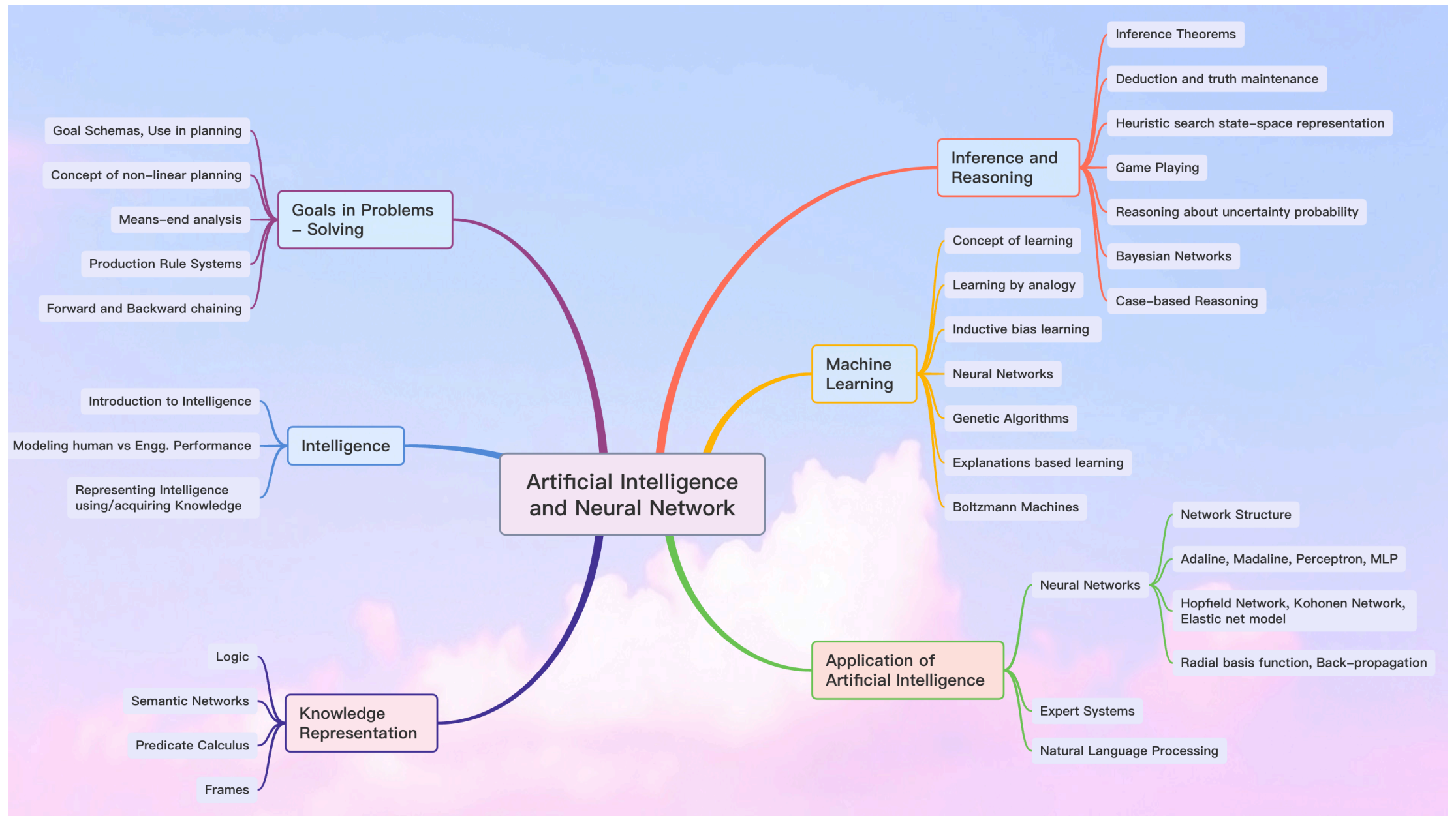


UNIT 3

Knowledge Representation



Contents

2

- Knowledge Representation

- ▣ Knowledge Based Agents
- ▣ Formal logic
- ▣ Connectives
- ▣ Truth tables
- ▣ Syntax
- ▣ Semantics
- ▣ Tautology
- ▣ Knowledge Models
- ▣ Validity
- ▣ Well Formed Formula

- Propositional Logic

- Predicate Logic

- ▣ FOPL
- ▣ Interpretation
- ▣ Quantification
- ▣ Horn Clauses

Outline

3

□ Inference

- ▣ Rules of Inference
- ▣ Unification
- ▣ Resolution Refutation System
- ▣ Answer Extraction from RRS
- ▣ Rule based Deduction System

□ Statistical Reasoning

- ▣ Probability and Bayes Theorem
- ▣ Causal Networks
- ▣ Reasoning in Belief Network

Knowledge Representation

4

- An area of AI whose fundamental goal is to represent knowledge in a manner that facilitates inferring or drawing conclusion from knowledge
- Analyses how to think formally, how to use symbol to represent a domain of discourse along with the function that allow inference about the objects

