EE2703: Applied Programming Lab - Assignment No. 3

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1 Abstract

The aim of this assignment is:

- To plot graphs and analyse data
- To generate noise and study how it affects the given data
- To use least squares fitting to model the data
- To study the variation of mean squared error and noise

2 Assignment

2.1 Parts 1 and 2

Importing relevant libraries

```
import pylab as pl
import scipy.special as sp
import sys
```

Defining function g(t;A,B), loading data from 'fitting.dat' and obtaining the true value of the function.

2.2 Part 3

The function with different noise amounts is plotted along with it's true value.

```
sigma = pl.logspace(-1,-3,9) #The Standard Deviations of noise
fig = pl.figure(0)
pl.title('Plot of Data')
pl.plot(t,pl.c_[Y,true_y])
pl.xlabel(r'$t$')
pl.legend(list(sigma) + ['true value'])
pl.grid(True)
pl.show()
```

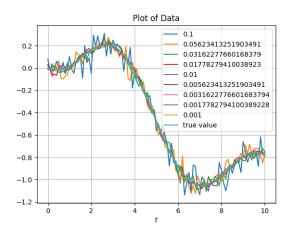


Figure 1: Value vs Time, for different error amounts

2.3 Part 4

We plot the true value of the function obtained from g(t;A,B) we already defined in Part 2.

```
fig = pl.figure(0)
pl.title('Plot of True value')
pl.plot(t,true_y,label = 'true value')
pl.xlabel(r'$t$')
pl.ylabel(r'$1.05*J(t)-0.105t$')
pl.grid(True)
pl.legend()
pl.show()
```

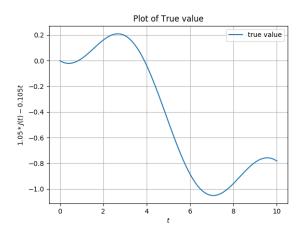


Figure 2: True value of Function obtained without Matrix multiplication

2.4 Part 5

We plot errorbars along with the data in column 1.

```
fig = pl.figure(1)
pl.title('Errorbars')
pl.plot(t,pl.c_[true_y,Y[:,0]])
stdev = pl.std(Y[:,0]-true_y)
pl.errorbar(t[::5],Y[::5,0],stdev,fmt='ro')
pl.xlabel(r'$t$')
pl.legend(['True value','Noisy curve'])
pl.show()
```

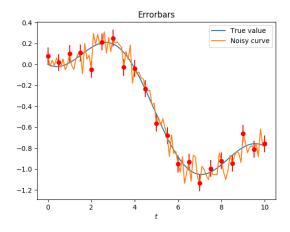


Figure 3: Function with Error Bars

2.5 Part 6

We define new g function which calculates values through matrix multiplication.

$$g_new(t, A, B) = \begin{pmatrix} J_2(t1) & t_1 \\ \dots & \dots \\ J_2(t_m) & t_m \end{pmatrix} \begin{pmatrix} A \\ B \end{pmatrix}$$
 (1)

The two functions are equal

Figure 4: Output of comparing the two vectors

2.6 Part 7

We find mean squared error between data in first column and the assumed model.

2.7 Part 8

We plot the contour plot of E_{ij} and we find that intensity of curves indicate the presence of one critical point (minima). We also mark the value of A = 1.05, B = -0.105 in the plot.

```
fig = pl.figure(2)
pl.title('Contour Plot')
pl.contour(A_list,B_list,E,40)
pl.plot(1.05,-0.105,'ro',label = 'Exact Value')
```

```
pl.annotate(s = 'Exact Value',xy = [0.8,-0.1])
pl.show()
```

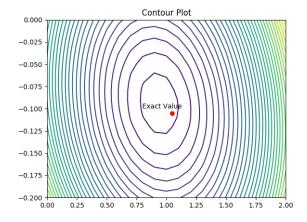


Figure 5: Contour plot of E_{ij}

2.8 Parts 9 and 10

We estimate A and B values from linear least squares fitting for data in all columns (with different noise amounts).

We find the A and B estimated for data of column 1.

```
(A,B),(mse),*_ = pl.linalg.lstsq(pl.c_[sp.jn(2,t),t],Y[:,0],rcond = None)
print('A : ',A)
print('B : ',B)
```

```
A: 1.0555060412435813
B: -0.10612201869553702
```

Figure 6: Output for predicted A and B

We then generate a mean squared error vs noise sigma plot. We also mark the absolute difference between original A,B and the predicted A,B for different columns of data.

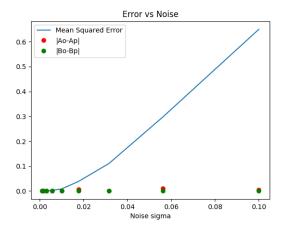


Figure 7: Error VS Noise

2.9 Part 11

We now plot the above graph of error vs noise in log-log scales. The blue line indicates that the mean squared error varies almost linearly with noise sigma in log-log scale.

```
fig = pl.figure(4)
pl.title('Log Error vs Log Noise')
pl.loglog(sigma,mse_list,label = 'Log of Mean Squared Error')
pl.loglog(sigma,pl.absolute(pred_A-1.05),'ro',label = 'log|Ao-Ap|')
pl.loglog(sigma,pl.absolute(pred_B+0.105),'go',label = 'log|Bo-Bp|')
pl.legend()
```

```
pl.xlabel(r'Noise sigma')
pl.show()
```

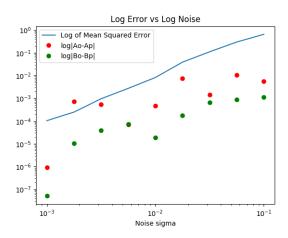


Figure 8: Log Error VS Log Noise

3 Conclusions

- Plotting graphs can make it easier to analyse a situation.
- Least Squares Fitting can be used to estimate the parameters of the linear model for an overdetermined system of equations.
- $\log(error)$ varies nearly linearly with $\log(noise)$.