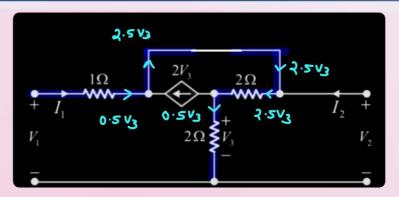


Chapter 5
2 Port Network
Lecture 3





$$\frac{\sqrt{1}}{\pm 1} = \frac{6.5 \, \text{V}_3}{0.5 \, \text{V}_3} = \frac{13}{2} \sim$$

The ABCD parameters of the following 2-port network are [GATE EC 2015 (Set 03), IIT Kanpur]

$$(5+j4)\Omega$$
 $(5-j4)\Omega$

$$(5+j4)\Omega$$
 $(5-j4)\Omega$
 $(5-j4)\Omega$
 $(5-j4)\Omega$
 $(5-j4)\Omega$
 $(5-j4)\Omega$
 $(5-j4)\Omega$
 $(5-j4)\Omega$
 $(5-j4)\Omega$

$$\begin{bmatrix}
3.5 + j2 & 30.5 \\
0.5 & 3.5 - j2
\end{bmatrix}$$

$$\begin{bmatrix}
10 & 2 + j0
\end{bmatrix}$$

$$3.5^{2} + 2^{2} - 1$$

$$\begin{bmatrix} 2+j0 & 10 \\ 7+j4 & 0.5 \end{bmatrix}$$
 | 2.25+4-15

$$V_2 = 2I_1 + (7-j4)I_2$$

$$\begin{bmatrix} V_1 \\ \mathbf{I}_1 \end{bmatrix} = \begin{bmatrix} A & \mathbf{B} \\ C & \mathbf{D} \end{bmatrix} \begin{bmatrix} V_2 \\ -\mathbf{I}_2 \end{bmatrix}$$

$$V_1 = A V_2 - B L_2$$

$$\beta = \frac{V_1}{-I_2} \Big|_{V_2 = 0}$$

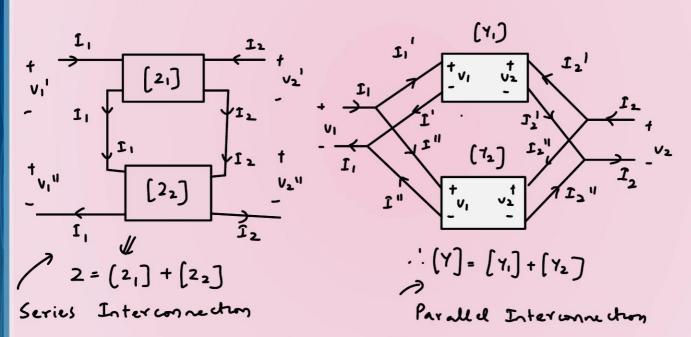
$$V_1 = \frac{(7+j4)(7-j4)}{-2}I_2 + 2I_2$$

$$B = \frac{V_1}{-12} = 30.5$$

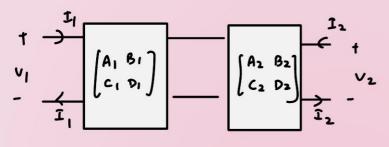
Interconnection of 2 port Networks

- Rules
- 1) Series -> 2 parameters are added
- @ Parallel Y parameters are added
- 3 cascade ABCD paremeters are multiplied.





Cascade Interconnection

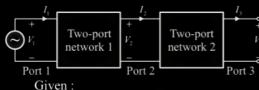


$$\begin{bmatrix}
A & B \\
C & D
\end{bmatrix} =
\begin{bmatrix}
A_1 & B_1 \\
C_1 & D_1
\end{bmatrix}
\begin{bmatrix}
A_2 & B_2 \\
C_2 & D_2
\end{bmatrix}$$



Two passive two-port networks are connected in cascade as shown in figure. A voltage source is connected at port 1.

