Linköpings Universitet Institutionen för Datavetenskap Patrick Doherty

# Tentamen TDDC17 <sup>1</sup>Artificial Intelligence 16 august 2008 kl. 08-12

Points:

The exam consists of exercises worth 37 points.

To pass the exam you need 18 points.

Auxiliary help items:

Hand calculators.

Directions:

You can answer the questions in English or Swedish.

Use notations and methods that have been discussed in the course.

In particular, use the definitions, notations and methods in appendices 1-3. Make reasonable assumptions when an exercise has been under-specified.

Begin each exercise on a new page. Write only on one side of the paper.

Write clearly and concisely.

Jourhavande: Piotr Rudol, 0703167242. Piotr will arrive for questions around 10:00.

 $<sup>^{1}\</sup>mathrm{This}$  exam should also be used for those students who have previously taken TDDA13 or TDDA58.

1. Consider the following theory (where x, y and z are variables and history, lottery and john are constants):

$$\forall x ([Pass(x, \mathsf{history}) \land Win(x, \mathsf{lottery})] \Rightarrow Happy(x)) \tag{1}$$

$$\forall x \forall y ([Study(x) \lor Lucky(x)] \Rightarrow Pass(x,y)) \tag{2}$$

$$\neg Study(\mathsf{john}) \land Lucky(\mathsf{john})$$
 (3)

$$\forall x(Lucky(x) \Rightarrow Win(x, \mathsf{lottery}))$$
 (4)

- (a) Convert formulas (1) (4) into clause form. [1p]
- (b) Prove that  $Happy(\mathsf{john})$  is a logical consequence of (1) (4) using the resolution proof procedure. [2p]
  - Your answer should be structured using a resolution refutation tree (as used in the book).
  - Since the unifications are trivial, it suffices to simply show the binding lists at each resolution step.
- 2. Constraint satisfaction problems consist of a set of variables, a value domain for each variable and a set of constraints. A solution to a CS problem is a consistent set of bindings to the variables that satisfy the contraints. A standard backtracking search algorithm can be used to find solutions to CS problems. In the simplest case, the algorithm would choose variables to bind and values in the variable's domain to be bound to a variable in an arbitrary manner as the search tree is generated. This is inefficient and there are a number of strategies which can improve the search. Describe the following three strategies:
  - (a) Minimum remaining value heuristic (MRV). [1p]
  - (b) Degree heuristic. [1p]
  - (c) Least constraining value heuristic. [1p]

Constraint propagation is the general term for propagating constraints on one variable onto other variables. Describe the following:

- (d) What is the Forward Checking technique? [1p]
- (e) What is arc consistency? [1p]
- 3. Consider the following example:

The fire alarm in a building can go off if there is a fire in the building or if the alarm is tampered with by vandels. If the fire alarm goes off, this can cause crowds to gather at the front of the building and fire trucks to arrive.

- (a) Represent these causal links in a Bayesian network. Let a stand for "alarm sounds", c for "crowd gathers", f for "fire exists", t for truck arrives", and v for "vandalism exists". [2p]
- (b) Given the independence assumptions implicit in the Bayesian network, what are the conditional (or prior) probabilities that need to be specified to fully determine the joint probability distribution? In other words, what are the conditional tables associated with each node? [2p]
- (c) Suppose there is a crowd in front of the building one day but that no fire trucks arrive. Given this, what is the probability that there is a fire, expressed as some function of the conditional (or prior) probabilities? [2p]
  - Appendix 2 provides you with some help in answering these questions.

- 4. A\* search is the most widely-known form of best-first search. The following questions pertain to A\* search:
  - (a) Explain what an admissible heuristic function is using the notation and descriptions in (c). [1p]
  - (b) Suppose a robot is searching for a path from one location to another in a rectangular grid of locations in which there are arcs between adjacent pairs of locations and the arcs only go in north-south (south-north) and east-west (west-east) directions. Furthermore, assume that the robot can only travel on these arcs and that some of these arcs have obstructions which prevent passage across such arcs.
    - The *Mahattan distance* between two locations is the shortest distance between the locations ignoring obstructions. Is the Manhattan distance in the example above an admissible heuristic? Justify your answer explicitly. [2p]
  - (c) Let h(n) be the estimated cost of the cheapest path from a node n to the goal. Let g(n) be the path cost from the start node  $n_0$  to n. Let f(n) = g(n) + h(n) be the estimated cost of the cheapest solution through n.
    - Provide a general proof that  $A^*$  using tree-search is optimal if h(n) is admissible. If possible, use a diagram to structure the proof. [2p]
- 5. Use the table below and the information in appendix 3 to answer the following questions pertaining to version spaces and the candidate elimination algorithm.

