

CSE460/560 DATA MODELS AND QUERY LANGUAGES

Relational Algebra - 1

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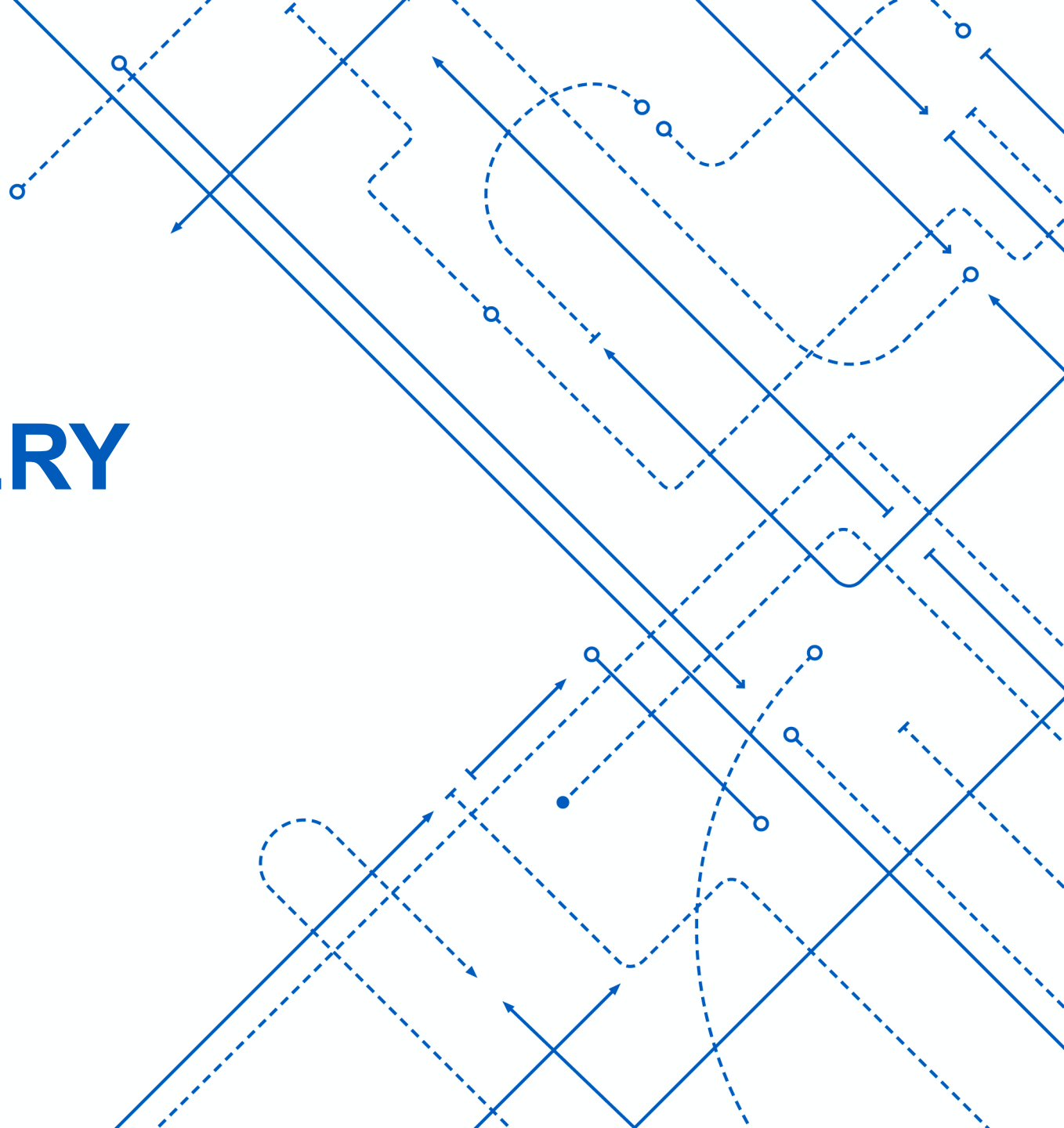
(Slides Adopted from Jan Chomicki and Ning Deng)



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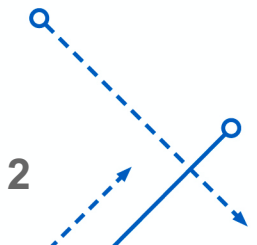
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School of Engineering and Applied Sciences



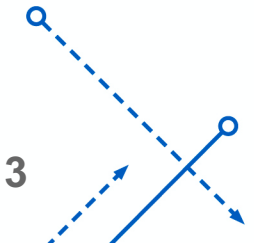
Outline

1. Imperative Languages and Declarative Languages
2. Overview of Relational Query Languages
3. Introduction to Relational Algebra
4. Minimal Set of Relational Algebra Operators