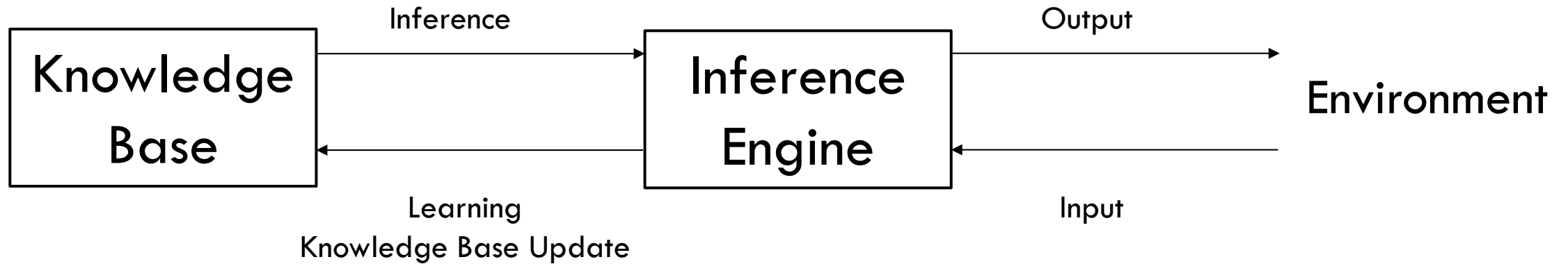
Knowledge Representation

5

- Helps to address problems like:
 - ▣ How do we represent facts about the world?
 - ▣ How do we reason about them?
 - ▣ What representations are appropriate for dealing with the real world?
- Its objective is to express knowledge in a computer tractable form so that agent can perform well.

Knowledge Representation

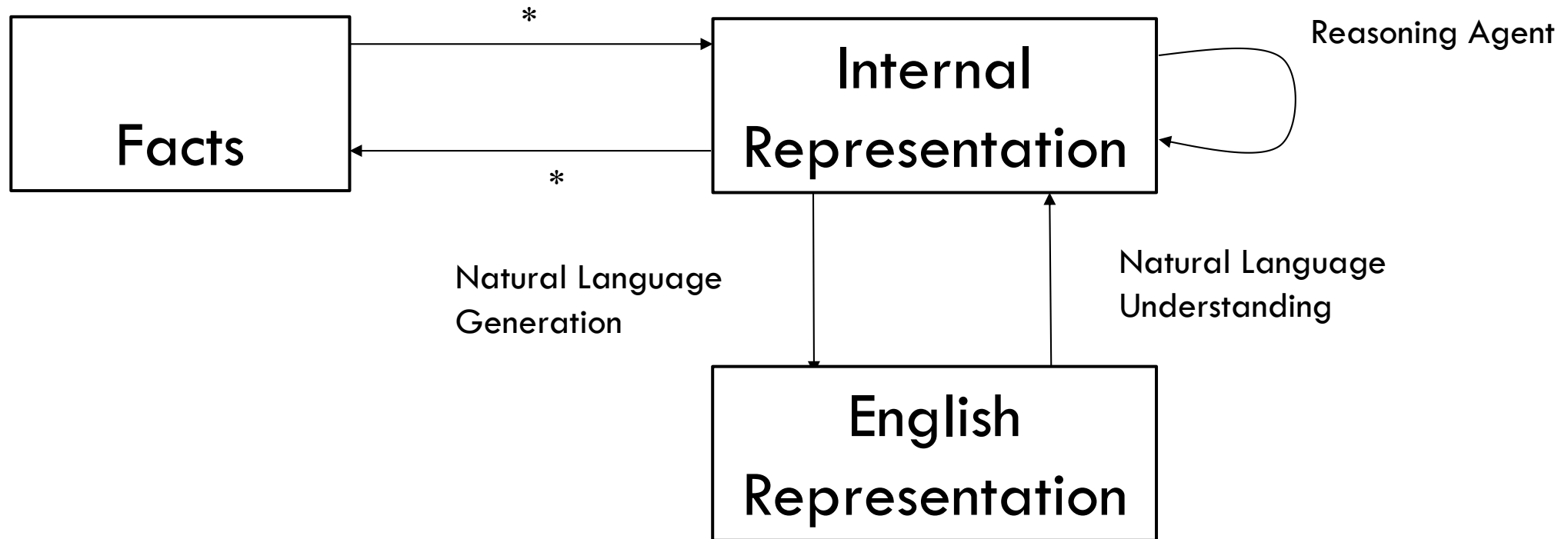
6



Knowledge Representation

7

Figure: Mapping Facts and Representation



Knowledge Representation: Approaches

8

- A good system for knowledge representation should have
 - ▣ Representable Adequacy: Ability to represent all kind of knowledge that are needed in the domain
 - ▣ Inferential Adequacy: Ability to manipulate the representational structure in such a way as to derive new structures corresponding to new knowledge inferred from old
 - ▣ Inferential Efficiency: Ability to incorporate into the knowledge structure additional information that can be used to focus the attention of the inference mechanism in the most promising direction
 - ▣ Acquisitional Efficiency: Ability to acquire new information easily

Knowledge Representation: Types

9

□ Simple Relational Knowledge

- ▣ The simplest way to represent declarative facts is as a set of relations of the same sort used in database system

□ Inheritable Knowledge

- ▣ Structure must be designed to correspond to the inference mechanism that are desired

□ Inferential Knowledge

- ▣ Represents knowledge as formal logic
- ▣ Based on reasoning from facts or from other inferential knowledge
- ▣ Useless unless there is also an inference procedure that can exploit it

□ Procedural (Imperative) Knowledge

- ▣ Knowledge exercised in the performance of some task
- ▣ Processed by an intelligent agent

Knowledge Representation: Issues

10

- Are any attributes of objects so basic that they have been occurred in almost every problem domain?
- Are there any important relationships that exist among attributes of objects
- At what level should knowledge be represented?
- How should sets of objects be represented?
- How can relevant parts be accessed when they are needed?

