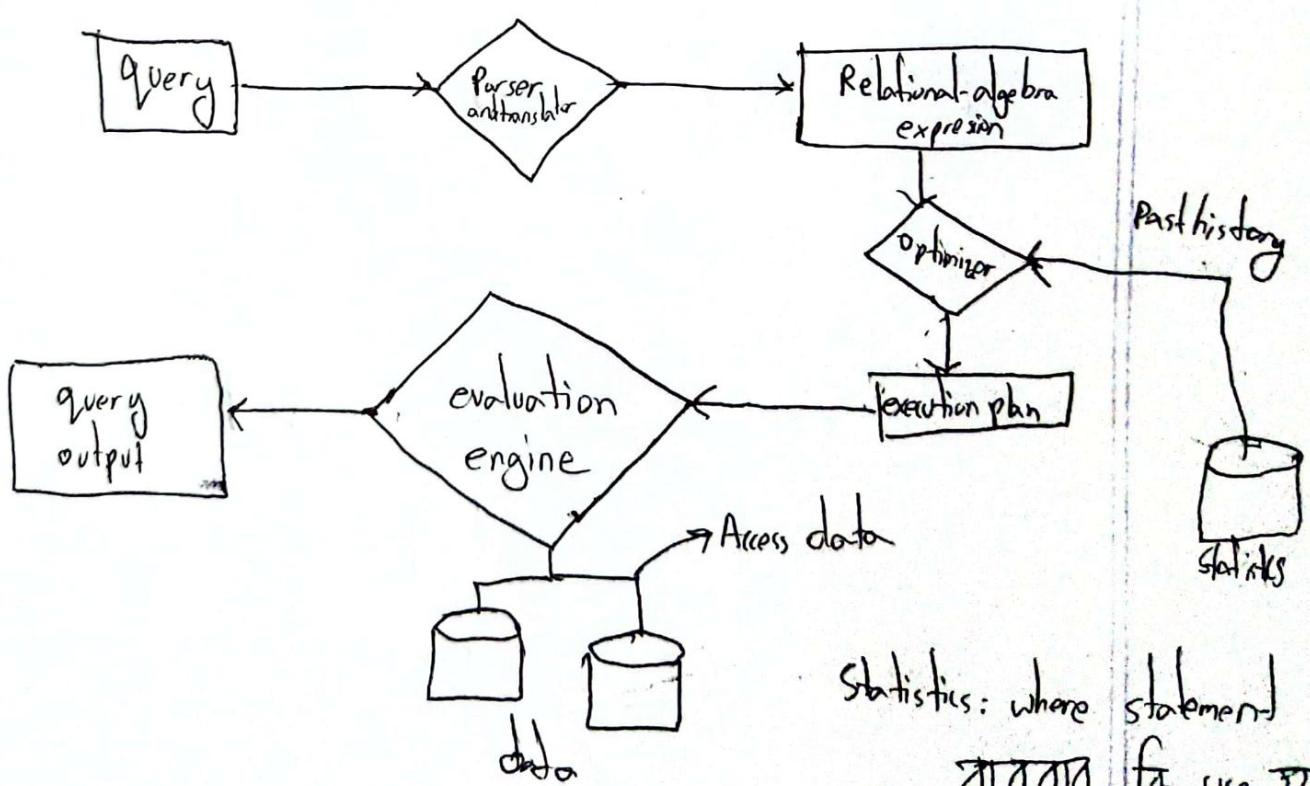


CPU time → time to parse query

elapsed time → Time to retrieve query and display
query results

Query Optimization

Query processing algorithms



Statistics: where statement
for use 2D
tuple for 1D access
2D

Relational algebra expression :

$\sigma_{\text{salary} < 75000} (\pi_{\text{salary}}(\text{instructor}))$ equivalent to
 $\pi_{\text{salary}} (\sigma_{\text{salary} \geq 75000} (\text{instructor}))$
[Select salary from instructor where salary < 75000]

Query optimization: Amongst all equivalent evaluation, choose the one with lower cost.

Query cost : Disk Cost + Access Cost + CPU processing cost
↓
Highest cost

Need to find average seek cost to find block
+ average block read cost
+ average block write cost

Transfer cost : $b \cdot t_r + s^2 \cdot t_s$ $t_r = \text{time do transfer one block}$
 $t_s = \text{time to...}$

If block is kept in buffer, performance better, but
to keep more blocks, needs A more buffer space.

Selections:

Linear search cost : $(br/2)$ block transfer + block
Using indexes : $hi = \text{height of BT tree}$
primary key index : (equality or key):
cost : $(hi+1) * (t_1 + t_2 + t_3)$

Join operations :

- ↳ Nested loop join
- ↳ Block nested loop join
- ↳ Indexed nested loop join

r \bowtie s

for each tuple t_r in r do begin

 for each tuple t_s in s do begin

 test(t_r, t_s) if they satisfy, join

r is outer relation, s is inner.

Since all pairs need to be checked this is

Total cost

$n_r \times b_s + b_r$ block transfers
↓
for every tuple of relation r Access all blocks of relations

$n_r + b_r$ total seek

Join of students and takes:

Number of records: Student: 5000 Take: 10000

Number of blocks: Student: 100 takes: 400

Student outer relation

Block transfers: ~~5000 + 10000 + 500~~

$$5000 \times 400 + 100 = 2000100$$

black transfer

Seeks: $5000 + 100 = 5100$

But if take is outer:

