

# Network Theory DA-2 solutions

$$\text{Phone number} = D_1 D_2 D_3 D_4 D_5 D_6 D_7 D_8 D_9 D_{10}$$

$$D_{avg} = \frac{\sum D_n}{10}, \text{ rounded off}$$

If  $D_{avg}$  is halfway between two numbers, it is rounded to the nearest even integer.

## Question 1

$$Z = \frac{\frac{D_1 - j}{D_2} D_3}{D_1 + D_3 - \frac{j}{D_2}}$$

$$i_1 = \frac{D_4}{D_3 + D_8}$$

$$i_2 = \frac{Z D_6}{D_8 + Z + j D_7}$$

$$i_3 = \frac{D_3 D_5}{(D_1 + D_3 - \frac{j}{2D_2})(D_3 + D_8 + j 2D_7) - D_3^2}$$

## Question 2

$$Z_{Th} = \frac{D_2 D_1 - j D_5}{D_1 + D_2 - j D_5} + \frac{D_4 D_3 + j D_6}{D_4 + D_3 + j D_6}$$

$$V_{Th} = D_{10} \angle \pi \frac{D_1 - j D_5}{D_1 + D_2 - j D_5 - \frac{D_4}{D_3 + D_4 + j D_6}}$$

$$P_{max} = \frac{|V_{Th}|^2}{8(Z_{real})}$$

## Question 3

$$\Delta = D_2 D_3 D_7 + D_2 D_3 D_{avg} + D_2 D_3 D_9 + D_2 D_6 D_7 + D_2 D_6 D_{avg} + D_2 D_6 D_9 + D_2 D_7 D_9 + D_2 D_{avg} D_9 + D_3 D_6 D_7 + D_3 D_6 D_{avg} + D_3 D_6 D_9 + D_3 D_7 D_{avg} + D_3 D_{avg} D_9 + D_6 D_7 D_{avg} + D_6 D_7 D_9 + D_7 D_{avg} D_9$$

$$\Delta_1 = D_1 D_3 D_7 + D_1 D_3 D_{avg} + D_1 D_3 D_9 + D_1 D_6 D_7 + D_1 D_6 D_{avg} + D_1 D_6 D_9 + D_1 D_7 D_9 + D_1 D_{avg} D_9 - D_3 D_7 D_{10} + D_5 D_3 D_7 - D_3 D_8 D_{avg} - D_3 D_{10} D_9 + D_5 D_3 D_{avg} + D_5 D_3 D_9 - D_4 D_6 D_7 - D_4 D_6 D_{avg} - D_4 D_6 D_9 - D_4 D_{avg} D_9 + D_6 D_7 D_8 - D_6 D_7 D_{10} - D_7 D_{10} D_9 + D_5 D_7 D_9$$

$$\Delta_2 = (D_7 + D_{avg} + D_9)(D_3(D_1 - D_4) + (D_2 + D_3 + D_7)(D_4 + D_5 - D_8)) + D_7(D_1 D_9 - D_4 D_7 - D_4 D_9 - D_5 D_7 + D_7 D_8) - (D_{(10)} - D_8)(D_2 D_9 + D_3 D_7 + D_3 D_9 + D_7 D_9)$$

$$\Delta_3 = -D_1 D_3 D_7 - D_1 D_3 D_9 - D_1 D_6 D_7 - D_1 D_7 D_9 - D_2 D_3 D_8 + D_2 D_3 D_{10} - D_2 D_4 D_9 - D_2 D_5 D_9 - D_2 D_6 D_8 + D_2 D_6 D_{10} + D_2 D_{10} D_9 - D_3 D_5 D_7 - D_3 D_5 D_9 - D_3 D_6 D_8 + D_3 D_6 D_{10} + D_3 D_7 D_{10} + D_3 D_{10} D_9 + D_4 D_6 D_7 - D_5 D_7 D_9 - D_6 D_7 D_8 + D_6 D_7 D_{10} + D_7 D_{10} D_9$$

$$i_1 = \frac{\Delta_1}{\Delta}, i_2 = \frac{\Delta_2}{\Delta}, i_3 = \frac{\Delta_3}{\Delta}$$