[GATE EE 2017 (Set - 01), IIT Roorkee]



$$V_1 = A_1 V_2 + B_1 I_2 \qquad I_1 = C_1 V_2 + D_1 I_2$$

$$V_2 = A_2 V_3 + B_2 I_3 \qquad I_2 = C_2 V_3 + D_2 I_3$$

 A_1 , B_1 , C_1 , D_1 , A_2 , B_2 , C_2 and D_2 are the generalized circuit constants. If the Thevenin equivalent circuit at port 3 consists of a voltage source V_T and an impedance Z_T connected in series, then

$$V_T = V_3 \mid_{I_3 = 0}$$

$$R_{\text{M}} = \frac{v_3}{-1_3} \Big|_{v_1 = 0}$$

(A)
$$V_T = \frac{V_1}{A_1 A_2}$$
, $Z_T = \frac{A_1 B_2 + B_1 D_2}{A_1 A_2 + B_1 C_2}$

(B)
$$V_T = \frac{V_1}{A_1 A_2 + B_1 C_2}, \ Z_T = \frac{A_1 B_2 + B_1 D_2}{A_1 A_2}$$

(C)
$$V_T = \frac{V_1}{A_1 + A_2}, \ Z_T = \frac{A_1 B_2 + B_1 D_2}{A_1 + A_2}$$

(D)
$$V_T = \frac{V_1}{A_1 A_2 + B_1 C_2}, \ Z_T = \frac{A_1 B_2 + B_1 D_2}{A_1 A_2 + B_1 C_2}$$

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$$\begin{bmatrix} v_1 \\ I_1 \end{bmatrix} = \begin{bmatrix} A_1 & B_1 \\ c_1 & D_1 \end{bmatrix} \begin{bmatrix} A_2 & B_2 \\ c_2 & D_2 \end{bmatrix} \begin{bmatrix} v_3 \\ I_3 \end{bmatrix}$$

$$\begin{bmatrix} A & B \\ C & P \end{bmatrix} = \begin{bmatrix} A_1 & A_2 + B_1 & C_2 \end{bmatrix}$$

$$V_1 = AV_3 + BI_3 = 0$$

$$U_1 = C V_3 + DI_3 = 0$$

$$V_3 = \frac{V_1}{A}$$
 or $V_3 = \frac{C}{I_3}$

$$V_{3} = \frac{V_{1}}{A_{1}A_{2} + B_{1}C_{2}} = V_{T}$$

←□ → ←□ → ←□ → ←□ →

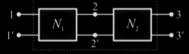
From
$$O$$
 when $V_1 = 0$
 $AV_3 = -BI_3$

$$\frac{V_3}{-I_3} = R_M = \frac{B}{A} = \frac{A_1 B_2 + B_1 D_2}{A_1 A_2 + B_1 C_2}$$

The connection of two 2-port networks is shown in the figure. The ABCD parameters of N_1 and N_2 networks are given as

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix}_{N_1} = \begin{bmatrix} 1 & 5 \\ 0 & 1 \end{bmatrix}$$
and

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix}_{N_2} = \begin{bmatrix} 1 & 0 \\ 0.2 & 1 \end{bmatrix}$$

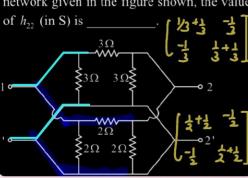


The ABCD parameters of the combined 2-port network are

$$\begin{array}{ccc}
(A) \begin{bmatrix} 2 & 5 \\ 0.2 & 1 \end{bmatrix} & (B) \begin{bmatrix} 1 & 2 \\ 0.5 & 1 \end{bmatrix} \\
\begin{bmatrix} 5 & 2 \end{bmatrix} & \begin{bmatrix} 1 & 2 \end{bmatrix}$$

$$\begin{bmatrix} A & B \\ c & D \end{bmatrix} = \begin{bmatrix} 1 & 5 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 \cdot 2 & 1 \end{bmatrix}$$
$$= \begin{bmatrix} 2 & 5 \\ 0 \cdot 2 & 1 \end{bmatrix} \quad (A)$$





