

# All about Linear Regression

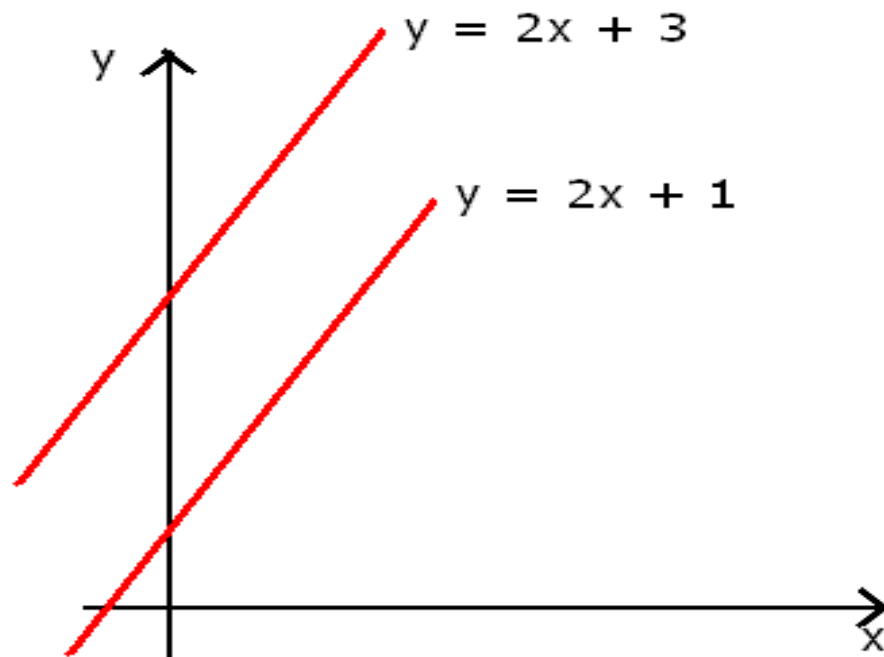
## (Least Squares Method)



- Theory Part:
  - Straight Line
  - Curve Line
  - Slope
  - Intercept
  - Cost Function
  - Lose Function
  - Mean Absolute Error (MAE)
  - Mean Squared Error (MSE)
  - Gradient Decent
- Coding with Python:
  - Implementing Linear Regression
  - Simple ML Project on Rent Prediction
- Discussion on Assignment:
  - Weight Prediction Based on Height

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## Linear Line



$x = 10, 30, 50$

$y = 2 * 10 + 3 = 23$

$y = 2 * 30 + 3 = 63$

$y = 2 * 50 + 3 = 103$

Fig: Straight Line

## Non-Linear Curve Line

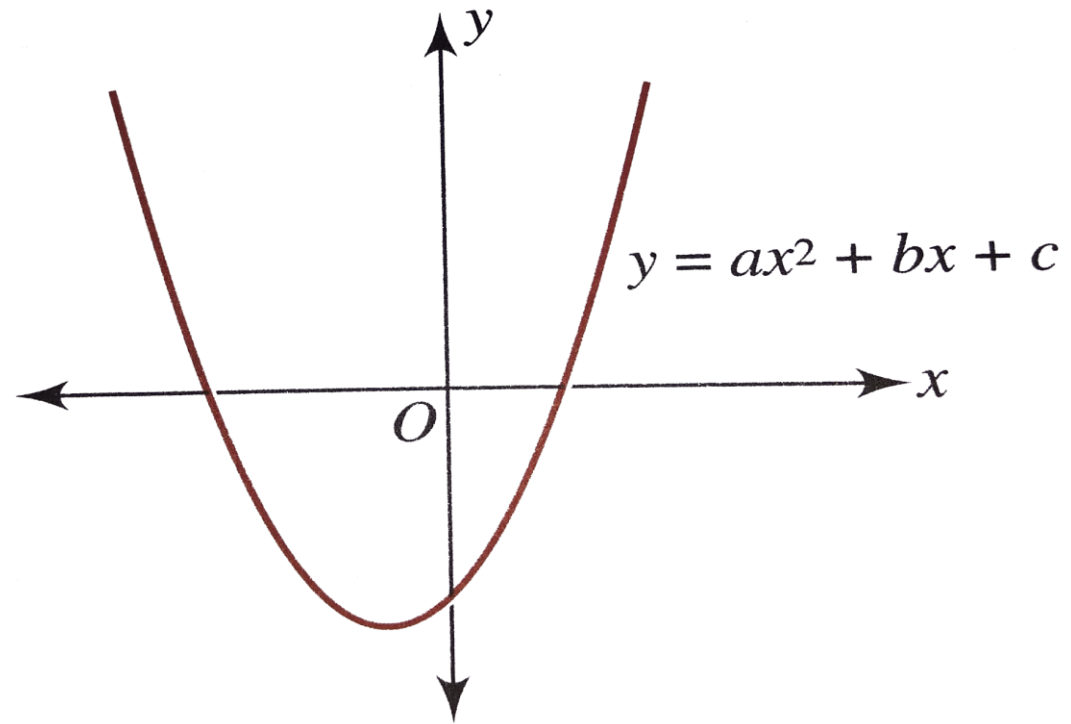
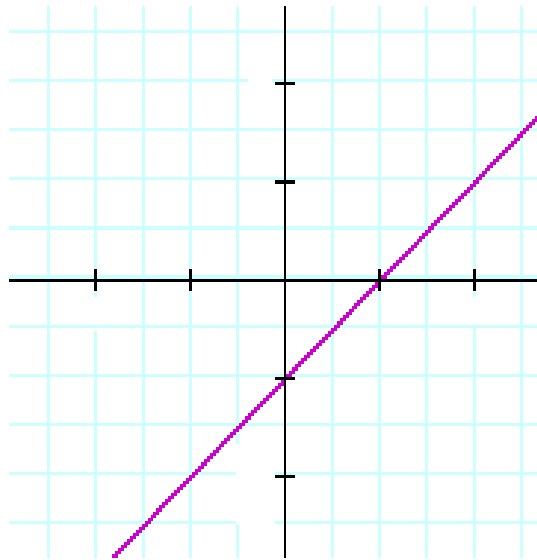
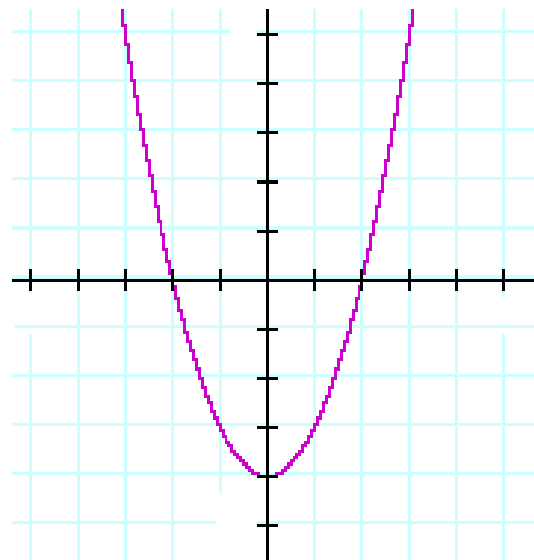


