CMU 10-715: Homework 6 Report

Implementation of Convolutional Neural Networks

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1 Results

- a I trained the classifiers for 3000 steps on Google Colab's GPU.
- b Refer table 1 for the final results of the training.

Model	Pooling	Training Time	Train Acc	Test Acc	Steps
M_{max}	max	518.707s	79.900	64.080	3000
M_{avg}	avg	515.660s	75.672	62.380	3000
M_{no}	no	528.855s	99.936	60.360	3000

Table 1: Table showing the final training and testing accuracies, total training time (including evaluation), and training steps for the three models with different pooling configurations

We can observe from the table that models M_{avg} and M_{max} have similar training times which is markedly less than that of M_{no} . This is because of removal of the subsampling pooling layers. In the CNN architecture under consideration, the Conv2d layers have a stride of 1 and do not result in much shrinkage to the feature maps's size. It is the pooling layers (max or avg configurations) with a stride of 2 that result in shrinkage of the feature maps' dimensions across the layers as the number of feature maps grow. Consequently, the first fully connected layer that comes up after the nn.Flatten() have smaller input dimensions in the case of M_{avg} and M_{max} (numerically, = 400) compared to M_{no} (input dim for first FC = 9216). Hence, there are far more parameters and bigger computation graph (for back-propagation) in the no pooling case (the pooling layers have no trainable parameters). This overparameterization is also evident in the way M_{no} overfits to the training data, as can be seen in table 1. Though there are additional computations in the pooling layers in M_{avg} and M_{max} models, it is seemingly outweighed by the computational time of M_{no} from its additional parameters, computational graph nodes, and back-propagation updates.

- c Refer figure 1.
- d Refer figure 2.
- e Refer figure 3.

Let's first compare the output of conv1 to the input image. We see that the six output feature maps of conv1 layer all capture/highlight varied

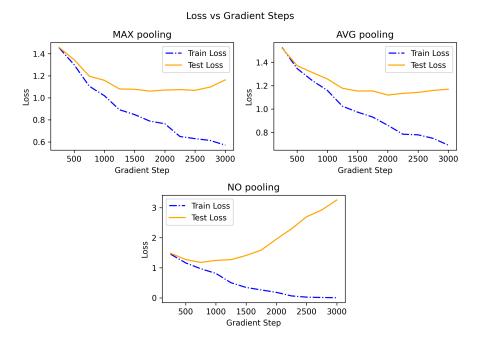


Figure 1: Loss vs Gradient Step plots for models M_{max} , M_{avg} , and M_{no} till 3000 training steps

features in the same input image, but they are truncated on the sides (we can notice missing pixels on the edges due to the convolution with no padding). In each of the feature maps, we can observe some characteristic edge or feature of the frog being highlighted and others being blurred out.

Now, let's compare the output of pool1 to the output of conv1. Clearly, the six images are now more pixelated due to the subsampling pooling layer that reduced the width and height dimensions by half. We can still observe that the features/edges that were highlighted in the six features maps after conv1 respectively seem to be preserved in the six feature maps after pool1 layer, but they are smoothened out and not sharp now. This might be due to the usage of average pooling - the boundaries of the features identified by conv1 are no longer uniform/sharp but contain mixed pixel values due to being affected by neighboring pixel values.

To sum it up, the convolution layers seem to be identifying features in the input image that it considers predictive of the output labels and the pooling layers seem to perform the job of reducing their dimensions for reducing overparameterization and computation cost, preserving as much

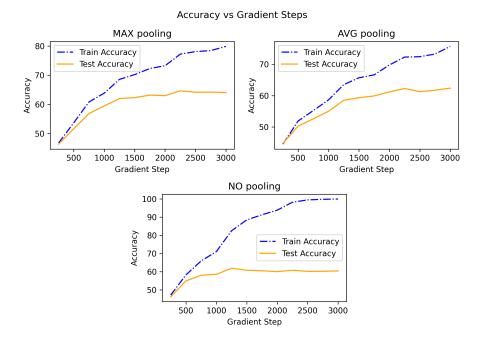


Figure 2: Accuracy vs Gradient Step plots for models M_{max} , M_{avg} , and M_{no} till 3000 training steps

information extracted by the convolutional layers as possible. Max pooling might be doing better than average pooling (as seen in table 1) because it will preserve the values of the important pixels without distorting them, thereby preserving information in a better manner than average pooling.

