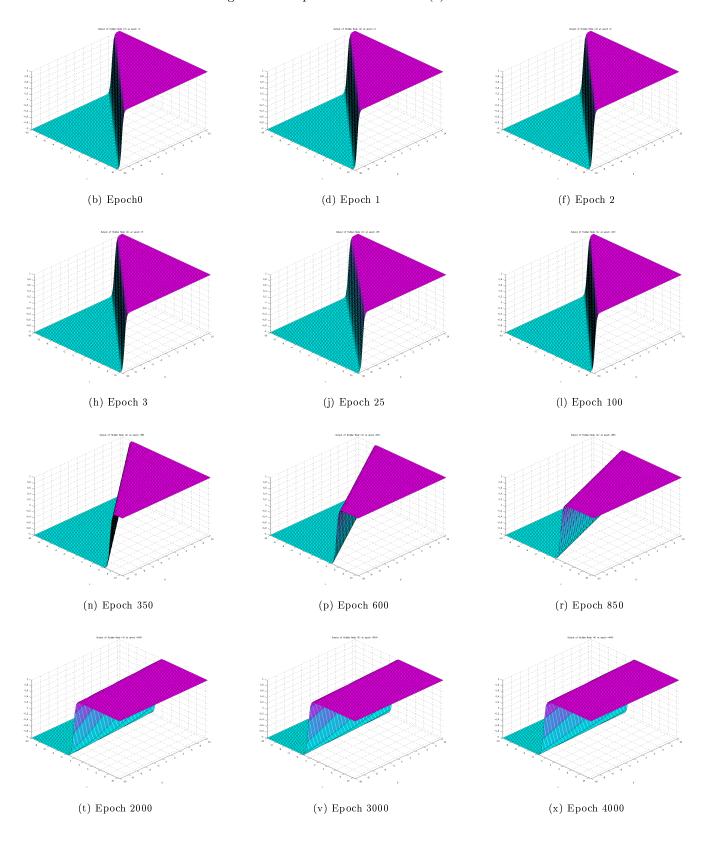


Figure 31: Outputs of Hidden Node (4)



5.2.5 Plots of outputs of the output nodes in MLFFNN after different number of epochs during training.

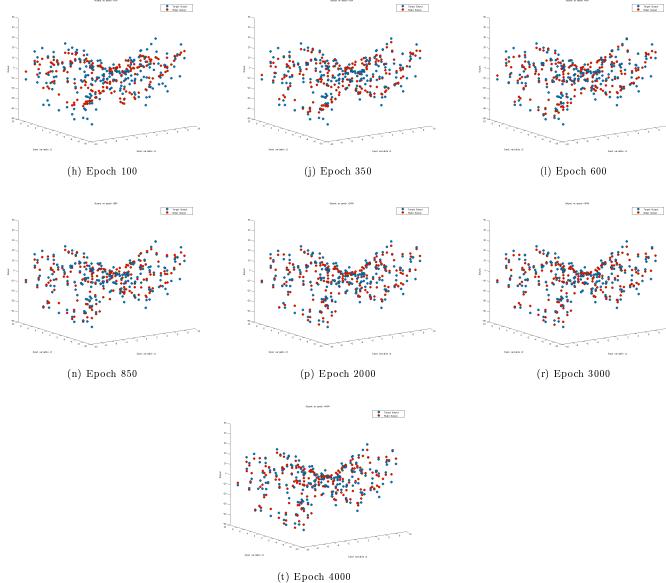
(b) Epoch0 (d) Epoch 2 (f) Epoch 25

Figure 32: Outputs of Output Layer

Target Dutput
Nodel Butest

Target Butput
 Rodel Distrut

Target Butput
Nodel Butput



5.2.6 Plots of Mean Squared Error versus Number of Epochs.

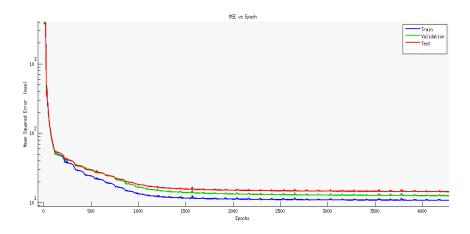


Figure 33: Mean Squared Error versus Number of Epochs.