Fig: Curve Line

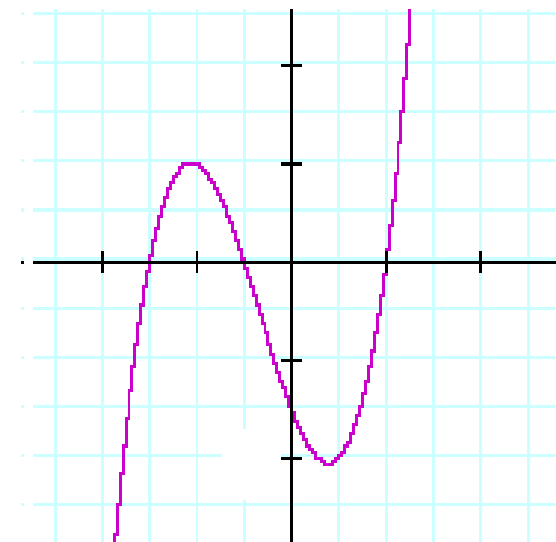
## Linear vs Non-Linear Curve Line



$$y = ax + b$$



$$y = ax^2 + bx + c$$

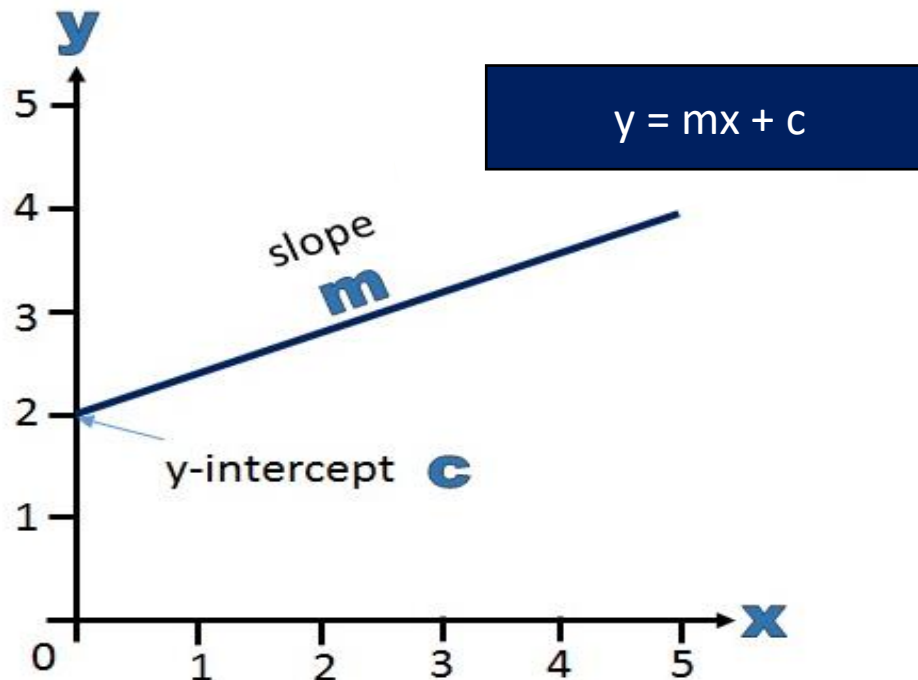


$$y = ax^3 + bx^2 + cx + d$$

Fig: Lines

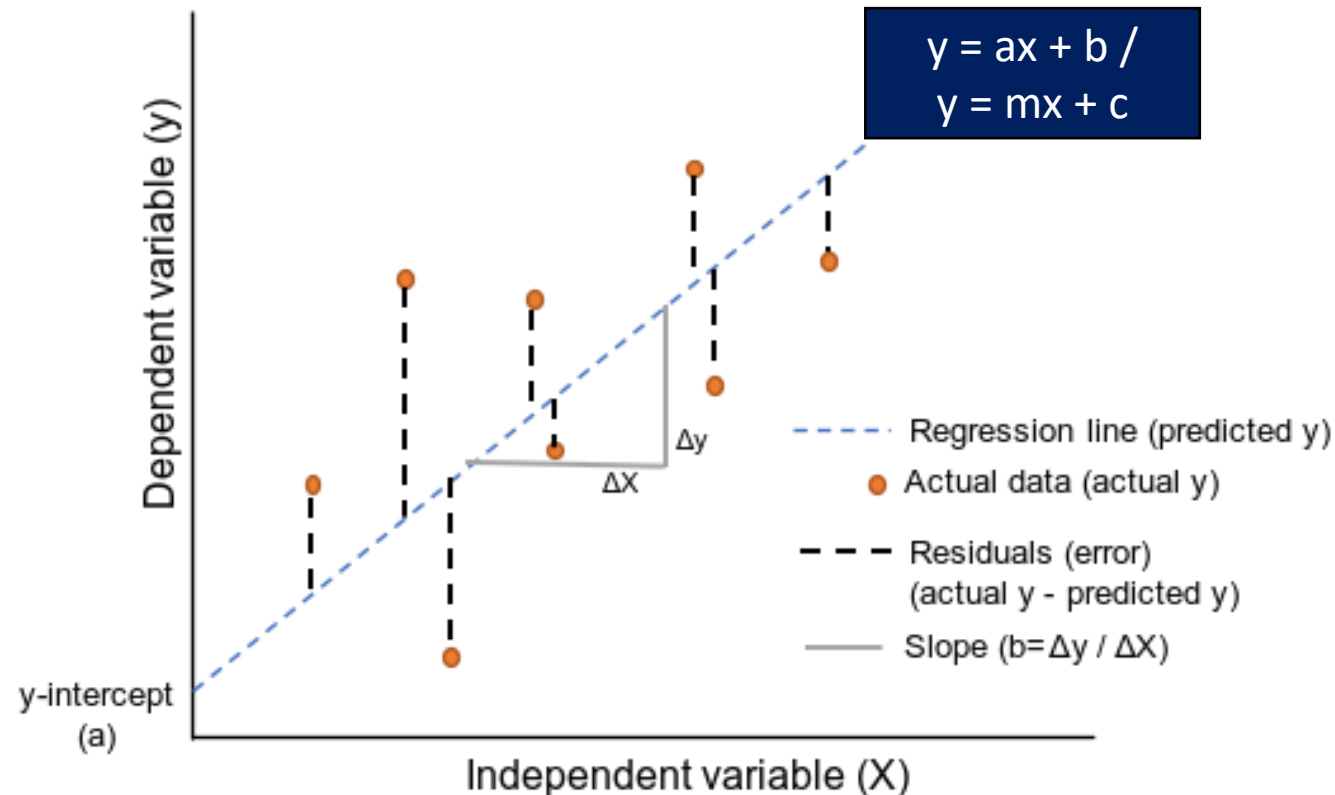
## All about Linear Regression

Linear regression is a statistical model that allows to explain a dependent variable  $y$  based on variation in one or multiple independent variables (denoted  $x$ ). It does this based on linear relationships between the independent and dependent variables.

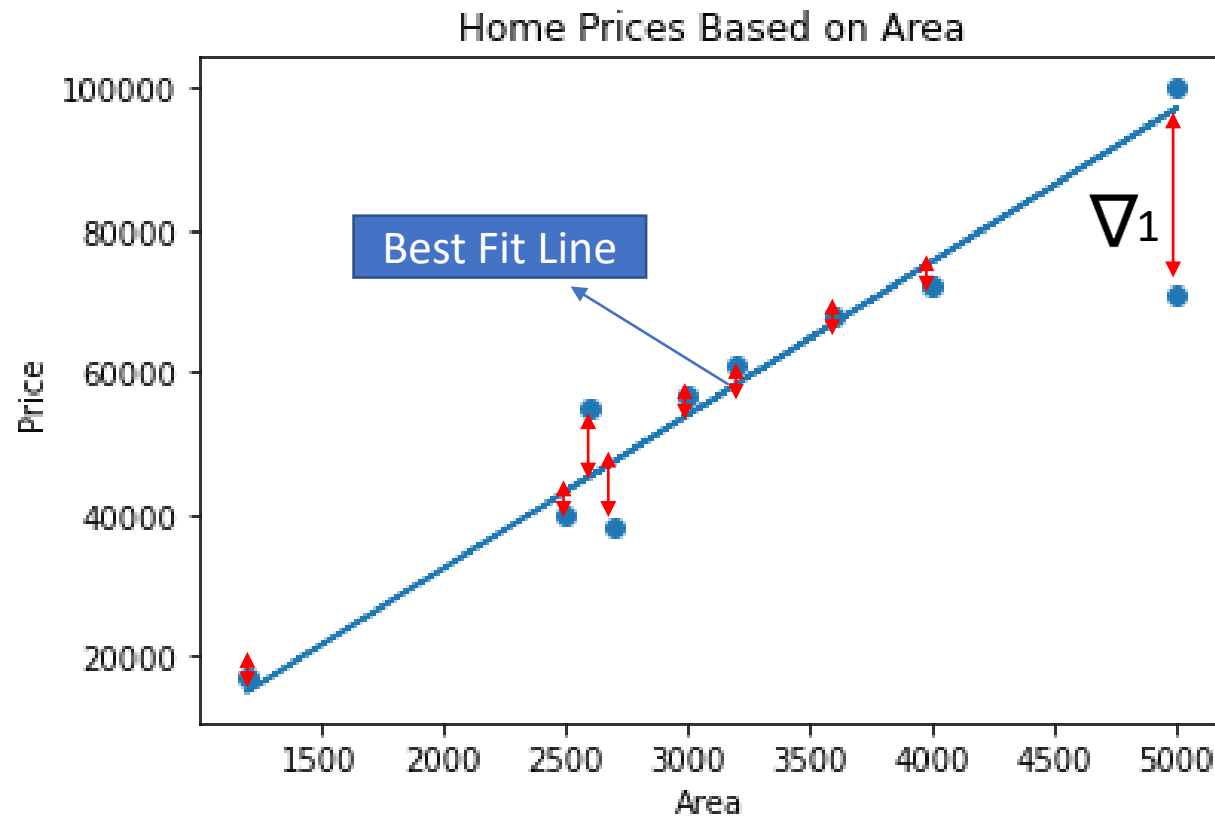


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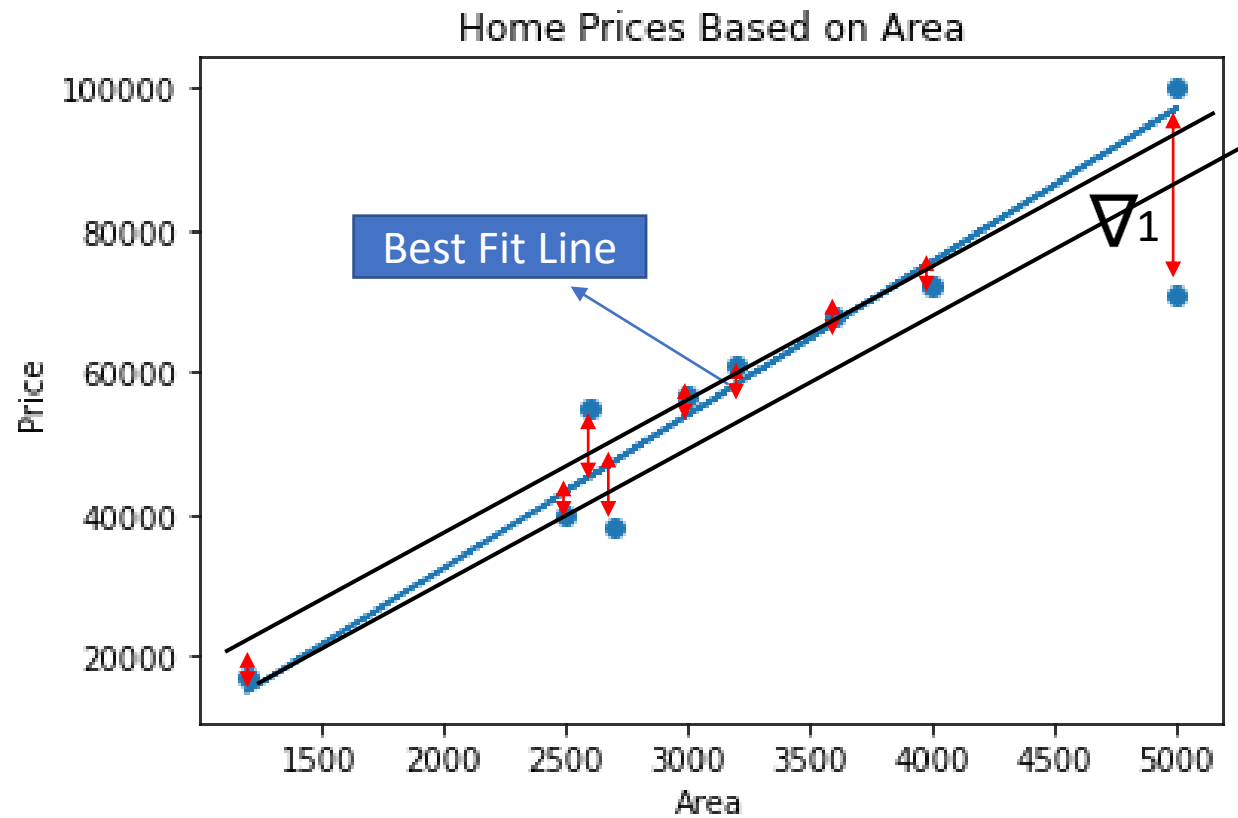
## All about Linear Regression



