

1 Introduction to Molecular Dynamics

- The interaction between molecules is represented by the interaction law specified by the potential $U(r_1, \dots, r_N)$ (aka force field) representing the potential energy of N interacting atoms as a function of their positions in 3D space $r_i = (x_i, y_i, z_i)$ [?].

$$\begin{aligned}
 U(\mathbf{r}_1, \dots, \mathbf{r}_N) = & \sum_{\text{bonds}} \frac{a_l}{2} (l_i - l_0)^2 + \sum_{\text{angles}} \frac{b_l}{2} (\theta_l - \theta_0)^2 \\
 & + \sum_{\text{torsions}} \frac{c_l}{2} [1 + \cos(n\omega_l - \gamma_l)] \\
 & + \sum_{\text{atom pairs}} 4\epsilon_{ij} \left[\left(\frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}} \right)^6 \right] \\
 & + \sum_{\text{atom pairs}} k \frac{q_i q_j}{r_{ij}}
 \end{aligned}$$

Typical force-field used in biosystem simulations

- Another set of equations used in MD simulate Potential Enenergy

$$E_P(x) = E_{bonded} + E_{non-bonded} \quad (1)$$

- ab initio* (from the beginning) Born-Oppenheimer:
In quantum chemistry, the computation of the energy and the wavefunction of an average-size molecule is a formidable task that is alleviated by the Born–Oppenheimer (BO) approximation, named after Max Born and J. Robert Oppenheimer[[from wikipedia](#)]
- van-der-Waals

- Energy minimization
- Schrodinger Equation One dimensional wave-function mathematical representation

$$\psi(x, t) = A \cos(\phi + kx - \omega t), \quad (2)$$