$$\text{Block transfers: } 10000 \times 100 + 400 = 1000400 \text{ much less}$$

Block nesting: Instead of matching tuple, match every block

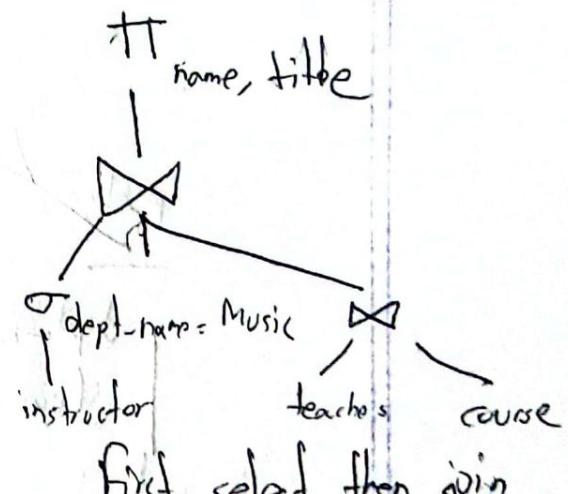
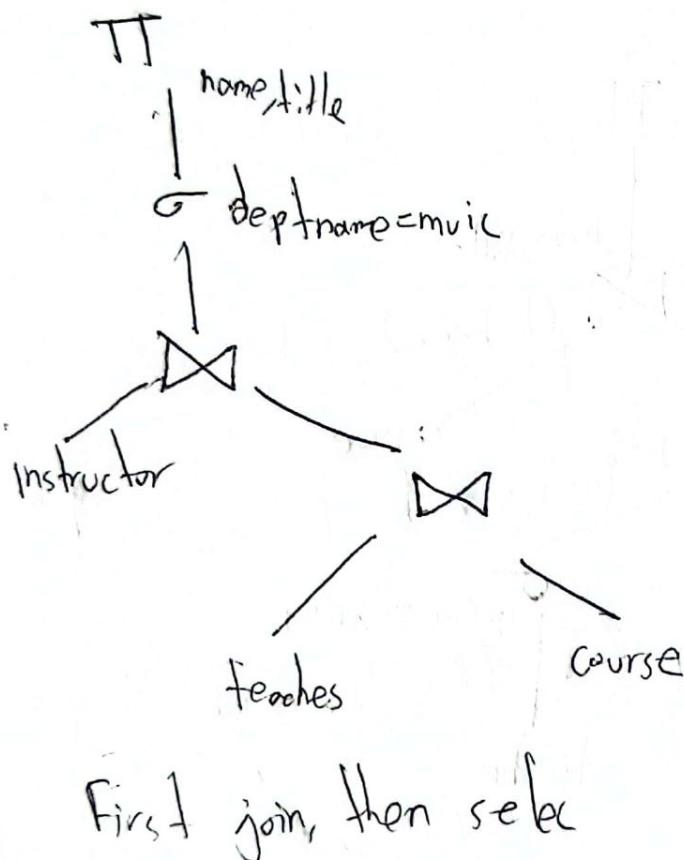
→ Cost will come down by a factor

of $M - 2$ where $M = \text{memory unit in size blocks}$

$$\text{Cost} = \left\lceil \frac{\text{br}}{(M-2)} \right\rceil * b_s + \text{br} \text{ block transfer}$$
$$2 \left\lceil \frac{\text{br}}{(M-2)} \right\rceil \text{ seeks}$$

Evaluating query:

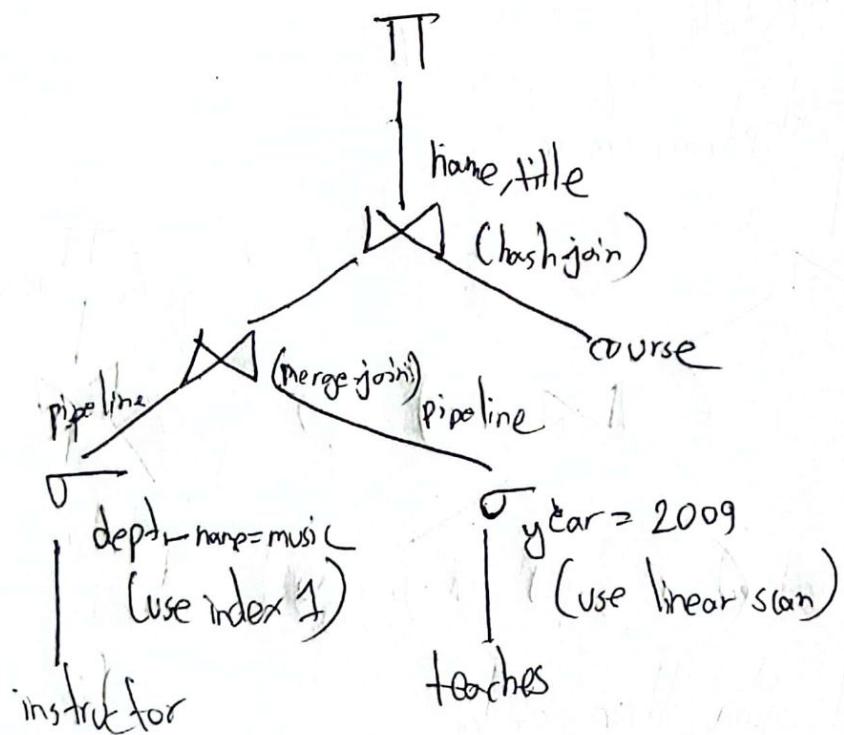
course (courseID, title, deptname)
 instructor (ID, name, deptname)
 teaches (ID, course ID, sec ID, sem)



These are equivalent
 Second one
 is ~~better~~ better

$\Pi_{\text{name}, \text{title}} (\sigma_{\text{dept_name} = \text{"Music"} \wedge \text{year} = 2009}$

(instructor \bowtie teaches \bowtie course)



Query optimization:

- Generate candidates using equivalence rules
- Alternative query plans
- Choose the cheapest plan using estimated cost

Cost: number of tuples number of distinct values

Transformation of relational expressions:

Equivalence rule \rightarrow Generate two expression that generates the same tuples
 \hookrightarrow Order of tuples are irrelevant.

Rules:

Conjunctive selection

$$\sigma_{\theta_1 \wedge \theta_2} (E) = \sigma_{\theta_1} (\sigma_{\theta_2} (E))$$

This is commutative

$$\sigma_{\theta_1} (\sigma_{\theta_2} (E)) = \sigma_{\theta_2} (\sigma_{\theta_1} (E))$$

But cost will be different

In sequence of projections

$$\begin{aligned}\text{PR}_{L_3}(\text{PR}_{L_2}(\dots(\text{PR}_{L_1}(E)))) \dots \\ = \text{PR}_{L_1}(E)\end{aligned}$$

Other projections can be ignored

Important

$$\sigma_{\theta} (E_1 \times E_2) = E_1 \bowtie_{\theta} E_2$$

$$\sigma_{\theta_1} (E_1 \bowtie_{\theta_2} E_2) = E_1 \bowtie_{\theta_1 \cap \theta_2} E_2$$

$$E_1 \bowtie_{\theta} E_2 = E_2 \bowtie_{\theta} E_1$$

Cost can be different

$$*(E_1 \bowtie E_2) \bowtie E_3 = E_1 \bowtie (E_2 \bowtie E_3)$$

$$*(E_1 \bowtie_{\theta_1} E_2) \bowtie_{\theta_2 \wedge \theta_3} E_3$$

$$= E_1 \bowtie_{\theta_1 \wedge \theta_3} (E_2 \bowtie_{\theta_2} E_3)$$

Provided θ_2 present in E_2 and E_3

* When all attributes in θ_0 involve only one E_i being joined

$$\sigma_{\theta_0} (E_1 \bowtie_{\theta_0} E_2) = (\sigma_{\theta_0} (E_1)) \bowtie_{\theta_0} E_2$$

$$*\sigma_{\theta_1 \wedge \theta_2} (E_1 \bowtie_{\theta_0} E_2) = (\sigma_{\theta_1} (E_1)) \bowtie_{\theta_0} (\sigma_{\theta_2} (E_2))$$

8(a)

$$\pi_{L_1 \cup L_2} (E_1 \bowtie_{\theta_0} E_2) = (\pi_{L_1} (E_1)) \bowtie_{\theta_0} (\pi_{L_2} (E_2))$$

$$\pi_{L_1 \cup L_2} (E_1 \bowtie_{\theta_0} E_2) = \pi_{L_1 \cup L_2} ((\pi_{L_1 \cup L_3} (E_1)) \bowtie_{\theta_0} (\pi_{L_4} (E_2)))$$

Query: Find the names of all instructors in the Music dept who have taught a course in 2009, along with the titles of the courses that they taught.