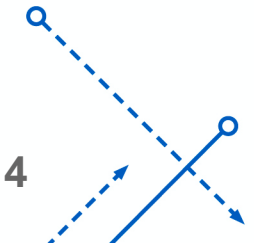
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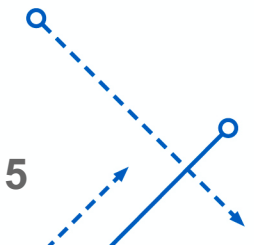
Imperative Languages and Declarative Languages

- Declarative Language: say WHAT you want
 - Give me a red pen
- Imperative Languages: say HOW you do it
 - Check every pen in the drawer
 - If the pen is red then give it to me and stop looking up



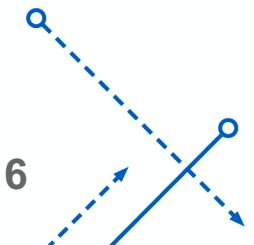
Why declarative language?

- Make it easier to explore **equivalent** computations to find the best one
 - Replace [thing] with better, but equivalent [thing]
 - How can we tell if one [thing] is equivalent?
 - How can we tell if one [thing] is better than the other?
- Example
 - Give me all red pens
 - Check every pen in the drawer, if the pen is red, then give it to me
 - Order the pens by color, then give me all pens in the red color bucket
 - $O(n)$ vs. $O(n \log n)$



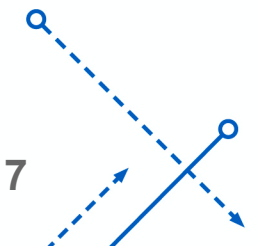
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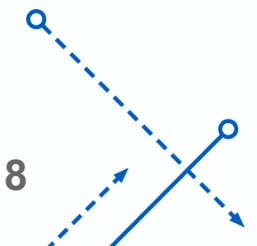
Relational Algebra and Relational Calculus

- Relational Algebra
 - A set of algebraic operators
 - Each operator take one or two **relations** as arguments
 - Returns a **relation** as the result
 - Operators can be nested to form expressions
 - Procedural query language
 - Expressions describe how the query can be evaluated
- Relational Calculus
 - A logic language: expressions include Boolean operators and quantifiers
 - Declarative query language
 - expressions do not describe how to evaluate the query $\{ t \mid \text{emp}(t) \wedge t.\text{salary} > 5000 \}$
 - We will not talk about it



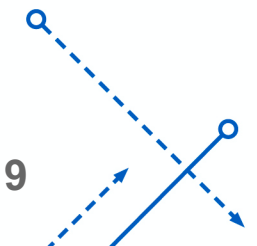
SQL

- RA and RC form the basis for relational query languages
 - SQL
 - A mix of relational algebra and relational calculus (logic)
 - The standard query language of the existing DBMS
- Preliminaries
 - Queries are applied to Relations
 - A query works on fixed relation schemas
 - But runs on any relation instance
 - The result of a query is also a **relation**!



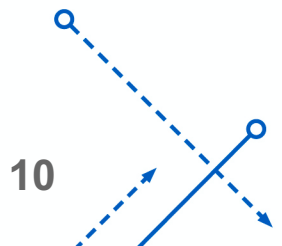
Subtle Issues

- Nulls
 - RA does NOT allow nulls
 - SQL does
- Duplicates
 - By default, RA operates on sets and does not allow duplicates
 - SQL allow duplicates and operates on bags
 - Duplicates irrelevant for most queries
- Order
 - Neither RA nor SQL can specify order within sets of tuples
 - In SQL top-level query results can be ordered (but not in sub-queries)



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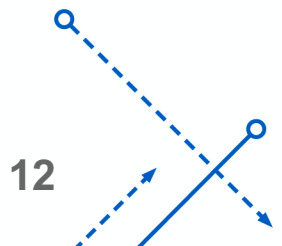
What is an “algebra”

- A mathematical system consisting of
 - Operands: variables or values from which new values can be constructed
 - Operators: symbol denoting procedures that construct new values from given values
- Relational Algebra
 - An algebra that can be used as a query languages for relations
 - The operands are relations or variable that represent relations
 - The operators are designed to do the most common things that we need to do with the relations in a database