Knowledge Based Agent

11

- Knowledge Base: a set of sentences
- An agent having a knowledge base
- Each sentence in a knowledge base is expressed in a language called a knowledge representation language
- There must be a way to add new sentences to the knowledge base
- Logical Agents must infer from the knowledge base that has the information from the past or background knowledge

Knowledge Based Agent: Levels of Knowledge Base

12

□ Knowledge Level

- ▣ The most abstract level
- ▣ Describes agent by saying what it knows
- ▣ Example:
 - An intelligent taxi might know that the Bagmati Bridge connects Kathmandu with Lalitpur

□ Logical Level

- ▣ The level at which the knowledge is encoded into formal sentences
- ▣ Example:
 - Joins(Bagmati bridge, Kathmandu, Lalitpur)

□ Implementation Level

- ▣ Physical representation of the sentences in the logical level
- ▣ Example:
 - Objects, string, dams, etc.

Approaches of system building

13

□ Declarative approach

- ▣ Designing the representation language to make it easy to express the knowledge in the form of sentences

□ Procedural approach

- ▣ Encoded desired behaviour directly as program code

Logic

14

- ❑ Logic
- ❑ Syntax: Formal standard to express sentences so that the sentences are well formed
- ❑ Semantics: Has to do with the meaning of sentences
 - ▣ Defines the truth of the sentences with respect to respective possible world
- ❑ Connectives: Joins the different components of the sentence
- ❑ Model and Real World
- ❑ Entailment: the idea that a sentence follows logically from another sentence
 - ▣ Example: $\alpha \models \beta$, where α & β are sentences and β follows from α

Logic

15

- An inference algorithm that derives only entailed sentences is called sound or truth preserving
- Completeness is desirable
 - ▣ An inference algorithm is complete if it can derive any sentence that is entailed
- If knowledge base is true in the real world, then any sentence derived from the knowledge base by a sound inference procedure is also true in the real world

Logic

16

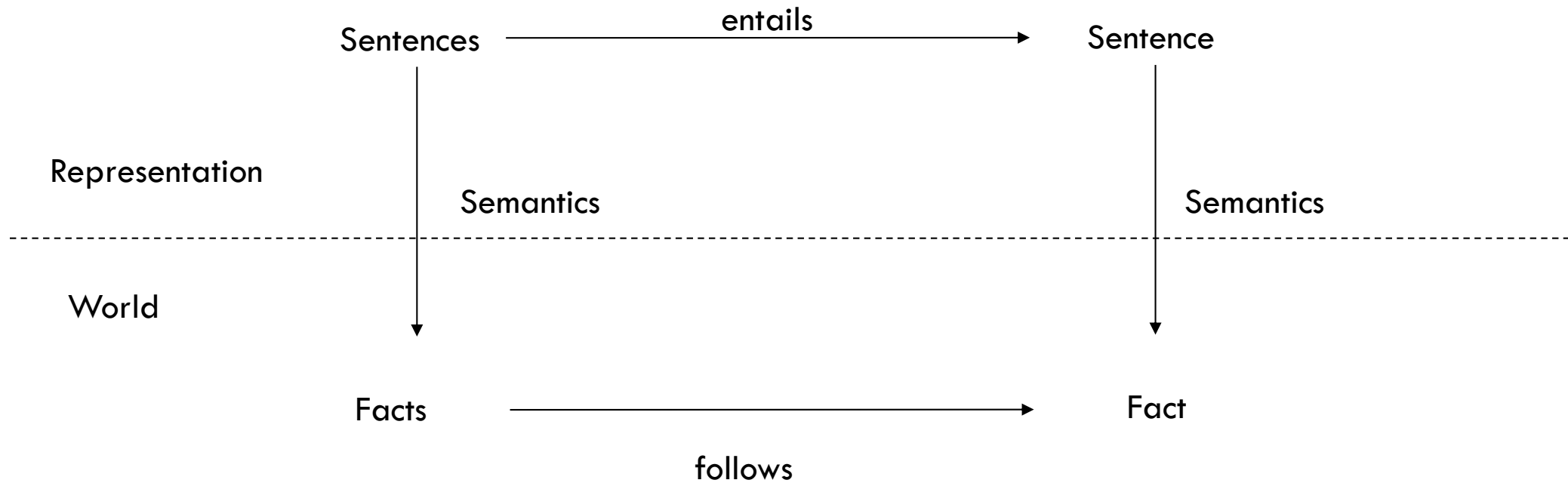


Figure: semantics map sentences in logic to fact in the world

Logic

17

- Example
- Knowledge Base
 - ▣ Socrates is a man
 - ▣ All men are Mortal
 - ▣ Äll men are kind
- Inference algorithm is applied to the above base
- Inferring “Socrates is Mortal”
- “Socrates is kind” follows the sentence “All men are Kind

Truth Table

18

| P | Q | $\neg P$ | $P \vee Q$ | $P \wedge Q$ |
|-------|-------|----------|------------|--------------|
| False | False | True | False | False |
| False | True | True | True | False |
| True | False | False | True | False |
| True | True | False | True | True |

Tautology and Validity

19

- A notation used in formal logic which is always true and valid.
- Example: $A \text{ OR } (\text{NOT } A)$
I am eating food OR I am not eating food
- If all the conditions for a statement is true its tautology
- Tautologies are also called valid sentences

Knowledge Models

20

- A model is a world in which a sentence is true under a particular interpretation
- There can be several models at once that have the same interpretations
- Types:
 - ▣ First order logic
 - ▣ Procedural Representation Model
 - ▣ Relational Representation Model
 - ▣ Hierarchical Representation Model
 - ▣ Semantic Nets