$\Pi_{name, title} (\sigma_{dept_name = "Music"} \wedge year = 2009$
 $(instructor \bowtie (teaches \bowtie \Pi_{course_id, title} (course)))$

$\Pi_{name, title} (\sigma_{dept_name = "Music"} \wedge year = 2009$
 $((instructor \bowtie teaches) \bowtie \Pi_{course_id, title} (course)))$

course(courseID, title, dept-name, credits)
instructor(ID, name, dept-name, salary)
teaches (ID, course id, secid, semester, year)

$\Pi_{name, title}$

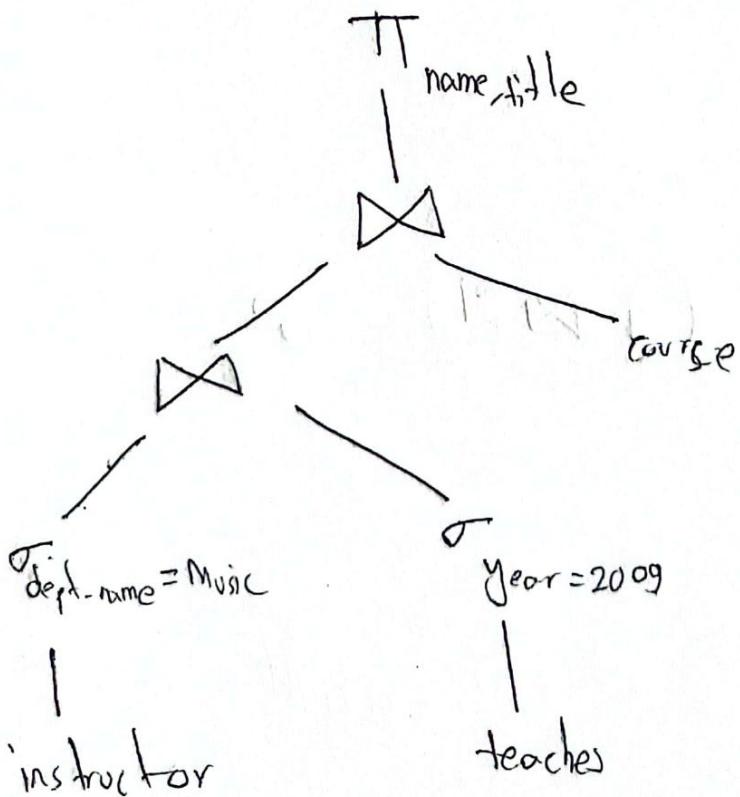
1.8

$\sigma_{dept_name = "Music"}(\text{instructor}) \bowtie \sigma_{year = 2009}(\text{teacher})$

(σ , \bowtie)

Do this, it is better

- * $\text{instructor} \bowtie \text{teachers}$ selects all tuples, so select first
then join this is bad!!



→ Equivalent and better

Push projections :

$\pi_{name, title} (\sigma_{dept_name} = "Music" \text{ (instructor)} \bowtie \text{teacher})$

$\bowtie \pi_{course-id, title} (course)$

Practice

45 45

key না হলে ?

এটি block র ক্ষমতা

$$b_r = \left[\frac{n_r}{f_r} \right]$$

Total tuple $\rightarrow n_r$

r relation A attribute ক্ষমতা

$V(A, r)$

$St(A, r) =$

Selection
Cardinality

$$\left[\frac{n_r}{V(A, r)} \right] \rightarrow$$

Total tuple

$\rightarrow A$ attribute
 r relation ক্ষমতা

প্রতি ক্ষমতা attribute বাটে block এ

Binary search ~~করে~~ $O(\log b_r)$ per
block র একটি attribute খুজতে ক্ষমতা

Ans: $\log b_r + \left[\frac{St(A, r)}{f_r} \right] - 1$

$$f_{ac} = 20$$

$$v(b.name, ac) = 50$$

$$v(bala, ac) = 500$$

$$h_{ac} = \frac{10000}{10000}$$

Select branch "perridge" from account

$$b_{ac} = \left\lceil \frac{n_{ac}}{f_{ac}} \right\rceil = 500$$

$$\frac{st(A, r)}{fr}$$

$$\log(500) + \frac{\frac{10000}{10000 - 50} - 1}{20} - 1 \\ = \log(500) + \frac{20}{10} - 1$$

Equality on key : B+ Tree height + 1

Equality on primary index : B+ Tree height +
 $\left\lceil \frac{s+1}{fr} \right\rceil$

Equality on key at 2nd

~~No. of~~ Fanout = 20 No. de = 50

treeheight (min) = 3

Equality on key = $3+1=4$

Equality on primary index = $3 + \left\lceil \frac{\frac{10000}{50}}{20} \right\rceil$
= $3 + 10 = 13$

DBMS Query

$\sigma \rightarrow \text{select}$

Select from webpage where

author = John

(σ index-lookup
author = "John")

(Webpage)

(\bowtie) index-job occur
url = url

(\bowtie) main-many -hash-join σ index-lookup
with join language = 'French' (bad)

X

(\bowtie)
Left outer join → Left side फिल्टर हो
Right Null Σ

(\bowtie) → तो फिल्टर Null

(\bowtie) → Inner join

Table join

Select index^ author from webpage where author = "French"
and language = "French".

$$T(\text{Webpage}) = V(\text{Occurs}, \text{url}) = 10^9$$

$$T(\text{Occurs}) = 10^{12}$$

$$T(\text{Word}) > 10^6 = V(\text{Occurs}, \text{wid})$$

$$V(\text{Webpage}, \text{author}) = 10^7$$

$$V(\text{Word}, \text{language}) = 100$$

Block size = 15

→ SST Data

$$Sc(\text{Webpage}, \text{Author}) = \left\lceil \frac{T(\text{Webpage})}{V(\text{Webpage}, \text{Author})} \right\rceil$$

Distinct average in total tuples

$$= \frac{10^9}{10^7} = 10^2$$

L → Number of author in per block average

$$Sc(\text{Occur}, \text{prl}) = \left\lceil \frac{T(\text{Occur})}{V(\text{Occurs}, \text{prl})} \right\rceil$$

$$Sc(\text{Occur}, \text{URL}) = \left\lceil \frac{T(\text{Occur})}{V(\text{Occurs}, \text{url})} \right\rceil$$

$$= \frac{10^{12}}{10^9} = 10^3$$

Join $Sc(\text{Webpage}, \text{Author}) \bowtie Sc(\text{Occur}, \text{URL}) = 10^5$