The following table shows a list of examples for a hypothetical credit-scoring application which might be used by a bank or credit-card company to filter prospective customers as to their credit worthiness. The target function is "person x is creditworthy".

Example	Age	Mortage	Default	Length Employed	Surplus %	Creditworthy
1	18-60	No	No	1-5	No	Yes
2	18-60	Yes	No	1-5	No	Yes
3	< 18	No	No	< 1	No	No
4	18-60	No	Yes	1-5	No	No
5	18-60	No	No	> 5	No	Yes

Figure 1: Positive and negative training examples for Target Attribute Creditworthy

In the problem above *Creditworthy* is described in terms of the five attributes: Age, Mortage (for house), Default (on loan), Length Employed, and Surplus (cash).

- (a) Is the Candidate-Elimination algorithm a supervised or unsupervised learning algorithm? Why?[1p]
- (b) Use the Candidate-Elimination algorithm to compute the version space containing all hypotheses from H (the space of hypotheses) that are consistent with the observed sequence of training examples in the table above for the target attribute Creditworthy. [4p]
  - Initialize the algorithm with  $G_0 = \{\langle ?, ?, ?, ?, ? \rangle\}$  and  $S_0 = \{\langle \emptyset, \emptyset, \emptyset, \emptyset, \emptyset \rangle\}$
  - Provide a hand trace of the Candidate-Elimination algorithm learning from the training examples in the table above. In particular, show the specific and general boundaries of the version space after it has processed the first training example, the second training example, etc.
- 6. The following questions pertain to partial-order planning:
  - (a) What is partial-order planning and how does it differ from STRIPS-based planning in terms of search space and output of the respective planning algorithms?[3p]
  - (b) Describe the four basic components in a partial-order plan according to Russell/Norvig. [2p]

- 7. The following questions pertain to the course article by Newell and Simon entitled *Computer Science* as an *Empirical Enquiry: Symbols and Search*..
  - (a) What is a physical symbol system (PSS) and what does it consist of? [2p]
  - (b) What is the Physical Symbol System Hypothesis? [1p]
- 8. Modeling actions and change in incompletely represented, dynamic worlds is a central problem in knowledge representation. The following questions pertain to reasoning about action and change.
  - (a) What is Temporal Action Logic? Explain by describing the ontology used in the formalism, that is, what is taken to exist, and what notation is used in the logical language to represent those things that are taken to exist. [2p]
  - (b) What is the frame problem? Use the Wumpus world to provide a concrete example of the problem. Represent the problem by representing an initial timepoint, an action and the result of the action using the TAL notation (either with macros or without). [2p]
  - (c) What is nonmonotonic logic? How can it be used to provide solutions to the frame problem? [2p]

# Appendix 1

Converting arbitrary wffs to clause form:

- 1. Eliminate implication signs.
- 2. Reduce scopes of negation signs.
- 3. Standardize variables within the scopes of quantifiers (Each quantifier should have its own unique variable).
- 4. Eliminate existential quantifiers. This may involve introduction of Skolem constants or functions.
- 5. Convert to prenex form by moving all remaining quantifiers to the front of the formula.
- 6. Put the matrix into conjunctive normal form. Two useful rules are:
  - $\omega_1 \vee (\omega_2 \wedge \omega_3) \equiv (\omega_1 \vee \omega_2) \wedge (\omega_1 \vee \omega_3)$
  - $\omega_1 \wedge (\omega_2 \vee \omega_3) \equiv (\omega_1 \wedge \omega_2) \vee (\omega_1 \wedge \omega_3)$
- 7. Eliminate universal quantifiers.
- 8. Eliminate  $\land$  symbols.
- 9. Rename variables so that no variable symbol appears in more than one clause.

# Appendix 2

A generic entry in a joint probability distribution is the probability of a conjunction of particular assignments to each variable, such as  $P(X_1 = x_1 \wedge ... \wedge X_n = x_n)$ . The notation  $P(x_1,...,x_n)$  can be used as an abbreviation for this.