Knowledge Models: Types

21

□ First Order Logic

- ▣ First Order Predicate Calculus
- ▣ Consists of objects, predicates on objects, connectives and quantifiers
- ▣ Predicates are the relations between objects or properties of the objects
- ▣ Connectives and quantifiers allow for universal sentences
- ▣ Relations between objects can be true or false

□ Procedural Representation Model

- ▣ This model of knowledge representation encodes facts along with the sequence of operations for manipulation and processing of the facts
- ▣ Expert systems are based on this model
- ▣ It works best when experts follow set of procedures for problem solving
- ▣ Example: doctor making diagnosis

Knowledge Models: Types

22

□ Relational Representation Model

- ▣ Collection of knowledge are stored in tabular form
- ▣ Mostly used in commercial databases, relational databases
- ▣ The information is manipulated with relational calculus use a language like SQL, Oracle, etc.
- ▣ Its flexible way of storing information by not good for storing complex relationships

- ▣ Problem arises when more than one subject area is attempted

- ▣ A new knowledge base from scratch has to be built for each area of expertise

□ Hierarchical Representation Model

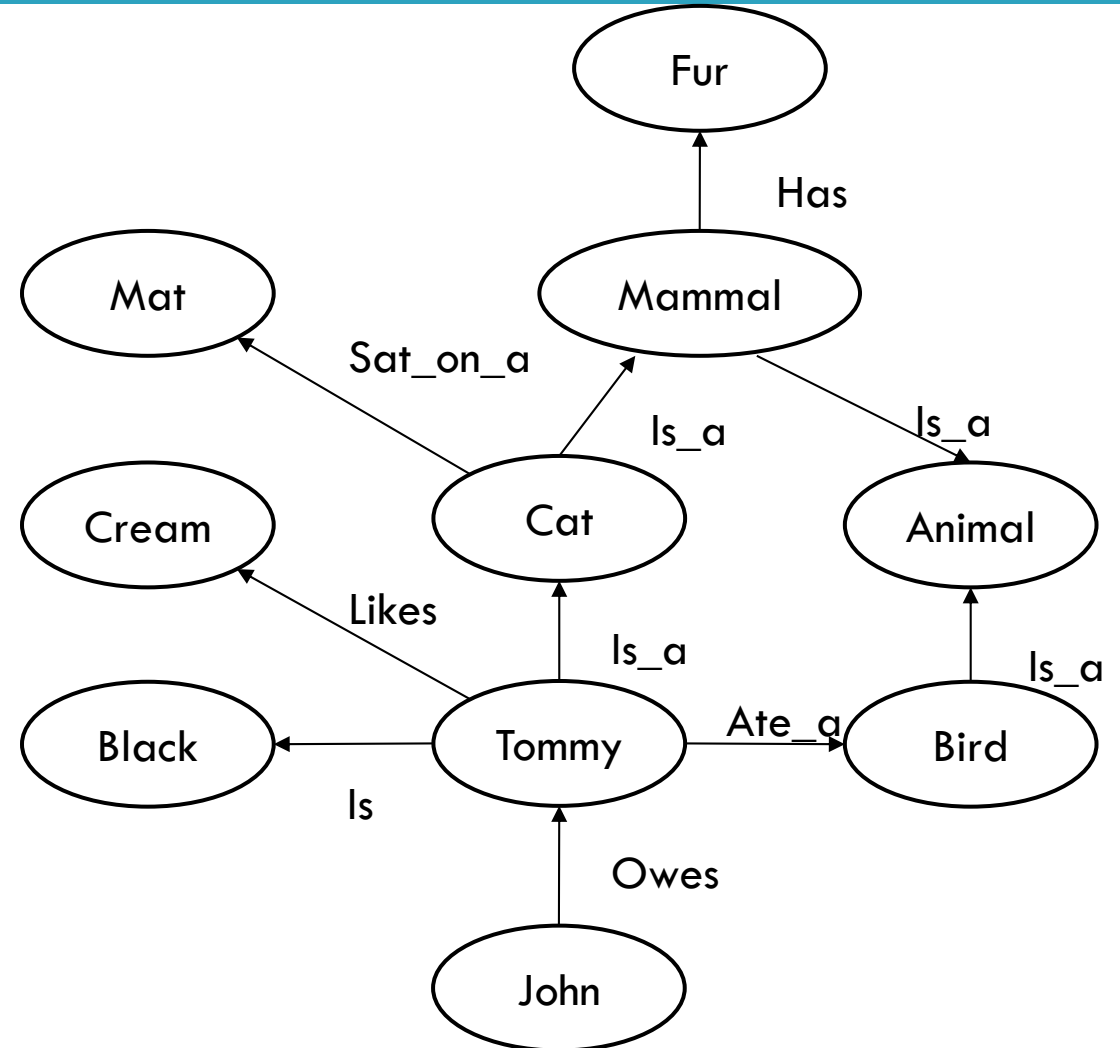
- ▣ Based on inherited knowledge and the relationship and shared attributes between objects

Knowledge Models: Types

23

□ Semantic Nets

- ▣ Semantic networks are an alternative to predicate logic as a form of knowledge representation
- ▣ The idea is that we can store our knowledge in the form of graph with nodes representing objects in the world and are representing relationships between those objects