Main-memory \rightarrow block access নাম না। So block access

Primary index হল 10 টির তার্ফে

3rd জো কুন্ত কোনো কিছু নই

$$T(\text{word}) = 10$$

$$S_c(\text{Word, language}) = \left[\frac{T(\text{word})}{V(\text{Word, Language})} \right]$$
$$= \frac{10^6}{100} = 10^4$$

Webpage.url = primary
Webpage.author = secondary
occurs.url = secondary
occurs.wid = primary
word.wid = primary

word.language = secondary index

Total =

$$\cancel{10^5 + 0 + 10^6}$$

$$\cancel{10^2 + 10}$$

Total =

$$10^2 + 10^5 + 10^4$$

\downarrow \downarrow \swarrow
 first lookup Join 4th lookup
 Primary ~~π~~ secondary fn(D) replace.



$$(i) \frac{10^2}{10} + \frac{10^5}{10} + \frac{10^4}{10} + 0$$

$$\begin{aligned}
 & \frac{10^2}{10} + 10^2 \times \frac{10^3}{10} + \frac{10^4}{10} + 0 \\
 & (i) \quad (ii) \quad (iii) \quad (iv)
 \end{aligned}$$

$$= 10 + 10^4 + 10^3 + 0$$

=

Left side এর পাই মানে কিন্তু আমি কিরণ করি
 Right side primary পাই মানে আমি করি কিরণ
 করি পাই করি কিরণ করি কিরণ করি

∞

Transaction

A transaction is a unit of program execution that accesses possibly updates various data items.

To ~~not~~ preserve integrity of database, a system must ensure:

Atomicity: Either all operations of the transaction are properly reflected in the database or none are.

Consistency: Execution of a transaction in isolation preserves consistency of database.

Isolation: Transaction can occur concurrently although each transaction must be unaware of the other executing transaction.

Durability: After a transaction completes successfully the changes it made to the database persist.

States:

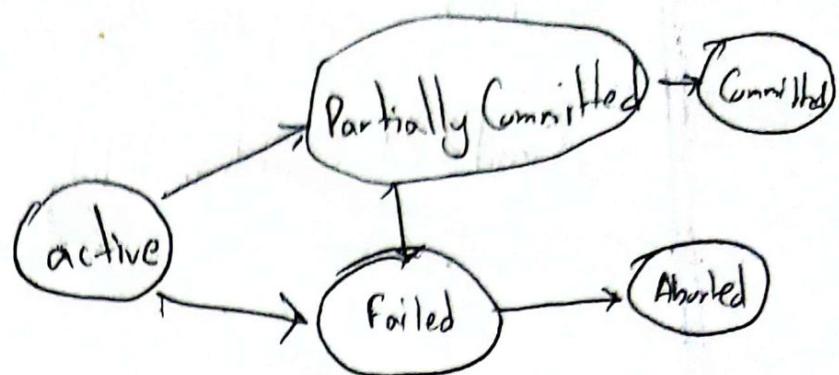
Active

Partially committed

Failed

Aborted

(Committed)



Concurrent executions: Multiple transaction are allowed to run concurrently in system

Schedule

Schedules: Sequence of instructions that specify the chronological order in which ~~one~~ instructions in concurrent transactions are executed.

A transaction that fails to successfully complete its execution will have an abort instruction as last statement

Serializability:

Each transaction preserves database consistency

Conflict serializability

	A	B
T	w	r
T	w	r
w	r	w
w	w	w



If a schedule S can be transformed into a ~~conflict~~ schedule S' by a series of non-conflicting instructions, we say S and S' is conflict equivalent.

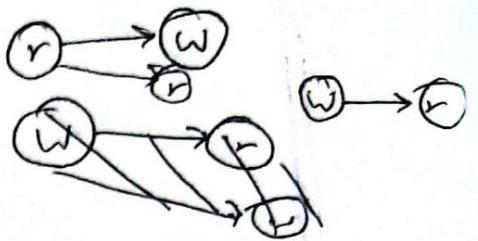
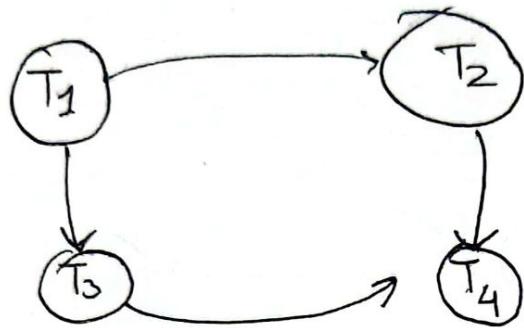
Schedule S is conflict serializable if it is conflict equivalent to serial schedule.

View Serializable

A schedule S is view serializable if its equivalent to a serial schedule.

$S \xrightarrow{\text{is}} \text{serial}$, $S' \xrightarrow{\text{is}} \text{serial}$

Testing serializability: Precedence graph



(T₅)

If precedence graph is acyclic, serializability order can be obtained by ~~by~~ topological sort

<u>A</u>	<u>Pre</u>	
1	1	TP
0	0	TN
0	1	FP
0	0	FN

Recovery System: Database ট্যান্ডেল করে কোর্স করে তার

- action recover করতে পারি,

stable system design \rightarrow Copy
 \rightarrow Disperse elements in HDD

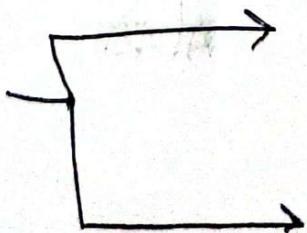
Log based recovery

Shadow based recovery

Log based recovery

Postpone করা

Deferred database modification



যা করার লগ এ করা, মডেলিং সিস্টেম গুলি করে
 So crash করলে Log গুলি data loss হবে

$\langle T_0 \text{ Start} \rangle$
 $\langle T_0, A, 950 \rangle$
 $\langle T_0, B, 2050 \rangle$

$\langle T_0 \text{ start} \rangle$
 $\langle T_0, A, 950 \rangle$
 $\langle T_0, B, 2050 \rangle$
 $\langle T_0 \text{ commit} \rangle$
 $\langle T_1 \text{ start} \rangle$
 $\langle T_1, C, 600 \rangle$
(b)

$\leq T_0$

Commit হওয়ার আগে crash হলে no need to roll

Atomicity: # Minimum individual unit. একটি স্থান
মুক্তি, partial হওতে না

A give B. A-50, B+50 $\xrightarrow{\text{করে}} \text{20}$

Consistency: ফল কোথায় হিসাব মিলতে 20 ,
A 3 B 20 হাতে দুটি same.