$$y = mx + b ; \text{ or, } Y = 9.782 * X + 1.48$$

Coefficient = 9.782  
Intercept = 1.48

# All about Linear Regression

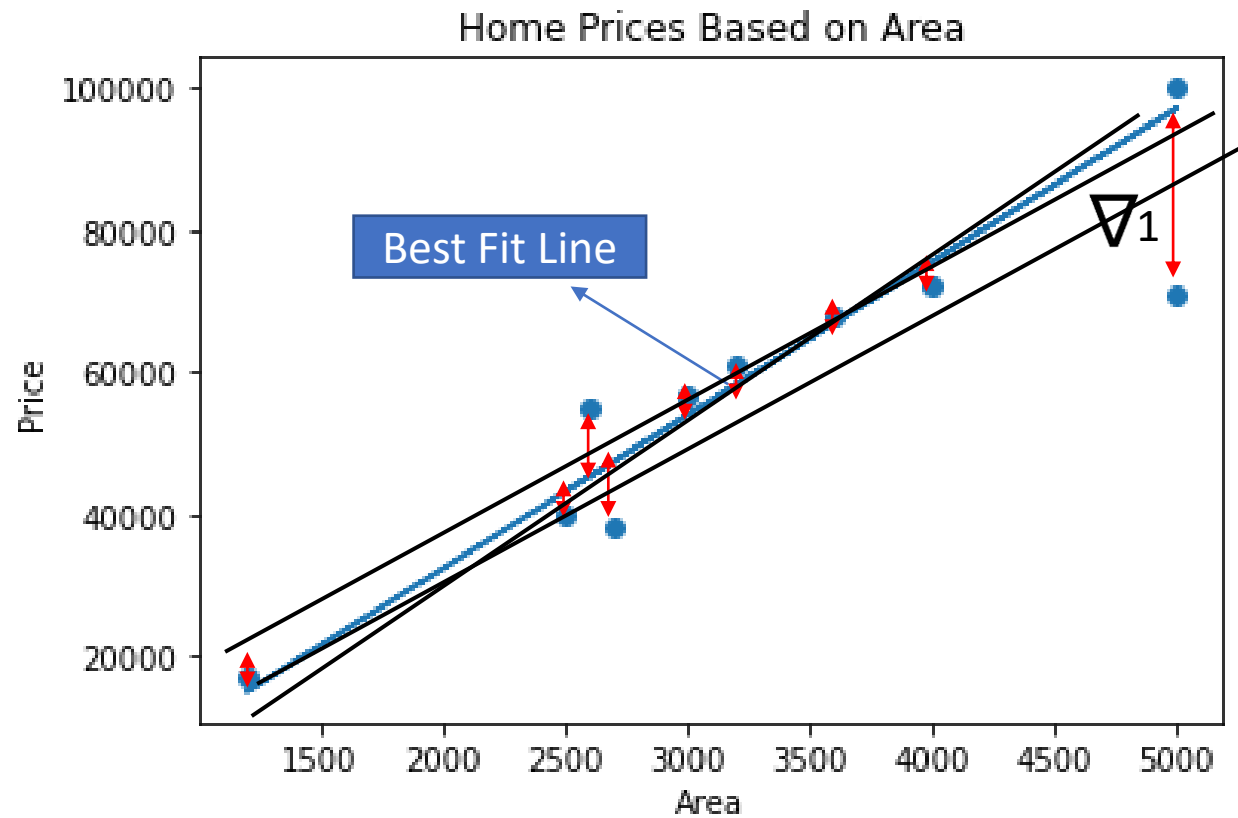


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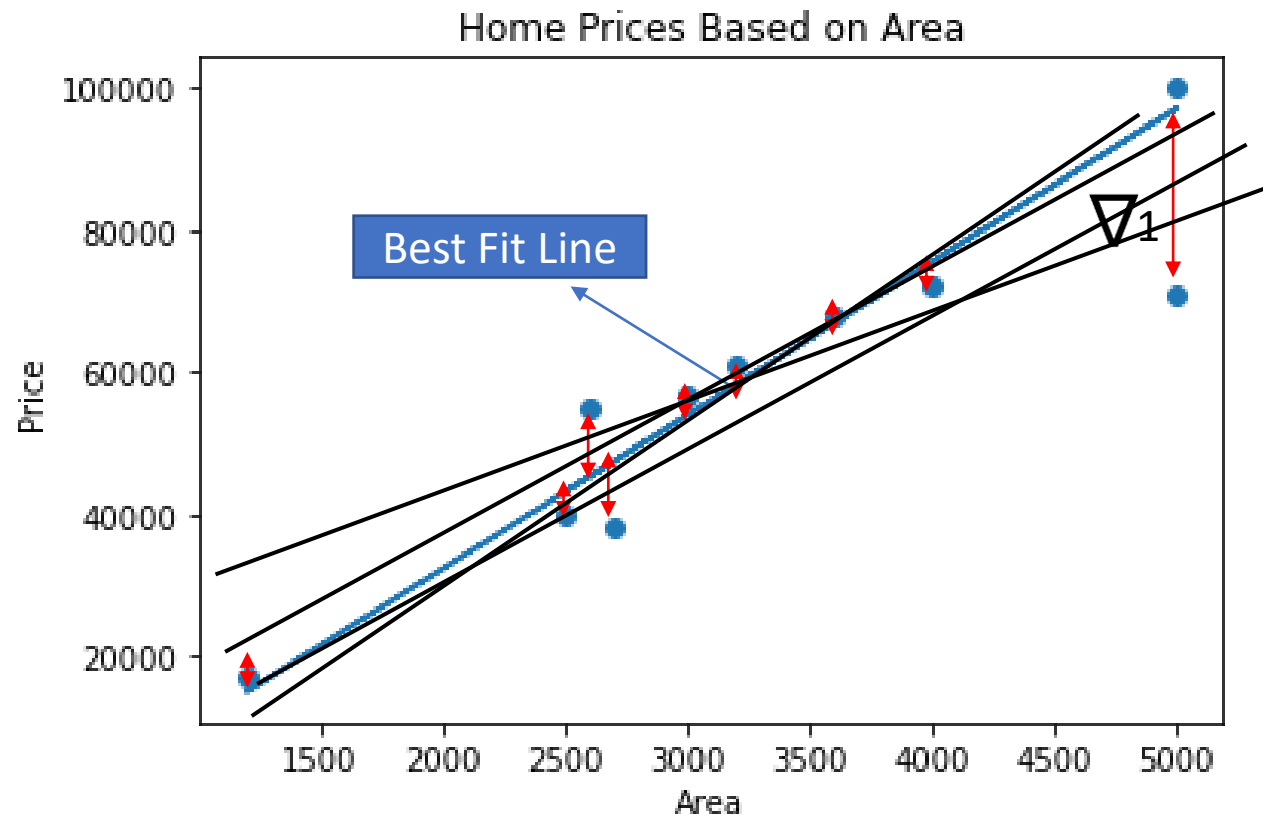
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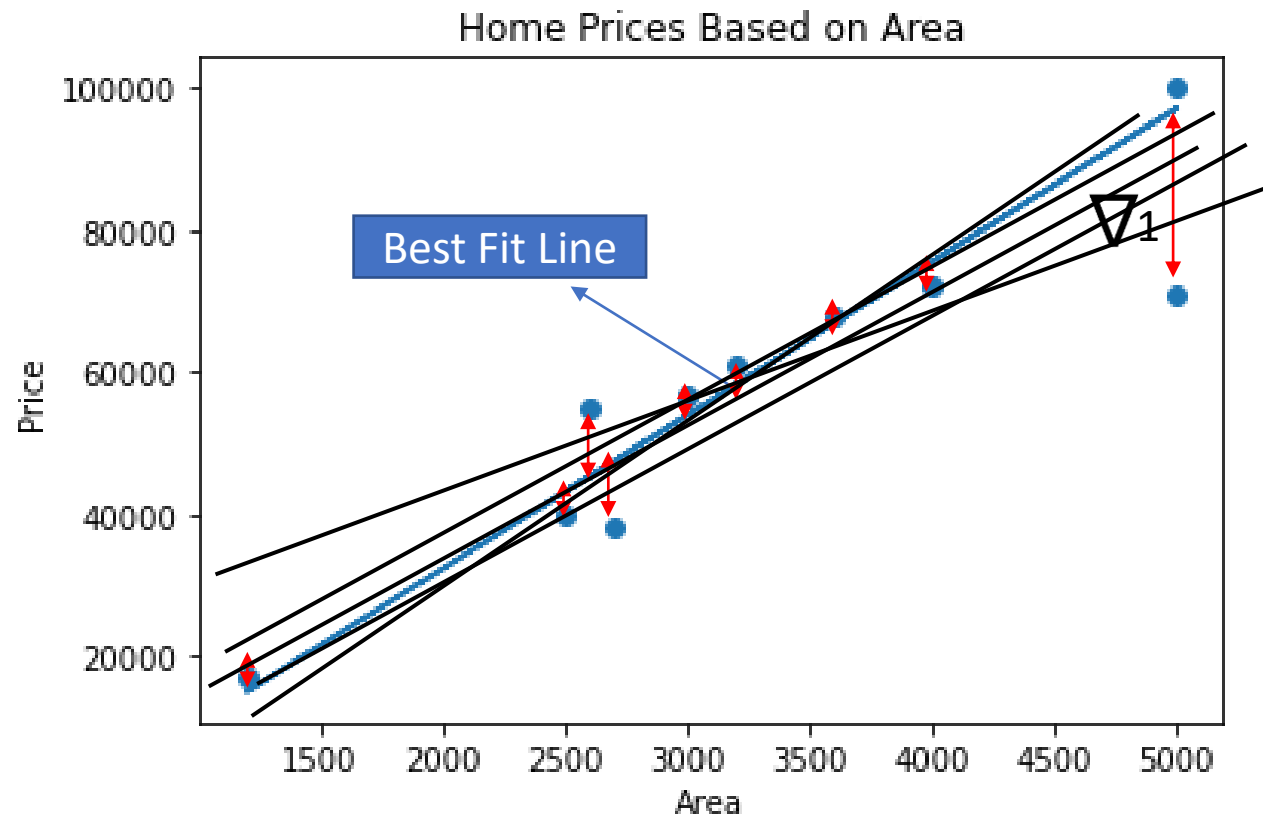
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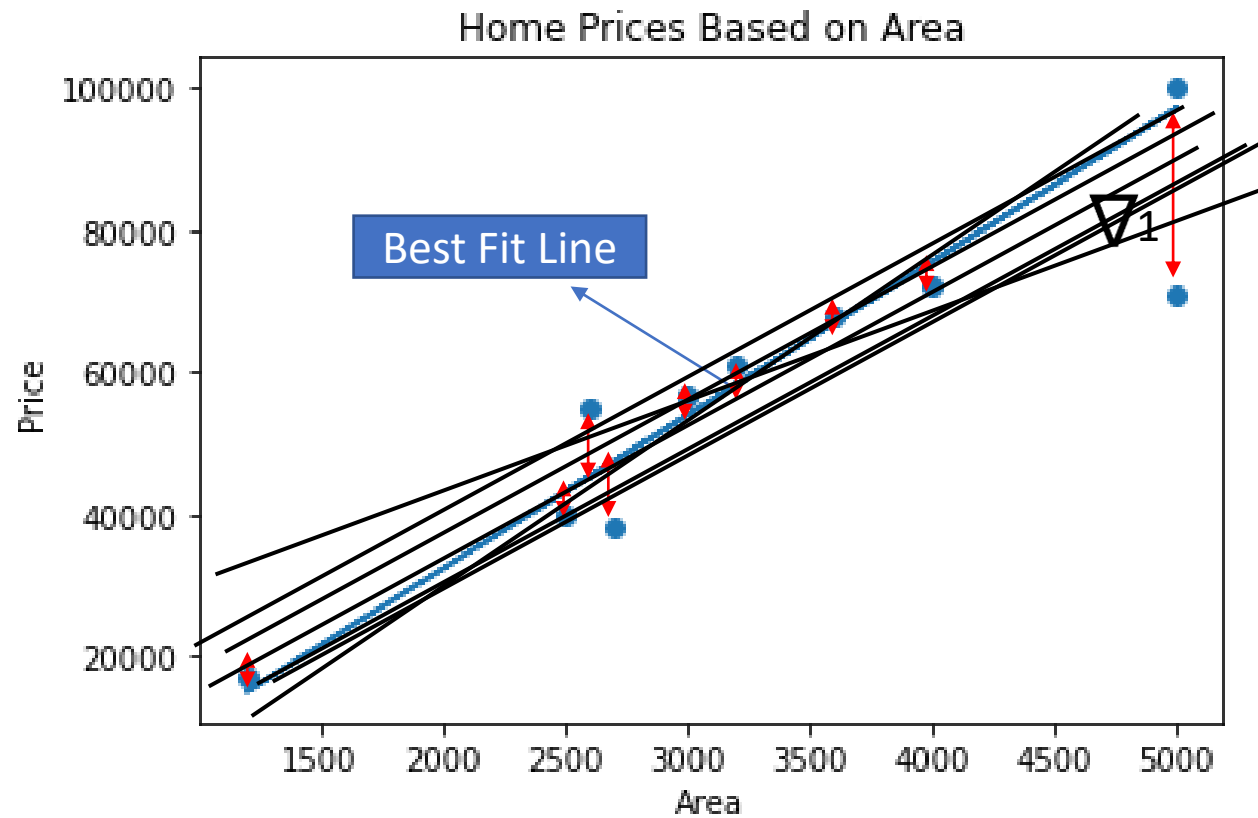
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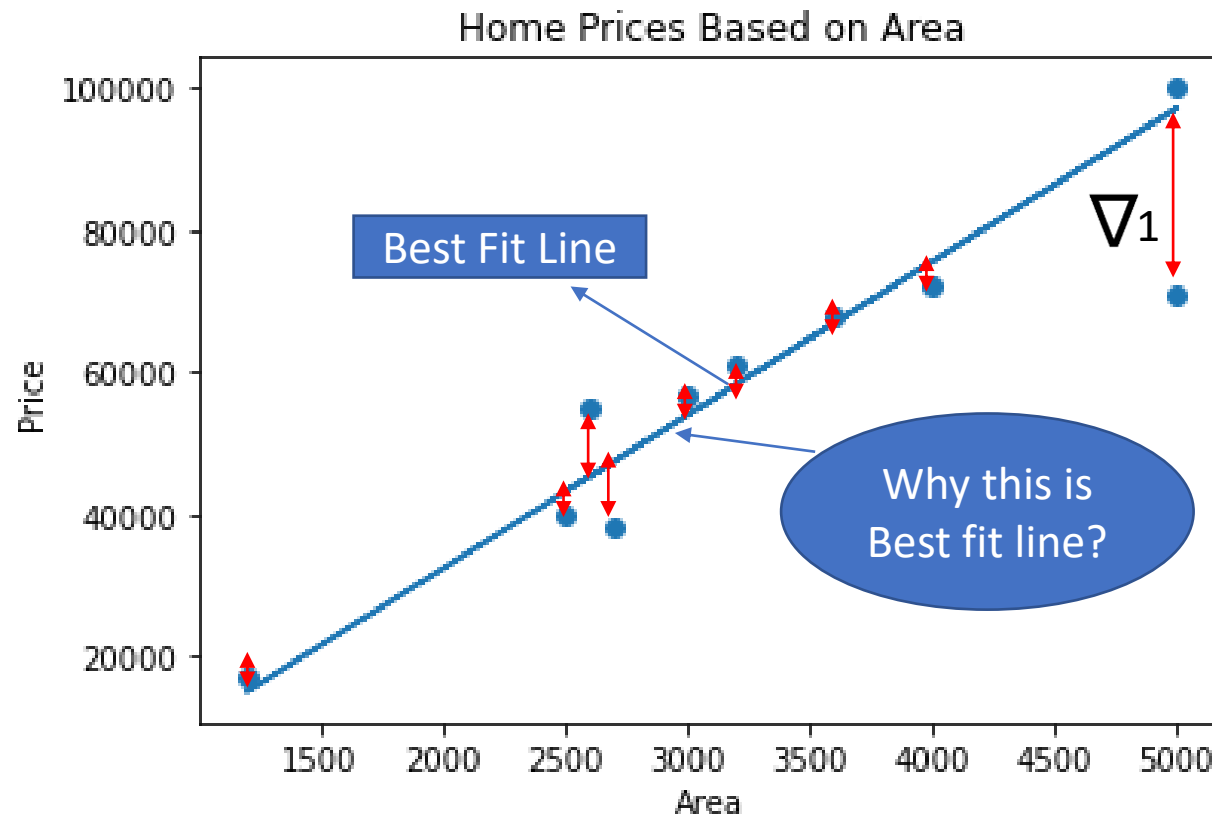
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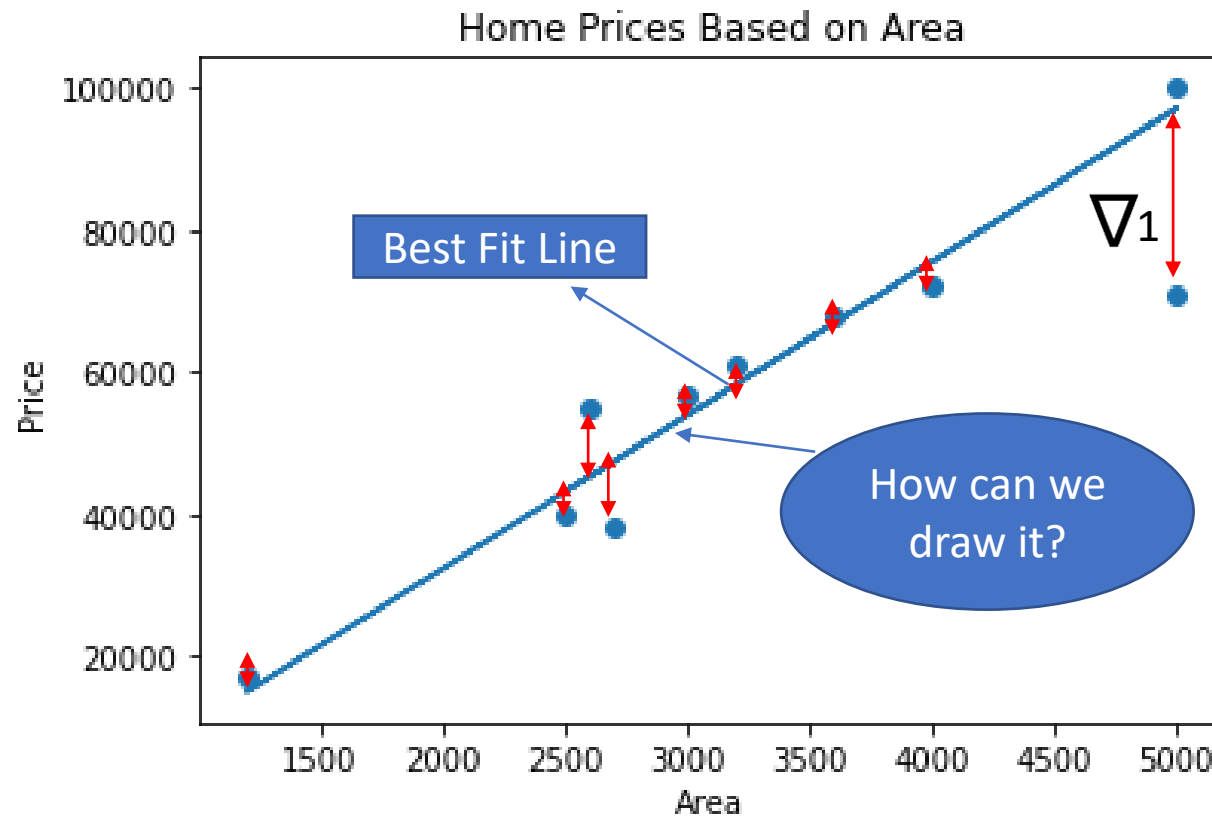