f The architecture of the convolutional neural network that I designed (M_{custom}) is as follows:

Input image \rightarrow 2D convolution with output channels = 8, kernel size 5, stride 1 and padding = 'same' \rightarrow ReLU \rightarrow Max Pooling with kernel size 2, stride 2 and no padding \rightarrow 2D convolution with output channels = 16, kernel size 5, stride 1 and padding = 'same' \rightarrow ReLU \rightarrow Max Pooling with kernel size 2, stride 2 and no padding \rightarrow 2D convolution with output channels = 64, kernel size 3, stride 1 and padding = 'same' \rightarrow ReLU \rightarrow Max Pooling with kernel size 2, stride 2 and no padding \rightarrow 2D convolution with output channels = 128, kernel size 4, stride 1 and no padding \rightarrow ReLU \rightarrow Fully connected linear layer with input dim = 128, output dim = 80 \rightarrow ReLU \rightarrow Fully connected linear layer with input dim = 80, output dim = 10 \rightarrow Output

The intuitions behind the modifications to LeNet architecture were drawn from the various observations during this assignment: used padding = 'same' for the convolutional layers for it to see the feature maps completely and not lose information at the sides of the feature maps (since images did extend till the sides); tried to create a slightly deeper network hence added an additional convolutional layer; to fight over-parameterization replaced the first FC layer by a convolutional layer and used subsampling layer after every convolutional layer; used max pooling since it performed better than average pooling by extracting extreme features well; finally, gradually increased number of output channels of convolutional layers as the feature map dimensions halved after the pooling layers.

I trained M_{custom} for the same number of training steps as LeNet for a fair comparison and obtained the final results as summarized in 2. The custom model does contain an additional layer and hence more parameters, that leads to the increased training set accuracy. But, the testing set accuracy (\Longrightarrow generalization performance) also increases by a non-trivial amount and validates the intuitions behind the architecture. The overall training time taken by M_{custom} is higher than M_{max} as expected due to deeper network, and just lesser than M_{no} , but the improved performance compensates for this marginal increase in training time.

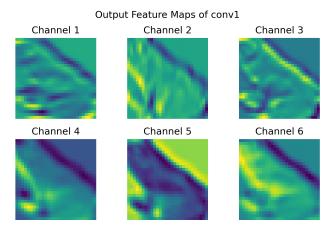
 M_{custom} actually achieves highest its best performance at ≈ 2250 steps, with a test accuracy of 70.940 and train accuracy of 91.222, which can be obtained by early stopping the training.

Model	Pooling	Training Time	Train Acc	Test Acc	Steps
M_{max}	max	518.707s	79.900	64.080	3000
M_{custom}	max	527.135s	94.538	69.340	3000

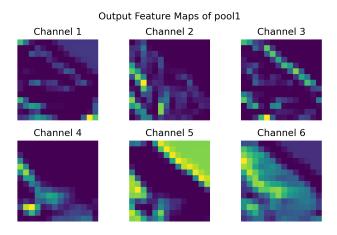
Table 2: Table showing the final training and testing accuracies, total training time (including evaluation), and training steps for the best LeNet model (M_{max}) and custom architectured CNN model



(a) The original image - one 32×32 image



(b) Output of the first layer (after the first convolutional layer but before the ReLU) - six 28×28 images



(c) Output of the second layer (after the first pooling layer and before the second convolutional layer) - six 14×14 images

Figure 3: Visualization of input image and initial layer outputs for the input image $\,$