5.2.7 Table showing weight change with epochs for a hidden layer.

| Epochs | | | Weig | $_{ m ghts}$ | | |
|--------|---------|---------|---------|--------------|---------|---------|
| 0 | 2.8044 | -3.4066 | -2.1670 | 2.2787 | 1.2365 | -2.2289 |
| 0 | -1.9737 | 0.3936 | 2.6578 | 2.5627 | -3.1986 | 2.6062 |
| 25 | 2.8817 | 3.4041 | -2.1120 | 2.2084 | 1.2412 | -2.2079 |
| 25 | -2.0407 | 0.3963 | 2.6635 | 2.6304 | -3.2110 | 2.6153 |
| 100 | 2.4499 | 3.4202 | -2.1097 | 2.2789 | 1.1886 | -1.9120 |
| 100 | -2.1671 | 0.0131 | 2.5813 | 2.4944 | -3.2437 | 2.5169 |
| 350 | 2.0055 | 3.0144 | -2.0077 | 2.2936 | 0.4445 | -2.1658 |
| 390 | -2.9059 | -0.4539 | 2.2872 | 1.8508 | -3.1856 | 2.4392 |
| 600 | 1.8382 | 2.6318 | -1.8042 | 2.2572 | 0.4026 | -2.2869 |
| 000 | -2.9779 | -0.4113 | 2.3297 | 1.3705 | -3.0470 | 2.3783 |
| 850 | 1.7862 | 2.3098 | -1.6038 | 2.2539 | 0.5530 | -2.3477 |
| 000 | -2.8663 | -0.2354 | 2.3937 | 0.8063 | -2.9250 | 2.3296 |
| 2000 | 1.6301 | 2.0357 | -1.3836 | 2.2555 | 0.8578 | -2.3491 |
| 2000 | -2.6738 | 0.0448 | 2.4059 | 0.1267 | -2.7609 | 2.2902 |
| 3000 | 1.5274 | 1.9581 | -1.2900 | 2.2097 | 0.9560 | -2.3071 |
| 3000 | -2.6309 | 0.0871 | 2.4142 | 0.0800 | -2.7035 | 2.2171 |
| 4000 | 1.4573 | 1.9023 | -1.2155 | 2.1569 | 1.0260 | -2.2450 |
| 4000 | -2.6122 | 0.1139 | 2.4177 | 0.0686 | -2.6583 | 2.1499 |
| 5000 | 1.4073 | 1.8575 | -1.1576 | 2.1037 | 1.0771 | -2.1771 |
| 3000 | -2.6041 | 0.1315 | 2.4124 | 0.0645 | -2.6250 | 2.1030 |
| 6000 | 1.3721 | 1.8191 | -1.1136 | 2.0535 | 1.1122 | -2.1127 |
| 0000 | -2.5996 | 0.1423 | 2.4000 | 0.0626 | -2.6011 | 2.0773 |
| 7000 | 1.3506 | 1.7893 | -1.0840 | 2.0136 | 1.1331 | -2.0620 |
| 7000 | -2.5962 | 0.1478 | 2.3856 | 0.0617 | -2.5860 | 2.0681 |
| 8000 | 1.3327 | 1.7570 | -1.0562 | 1.9709 | 1.1505 | -2.0080 |
| 8000 | -2.5915 | 0.1513 | 2.3660 | 0.0610 | -2.5729 | 2.0680 |
| 0000 | 1.3219 | 1.7310 | -1.0366 | 1.9374 | 1.1618 | -1.9655 |
| 9000 | -2.5866 | 0.1526 | 2.3475 | 0.0603 | -2.5645 | 2.0743 |
| 10000 | 1.3144 | 1.7070 | -1.0204 | 1.9076 | 1.1711 | -1.9271 |
| 10000 | -2.5813 | 0.1526 | 2.3286 | 0.0595 | -2.5581 | 2.0843 |

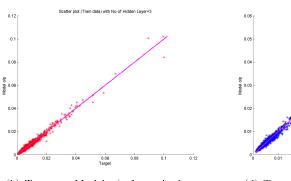
5.2.8 Results

| No. of Hidden Nodes | 6 |
|------------------------|-----------------|
| MSE on Validation Data | $1.23844e{+01}$ |
| MSE on Test Data | 1.4142e+01 |

5.3 Multivariate Data (Data-set 3)

Aim was to build MLFFNN regression model for the given data-set. Data is multivariate with 18 dimensions and the regression task was to approximate the underlying function for the test data-set using the trained model

5.3.1 Scatter Plot of Target versus Model Output



Scatter plot (test data) with No of Hidden Layer-3

0.05

0.04

0.02

0.01

0.02

0.01

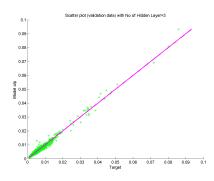
Terget

0.4

0.05

0.06

0.00



- (b) Target vs Model o/p for train data
- (d) Target vs Model o/p for test data
- (f) Target vs Model o/p for validation data

Figure 34: Target vs Model output, N=1000

5.3.2 Results

| No. of Hidden Nodes | 4 |
|------------------------|------------|
| MSE on Validation Data | 6.3983e-07 |
| MSE on Test Data | 6.7703e-07 |

5.4 Observations

- Mean Squared Error first decreases w.r.to increase in number of hidden nodes, then increases. (we can see this clearly for N=20, bi-variate case)
- Weights of hidden layer changes very slowly during higher epochs compared to that of lower epochs.
- The model output tries to match with the target faster at lower epochs and fine tunes it at higher epochs.
- For the multivariate data, the approximation seems to be better as compared with other regression methods.
- Best possible value of number of nodes in hidden layer are 10 for uni-variate data, 6 for Bi-variate data and 4 for Multivariate data.