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# All about Linear Regression



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## All about Linear Regression (Least Squares Method)

### Formula of Linear Regression

$$Y = MX + C$$

$$C = \bar{Y} - M\bar{X}$$

$$M = \frac{\bar{X} \cdot \bar{Y} - \bar{XY}}{(\bar{X})^2 - \bar{X}^2}$$

$$\bar{X} = \text{Mean } X$$

$$\bar{Y} = \text{Mean } Y$$

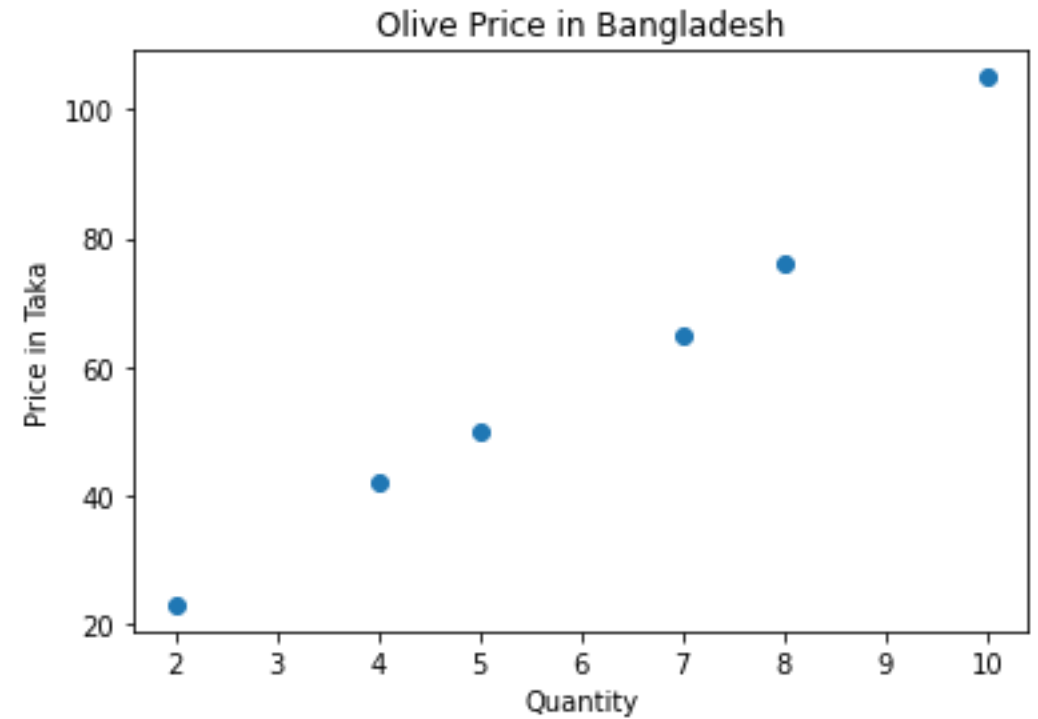
Now  
Solve it

### Data Set

	A	B	
1	x	y	
2	5	50	
3	7	65	
4	4	42	
5	8	76	
6	2	23	
7	10	105	
8	7	?	