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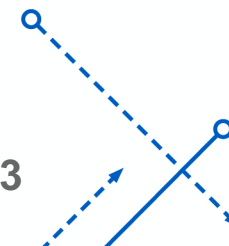
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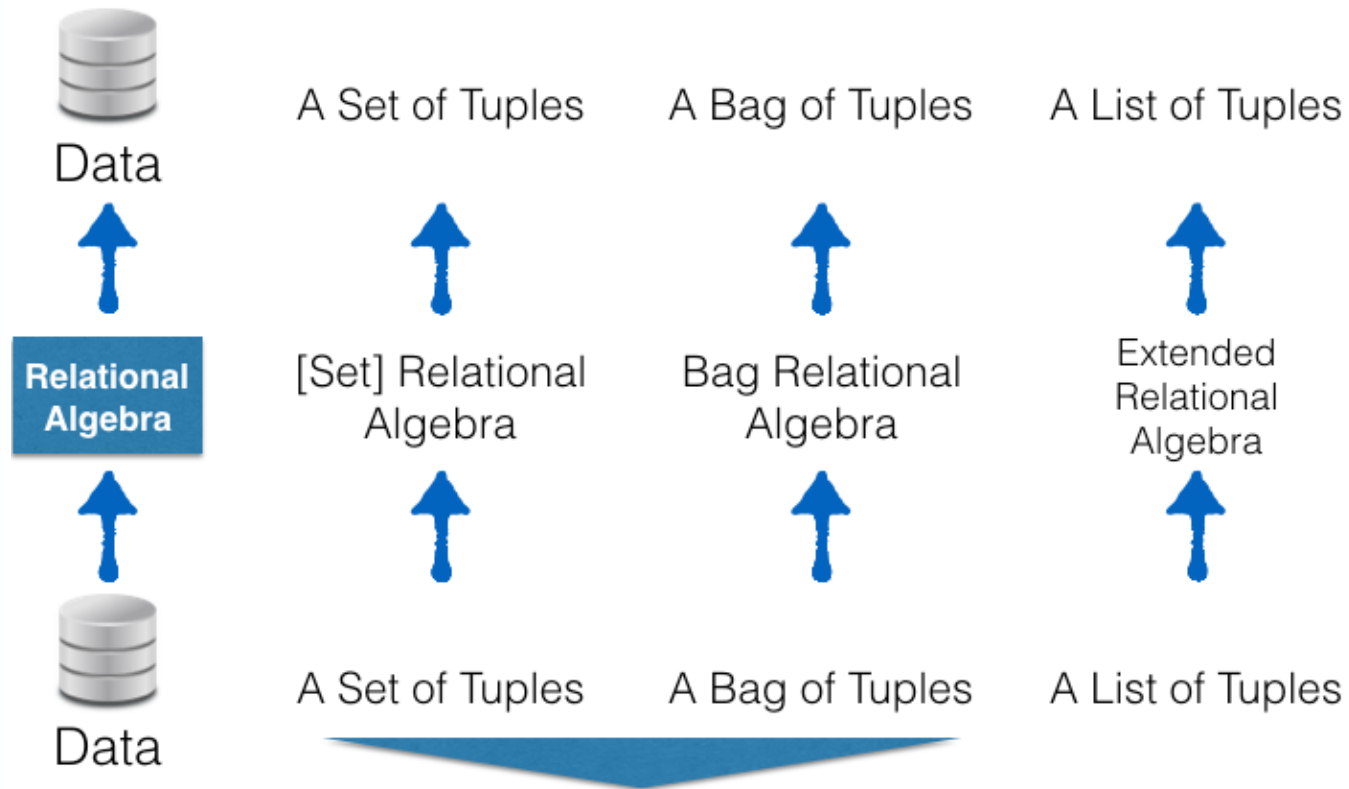
Relational Algebra Operators

Operation	Symbol	Meaning
Selection	σ	Selection a subset of the input tuples in a given relation
Projection	π	Pick wanted attributes (Delete unwanted attributes)
Cross-Product	\times	Combine two relations
Renaming	ρ	Rename attribute names
Set-difference	$-$	Tuples in R1 but not in R2
Union	\cup	Tuples either in R1 or in R2

- Also: Intersection \cap , **Join** \bowtie , Division $/$
 - Not essential, but very useful
- Each operation returns a relation
- Operations are composable (RA operators are **closed**)



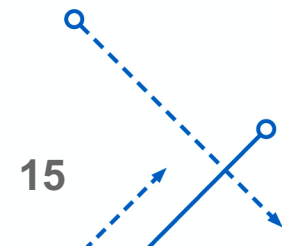
Relational Algebra



[Graph: Dr. Oliver Kennedy CSE 562]

Sets vs. Bags

- Rule of thumb
 - Papers: assume set semantics, i.e. Set RA
 - Implementation: assume bag semantics, i.e. Bag RA



Recommended Reading

Database Systems: The Complete Book
Chapter 2.4, 5.2