2 Code

```
Colab_Cell_1

1 from google.colab import drive
2 drive.mount('/content/drive')

3
4 %cd /content/drive/MyDrive/10-715/HW6
5 !mkdir -p ./results ./plots ./models
```

```
Colab_Cell_2
1 %matplotlib inline
3 import time
4 import numpy as np
5 import matplotlib.pyplot as plt
6 import torch as t
7 from torch import nn
8 from torch import optim
9 from torch.nn import functional as F
10 import torchvision
import torchvision.transforms as transforms
12 import pickle
13 import itertools
14
15
16 def divide_no_nan(a, b):
17
      a/b where the resulted NaN or Inf are replaced by 0.
      11 11 11
19
      result = a / b
20
      result[result != result] = .0
21
      result[result == np.inf] = .0
22
      return result
23
24
25
26 class WeightNormConstrainer(object):
      def __init__(self, norm):
27
        self.norm = norm
28
29
      def __call__(self, module):
30
        if hasattr(module, 'weight'):
^{31}
            w = module.weight.data
32
```

```
wn = t.norm(w, p=2, dim=1).detach()
33
34
             ind = t.gt(wn, self.norm)
             div = (divide_no_nan(wn, self.norm) * ind) + (1 *
35

    t.logical_not(ind))

             div = div.unsqueeze_(1)
36
             w.div_(div)
37
38
  class _LeNet(nn.Module):
39
      def __init__(self, layers):
40
         super(_LeNet, self).__init__()
41
        self.input_layer = nn.Sequential(*layers['input_layer'])
42
        self.hidden_layers = nn.Sequential(*layers['hidden_layers'])
43
        self.output_layer = nn.Sequential(*layers['output_layer'])
        self.activation = {}
45
      def layer_features(self, x):
47
        input_layer = self.input_layer(x)
        hidden = self.hidden_layers(input_layer)
49
        logits = self.output_layer(hidden)
        layer_features = {'input_layer': input_layer.data.cpu().numpy(),
51
                            'hidden': hidden.data.cpu().numpy(),
52
                            'logits': logits.data.cpu().numpy()}
53
        return layer_features
54
55
      def get_activation(self, name):
56
           def hook(model, input, output):
57
               self.activation[name] = output.detach().cpu().numpy()
58
          return hook
59
60
      def get_intermediate(self, x):
61
           #TODO: complete this function to return the outputs of first conv and
62
           → first pooling layer - Done
           # Returns the output as a numpy aray for ease of plotting it later
63
           self.input_layer[1].register_forward_hook(self.get_activation('conv1')
           pool1_out = self.input_layer(x)
           return self.activation['conv1'], pool1_out.detach().cpu().numpy()
66
      def forward(self, x):
67
         input_layer = self.input_layer(x)
68
        hidden = self.hidden_layers(input_layer)
69
        logits = self.output_layer(hidden)
70
71
        return logits
72
```

```
73 # We recommend you make this modules as the first component of your input
   → layers
74 class Reshape(t.nn.Module):
       def forward(self, x):
         return x.view(-1,3,32,32)
76
77
  class LeNet(object):
78
       def __init__(self, params, use_custom=False):
79
           super().__init__()
           self.params = params
81
           self.device = t.device('cuda' if t.cuda.is_available() else 'cpu')
82
           self.activations = {'logistic': nn.Sigmoid(), 'relu': nn.ReLU()}
83
           self.pooling = {'avg':nn.AvgPool2d(kernel_size=2,

    stride=2), 'max':nn.MaxPool2d(kernel_size=2, stride=2)}

           # Instantiate model
           t.manual_seed(self.params['random_seed'])
86
           np.random.seed(self.params['random_seed'])
87
           layers = self._initialize_network() if not use_custom else
88

    self._initialize_network_custom()

           self.model = _LeNet(layers).to(self.device)
89
90
       def _initialize_network(self):
91
           # TODO: complete this function - Done
92
           # You may have to use Reshape() and nn.Flatten()
93
           # The architecture may be slightly different with no pooling
94
           if self.params['pooling'] != 'no':
95
               input_layers = [
96
                   Reshape(),
97
                   nn.Conv2d(3, 6, kernel_size=5, stride=1, padding=0),
98
                   self.activations[self.params['activation']],
99
                   self.pooling[self.params['pooling']]
100
101
               hidden_layers = [
102
                   nn.Conv2d(6, 16, kernel_size=5, stride=1, padding=0),
                   self.activations[self.params['activation']],
104
                   self.pooling[self.params['pooling']],
105