Isolation: Parallel operation must occur in
isolation. A-50 B+50 আন্তর্ভুক্ত operation

Durability: পুরুষ ধ্রুব হিসেব হিসাব থাকতে

Inconsistent state জ পুরুষ back হ্যায়.

redo(T_0) if database is not done. R. Idempotent.

প্রতিটি redo করলে 3 ক্ষেত্রে



$T_2 \Rightarrow T$

$$\text{Confidence } (A \Rightarrow B) = P(B|A) = \frac{\text{Sup}(A \cup B)}{\text{Sup } A}$$

$$T_2 \Rightarrow \{T_1, T_5\} = \frac{2}{7}$$

Immediate DB modification:

Immediately DB modify \exists

So, log \circ ~~trace~~ value present value ~~trace~~

$\langle T_0 \text{ start} \rangle$

$\langle T_0, A, 1000, 950 \rangle$

$\langle T_1, B, 2000, 2050 \rangle$

$\langle T_0 \text{ start} \rangle$

$\langle T_0, A, 1000, 950 \rangle$

$\langle T_0, B, 2000, 2050 \rangle$

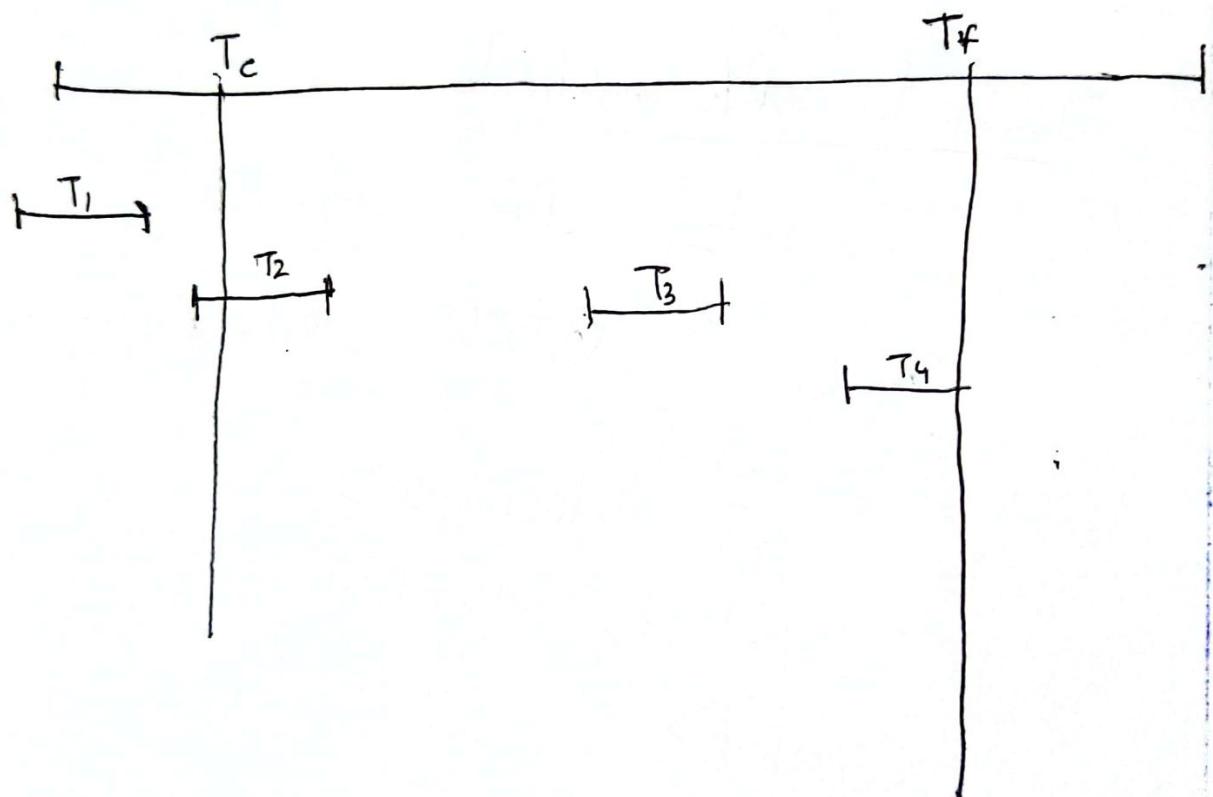
$\langle T_0 \text{ commit} \rangle$

\downarrow
Undo ~~redo~~ redo

Example of Checkpoints.