## All about Linear Regression

	x	y
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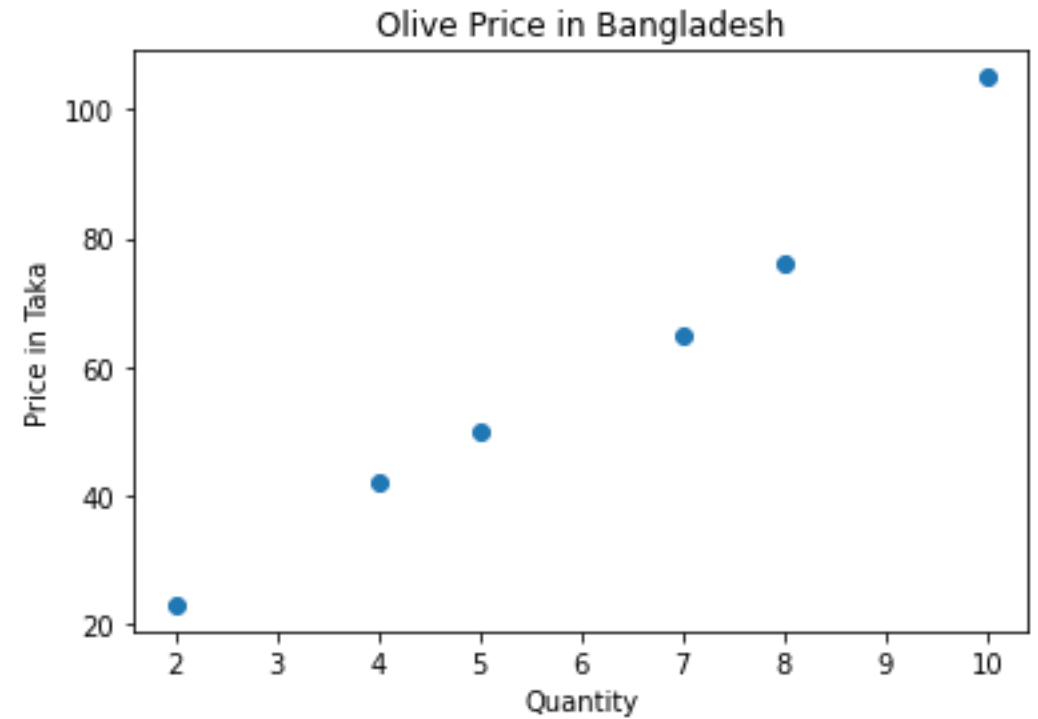
### Mean Values

```
df.x.mean()
```

```
6.0
```

```
df.y.mean()
```

```
60.166666666666664
```



## All about Linear Regression

	x	y
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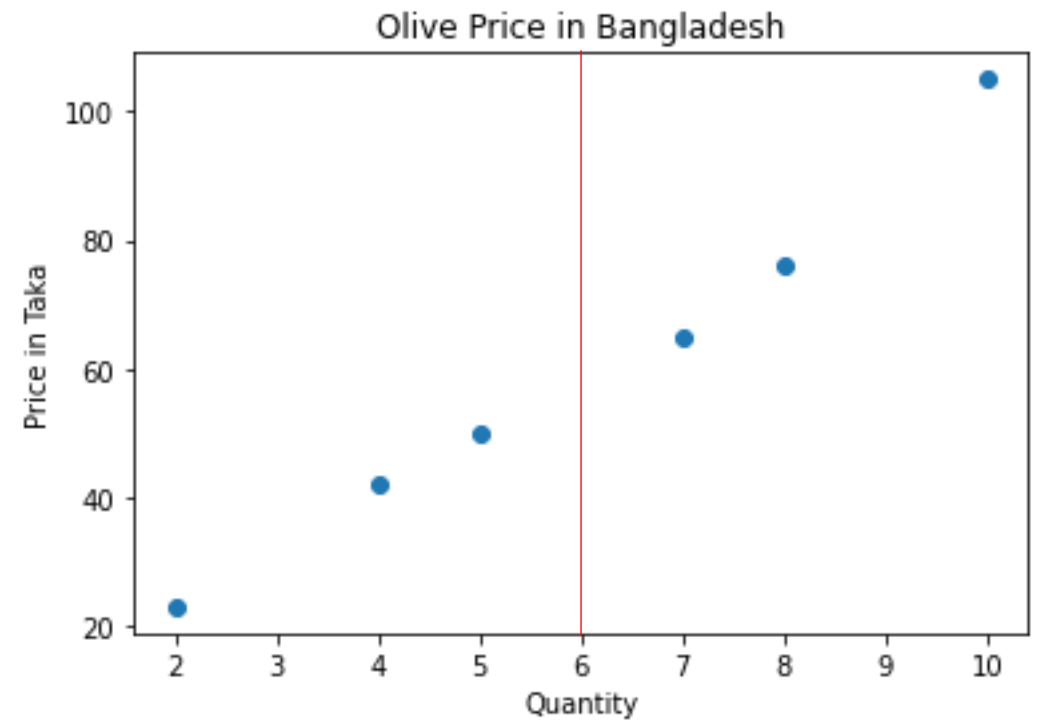
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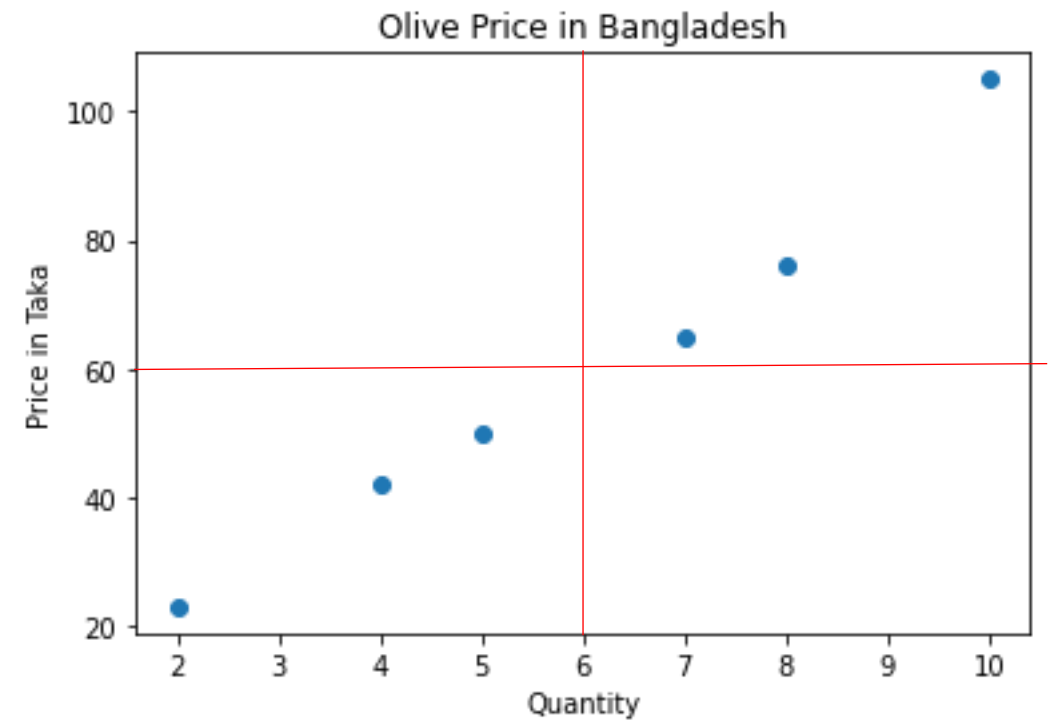
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# All about Linear Regression

## Formula of Linear Regression

$$Y = MX + C$$

$$C = \bar{Y} - M\bar{X}$$

$$M = \frac{\bar{X} \cdot \bar{Y} - \bar{XY}}{(\bar{X})^2 - \bar{X}^2}$$

$\bar{X}$  = Mean X  
 $\bar{Y}$  = Mean Y

Now  
Solve it



## Data Set

	A	B	
1	x	y	
2	5	50	
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7	10	105	
8	7	?	