                    # nn.Conv2d(16, 120, kernel_size=5, stride=1, padding=0),
106
                    # self.activations[self.params['activation']],
107
                   nn.Flatten(),
108
                   nn.Linear(400, 120),
109
                   self.activations[self.params['activation']],
110
111
                   nn.Linear(120, 84),
                   self.activations[self.params['activation']]
112
               ]
113
```

```
output_layer = [
114
115
                    nn.Linear(84, 10)
116
           else:
117
                input_layers = [
118
                    Reshape(),
119
                    nn.Conv2d(3, 6, kernel_size=5, stride=1, padding=0),
120
                    self.activations[self.params['activation']]
121
                ٦
122
                hidden_layers = [
123
                    nn.Conv2d(6, 16, kernel_size=5, stride=1, padding=0),
124
                    self.activations[self.params['activation']],
125
                    # nn.Conv2d(16, 120, kernel_size=5, stride=1, padding=0),
126
                    # self.activations[self.params['activation']],
127
                    nn.Flatten(),
128
                    nn.Linear(9216, 120),
129
                    self.activations[self.params['activation']],
130
                    nn.Linear(120, 84),
131
                    self.activations[self.params['activation']]
132
                ]
133
                output_layer = [
134
                    nn.Linear(84, 10)
135
                ]
136
           layers = {'input_layer': input_layers,
137
              'hidden_layers': hidden_layers,
138
              'output_layer': output_layer}
139
           return layers
140
141
       def _initialize_network_custom(self):
142
           # Custom CNN network
143
           assert self.params['pooling'] != 'no'
144
145
           input_layers = [
146
147
                Reshape(),
                nn.Conv2d(3, 8, kernel_size=5, stride=1, padding='same'),
148
                self.activations[self.params['activation']],
149
                self.pooling[self.params['pooling']]
150
151
           hidden_layers = [
152
                nn.Conv2d(8, 16, kernel_size=5, stride=1, padding='same'),
153
                self.activations[self.params['activation']],
154
155
                self.pooling[self.params['pooling']],
                nn.Conv2d(16, 64, kernel_size=3, stride=1, padding='same'),
156
                self.activations[self.params['activation']],
157
```

```
self.pooling[self.params['pooling']],
158
                nn.Conv2d(64, 128, kernel_size=4, stride=1, padding=0),
159
                self.activations[self.params['activation']],
160
                nn.Flatten(),
161
                nn.Linear(128, 80),
162
                self.activations[self.params['activation']]
163
164
165
           output_layer = [
                nn.Linear(80, 10)
166
167
168
           layers = {'input_layer': input_layers,
169
              'hidden_layers': hidden_layers,
170
              'output_layer': output_layer}
171
           return layers
172
173
174
       def evaluate_accuracy(self, dataloader):
175
176
           self.model.eval()
           with t.no_grad():
177
                n_correct = 0
178
                n_samples = 0
179
                for batch in iter(dataloader):
180
                    batch_x = t.flatten(batch[0].to(self.device), start_dim=1)
181
                    batch_y = batch[1].to(self.device)
182
                    logits = self.model(batch_x)
183
                    y_hat = t.argmax(logits, dim=1)
184
                    correct = t.sum(y_hat==batch_y)
185
                    n_correct += correct.data.cpu().numpy()
186
                    n_samples += len(batch_x)
187
           accuracy = (n_correct/n_samples) * 100
188
           self.model.train()
189
           return accuracy
190
191
       def evaluate_cross_entropy(self, dataloader):
192
           self.model.eval()
193
           loss_func = nn.CrossEntropyLoss()
194
           with t.no_grad():
195
                n_samples = 0
196
                total_loss = 0
197
                for batch in iter(dataloader):
198
199
                    pass
                    # TODO: Write the code to measure the cross_entropy
200
                    # (Hint, look at the evaluate_accuracy method)
201
```

```
# Be careful with the eval and train modes of the model
202
                    # This should be same as HW5 - Done
203
                    batch_x = t.flatten(batch[0].to(self.device), start_dim=1)
204
                    batch_y = batch[1].to(self.device)
205
206
                    logits = self.model(batch_x)