Database recovery : Undo redo crash করল
তখনে ট্র্যাক স্থাপ

Checkpoint: Flag. অজনক ফিল গোমাতা জু স্ট্রাক
ফিল আছে



$T_2 \rightarrow$ redo

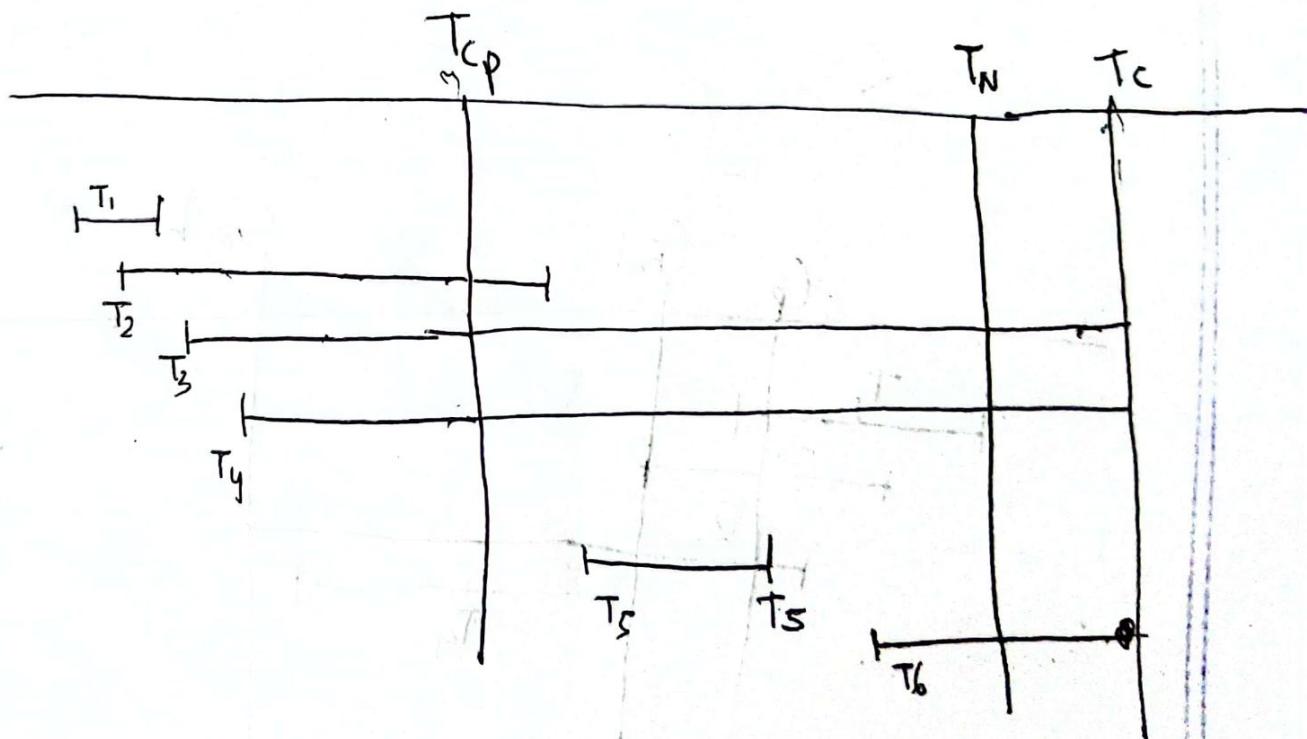
$T_3 \rightarrow$ Redo

$T_4 \rightarrow$ Undo করে redo (Commit হ্য নাই)

T_1

$\langle Ckpt(T_2, T_3, T_4) \rangle$

$\langle End\ Ckpt \rangle$



$T_2 \rightarrow$ Redo $T_3 \rightarrow$ Undo and Redo $T_4 \rightarrow$ Undo and Redo

$T_1 \rightarrow$ ~~for T_2~~

$T_2 \rightarrow$ Redo

$T_3 \rightarrow$ Undo & ~~for T_2~~ Redo

$T_4 \rightarrow$ //

$T_5 \rightarrow$ Redo
 $T_6 \rightarrow$ Undo

~~$T_5 \rightarrow$ Redo~~

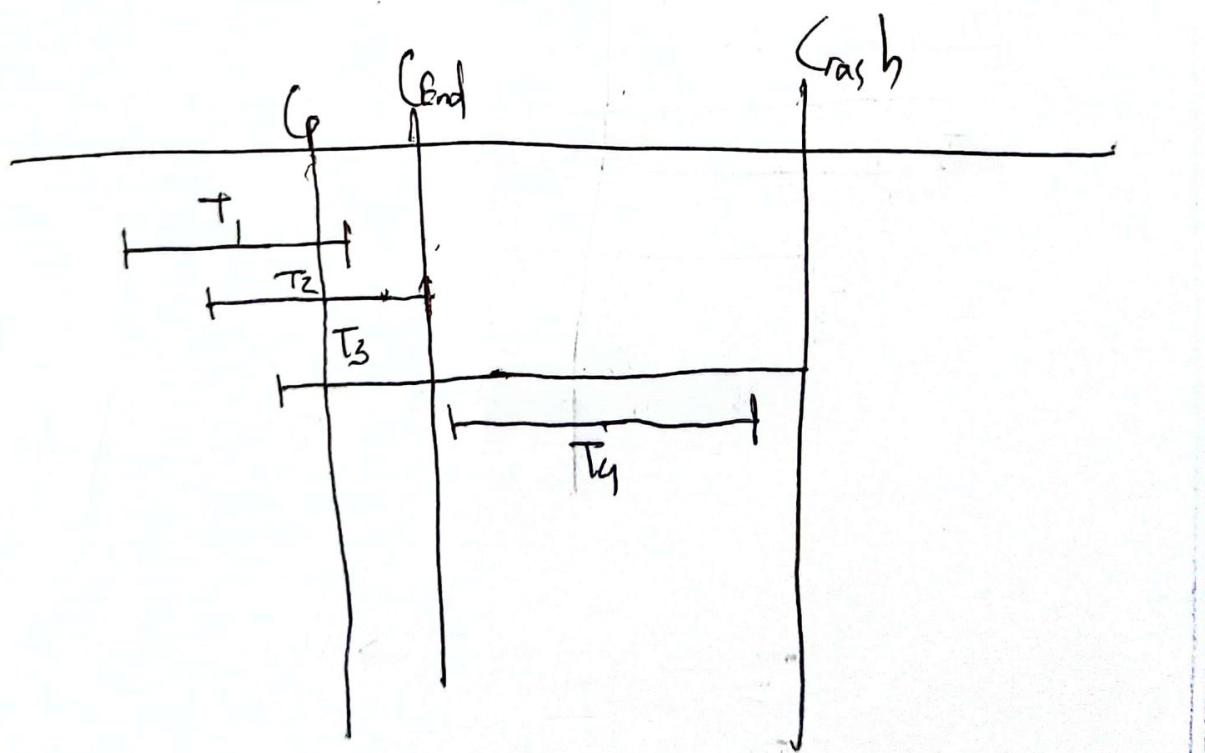
~~$T_6 \rightarrow$ Undo and redo~~

$A \rightarrow \underline{B}$ $B \rightarrow 20$
 $D \rightarrow 2000$
 $C \rightarrow 100$

(b) $\exists \text{ start } T_i >$

~~start~~

<



$T_3 \rightarrow \text{undo and redo}$ $T_4 \rightarrow \text{redo}$

DBMS

Concurrency Control:

A database must be

↳ Conflict Serializable

↳ Recoverable and possibly cascadeless

Goal → To develop concurrency protocols that will assure serializability

↳ Cascadeless database

Make transactions ACID

I → Isolation → Once a portion is at use others cannot use it → Bad for concurrency

So, Lock must be in such a way concurrency has to ensured.

Lock-based protocols: Two ~~not~~ modes

Exclusive mode: Two try to write, you do not know who ~~write~~ have written.

Shared mode: Anyone can read at any time

Transaction can be X-lock S-lock and
unlocked using unlock(Q)

Lock compatibility mode:

	S	X
S	true	false
X	false	false

Reading and writing together is incompatible and vice versa.

If a lock cannot be granted, the tx must wait until all locks are released.

Let A and B be two Tx on T1 and T2

* Tx T1 transfers \$50 from B to A.

* Tx T2 displays total amount of money in A and B, A+B

$$A = \$100 \quad B = \$200$$

T1 :

lock - X(B)
read (B)

$B := B - 50;$
^{write(B)}
unlock (B);

lock - X(A);

$A := A + 50;$

write(A)

unlock (A);

T2 :

lock - S(A)
read (A);

unlock (A);
lock - S(B);
read (B);
unlock (B)

display (A+B);

If ~~T1 and T2~~ T2 run after T1 then
Concurrency is maintained.

Another concurrency

T1
lock - X(B)

read (B)

$B := B - 50$

write(B)

unlock (B)

T2

Concurrency control

grant - X(B, T₁)

T₁

T₂

Concurrency control manager

lock - S(A)

read(B)

B := B - 50

write(B)

unlock(B)

grant - S(A, T₂)

lock - S(A)

read(A)

unlock(A)

lock - S(B)

grant - S(A, T₂)

read(B)

unlock(B)

display(A+B)

grant - S(B, T₂)

lock - X(A)

A := A + 50

write(A)

unlock(A)

grant - X(A, T₁)

This is concurrent. But here Total is 50\$ is less.