The chain rule states that any entry in the full joint distribution can be represented as a product of conditional probabilities:

$$P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i \mid x_{i-1}, \dots, x_1)$$
 (5)

Given the independence assumptions implicit in a Bayesian network a more efficient representation of entries in the full joint distribution may be defined as

$$P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i \mid parents(X_i)), \tag{6}$$

where  $parents(X_i)$  denotes the specific values of the variables in  $Parents(X_i)$ .

Recall the following definition of a conditional probability:

$$\mathbf{P}(X \mid Y) = \frac{\mathbf{P}(X \land Y)}{\mathbf{P}(Y)} \tag{7}$$

The following is a useful general inference procedure:

Let X be the query variable, let **E** be the set of evidence variables, let **e** be the observed values for them, let **Y** be the remaining unobserved variables and let  $\alpha$  be the normalization constant:

$$\mathbf{P}(X \mid \mathbf{e}) = \alpha \mathbf{P}(X, \mathbf{e}) = \alpha \sum_{\mathbf{y}} \mathbf{P}(X, \mathbf{e}, \mathbf{y})$$
(8)

where the summation is over all possible  $\mathbf{y}$ 's (i.e. all possible combinations of values of the unobserved variables  $\mathbf{Y}$ ).

Equivalently, without the normalization constant:

$$\mathbf{P}(X \mid \mathbf{e}) = \frac{\mathbf{P}(X, \mathbf{e})}{\mathbf{P}(\mathbf{e})} = \frac{\sum_{\mathbf{y}} \mathbf{P}(X, \mathbf{e}, \mathbf{y})}{\sum_{\mathbf{x}} \sum_{\mathbf{y}} \mathbf{P}(\mathbf{x}, \mathbf{e}, \mathbf{y})}$$
(9)

# Appendix 3

## Begin:Candidate-Elimination Learning Algorithm

Initialize G to the set of maximally general hypotheses in H Initialize S to the set of maximally specific hypotheses in H For each training example d, do

- If d is a positive example
  - Remove from G any hypothesis inconsistent with d
  - For each hypothesis s in S that is not consistent with d
    - \* Remove s from S
    - \* Add to S all minimal generalizations h of s such that
      - $\cdot$  h is consistent with d, and some member of G is more general than h
    - \* Remove from S any hypothesis that is more general than another hypothesis in S
- If d is a negative example
  - Remove from S any hypothesis inconsistent with d
  - For each hypothesis g in G that is not consistent with d
    - \* Remove q from G
    - \* Add to G all minimal specializations h of q such that
      - · h is consistent with d, and some member of S is more specific than h
    - \* Remove from G any hypothesis that is less general than another hypothesis in G

## End: Candidate-Elimination Learning Algorithm

**Hypothesis representation**: Let each hypothesis be a vector of n constraints, specifying the values of each of the n attributes in a problem. For each attribute, the hypothesis will either

- indicate by a "?" that any value is acceptable for this attribute,
- specify a single required value for the attribute
- indicate by a "\O" that no value is acceptable.

#### Definition 1

A hypothesis h is **consistent** with a set of training examples D if and only if h(x) = c(x) for each example  $\langle x, c(x) \rangle$  in D.<sup>2</sup>

$$Consistent(h, D) \equiv (\forall \langle x, c(x) \rangle \in D) h(x) = c(x).$$

## Definition 2

The **general boundary** G, with respect to hypothesis space H and training data D, is the set of maximally general members of H consistent with D.<sup>3</sup>

$$G \equiv \{g \in H \mid Consistent(g, D) \land (\neg \exists g' \in H) [(g' >_g g) \land Consistent(g', D)] \}$$

### Definition 3

The **specific boundary** S, with respect to hypothesis space H and training data D, is the set of minimally general (i.e., maximally specific) members of H consistent with D.

$$S \equiv \{s \in H \mid Consistent(s, D) \land (\neg \exists s' \in H) [(s >_q s') \land Consistent(s', D)] \}$$

<sup>&</sup>lt;sup>2</sup>Here, x is an example, h is a hypothesis returning true or false and c is the target concept returning true or false.

 $<sup>{}^3</sup>h >_q h'$  states that h is strictly more general than h'.  $h_i \ge_q h_k$  if and only if:  $\forall (x \in X)[(h_k(x) = 1) \to (h_i(x) = 1)]$ .