207
                    loss = loss_func(logits, batch_y)
208
209
                    total_loss += loss.item() * len(batch_x)
210
                    n_samples += len(batch_x)
211
212
           cross_entropy = total_loss/n_samples
213
214
           self.model.train()
215
216
217
           return cross_entropy
       def adjust_lr(self, optimizer, lr_decay):
219
           for param_group in optimizer.param_groups:
220
                param_group['lr'] = param_group['lr'] * lr_decay
221
222
       def adjust_momentum(self, optimizer, step, momentum_change_steps,
223
                             initial_momentum, final_momentum):
224
           mcs = momentum_change_steps
225
           s = min(step, mcs)
226
           momentum = (initial_momentum) * ((mcs-s)/mcs) + \
227
                       (final_momentum) * (s/mcs)
228
           for param_group in optimizer.param_groups:
229
                param_group['momentum'] = momentum
230
231
       def save_weights(self, path):
232
           t.save(self.model.state_dict(), path)
233
234
       def load_weights(self, path):
235
           self.model.load_state_dict(t.load(path,
236
                                                map_location=t.device(self.device)))
237
           self.model.eval()
238
239
       def fit(self, insample_dataloader, outsample_dataloader):
240
           # Instantiate optimization tools
241
           loss = nn.CrossEntropyLoss()
242
243
           optimizer = optim.SGD([{'params':

    self.model.input_layer.parameters()},
```

```
{'params':
244

→ self.model.hidden_layers.parameters()},
                                     {'params':
245

→ self.model.output_layer.parameters(),
                                     'weight_decay':
246

    self.params['output_12_decay']}],
                                     lr=self.params['initial_lr'],
247
248
                                     momentum=self.params['initial_momentum'])
249
           constrainer = WeightNormConstrainer(norm=self.params['weight_norm'])
250
           # Initialize counters and trajectories
251
           step = 0
252
           epoch = 0
253
           metric_trajectories = {'step': [],
254
                                     'epoch': [],
255
                                     'insample_accuracy': [],
256
                                     'outsample_accuracy': [],
257
                                     'insample_cross_entropy': [],
258
259
                                     'outsample_cross_entropy': []
                                     }
260
261
           print('\n'+'='*36+f' Fitting LeNet ({self.params["pooling"]} pooling)
262
            \rightarrow '+'='*36)
           while step <= self.params['iterations']:</pre>
263
264
                # Train
265
                epoch += 1
266
                start_time = time.time()
267
                self.model.train()
268
                for batch in iter(insample_dataloader):
269
                    step+=1
270
                    if step > self.params['iterations']:
271
                         continue
272
273
                    batch_x = t.flatten(batch[0].to(self.device), start_dim=1)
274
275
                    batch_y = batch[1].to(self.device)
276
                    optimizer.zero_grad()
277
278
                    # TODO: make predictions, compute the cross entropy loss and
279
                    → perform backward propagation
                    # This should be same as HW5 - Done
280
                    logits = self.model(batch_x)
281
                    cross_entropy = loss(logits, batch_y)
282
```

```
cross_entropy.backward()
283
284
                  t.nn.utils.clip_grad_norm_(self.model.parameters(), 20)
285
                  optimizer.step()
286
287
                  # Evaluate metrics
288
                  if (step % self.params['display_step'] == 0):
289
                      in_cross_entropy
290
                      out_cross_entropy =
291
                      292
                      in_accuracy

→ self.evaluate_accuracy(insample_dataloader)
                      out_accuracy
293

→ self.evaluate_accuracy(outsample_dataloader)
294
                      print('Epoch:', '%d,' % epoch,
295
                            'Step:', '%d,' % step,
296
                            'In Loss: {:.7f}, '.format(in_cross_entropy),
297
                            'Out Loss: {:.7f}, '.format(out_cross_entropy),
298
                            'In Acc: {:03.3f},'.format(in_accuracy),
299
                            'Out Acc: {:03.3f}'.format(out_accuracy))
300
301