Hence, this is not proper concurrency

If unlocking is pushed to the end.

T3:

lock-X(B)

T4:

lock-S(A)
read(A)

~~lock-X(A)~~

}

unlock(B)
unlock(A)

Here, T4 will correctly show sum

T3

T4

lock-X(B)

lock-S(A)

read(A)

lock-S(B) →

B is locked
so T4 waiting

lock-X(A) →

T4 holds shared

This is "deadlock"!!

When deadlock occurs, system must rollback transactions.

Locking protocol → Conflict ensured. serializability must be

Two phase locking protocol :

Phase - 1 : Grow Phase

↳ T_x may obtain locks

→ T_x may not release locks

Phase 2 : Shrinking phase

↳ T_x may release locks

→ T_x may not obtain locks

lock conversions in two phase locking

first phase: Can obtain lock-S
" " lock-X
upgrade lock-S to lock(X) (upgrade)

Second phase: Release lock-S
Release lock-X
downgrade lock-X to lock-S

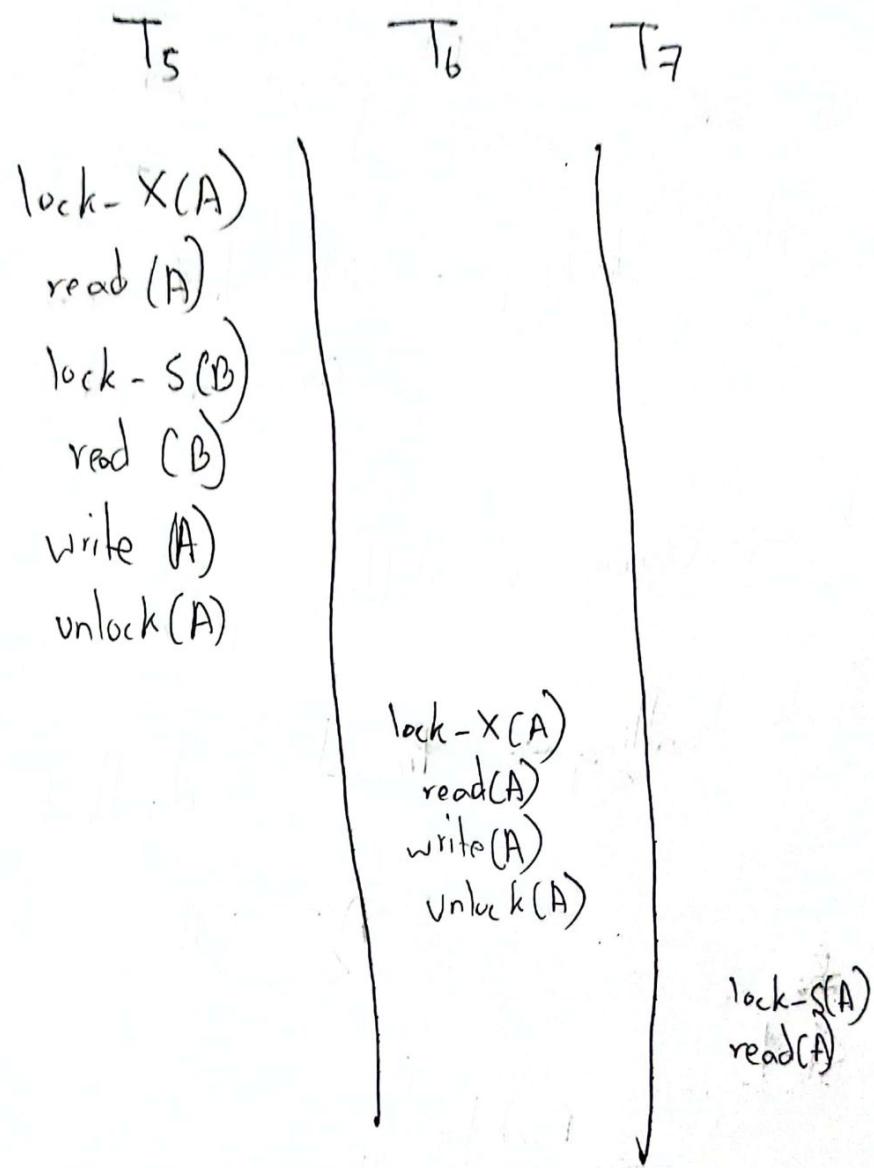
Starvation \rightarrow lock ~~गूँड़ी~~ घार घाड़ि ना \rightarrow starvation,
~~जुहो~~ tx lock ~~मार्गदर्शक~~ ना

Starvation occurs if concurrency is badly designed.

↳ Can cause repeated ~~repeated~~ deadlocks and roll-backs

Deadlocks can occur in any system, they are necessary evil.

Possibility of cascading roll Back



Here After failure of T5 to read A

prevent cascading roll-back, strict two phase

locking → All exclusive locks are held till commit or abort
OR even stricter rigorous two phase locking → All locks are held till commit or abort

Lock → occurs on different processes

Deadlock handling → prevent deadlock



Strategies

→ Each tx lock all data items before execution

→ Partial ordering of all data items, lock items in that order

Problem: Brings down concurrency
Delay transactions

Schemes \rightarrow wait-die scheme \rightarrow non preemptive

Older transaction should never wait for younger, younger transactions never wait for older ones, they are rolled back.

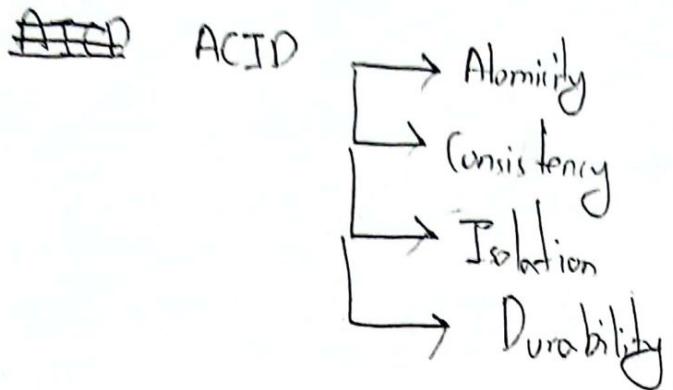
A tx may do several times before acquiring lock round-wait \rightarrow preemptive

Older tx preempts younger tx
younger tx wait for older ones

Timeout based schemes

\hookrightarrow starvation possible

Recovery:



④ Transaction failure:

Logical errors

System errors

④ System crash

④ Disk failure

Recovery algorithm:

1. During normal tx, collect info to recover from failures.

2. Ensure atomicity, consistency and durability of the tx.

Failure during data transfer can result in inconsistent copies.

