$$Q \cdot I = \int_{0}^{\infty} \frac{\chi^{n-1}}{1+\chi} d\chi$$

Let,
$$x = \tan^2 \theta$$

 $\Rightarrow dx = 2 \tan \theta \sec^2 \theta d\theta$

×	0	oc
0	0	34/2

Now, $I = \int \frac{(\tan^{2} \theta)^{n-1}}{1 + \tan^{2} \theta} \quad 2 \tan \theta \sec^{2} \theta \, d\theta$ $= 2i \int \frac{\tan^{2n-2i} \theta}{\sec^{2} \theta} \cdot \tan \theta \cdot \sec^{2} \theta \, d\theta$ $= 2i \int \frac{\tan^{2n-2i} \theta}{\sec^{2} \theta} \cdot \tan \theta \cdot \sec^{2} \theta \, d\theta$ $= 2i \int \frac{\tan^{2n-2i} \theta}{\tan^{2n-2i} \theta} \cdot \tan \theta \, d\theta$ $= 2i \int \frac{\tan^{2n-1} \theta}{\cot^{2n} \theta} \, d\theta$ $= 2i \int \frac{\sin \theta}{\cot^{2n-1} \theta} \, d\theta$ $= 2i \int \frac{\sin \theta}{\cot^{2n-1} \theta} \, d\theta$ $= 2i \int \frac{\sin \theta}{\cot^{2n-1} \theta} \, d\theta$

$$= 2 \cdot \frac{1}{2} \frac{2n - 1 + 1}{2n - 1 + 1} \frac{1 - 2n + 1}{2n}$$

$$= \frac{2n}{2} \frac{2 - 2n}{2n}$$

$$= \frac{2n}{2} \frac{2n}{2n}$$

$$= \frac{2n}{2} \frac{2n}{2}$$

$$= \frac{2n}{2} \frac{2n}{2$$

$$= \frac{1}{2i} \frac{3t}{\sin^{3} 74}$$

$$= \frac{\sqrt{2}}{1} 3t$$

$$= \frac{1}{12} \times Answert.$$

Q.
$$0! = \sqrt{(0+1)} = \sqrt{1} = 1$$

We know,
$$n! = \lceil n+1 \rceil$$

 $50, 0! = \lceil 0+1 \rceil$
 $= \lceil 1 \rceil$
 $= 1 \qquad : \lceil \lceil 1 = 1 \rceil$

Answer.

$$G$$
 $[a-m] = \frac{3c}{\sin m 3c}$

Taking by Region O < Re(m) < 1 [By definition

of Analytic continuation Proporty7

$$\frac{\lceil m \rceil 1 - m}{\lceil m + (1 - m) \rceil} = \beta (m, 1 - m)$$

$$\frac{\lceil m \rceil n}{\lceil m + (1 - m) \rceil} = \beta (m, n)$$

$$\frac{1}{\sum_{i=1}^{n} \frac{(1-x_{i})}{\sum_{i=1}^{n} \frac{$$

$$= \int_{0}^{1} t^{m-1} (1-t)^{m} dt$$

$$= \int_{0}^{1} \frac{t^{m-1}}{(1-t)^{m}} dt$$

$$= \int_{0}^{1} \left\{ \frac{t}{1-t} \right\}_{0}^{m} dt$$

$$= \int_{0}^{1} \left\{ \frac{t}{1-t} \right\}_{0}^{m} dt$$

$$\Rightarrow dt = \left\{ \frac{1}{(1-t)^{2}} + \frac{t^{2}}{(1-t)^{2}} \right\}_{0}^{2} dt$$

$$\Rightarrow dt = \left\{ \frac{1}{(1-t)^{2}} dt \right\}_{0}^{m} dt$$

$$t = 0, t = 0$$

$$t = 1 \Rightarrow t = 0$$

$$\boxed{m} \boxed{1-m} = \int_{0}^{\infty} \frac{d^{m}(1-t)^{2} dy}{t} = \int_{0}^{\infty} d^{m} \left(1-\frac{t}{t+1}\right)^{2} dy \qquad \boxed{1}$$

$$\boxed{m} \boxed{1-m} = \int_{0}^{\infty} \frac{d^{m-1}}{1+t} dy \qquad \boxed{1}$$

Now, eq evalute integral

$$\int_{0}^{\infty} \frac{y^{m-1}}{1+y} dy \qquad \text{by Complex variable method.}$$

$$\int_{0}^{\infty} \frac{w^{m-1}}{1+w} dw$$

Pole of the given integral

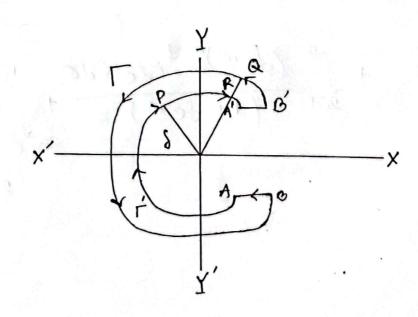
Men by Cauchy Residue theorem

$$\int_{C} \frac{\omega^{m-1}}{(1+w)} dw = 2\pi i \times \text{Residue at } w = -1$$

$$= 2\pi i \times \{\lim_{w \to -1} (w+1) f(w) \}$$

$$= 2\pi i \times \{\lim_{w \to -1} (w+1) \frac{w^{m-1}}{(1+w)}\}$$

We draw the figure then



let radius of corcle T and radius of corcle of T'ore R and nexpectively.