                      metric_trajectories['insample_cross_entropy'].append(in_c | 
302
                      → ross_entropy)
                      metric_trajectories['outsample_cross_entropy'].append(out_
303
                      metric_trajectories['insample_accuracy'].append(in_accura_
304

    cy)

                      metric_trajectories['outsample_accuracy'].append(out_accu_
305

→ racy)

                      metric_trajectories['step'].append(step)
306
                      metric_trajectories['epoch'].append(epoch)
307
                  # Update optimizer learning rate
309
                  if step % self.params['adjust_lr_step'] == 0:
310
                      self.adjust_lr(optimizer=optimizer,
311
                       → lr_decay=self.params['lr_decay'])
312
                  # Update optimizer momentum
313
                  if step % self.params['adjust_momentum_step'] == 0 and \
314
315
                      step < self.params['momentum_change_steps']:</pre>
                      self.adjust_momentum(optimizer=optimizer, step=step,
316
```

```
momentum_change_steps=self.params['m |
317

→ omentum_change_steps'],

                                               initial_momentum=self.params['initia|
318
                                                → l_momentum'],
                                               final_momentum=self.params['final_mo_|
319
                                                   mentum'])
320
                    # Constraint max_norm of weights
321
                    if self.params['apply_weight_norm'] and \
322
                      (step % self.params['adjust_norm_step'] == 0):
323
                        self.model.apply(constrainer)
324
325
                print(f"Time elapsed for epoch {epoch}: {time.time()-start_time}
326

→ seconds")
327
           # Store trajectories
328
           print('\n'+'='*35+' Finished Train '+'='*35)
329
           self.trajectories = metric_trajectories
330
331
332
  def main(POOLING, custom=False):
333
       params = {'model': 'lenet',
334
335
              'display_step': 250,
              'batch_size': 256,
336
              'iterations': 3000, # 3000 or 500
337
              'initial_lr': 0.05,
338
              'lr_decay': 0.5,
339
              'adjust_lr_step': 1000,
340
              'initial_momentum': 0.9,
341
              'final_momentum': 0.95,
342
              'momentum_change_steps': 5_000,
343
              'adjust_momentum_step': 2_000,
344
              'apply_weight_norm': True,
345
346
              'weight_norm': 3.5,
              'adjust_norm_step': 1_000,
347
              'output_12_decay': 0.001,
348
              'pooling': POOLING, # TODO try three options: 'max', 'avg', 'no'
349
              'activation': 'relu',
350
              'random_seed': 0}
351
352
       transform = transforms.Compose([transforms.ToTensor(),
353
       \rightarrow transforms. Normalize((0.5, 0.5, 0.5), (0.5, 0.5, 0.5))])
       trainset = torchvision.datasets.CIFAR10(root='./data', train=True,
354
           download=True, transform=transform)
```

```
insample_dataloader = t.utils.data.DataLoader(trainset,
355
       → batch_size=params['batch_size'], shuffle=True)
       testset = torchvision.datasets.CIFAR10(root='./data', train=False,
356
       → download=True, transform=transform)
       outsample_dataloader = t.utils.data.DataLoader(testset,
357
       → batch_size=params['batch_size'], shuffle=False)
358
       clf = LeNet(params, custom)
359
360
       t0 = time.time()
361
       clf.fit(insample_dataloader, outsample_dataloader)
362
       print(f"Total time elapsed for training: {time.time()-t0} seconds")
363
364
       # TODO: save trajectories and/or plot trajectories, final accuracy, and
365
       \hookrightarrow time elapsed - Done
       # TODO: plot the intermediate outputs using get_intermediate in _LeNet
366
       # To avoid unnecesary pain, saving classifier weights
       if not custom:
368
           clf.save_weights(f'./models/model_{POOLING}.pth')
369
           clf.load_weights(f'./models/model_{POOLING}.pth')
370
371
           with open(f'./results/results_{POOLING}.pkl', 'wb') as file:
372
373
               pickle.dump(clf.trajectories, file)
374
           # Pick one sample from the training set (so that its easier to
375
           → explain what the model is learning)
           index = 1
376
           batch_x, batch_y = next(itertools.islice(iter(insample_dataloader),
377

    index, None))

           sample_x, sample_y = t.flatten(batch_x[:1].to(clf.device),
378

    start_dim=1), batch_y[0].item()

           conv1_out, pool1_out = clf.model.get_intermediate(sample_x)
