

Assignment II

⇒ Given

Not Spam.

① Hi there, how are you today?

② Meeting at BPM today!

③ Please send the Report.

Spam.

① Win a free prize now!

② claim your discount now!

③ limited time offer, click here,

now.

$$P(\text{Not Spam}) = 3/6 = 0.5$$

$$P(\text{Spam}) = 3/6 = 0.5$$

Total vocabulary Size $(V) = 28$.

$$\text{notspam word } (N_{NS}) = 14$$

$$\text{Spam word } (N_S) = 14.$$

Classifying "free meeting tomorrow"

for not spam.

~~for~~ ~~spam~~

$$P(\text{Free} | \text{Notspam}) = 0 + 1/42$$

$$P(\text{Meeting} | \text{notspam}) = 1 + 1/42$$

$$P(\text{tomorrow} | \text{notspam}) = 1 + 1/42$$

$$P(\text{Total} | \text{Notspam}) = P(N_S) \times P(\text{Free} | \text{Notspam}) \times P(\text{meeting} | \text{notspam}) \times P(\text{tomorrow} | \text{notspam})$$

$$= 0.5 \times 1/42 + 2/42 + 2/42$$

$$= 2/74,088 = 0.00002699$$

for Spam.

$$P(\text{free} | \text{spam}) = 1+1/42 = 2/42.$$

$$P(\text{meeting} | \text{spam}) = 0+1/42 = 1/42.$$

$$P(\text{tomorrow} | \text{spam}) = 0+1/42 = 1/42.$$

$$\begin{aligned} P(\text{Total} | \text{spam}) &= P(s) \times P(\text{free} | \text{spam}) \times P(\text{meeting} | \text{spam}) \times \\ &\quad P(\text{tomorrow} | \text{spam}) \\ &= 0.5 \times 2/42 + 1/42 + 1/42 \\ &= 0.000013497. \end{aligned}$$

now

~~for~~ for normalization of "free meeting tomorrow"

$$\begin{aligned} P(NS|N) &= \frac{P(\text{Total} | \text{Not Spam})}{P(\text{total} | \text{Not Spam}) + P(\text{total} | \text{Spam})} \\ &= \frac{0.00002699}{0.00002699 + 0.000013497} \times 100\% \\ &= 66.67\% \end{aligned}$$

$$\begin{aligned} P(S|N) &= \frac{P(\text{Total} | \text{Spam})}{P(\text{Total} | \text{spam}) + P(\text{total} | \text{Not Spam})} \\ &= \frac{0.000013497}{0.000026699 + 0.000013497} \times 100\% \\ &= 33.33\%. \end{aligned}$$

Since $P(NS|N) > P(S|N)$ "free meeting tomorrow" is not Spam.

Again

classifying "claim your free price"

Since All words ("claim", "your", "free", "price") appeared 0 times in Not Spam.

$$\text{Probability} = 0 + 1/42 = 1/42.$$

$$P(\text{Total} / \text{Not Spam}) = 0.5 \times 1/42 \times 1/42 \times 1/42 \times 1/42 \\ = 0.5 / 3111,696$$

again

for Spam.

$$\text{Probability} = 1 + 1/42 = 2/42$$

$$P(\text{Total} | \text{Spam}) = 0.5 \times 2/42 \times 2/42 \times 2/42 \times 2/42 \\ = 8 / 3,111,696$$

for Normalization.

$$\text{Total Sum} = 0.5 + 8 \quad (\text{ignoring common denominator}) \\ = 8.5.$$

$$P(\text{NS} | \text{N}) = 0.5 / 8.5 \approx 5.88\%$$

$$P(\text{S} | \text{N}) = 8 / 8.5 \approx 94.12\%$$

Since $P(\text{S} | \text{N}) > P(\text{NS} | \text{N})$ it's Spam