Propositional Logic

24

- It is declarative sentences which can either be true or false but not both or neither
- A Very simple logic
- A Mathematical model that allows us to reason about the truth or falsehood of logical expressions
- There are sentences and connectives to describe an expression
- Its syntax defines allowable sentences
- Example:
 - ▣ Is it raining?
 - ▣ Is $2+2=5$?
- Logical Connectives in Propositional Logic
 - ▣ \wedge : Conjunction (and)
 - ▣ \vee : Disjunction (or)
 - ▣ \neg : Negation (not)
 - ▣ $\Rightarrow \rightarrow$: Implication (if...then...)
 - ▣ $\Leftrightarrow \leftrightarrow$: Logical Equivalence (If and only If)

Propositional Logic: Truth Tables

25

| A | $\neg A$ |
|---|----------|
| T | F |
| F | T |

| A | B | $A \wedge B$ |
|---|---|--------------|
| F | F | F |
| F | T | F |
| T | F | F |
| T | T | T |

| A | B | $A \vee B$ |
|---|---|------------|
| F | F | F |
| F | T | T |
| T | F | T |
| T | T | T |

| A | B | $A \Rightarrow B$ |
|---|---|-------------------|
| F | F | T |
| F | T | F |
| T | F | T |
| T | T | T |

| A | B | $A \Leftrightarrow B$ |
|---|---|-----------------------|
| F | F | T |
| F | T | F |
| T | F | F |
| T | T | T |

Propositional Logic

26

□ Sentence Properties

- ▣ T or F itself is a sentence
- ▣ Individual Proposition symbols are sentences
eg. P , Q , ...
- ▣ If s is a sentence, so is (s)
- ▣ If $S1$ and $S2$ are sentences, so are:
 $\neg S1$, $\neg S2$, $S1 \wedge S2$, etc.

□ Order of Precedence

- ▣ \neg : Negation (not)
- ▣ \wedge : Conjunction (and)
- ▣ \vee : Disjunction (or)
- ▣ $\Rightarrow \rightarrow$: Implication
(if...then...)
- ▣ $\Leftrightarrow \leftrightarrow$: Logical
Equivalence (If
and only If)

Propositional Logic

27

□ Atomic Sentences

- ▣ Single sentence
- ▣ T, F, P, Q, ...
where, each symbol stands for proposition that can be true or false.
- ▣ Example: P = "Ram likes Rice"
Q = "Sita is women"

□ Complex Sentences

- ▣ Sentences constructed from simple sentences using logical connectives
- ▣ Example: P = "It is hot today"
Q = "It is humid today"
 $P \wedge Q$
"It is hot and humid today"

Propositional Logic

28

□ Unsatisfiable (Contradiction)

- ▣ If all the sentences or statements are always false
- ▣ Example: “There will be a clear sky during rainy day”

□ Satisfiable

- ▣ If at least one sentence in the knowledge base is true

Propositional Logic: Equivalence Laws

29

1. $P \Rightarrow Q \equiv \neg P \vee Q$
2. $P \Leftrightarrow Q \equiv (P \Rightarrow Q) \wedge (Q \Rightarrow P)$
3. Distributive Laws
 $A \wedge (B \vee C) \equiv (A \wedge B) \vee (A \wedge C)$
 $A \vee (B \wedge C) \equiv (A \vee B) \wedge (A \vee C)$
4. De-Morgan's Law
 $\neg(A \wedge B \wedge C) \equiv (\neg A) \vee (\neg B) \vee (\neg C)$
 $\neg(A \vee B \vee C) \equiv (\neg A) \wedge (\neg B) \wedge (\neg C)$

Propositional Logic: Inference Rules

30

1. Modus Ponens Rule

Whenever any sentence of the form $P \Rightarrow Q$ and P are given, then the sentence Q can be inferred

$$\frac{P \Rightarrow Q, P}{Q}$$

2. And Elimination

$$\frac{A \wedge B}{A \mid B}$$

sentence A or B can be inferred if A and B is given

3. And Introduction

$$\frac{A, B, \dots, N}{A \wedge B \wedge \dots \wedge N}$$

4. Or Introduction

$$\frac{A, B, \dots, N}{A \vee B \vee \dots \vee N}$$

5. Double Negation Elimination

$$\frac{1 \mid \neg P}{P}$$

Propositional Logic: Inference Rules

31

6. Unit Resolution

$$\frac{A \vee B, \neg A}{B}$$

7. Modus Tollens

$$\frac{P \Rightarrow Q, \neg Q}{\neg P}$$

8. Resolution Chaining

$$\frac{P \Rightarrow Q, Q \Rightarrow R}{P \Rightarrow R}$$

$$\frac{\neg P \Rightarrow Q, Q \Rightarrow R}{\neg P \Rightarrow R}$$

Propositional Logic

32

- The semantics defines the rules for determining the truth of sentences with respect to a particular model, i.e. semantic must specify how to compute the truth value of any sentence in a given model.