## Calculation Table for Single Variable Linear Regression

## All about Linear Regression

### Formula of Linear Regression

$$Y = MX + C$$

$$C = \bar{Y} - M\bar{X}$$

$$M = \frac{\bar{X} \cdot \bar{Y} - \bar{X} \bar{Y}}{(\bar{X})^2 - \bar{X}^2}$$

$$\bar{X} = \text{Mean } X$$

$$\bar{Y} = \text{Mean } Y$$



### Final Calculations

$$M = ((6 * 60.17) - 429.5) / (36 - 43)$$

$$M = 9.782$$

$$C = 60.17 - (9.782 * 6)$$

$$C = 1.48$$

$$Y = (9.782 * X) + 1.48$$

$$\text{Predict, } y = (9.782 * 7) + 1.48$$

$$\text{Ans} = 69.95$$

[illegible]

# All about Linear Regression

	A	B	C	D	E	F	G	H	I	J
1	x	y	xy	x <sup>2</sup>	$\bar{x}$	$\bar{y}$	(xy) bar	( $\bar{x}$ ) <sup>2</sup>	(x <sup>2</sup> ) bar	Final Calculations
2	5	50	250	25						$M = ((6*60.17)-429.5) / (36-43)$
3	7	65	455	49	Sum=36	Sum=361	Sum=2577		Sum=258	$M = 9.782$
4	4	42	168	16	36/6	361/6	2577/6		258/6	$C = 60.17 - (9.782*6)$
5	8	76	608	64						$C = 1.48$
6	2	23	46	4	Avg=6	Avg=60.17	Avg=429.5	36	Avg=43	$Y = (9.782 * X) + 1.48$
7	10	105	1050	100	Average	Average	Average		Average	Predict, $y = (9.782*7)+1.48$
8	7	69.95		49						Ans = 69.95
9										

## Formula of Linear Regression

$$Y = MX + C$$

$$C = \bar{Y} - M\bar{X}$$

$$M = \frac{\bar{x} \cdot \bar{y} - \bar{xy}}{(\bar{x})^2 - \bar{x^2}}$$

$$\bar{x} = \text{Mean } x$$

$$\bar{y} = \text{Mean } y$$



## All about Linear Regression

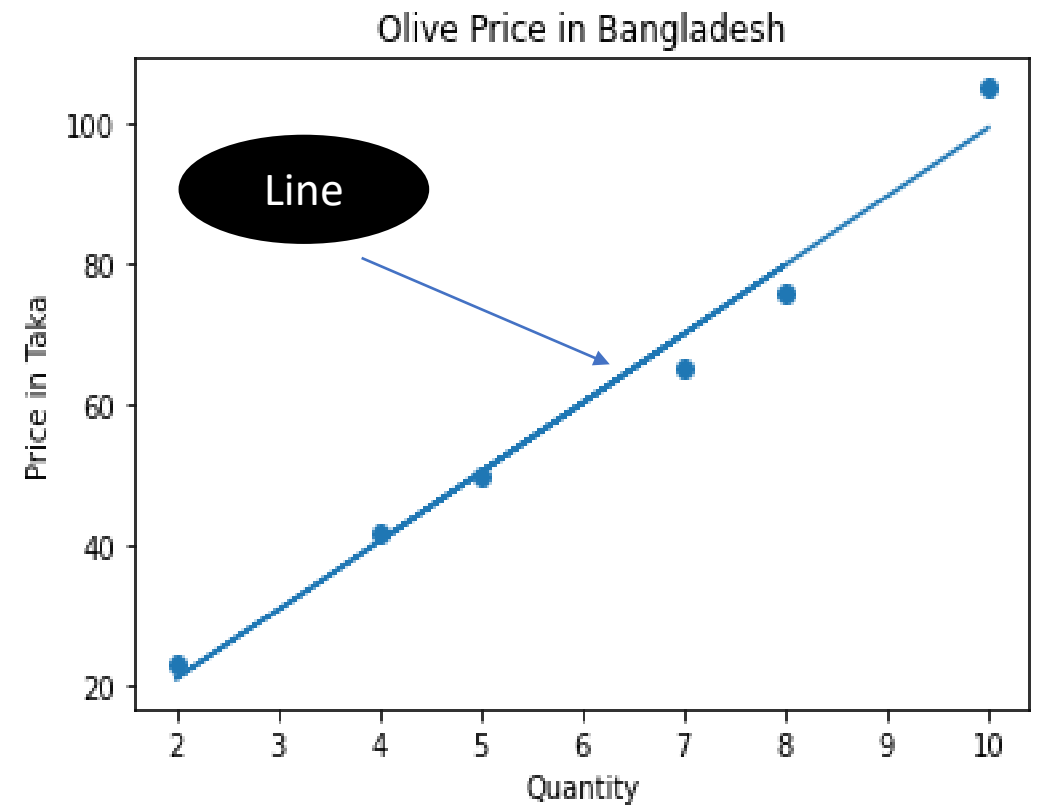
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	x	y
0	5	50
1	7	65
2	4	42
3	8	76
4	2	23
5	10	105

### Value of M & C

```
reg.coef_  
array([9.78571429])
```

```
reg.intercept_  
1.4523809523809703
```



## All about Linear Regression

### Data Set

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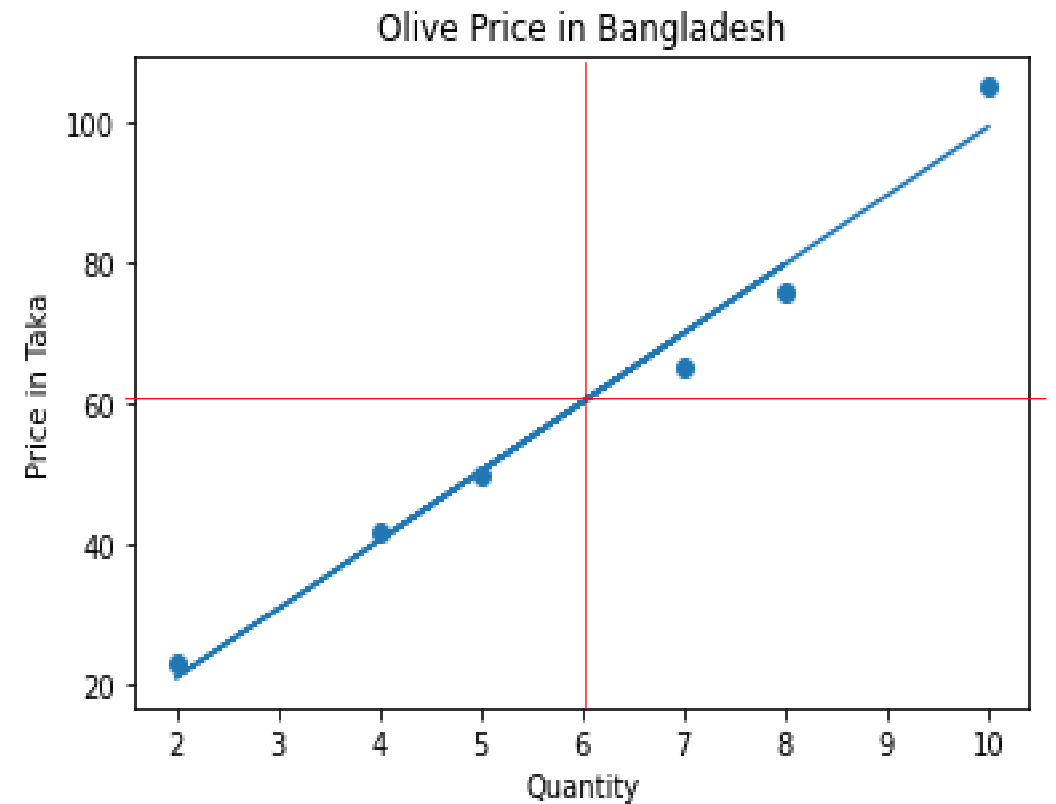
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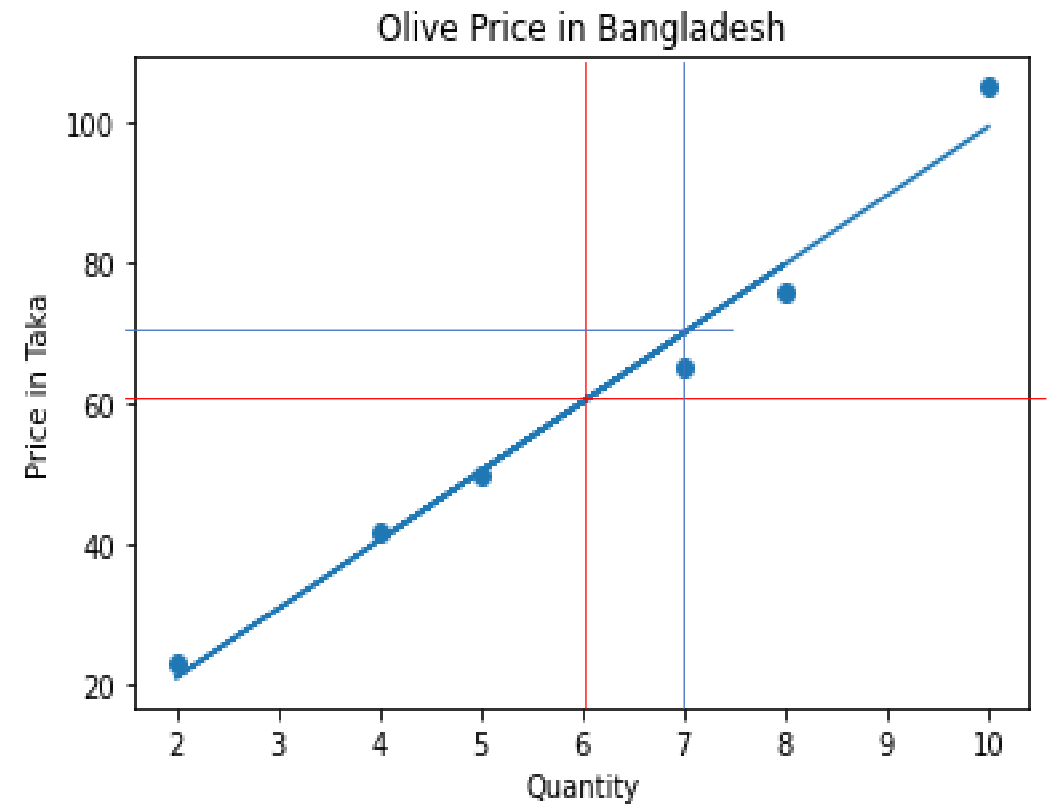
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reg.intercept_
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```
1.4523809523809703
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## All about Linear Regression

