

Let's say we start out with an unsorted list, and after 3 steps we sort it out:

In each step of Radix Sort, there is a Counting Sort using each digit as the key:

53	89	150	36	633	233
150	53	633	233	36	89
633	233	36	150	53	89
36	53	89	150	233	633

... to explain the variables:

**n** = 6 (ie, the number of elements in the list).

**d** = 3 (ie, the digits of numbers in our list).

**b** = 10 (ie, the base of 10 comprises of numbers 0 through 9).

Remember: the time complexity of a Counting Sort is  $O(n+k)$

### Complexity of Radix Sort

$n = 6$        $d = 3$        $b = 10$

53	89	150	36	633	233
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150	53	633	233	36	89
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633	233	36	150	53	89
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36	53	89	150	233	633
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**k** is the range of keys for each number (ie, 0 through 9)... so **k** is the same as **b**...

...thus, each step takes  $O(n+b)$ , and in this case it was repeated 3 times (or **d** times).

... so to sum it all up, the time complexity for the algorithm of the Radix Sort will be:  $O(d(n+b))$

Depending on the nature of input, a Radix Sort can outperform a Quick Sort or Merge Sort  $O(n \log n)$ .

# Complexity of Radix Sort

$n = 6$        $d = 3$        $b = 10$

	53	89	150	36	633	233
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150	53	633	233	36	89
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➡

633	233	36	150	53	89
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36	53	89	150	233	633
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... for simplicity purpose, we choose base of 10 with digit of 3.

If  $b$  was larger than 10, like say, 1,000, it would imply a smaller  $d$ , meaning smaller digits, so we would need less sorting steps, so  $d$  would be comparatively smaller.

Likewise, if  $b$  was smaller, it would imply a larger  $d$ , meaning larger digits, so we may need more sorting steps, so  $d$  would be comparatively larger than...

...what does this all mean to us?... it means there is a trade-off between space and time.

...basically, if  $b$  is larger, it occupies more space, but it would save us time since less steps are required.... and likewise, if  $b$  was smaller and occupied less space, this would require more time for the extra steps.