6 Experiment No.2: Generalized RBF model

Multi Layer Feed Forward Neural Network Model is built to classify various types of data. Given data is split into Training, Validation and Test data-sets based on their index. Training function, Performance function, Transfer function are chosen appropriately.

6.1 Uni-variate Data (Data-set 1)

Aim was to build Generalized RBF Model for the given data-set. Data is uni-variate and the regression task was to approximate the underlying function for the test data-set using the trained model.

6.1.1 Plots of MSE Error on Training data, Validation data and Test data.

Following are the plots of Mean Squared Error for (a) different model complexities and for (b) different regularization parameter values.

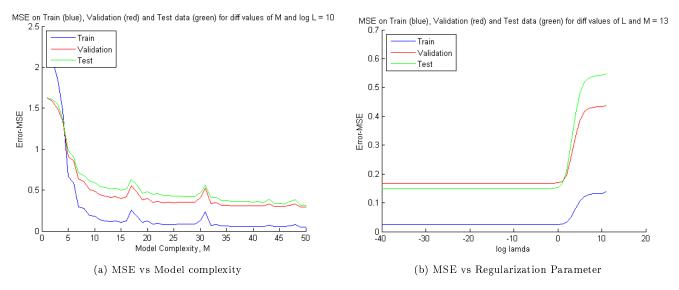


Figure 35: Generalized RBF Model

6.1.2 Plots of model output and target output

Below are the plots of model output and target output for training data, validation data and test data using Generalized RBF Model.

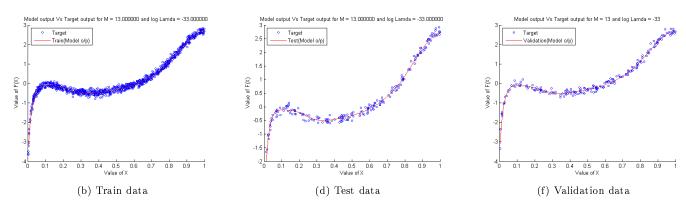
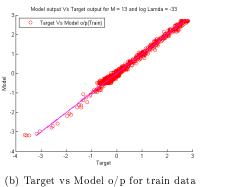
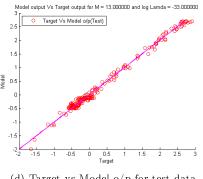
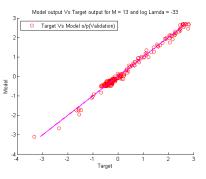


Figure 36: Realization model output and target output

Scatter Plot of Target versus Model Output







(d) Target vs Model o/p for test data

(f) Target vs Model o/p for validation data

Figure 37: Target vs Model output

6.2Bi-variate Data (Data-set 2)

Aim was to build Generalized RBF Model for the given data-set. Data is bi-variate and the regression task was to approximate the underlying function for the test data-set using the trained model.

6.2.1Results

| Error on Validation Data | $4.517522\mathrm{e}{+03}$ |
|------------------------------------|---------------------------|
| Least MSE | $1.505841\mathrm{e}{+01}$ |
| M | 40 |
| $\log(\mathrm{lambda})$ | -4 |
| lambda | 2.478752e-03 |
| Error on Test Data with best model | $3.438185\mathrm{e}{+03}$ |
| Least MSE | 1.719092e+01 |

Plots of MSE Error on Training data, Validation data and Test data.

Following are the plots of Mean Squared Error for (a) different model complexities and for (b) different regularization parameter values.

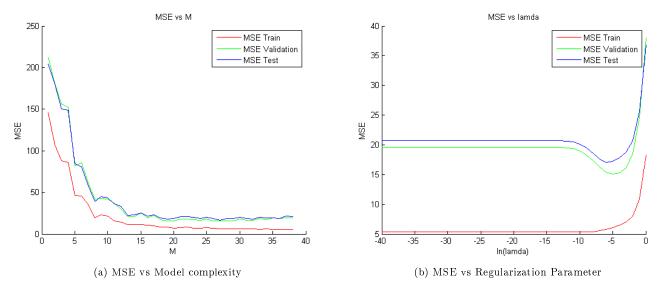


Figure 38: Generalized RBF Model

6.2.3 Plots of model output and target output

Below are the plots of model output and target output for training data, validation data and test data using Generalized RBF Model.