### Data Set

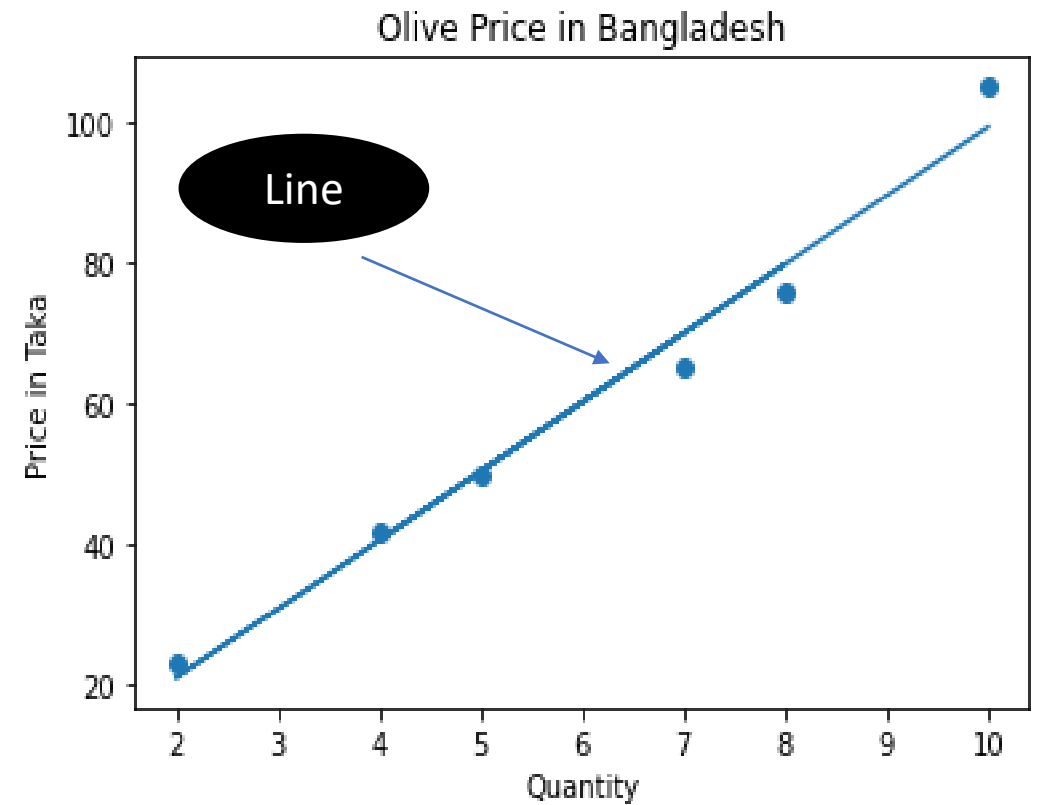
	x	y
0	5	50
1	7	65
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4	2	23
5	10	105

### Predict New Value

```
pred = reg.predict([[7]])
```

```
pred
```

```
array([69.95238095])
```

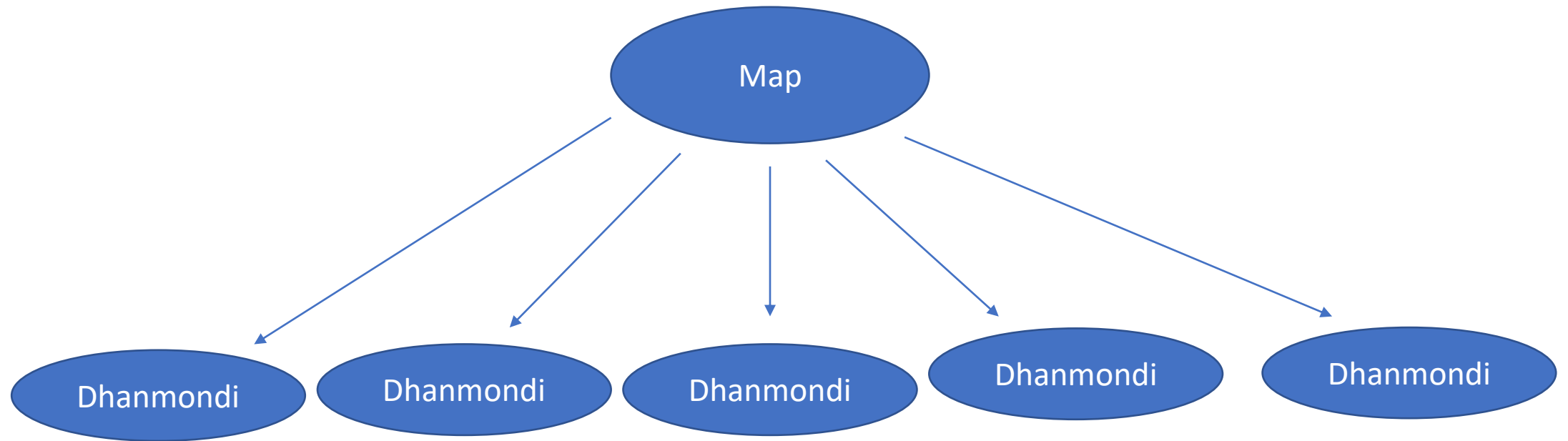


*Let's Implement Linear Regression with Python*

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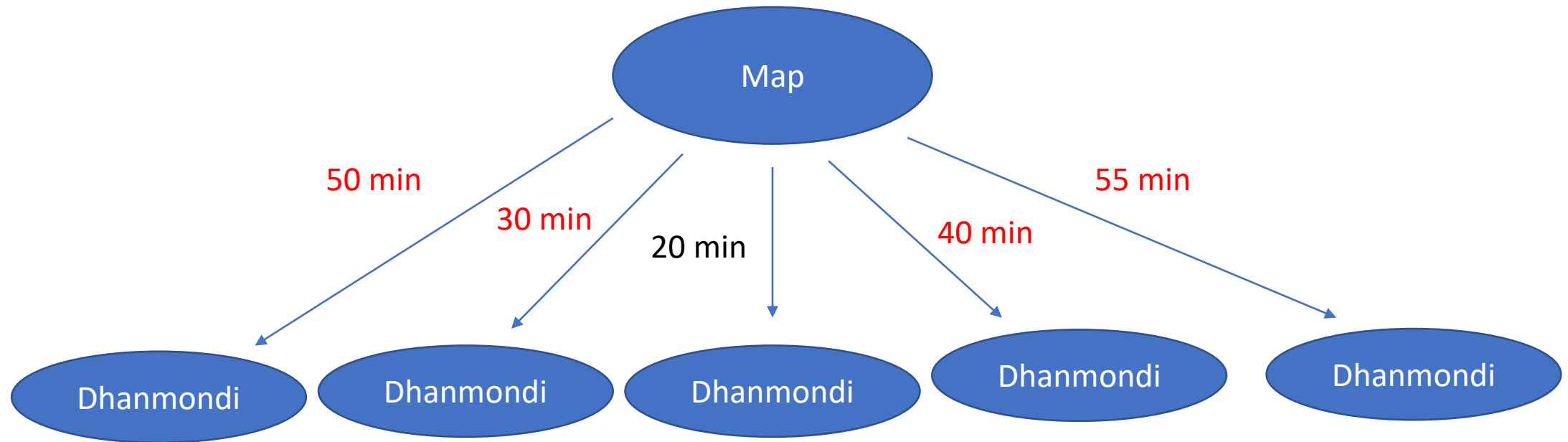
## Cost Function

The cost function is a function, which is associates a cost with a decision.



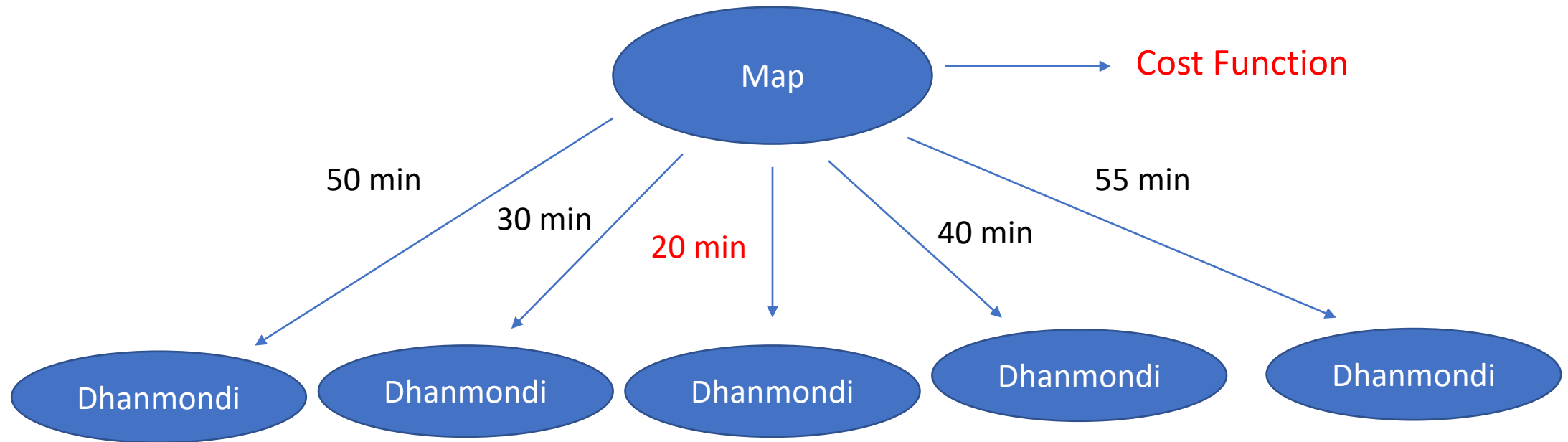
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# Loss & Cost Function

A loss function is for a single training example. It is also sometimes called an error function. A cost function, on the other hand, is the average loss over the entire training dataset. The optimization strategies aim at minimizing the cost function

$$\text{Predicted Price (Y)} = m * \text{area} + c$$

$$\text{L1 Loss (error)} = (1/n) * | (y_i - \hat{y}) |$$

$Y_i$  = Area for each row

$\hat{Y}$  = Predicted Value

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$

	A	B	C	D
1	area	price	predicted	error
2	2600	55000	55100	100
3	3000	56500	51000	-5500
4	3200	61000	53000	-8000
5	3600	68000	70000	2000
6	4000	72000	74000	2000
7	5000	71000	69000	-2000
8	2500	40000	30000	-10000
9	2700	38000	37000	-1000
10	1200	17000	18000	1000
11	5000	100000	110000	10000
12				

## Cost Function

The cost function is a function, which is associates a cost with a decision. It indicates the difference between the predicted and the actual values for a given dataset. An ideal value of the cost function is **zero**. In regression, the typical cost function (CF) used is the mean squared error (MSE) cost function. The form of the function is shown below.