Propositional Logic: BNF Grammar

33

- Backus Normal Form or Backus Naur Form
- It's a notation technique for context free grammars often used to describe the syntax of languages used in computing
- BNF can be used in two ways:
 - ▣ To generate strings belonging to the grammar
 - ▣ To recognize strings belonging to the grammar

Normal Forms of Propositional Logic Sentences

34

1. Conjunctive (disjunction of conjunction of literals)

Normal Form

- ▣ In which a sentence is written as the conjunction of literals

$$(A \vee B) \Rightarrow Q$$

$$\equiv \neg (A \vee B) \vee Q$$

$$\equiv (\neg A \wedge \neg B) \vee Q$$

$$\equiv (\neg A \vee Q) \wedge (\neg B \vee Q)$$

2. Disjunctive (conjunction of disjunction of literals) Normal Form

- ▣ In which a sentence is written as the disjunction of literals
 $(A \wedge Q) \vee (B \wedge Q)$

First Order Predicate Logic (FOPL)

35

- Propositional logic assumes that the world or system being modelled can be described in terms of fixed, known set of propositions
- This assumption can make it awkward or even impossible to specify many pieces of knowledge
- Example:
 - ▣ Consider a general sentence “if a person is rich then they have a nice car”
 - ▣ In propositional logic, we can generate rule for each person as
 - $\text{Bob_is_rich} \rightarrow \text{Bob_has_a_nice_car}$
 - $\text{John_is_rich} \rightarrow \text{John_has_a_nice_car}$
 - ▣ This seems to be an impractical way to represent knowledge, hence, generalization to represent this type of knowledge is a must

First Order Predicate Logic (FOPL)

36

- FOPL is a logic that gives us the ability to quantify over objects
- In FOPL, statements from a natural language like English are translated into symbolic structure composed of predicates, functions, variables, constants, quantifiers and logical connectives
- First Order Predicate Logic represents facts by separating classes and individuals and consider that world consists of different objects and relations between those objects

FOPL: Syntax

37

| | | |
|----------------|---|--|
| Sentence | → | AtomicSentence (Sentence Connective Sentence) Quantifier Variable,...Sentence \neg Sentence |
| AtomicSentence | → | Predicate(Term,...) Term = Term |
| Term | → | Function (Term,...) Constant Variable |
| Connective | → | \neg \vee \wedge \Rightarrow \Leftrightarrow |
| Quantifier | → | \forall \exists |
| Constant | → | A X John ... |
| Variable | → | a x s ... |
| Predicate | → | Before HasColor Raining ... |
| Function | → | Mother Leftleg ... |

FOPL: Syntax

38

- Constant Symbols are the strings that will be interpreted as representing objects
- Variable Symbols are used as place holders for quantifying over objects
- Predicate symbols are used to denote properties of objects and relationship among them
- Function Symbols map the specified number of input objects to objects
- Quantifiers are used to quantify objects
 - ▣ Universal Quantifier represents for all
 - ▣ Existential Quantifier represents the existence of an object

FOPL: Variable Scope

39

- The scope of the variable is in the sentence to which the quantifier syntactically applies
- In a block structured programming language, a variable in a logical expression refers to the closest quantifier within whose scope it appears
- In a well formed formula all the variables should be properly introduced

Relation Between Quantifiers

40

- $\forall x \neg P \equiv \neg \exists x P$
- $\neg \forall x P \equiv \exists x \neg P$
- $\forall x P \equiv \neg \exists x \neg P$
- $\exists x P \equiv \neg \forall x \neg P$
- $\forall x P(x) \cap Q(x) \equiv$
 $\forall x P(x) \cap \forall x Q(x)$
- $\exists x P(x) \cup Q(x) \equiv$
 $\exists x P(x) \cup \exists x Q(x)$

Examples

41

- All birds can't fly
 $\forall x \text{ Bird}(x) \rightarrow \neg \text{Fly}(x)$
OR
 $\neg(\exists x (\text{Bird}(x) \cap \text{Fly}(x)))$

- Not all birds can fly
 $\neg(\forall x \text{ Bird}(x)$
OR
Type equation here.

- If anyone can solve the problem then Raju can
 $\exists x \text{ Solves}(x, \text{problem}) \rightarrow \text{Solves}(\text{Raju}, \text{problem})$
- Try these
 - ▣ Nobody in electrical class is smarter than everyone in AI class
 - ▣ John hates all the people who don't hate themselves

Equality

42

- Can include equality as a primitive predicate in the logic or require it to be introduced and axiomatized as the identity relation
- Useful in representing certain types of knowledge
 - ▣ Example: Sita owns two cars
$$\exists x \exists y (Owns(Sita, x) \wedge Owns(Sita, y) \wedge Car(x) \wedge Car(y) \wedge \neg(x = y))$$
- Try these:
 - ▣ There are exactly two purple flowers out of three
 - ▣ Everyone is married to exactly one person

Every gardener likes the sun.

$$\forall x \text{ gardener}(x) \rightarrow \text{likes}(x, \text{Sun})$$

You can fool some of the people all of the time.

$$\exists x \forall t \text{ person}(x) \wedge \text{time}(t) \rightarrow \text{can-fool}(x, t)$$

You can fool all of the people some of the time.

$$\forall x \exists t (\text{person}(x) \rightarrow \text{time}(t) \wedge \text{can-fool}(x, t))$$

$$\forall x (\text{person}(x) \rightarrow \exists t (\text{time}(t) \wedge \text{can-fool}(x, t)))$$

All purple mushrooms are poisonous.

$$\forall x (\text{mushroom}(x) \wedge \text{purple}(x)) \rightarrow \text{poisonous}(x)$$

No purple mushroom is poisonous.

$$\neg \exists x \text{ purple}(x) \wedge \text{mushroom}(x) \wedge \text{poisonous}(x)$$

$$\forall x (\text{mushroom}(x) \wedge \text{purple}(x)) \rightarrow \neg \text{poisonous}(x)$$

There are exactly two purple mushrooms.

$$\begin{aligned} \exists x \exists y \text{ mushroom}(x) \wedge \text{purple}(x) \wedge \text{mushroom}(y) \wedge \text{purple}(y) \wedge \neg(x=y) \wedge \forall z (\text{mushroom}(z) \\ \wedge \text{purple}(z)) \rightarrow ((x=z) \vee (y=z)) \end{aligned}$$