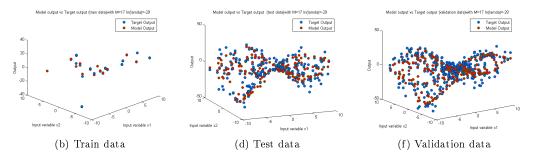


Figure 39: Realization of model output and target output, N=20

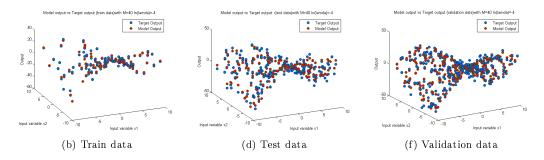


Figure 40: Realization of model output and target output, N=100

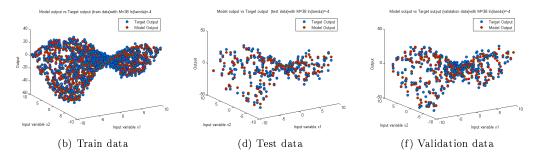


Figure 41: Realization of model output and target output, N=1000 $\,$

6.2.4 Scatter Plot of Target versus Model Output

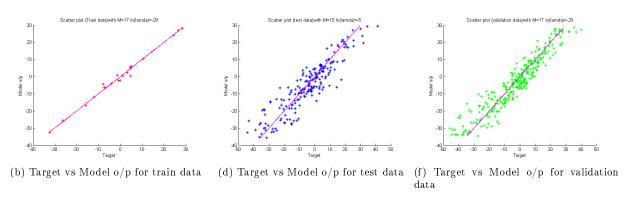


Figure 42: Target vs Model output, N=20

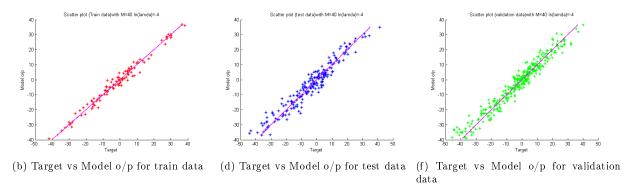


Figure 43: Target vs Model output, N=100

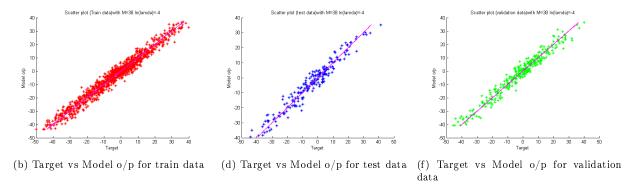


Figure 44: Target vs Model output, N=1000

6.3 Multivariate Data (Data-set 3)

Aim was to build Generalized RBF Model for the given data-set. Data is multivariate with input vector of dimension 18 and the regression task was to approximate the underlying function for the test data-set using the trained model.

6.3.1 Results

| Error on Validation Data | 5.226922e-02 |
|------------------------------------|-----------------|
| Least MSE | 5.903062e- 03 |
| M | 36 |
| $\log(\mathrm{lambda})$ | -32 |
| lambda | 1.713908e-15 |
| Error on Test Data with best model | 3.587622e- 02 |
| Least MSE | 5.108013e-03 |

6.3.2 Plots of MSE Error on Training data, Validation data and Test data.

Following are the plots of Mean Squared Error for (a) different model complexities and for (b) different regularization parameter values.

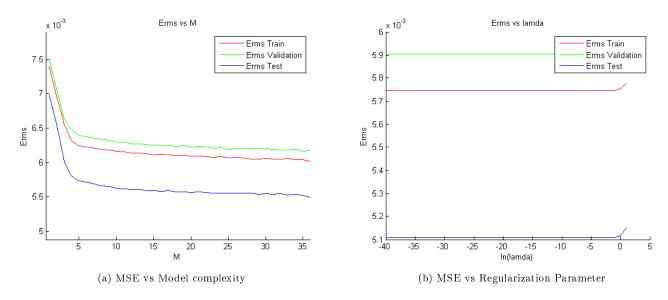


Figure 45: Generalized RBF Model

6.3.3 Scatter Plot of Target versus Model Output

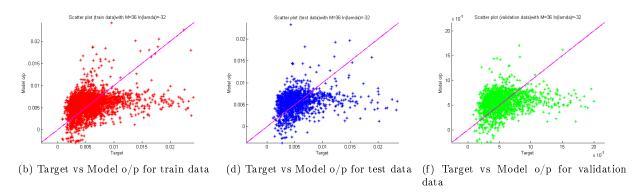


Figure 46: Target vs Model output

6.4 Observations

- MSE is lesser as compared to linear regression models with Gaussian basis function for all the given data-sets.
- Best possible values of Model Complexity are 13 for uni-variate data, 40 for Bi-variate data and 36 for Multivariate data.