we show that,

$$lwl=f=ie^{i\theta}d\theta$$
 $dw=fie^{i\theta}d\theta$
 $lwl=R=ie^{i\theta}d\theta$
 $dw=Rie^{i\theta}d\theta$

from @ equation @
$$\frac{2^{37} (Re^{i0})^{m-1}}{1+Re^{i0}}$$
 Rie 0 d0 + $\int_{R}^{6} \frac{y^{m-1}e^{2\pi i(m-1)}e^{2\pi idy}}{(1+y)}$ + $\int_{2\pi}^{0} \frac{(Je^{i0})^{m-1}ide^{i0}d0}{(1+y)} + \int_{1+y}^{0} \frac{(Je^{i0})^{m-1}ide^{i0}d0}{(1+y)} + \int_{1+y}^{0} \frac{y^{m-1}dy}{(1+y)} = \frac{1}{1+y} dy = \frac{1$

25ci { e sci (m-2)

Let
$$d \rightarrow 0$$
 and $R \rightarrow \infty$ and also $0 < Re(m) < 1$
then,
$$0 + \int_{\infty}^{0} \frac{1}{(1+3)} e^{2\pi i m} dt + 0 + \int_{0}^{\infty} \frac{1}{1+3} dt = -2\pi i ? e^{\pi i m} ? e^{2\pi i m} ?$$

from equ. 1 and 3

Answer.

=
$$\int \sin^{9} 0 \cos^{9} 0 d0$$
 [: $\sin^{9} 0 = 1$]

$$= \frac{\boxed{0+1} \sqrt{9+1}}{\boxed{0+9+2}}$$

$$= \frac{12+1}{2} \sqrt{31}$$

$$= \frac{12+1}{2} \sqrt{31}$$

$$= \frac{12+1}{2} \sqrt{31}$$

Answer.

Evaluate
$$\int_{0}^{\pi/2} \sin^{2}\theta \, d\theta$$

$$= \int_{0}^{\pi/2} \sin^{2}\theta \, \cos^{2}\theta \, d\theta$$

$$= \frac{\frac{p+1}{2}}{2} \frac{\frac{0+1}{2}}{2}$$

$$= \frac{\frac{p+2}{2}}{2} \frac{\sqrt{37}}{2} \frac{\sqrt{29}}{2}$$
Answer:

$$I = \int_{0}^{\pi/2} \sin^{6}\theta \, dx$$

$$I = \int_{0}^{\pi/2} \sin^{6}\theta \, dx$$

$$= \frac{\frac{6+2}{2}}{2} \frac{\sqrt{77}}{2}$$

= \frac{7}{2} \sqrt{7}

= = = - 3.2.1.0

$$I = \int_{0}^{5/2} \frac{1}{2} \frac{1}$$

$$I = \int_{0}^{1} x^{4-1} (1-x)^{4-1} dx$$

Answer:

$$I = \int_{0}^{\pi/2} \sqrt{\cot \theta} \ d\theta$$
 (2)

Adding equation 5 (1) and (2), we get

$$2I = \int_{0}^{\pi/2} \left(\sqrt{\tan \theta} + \sqrt{\cot \theta} \right) d\theta$$

$$= -\sqrt{2} \int_{0}^{\pi/2} \frac{2 in 2\theta + \cos \theta}{\sqrt{2 in 2\theta}} dx$$

$$= -\sqrt{2} \int_{0}^{\pi/2} \frac{2 in 2\theta + \cos \theta}{\sqrt{1 - (2in 2\theta - \cos \theta)^{2}}} dx$$

$$= \sqrt{2} \int_{-1}^{1} \frac{dt}{\sqrt{1 - t^{2}}} \quad \text{(Where sin } \theta - \cos \theta = t)$$

$$= 2\sqrt{2} \int_{0}^{1} \frac{dt}{\sqrt{1 - t^{2}}}$$

$$= -\sqrt{2}\pi$$

or $I = \frac{\pi}{\sqrt{2}}$

Answer

Bralute, (1x6 J2-xt dx.

Solno We have,

Liet, sino = x

$$=\frac{\Gamma\left(\frac{6+1}{2}\right)\Gamma\left(\frac{2+1}{2}\right)}{2\Gamma\left(\frac{6+2+2}{2}\right)}$$

$$=\frac{\Gamma(7/2)\Gamma(\frac{2}{5})}{2\Gamma(5)}$$

$$=\frac{5\pi}{256}$$