379
           sample_x = sample_x.detach().cpu().numpy()
380
           intermediates = {
381
                'input': sample_x,
382
                'label': sample_y,
383
                'conv1': conv1_out,
384
                'pool1': pool1_out
385
           }
386
387
           with open(f'./results/visualize_{POOLING}.pkl', 'wb') as file:
388
               pickle.dump(intermediates, file)
389
390
       del clf
391
```

```
Colab_Cell_3

1 import gc
2 import torch

3

4 # Code to clear any memory trace left by previous models to get proper

$\top \text{ training times}$

5 gc.collect()

6 with torch.no_grad():

7 torch.cuda.empty_cache()
```

```
Colab_Cell_4
1 %matplotlib inline
2 import matplotlib.gridspec as gridspec
3 import matplotlib.pyplot as plt
4 from google.colab import files
6 plt.rcParams['figure.dpi'] = 300
7 plt.rcParams['savefig.dpi'] = 300
9 # Function to plot the accuracy and loss graphs for the three configurations
   → of LeNet
10 def plot():
      trajectories = []
11
      config = ['max', 'avg', 'no']
12
      for POOLING in config:
13
          with open(f'./results/results_{POOLING}.pkl', 'rb') as file:
              trajectories.append(pickle.load(file))
15
16
      idx = 0
17
      def plot_trajectory(trajectory_name):
          nonlocal idx, trajectories, config
19
          plot_name = 'Loss' if trajectory_name == 'cross_entropy' else
          → 'Accuracy'
          gs = gridspec.GridSpec(4, 4)
21
          m = 0
22
```

```
23
           plt.figure(idx, figsize = (8,6))
           for i in range(0, 4, 2):
25
                for j in range(0, 4, 2):
26
                    if m == 3:
27
                         break
28
                    if m < 2:
29
                         ax = plt.subplot(gs[i:i+2, j:j+2])
30
                    else:
31
                         ax = plt.subplot(gs[i:i+2, 1:3])
32
33
                    ax.plot(trajectories[m]['step'],
34

    trajectories[m][f'insample_{trajectory_name}'],
                     \  \, \rightarrow \  \, linestyle=\text{'-.'}, \,\, color=\text{'b'}, \,\, label=\text{f'Train} \,\, \{plot\_name\}\text{'})
                    ax.plot(trajectories[m]['step'],
                         trajectories[m][f'outsample_{trajectory_name}'],
                         linestyle='-', color='orange', label=f'Test {plot_name}')
                    ax.set_ylabel(plot_name)
36
                    ax.set_xlabel('Gradient Step')
                    ax.set_title(f'{config[m].upper()} pooling')
38
                    ax.legend(loc='best')
39
40
41
                    m+=1
42
           plt.tight_layout(rect=[0, 0.03, 1, 0.95])
43
           plt.suptitle(f'{plot_name} vs Gradient Steps')
44
           plt.savefig(f'./plots/{plot_name}.png')
45
           plt.show()
46
           files.download(f'./plots/{plot_name}.png')
47
           idx += 1
48
49
       plot_trajectory('cross_entropy')
       plot_trajectory('accuracy')
51
53 plot()
```

```
Colab_Cell_5

1 %matplotlib inline
2 import matplotlib.pyplot as plt
3 from google.colab import files

4
5 plt.rcParams['figure.dpi'] = 300
```

```
6 plt.rcParams['savefig.dpi'] = 300
s # Function to plot the feature map visualizations for a given configuration
   \hookrightarrow of LeNet
9 def visualize(POOLING='avg'):
      with open(f'./results/visualize_{POOLING}.pkl', 'rb') as file:
          intermediates = pickle.load(file)
11
12
      idx = 0
13
      def visualize_images(out, out_name, nrows=2, ncols=3):
14
          nonlocal idx
15
          fig = plt.figure(idx, figsize=(ncols*2,nrows*2))
16
          for fig_idx in range(1, nrows*ncols+1):
17
              ax = fig.add_subplot(nrows, ncols, fig_idx)
18
              ax.imshow(out[fig_idx-1], interpolation='nearest')
              if out_name != 'input':
20
                   ax.set_title(f'Channel {fig_idx}')
21
              ax.axis('off')
22
          plt.suptitle(f'Output Feature Maps of {out_name}' if out_name !=
          plt.tight_layout(rect=[0, 0.03, 1, 0.95])
24
          plt.savefig(f'./plots/visualize_{out_name}.png')
25
26
          plt.show()
          files.download(f'./plots/visualize_{out_name}.png')
27
          idx += 1
28
29
      print(intermediates['label'])
30
      visualize_images(np.transpose(intermediates['input'].reshape((1, 3, 32,
31
      → 32)), (0, 2, 3, 1)), 'input', 1, 1)
      visualize_images(intermediates['conv1'].reshape((-1, 28, 28)), 'conv1',
      \rightarrow 2, 3)
      visualize_images(intermediates['pool1'].reshape((-1, 14, 14)), 'pool1',
       \rightarrow 2, 3)
35 visualize('avg')
```