Clinton is not tall.

$$\neg \text{tall}(\text{Clinton})$$

X is above Y iff X is on directly on top of Y or there is a pile of one or more other objects directly on top of one another starting with X and ending with Y.

$$\forall x \forall y \text{ above}(x,y) \leftrightarrow (\text{on}(x,y) \vee \exists z (\text{on}(x,z) \wedge \text{above}(z,y)))$$

Try few more

45

- ☐ Ram likes all kinds of food
- ☐ Anything anyone eats and is not killed by is food
- ☐ Rita eats samosa and is still alive
- ☐ Gita eats everything Rita eats
- ☐ Someone who hates something owned by another person will not love that person
- ☐ There is a barber in the town who shaves all men in the town who don't shave themselves
- ☐ Everyone loves somebody
- ☐ No one likes everyone
- ☐ There is someone who is liked by everyone
- ☐ You can fool some of the people every time
- ☐ All employee earning Rs.200000 | - or more per year pay taxes
- ☐ Some employee are sick today
- ☐ Nobody earns more than the chairman

Horn Clause

46

- Disjunction of literals of which at most one is positive is Horn Clause

$$P1 \wedge P2 \wedge \dots \wedge Pn \Rightarrow Q \equiv \neg P1 \vee \neg P2 \vee \dots \vee \neg Pn \vee Q$$

- Clause with exactly one positive literals giving definite clause (fact)
- Horn clause with no positive literals can be written as an implication whose conclusion is the literal false

$$\neg x1 \vee \neg x2 \equiv x1 \wedge x2 \Rightarrow \text{False}$$

Horn Clause

47

Reason for its importance

- Every horn clause can be written as an implication whose premises is a conjunction of positive literals and whose conclusion is a single positive literal

Example: $\neg L1 \cup \neg L2 \cup B$ can be written as $L1 \cap L2 \Rightarrow B$

- Inference with horn clauses can be done with the forward chaining and backward chaining
- Deciding entailment with horn clauses can be done in time that is linear in the size of knowledge base

Well Formed Formula

48

- A sentence that has all its variables properly introduced using quantifiers is a well formed formula
- Example:
 $\forall x P(x, y)$ is not a well formed formula where x is bounded as universal quantifier and y is free
 $\forall x \exists y Q(x, y)$ is a well formed formula where both x and y are bounded

- Notes:

- Predicate can't be quantifiers
- Constant can't be negative
- Letter cases must be well considered

Inference in FOL

49

- If x is a parent of y , then x is older than y
- If x is the mother of y then x is a parent of y
- Devaki is the mother of Krishna
- Conclusion:
Devaki is older than Krishna

Mapping in FOL

- $\forall x \forall y \text{ parent}(x, y) \Rightarrow \text{older}(x, y)$
- $\forall x \forall y \text{ mother}(x, y) \Rightarrow \text{parent}(x, y)$
- $\text{mother}(\text{Devaki}, \text{Krishna})$
- Conclusion:
 $\text{older}(\text{Devaki}, \text{Krishna})$

Inference Rules in FOL

50

□ Universal Instantiation

- ▣ If a person is a student, studies in KEC and studies AI, then he/she is a third year student

- ▣ $\forall x \text{student}(x) \cap \text{studiesin}(x, \text{KEC}) \cap \text{studies}(x, \text{AI}) \Rightarrow \text{thirdyearstudent}(x)$

□ Existential Instantiation

- ▣ There must be a topper in KEC
- ▣ $\exists x \text{student}(x) \cap \text{studiesin}(x, \text{KEC}) \cap \text{topper}(x)$

□ Propositionization

- ▣ All people are kind
 $\forall x \text{person}(x) \Rightarrow \text{kind}(x)$
It can be inferred as
 $\text{person}(\text{Ram}) \Rightarrow \text{kind}(\text{Ram})$

Inference Rules in FOL

51

□ Generalized Modus Ponens

- $\forall x \text{student}(x) \cap \text{studieshard}(x) \Rightarrow \text{good student}(x)$
- $\text{student}(\text{Arjun})$
- $\text{studieshard}(\text{Arjun})$
- Conclusion:
 $\text{goodstudent}(\text{Arjun})$

□ Unification

- $[\text{knows}(\text{Sita}, x), \text{knows}(\text{Sita}, \text{Rita})] \Rightarrow x = \text{Rita}$
- $[\text{knows}(\text{Sita}, x), \text{knows}(y, \text{Rita})] \Rightarrow x = \text{Rita}, y = \text{Sita}$
- $[\text{knows}(\text{Sita}, x), \text{knows}(y, \text{ismother}(y))] \Rightarrow y = \text{Sita}, x = \text{mother}(\text{Sita})$
- $[\text{knows}(\text{Sita}, x), \text{knows}(x, \text{Rita})] \Rightarrow \text{false}$

Inference Rules in FOL

52

□ Resolution

- ▣ Produces proof by refutation (proof person or statement that is wrong)
- ▣ Resolution can be applied to sentences in CNF (conjunctive normal form)

□ Process of Resolution

- ▣ Convert all sentences to CNF
- ▣ Negate x
- ▣ Add negate x to premises
- ▣ Repeat until either a contradiction is detected or no progress is being made

CNF Conversion Process

53

1. Elimination of all implications with equivalence symbols

- ▣ $P \rightarrow Q \equiv \neg P \cup Q$
- ▣ $P \iff Q \equiv (\neg P \cup Q) \cap (\neg Q \cup P)$