$$\begin{bmatrix} Y \end{bmatrix} = \begin{bmatrix} 5/3 & -5/6 \\ -5/6 & 5/3 \end{bmatrix}$$

$$I_1 = 5/3 V_1 - 5/6 V_2 \quad 0$$

$$I_2 = -5/6 V_1 + 5/3 V_2 \quad 0$$

$$\frac{5}{6} V_2 = 5/6 V_1 + 5/3 V_2 \quad 0$$
Subs in 2

In the h-parameter model of the 2-port network given in the figure shown, the value of
$$h_{22}$$
 (in S) is
$$\begin{array}{c} 3\Omega \\ 3\Omega \\ \end{array}$$

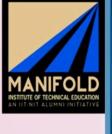
$$y = \begin{bmatrix} \frac{2}{3} + 1 & -\frac{5}{6} \\ -\frac{5}{6} & \frac{2}{3} + 1 \end{bmatrix}$$

$$\begin{bmatrix} V_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} \\ h_{21} & h_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ V_2 \end{bmatrix}$$

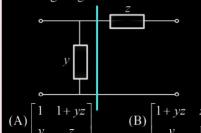
$$I_2 = h_{21} I_1 + h_{22} V_2$$

$$\therefore h_{22} = \frac{I_2}{V_2} \Big|_{I_1=0}$$

$$I_1 = -\frac{5}{6} \left(\frac{1}{4} V_2 \right) + \frac{5}{3} V_2 = -\frac{5}{12} V_2 + \frac{20}{12} V_2 = \frac{15}{12} V_2$$



Which one of the following is the transmission matrix for the network shown in the figure given below?



$$\begin{bmatrix}
A & B \\
C & P
\end{bmatrix} = \begin{bmatrix}
I & O \\
Y & I
\end{bmatrix} \begin{bmatrix}
I & 2 \\
O & I
\end{bmatrix}$$

$$= \begin{bmatrix}
I & 2 \\
Y & 1+Y2
\end{bmatrix}$$



$$\uparrow \qquad \qquad \downarrow^{2} \qquad \qquad \downarrow^{1_{2}} \qquad \downarrow^{V_{1}} \qquad \downarrow^{V_{1}} \qquad \downarrow^{V_{2}} \qquad$$

$$\begin{array}{ll}
\mathbb{T}_1 = \mathbb{T}_2 & \mathbb{O} \\
V_1 - 2 \mathbb{T}_2 = V_2 \\
V_1 = V_2 + 2 \mathbb{T}_2 & \mathbb{Q}
\end{array}$$

$$\begin{bmatrix} V_1 \\ I_1 \end{bmatrix} = \begin{bmatrix} 30 & 23 \\ 13 & 10 \end{bmatrix} \begin{bmatrix} V_2 \\ -I_2 \end{bmatrix}$$

ABCD parameter of Network N_0 is

$$\begin{array}{c|cccc}
I_1 & 2\Omega & I_2 \\
V_1 & N_0 & 1\Omega & V_2 \\
\hline
\bullet & & & & & & \\
\hline
(A) \begin{bmatrix} 7 & -9 \\ 3 & -4 \end{bmatrix} & (B) \begin{bmatrix} 7 & 9 \\ 3 & 4 \end{bmatrix}
\end{array}$$

$$(C)\begin{bmatrix} -7 & 9 \\ 3 & -4 \end{bmatrix} \qquad (D)\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

$$\begin{bmatrix} 3 & 3 \\ 3 & 6 \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 23 \\ 10 \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} 3 & 2 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} \frac{3a+b}{2c+d} & \frac{2a+b}{2c+d} \\ \frac{3c+d}{2c+d} & \frac{2c+d}{2c+d} \end{bmatrix}$$

$$a = 30 - 23 = 7$$
 $b = 9$ $\begin{pmatrix} 7 & 9 \\ 3 & 4 \end{pmatrix}$ (B)

