

Determine whether the ordered pairs (3, 5) and (1, -7) are solutions to the inequality  $5x - 3y \geq 25$ .

Let's try the first ordered pair (3, 5):

$$\begin{aligned} 5 \cdot 3 - 3 \cdot 5 &\geq 25 ? \\ 15 - 15 &\geq 25 ? \\ 0 &\geq 25 \end{aligned}$$

... this is not true; 0 is not greater than or equal to 25.

Let's try the other ordered pair (1, -7):

$$\begin{aligned} 5 \cdot 1 - 3(-7) &\geq 25 \\ 5 - -21 &\geq 25 \\ 5 + 21 &\geq 25 \\ 26 &\geq 25 \end{aligned}$$

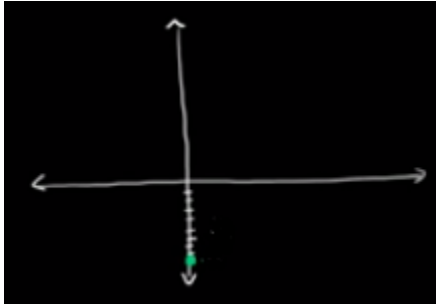
... this is true; 26 is greater than or equal to 25.

Let's graph the inequality:

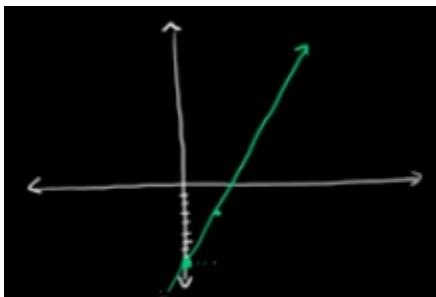
$$\begin{aligned} 5x - 3y &\geq 25 \\ -3y &\geq -5x + 25 \\ \boxed{y &\leq \frac{5}{3}x - \frac{25}{3}} \end{aligned}$$

... notice that when we divide both sides of an inequality by a negative number (in this case, negative 3), we also invert the greater than or equal to sign to face the other side.

The y intercept is  $-25/3$ , which is the same as negative 8 and  $1/3$ :

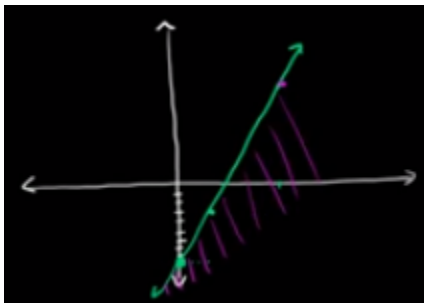


The slope is  $5/3$ . This means that for every 3 units to the right, it moves upward of 5 units.



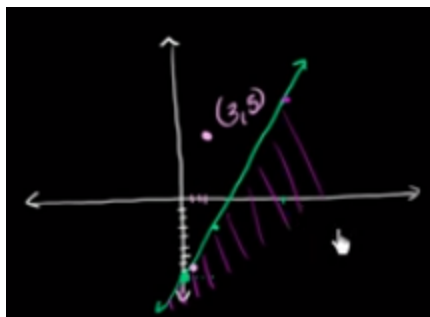
... this graph is if y was **equal** to  $5/3x$  minus  $25/3$ . The solution is any y value directly on the line. These y values satisfy the inequality.

If the graph is y is **less than**  $5/3x$  minus  $25/3$ :



... the solution is on the line, as well as the shaded purple area. These are the y values that satisfy the inequality.

When we plot the original ordered pairs:



... we see that  $(3, 5)$  is outside the solution area, whereas  $(1, -7)$  is within the solution area.