

Assignment II

⇒ Given

Not Spam.

- ① Hi there, how are you today?
- ② Meeting at 3PM today!
- ③ Please send the Report.

Spam.

- ④ Win a free prize now!
- ⑤ claim your discount
- ⑥ limited time offer. click here,

now.

$$P(\text{Not Spam}) = 3/6 = 0.5$$

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Total vocabulary Size (V) = 28.

notspam word (N_{NS}) = 14

Spam word (N_S) = 14.

Classifying "free meeting tomorrow"

for not spam.

$$P(\text{Free} | \text{Notspam}) = 0+1/42$$

$$P(\text{Meeting} | \text{Notspam}) = 1+1/42$$

$$P(\text{tomorrow} | \text{Notspam}) = 1+1/42$$

$$P(\text{Total} | \text{Notspam}) = P(N_S) : x \cancel{P(\text{Free} | \text{Notspam})} \times P(\text{Meeting} | \text{Notspam}) \times P(\text{tomorrow} | \text{Notspam})$$

$$= 0.5 \times 1/42 + 2/42 + 2/42$$

$$= 2/74,088 = 0.00002699$$

for Spam.

$$P(\text{free} \mid \text{spam}) = 2+1/42 = 3/42$$

$$P(\text{meeting} \mid \text{spam}) = 0+1/42 = 1/42$$

$$P(\text{tomorrow} \mid \text{spam}) = 0+1/42 = 1/42$$

$$\begin{aligned} P(\text{Total} \mid \text{spam}) &= P(s) \times P(\text{free} \mid \text{spam}) \times P(\text{meeting} \mid \text{spam}) \times \\ &\quad P(\text{tomorrow} \mid \text{spam}) \\ &= 0.5 \times 3/42 \times 1/42 \times 1/42 \\ &= 0.000013497 \end{aligned}$$

now

~~for~~ for normalization of "free meeting tomorrow"

$$\begin{aligned} P(NS|N) &= \frac{P(\text{Total} \mid \text{Not Spam})}{P(\text{total} \mid \text{Not Spam}) + P(\text{total} \mid \text{spam})} \\ &= \frac{0.00002699}{0.00002699 + 0.000013497} \times 100\% \\ &= 66.67\% \end{aligned}$$

$$\begin{aligned} P(S|N) &= \frac{P(\text{Total} \mid \text{Spam})}{P(\text{Total} \mid \text{spam}) + P(\text{total} \mid \text{Not Spam})} \\ &= \frac{0.000013497}{0.00002699 + 0.000013497} \times 100\% \\ &= 33.33\% \end{aligned}$$

Since $P(NS|N) > P(S|N)$ "free meeting tomorrow" is not Spam.

Again

classifying "claim your free price"

Since all words ("claim", "your", "free", "price") appeared 0 times in Not Spam.

$$\text{Probability} = 0 + \frac{1}{42} = \frac{1}{42}$$

$$P(\text{Total} | \text{Not Spam}) = 0.5 \times \frac{1}{42} \times \frac{1}{42} \times \frac{1}{42} \times \frac{1}{42}$$
$$= \frac{0.5}{3,111,696}$$

again

for spam.

$$\text{Probability} = 1 + \frac{1}{42} = \frac{2}{42}$$

$$P(\text{Total} | \text{spam}) = 0.5 \times \frac{2}{42} \times \frac{2}{42} \times \frac{2}{42} \times \frac{2}{42}$$
$$= \frac{8}{3,111,696}$$

for Normalization.

$$\text{Total Sum} = 0.5 + 8 \quad (\text{ignoring common denominator})$$
$$= 8.5$$

$$P(\text{NS} | N) = 0.5 / 8.5 \approx 5.88\%$$

$$P(S | N) = 8 / 8.5 \approx 94.12\%$$

Since $P(S | N) > P(\text{NS} | N)$ its spam