2. Move \neg inward (use De'Morgans law)

- ▣ $\neg(P \cap Q) \equiv \neg P \cup \neg Q$
- ▣ $\neg(P \cup Q) \equiv \neg P \cap \neg Q$

- ▣ $\forall x \neg P \equiv \neg \exists x P$

- ▣ $\neg \forall x P \equiv \exists x \neg P$

- ▣ $\forall x P \equiv \neg \exists x \neg P$

- ▣ $\exists x P \equiv \neg \forall x \neg P$

3. Standardize Variables

- ▣ Rename variables if necessary so that all quantifiers have different variable assignments

CNF Conversion Process

54

4. Skolemization

- The process of eliminating the existential quantifiers through a substitution process
- The process requires that all such variables be replaced by short term functions, which can always assume a Skolem function, a correct value required for an existential quantifier variable
- If leftmost quantifier in an expression is existential quantifier (\exists), replace all occurrence of the variables that quantifies with an arbitrary constant not appearing elsewhere in the expression and delete the quantifier
 - Example: $\exists x \exists y \forall z P(x, y, z) \cup Q(x, y) \equiv \forall z P(a, b, z) \cup Q(a, b)$

CNF Conversion Process

55

4. Skolemization

- ▣ If existential quantifier (\exists) is preceded by universal quantifier (\forall), replace the existentially quantified variable by a function symbol whose arguments are variable appearing in those universal quantifiers

▣ Example:

$$\begin{aligned} & \exists u \forall x \forall y \exists z P(f(u), x, y, z) \\ & \quad \cup Q(x, y, z) \\ \equiv & \forall x \forall y \exists z P(f(a), x, y, z) \\ & \quad \cup Q(x, y, z) \\ \equiv & \forall x \forall y P(f(a), x, y, f(x, y)) \\ & \quad \cup Q(x, y, f(x, y)) \end{aligned}$$

- 5. Drop all universal quantifiers
- 6. Distribute \wedge over \vee

Example: Given Premises

56

1. If x is on top of y , y support x
2. If x is above y and they are touching each other, x is on top of y
3. Everything is on top of another thing
4. A cup is above a book
5. A cup is touching a book

□ Answer:

Is the book supporting
the cup?

Example: Solution

57

□ $\forall x \forall y \text{ ontop}(x, y) \Rightarrow \text{supports}(y, x)$
Implication Elimination
 $\forall x \forall y \neg \text{ontop}(x, y)$
 $\Rightarrow \text{supports}(y, x)$
Drop $\forall x$ and $\forall y$
 $\neg \text{ontop}(x, y)$
 $\Rightarrow \text{supports}(y, x)$

□ $\forall x, y \text{ above}(x, y) \cap \text{touch}(x, y) \Rightarrow \text{ontop}(x, y)$
Implication Elimination
 $\forall x, y \neg \text{above}(x, y)$
 $\cup \neg \text{touch}(x, y)$
 $\cup \text{ontop}(x, y)$
Drop $\forall x, y$
 $\neg \text{above}(x, y) \cup \neg \text{touch}(x, y)$
 $\cup \text{ontop}(x, y)$

Example: Solution

58

- $\forall x, y \text{ ontop}(x, y)$
 Drop $\forall x, y$
 ontop(x, y)
- *above*(*cup*, *book*)
- *touch*(*cup*, *book*)

Solution

59

Conclusion

□ *supports(book, cup)*

Let

$\neg \text{supports}(\text{book}, \text{cup})$

using second and fifth conditions

$\neg \text{above}(x, y) \cup \neg \text{touch}(x, y)$

$\cup \text{ontop}(x, y)$

touch(cup, book)

$\neg \text{above}(x, y) \cup \text{ontop}(x, y)$

using fourth condition

above(cup, book)

ontop(x, y)

using first condition

$\neg \text{ontop}(x, y) \cup \text{supports}(y, x)$

supports(book, cup)

using assumed condition

$\neg \text{supports}(\text{book}, \text{cup})$

Empty Clause

Hence, the book is supporting the cup

Try these

60

- Every American who sells weapon to hostile nation is a criminal. The country Iraq is an enemy of America. All of the missiles in Iraq were sold by George. George is an American.

Prove:

George is a Criminal

- All Pompeians are Romans. All Romans were either loyal to Caesar or hated him. Everyone is loyal to someone. People only try to assassinate rulers they are not loyal to. Marcus tried to assassinate Caesar. Marcus was a Pompeian.
Conclude:
Did Marcus hate Caesar?

Forward Chaining

61

- One of the two main methods for reasoning using inference rules
- Can be described logically as repeated application of Modus Ponens
- It's a popular strategy of reasoning in expert system and production systems
- It starts with the available data and uses inference rules to extract more data until a goal is reached
- An inference engine using forward chaining searches the inference rules until it finds one where antecedent (If clause) is known to be true

Forward Chaining

62

- When it found if clause it can conclude or infer the consequent (then clause) to its data resulting in the addition of new information
- Example: (Animal Identification System)
If X croaks and eats flies then it's a frog
If X chirps and sings then it's a canary

- If X is a frog then X is green
If X is a canary then X is yellow
goal: colour of pet
given that it croaks and eat flies

References

63

- Russell, S. and Norvig, P., 2011, Artificial Intelligence: A Modern Approach, Pearson, India.
- Rich, E. and Knight, K., 2004, Artificial Intelligence, Tata McGraw hill, India.

64

Thank You

Any Queries?

Now, Search for yourself.