Block transfer can result in successful completion, partial failure and total failure

Protecting storage media from failure during transfer

→ Write the information into two physical blocks, first followed by second

Copies of a block may differ. ~~in~~ during failure

To recover from failure:

1. Find inconsistent blocks

→ If error in checksum, replace error

2. If no error, replace second by first.

Data Access:

Physical block \rightarrow Main disk block

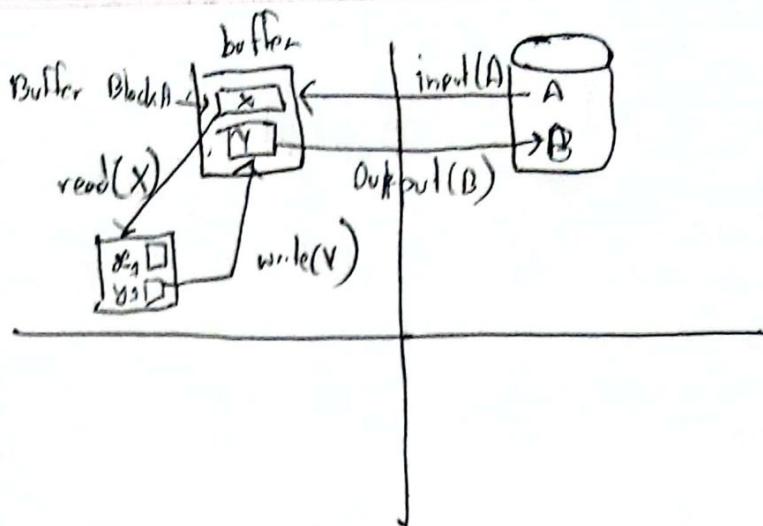
System buffer blocks \rightarrow blocks temporarily residing in main memory

$\text{input}(B)$ \rightarrow physical block (B) to main memory
 $\text{output}(B)$ \rightarrow transfers the buffer block B
on to the disk

$\text{read}(X) \rightarrow$ assign ~~to~~ the value of data item

$\text{write}(X) \rightarrow$ X to local variable x;

assign the value of local variable x; to buffer block.



Log based recovery mechanism

A log is kept on stable storage

Database modification
log

Update log must be written before a database item is written

Immediate modification → allows updates to the buffer before tx commits

Deferred modification → performs updates only at the time of tx commit.

Log

Write

Output

$\langle T_0 \text{ start} \rangle$

$\langle T_0, A, 1000, 950 \rangle$

$\langle T_0, B, 2000, 2050 \rangle$

$$A = 950$$

$$B = 2050$$

$\langle T_0 \text{ commit} \rangle$

$\langle T_1 \text{ start} \rangle$

$\langle T_1, C, 700, 600 \rangle$

$$C = 600$$

Contains updated value of B
 B_B, B_C
→ Update of file
 C , happening
before T_1 commit

B_A

Undo and redo operations

Undo → Revert the effect of an update

Redo → Doesn't revert to odd.

Rewrite the new value

$\langle T_0 \text{ start} \rangle$

$\langle T_0, A, 1000, 950 \rangle$

$\langle T_0, B, 2000, 2050 \rangle$

(A)

$\text{undo}(T_0)$: B restored to 2000 and A to 10000

$\langle T_0 \text{ start} \rangle$

$\langle T_0, A, 1000, 950 \rangle$

$\langle T_0, B, 2000, 2050 \rangle$

$\langle T_0 \text{ commit} \rangle$

$\langle T_1 \text{ start} \rangle$

$\langle T_1, C, 700, 100 \rangle$

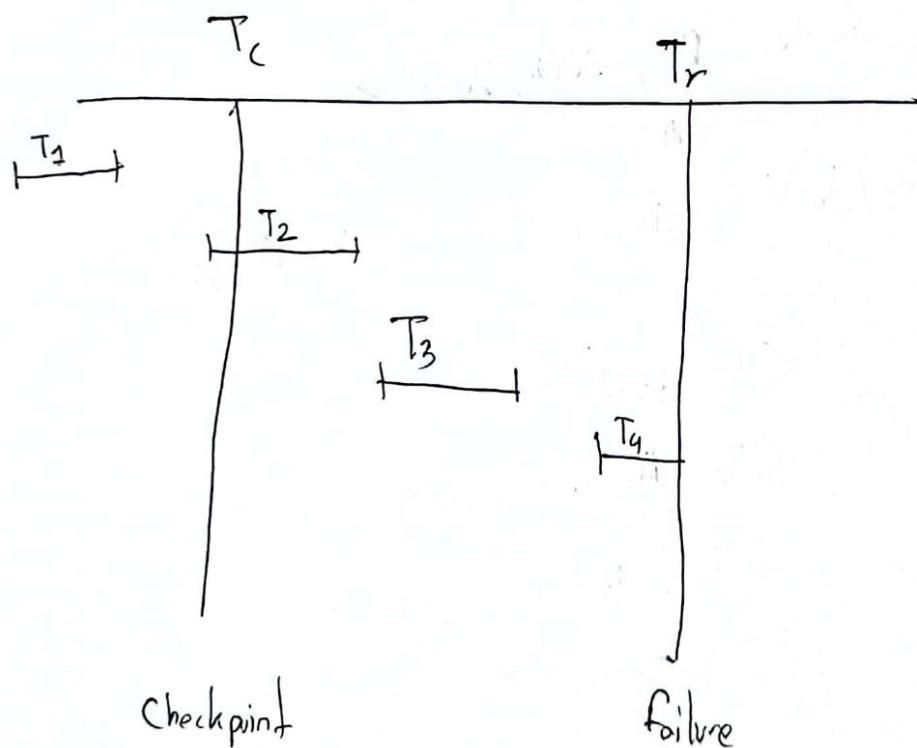
$\text{redo}(T_0)$ and $\text{undo}(T_1)$

Commit 2012 TRAN to fix the tx → Do redo

Checkpointing:

Completed tx are fully secured after passing checkpoint

This time, we can just go back to the checkpoint
and which tx were live during checkpointing



$T_2 \rightarrow$ redo

$T_3 \rightarrow$ redo

$T_4 \rightarrow$ Do not know final
results. Undo

Concurrency control and recovery

$\langle T_0 \text{ start} \rangle$

$\langle T_0, B, 2000, 2050 \rangle$

$\langle T_1 \text{ start} \rangle$

$\langle \text{checkpoint } \{T_0, T_1\} \rangle$

$\langle T_1, C, 700, 100 \rangle$

$\langle T_1 \text{ Commit} \rangle$

$\langle T_2 \text{ start} \rangle$

$\langle T_2, A, 500, 400 \rangle$

$\langle T_0, B, 2000 \rangle$

$\langle T_0 \text{ abort} \rangle$

(crash) $\xrightarrow{\quad} \langle T_2, A, 500 \rangle$

$\langle T_2 \text{ abort} \rangle$