$$\text{MAE} = \frac{\sum_{i=1}^n |y_i - x_i|}{n}$$

**MAE** = mean absolute error

$y_i$  = prediction

$x_i$  = true value

$n$  = total number of data points

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$

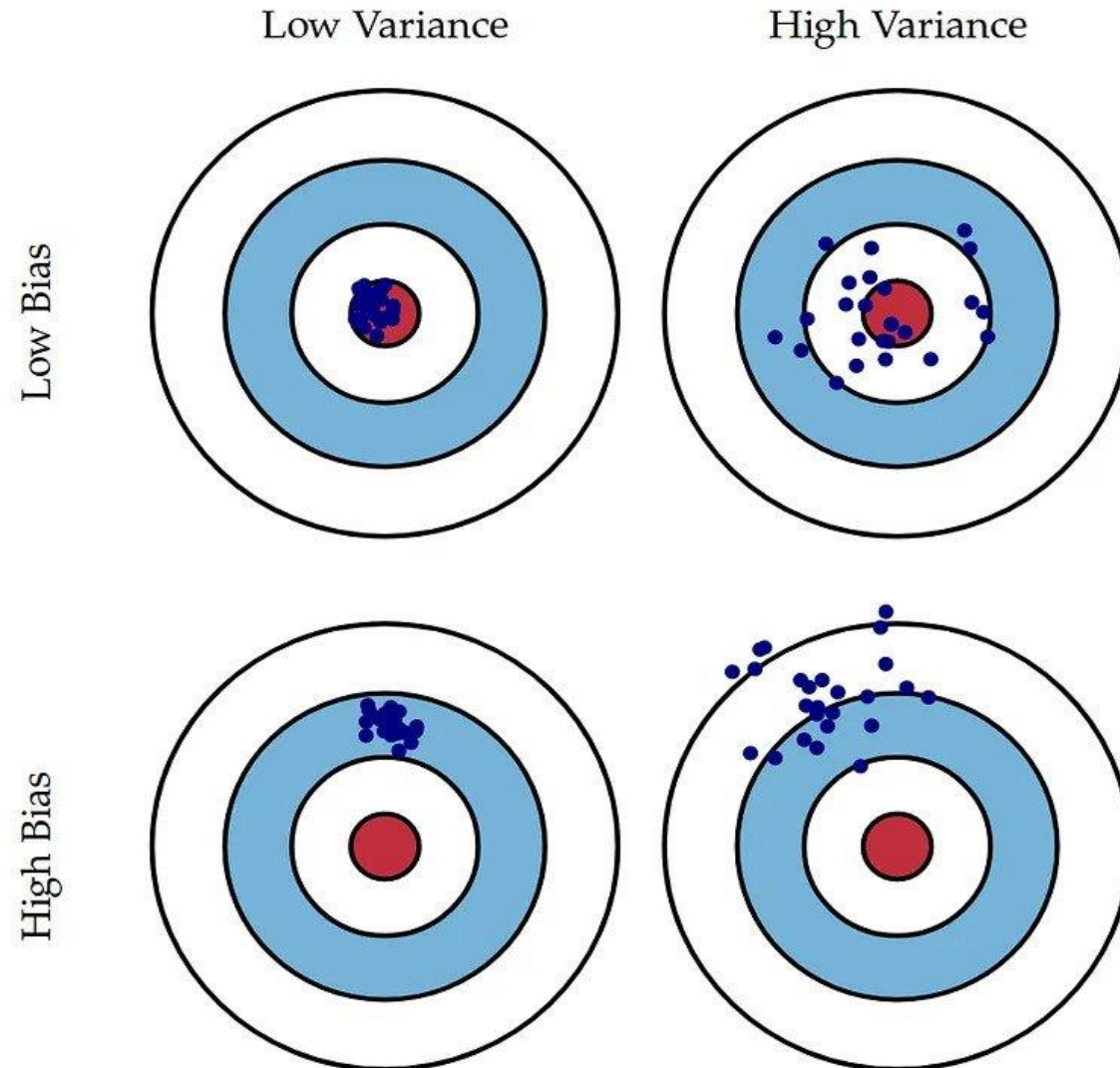
**MSE** = mean squared error

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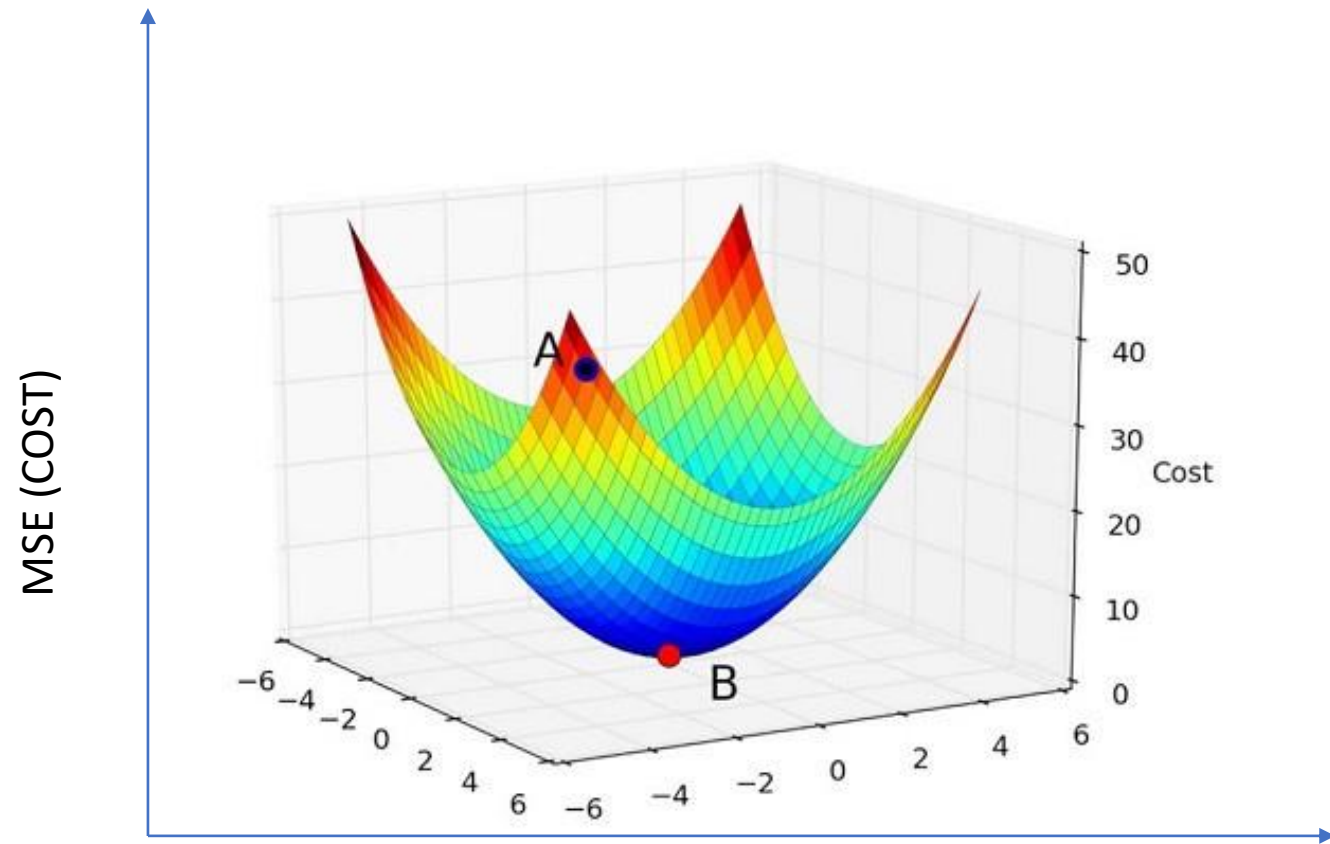
$Y_i$  = observed values

$\hat{Y}_i$  = predicted values

# Bias-Variance Tradeoff



# Minimizing the cost function: Optimizer Gradient Descent

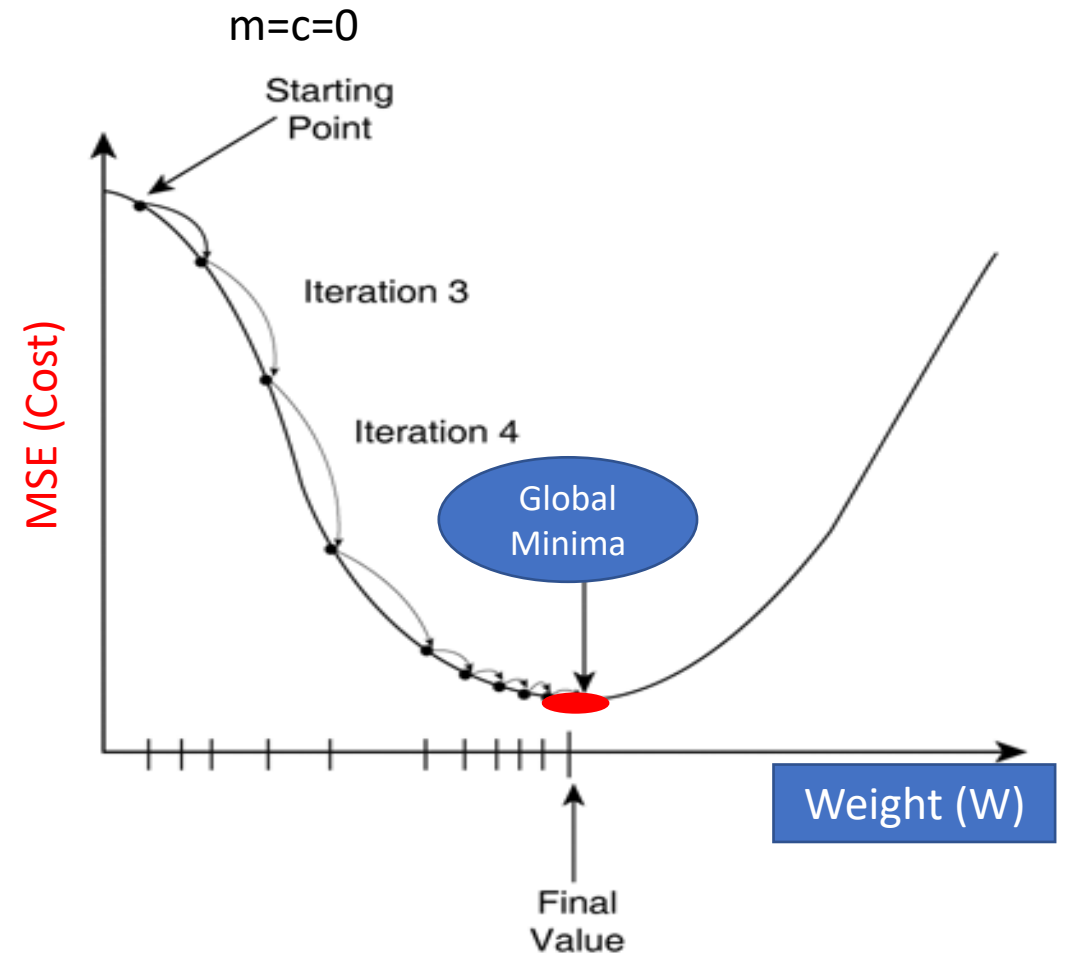


## Minimizing the cost function: Optimizer Gradient Descent

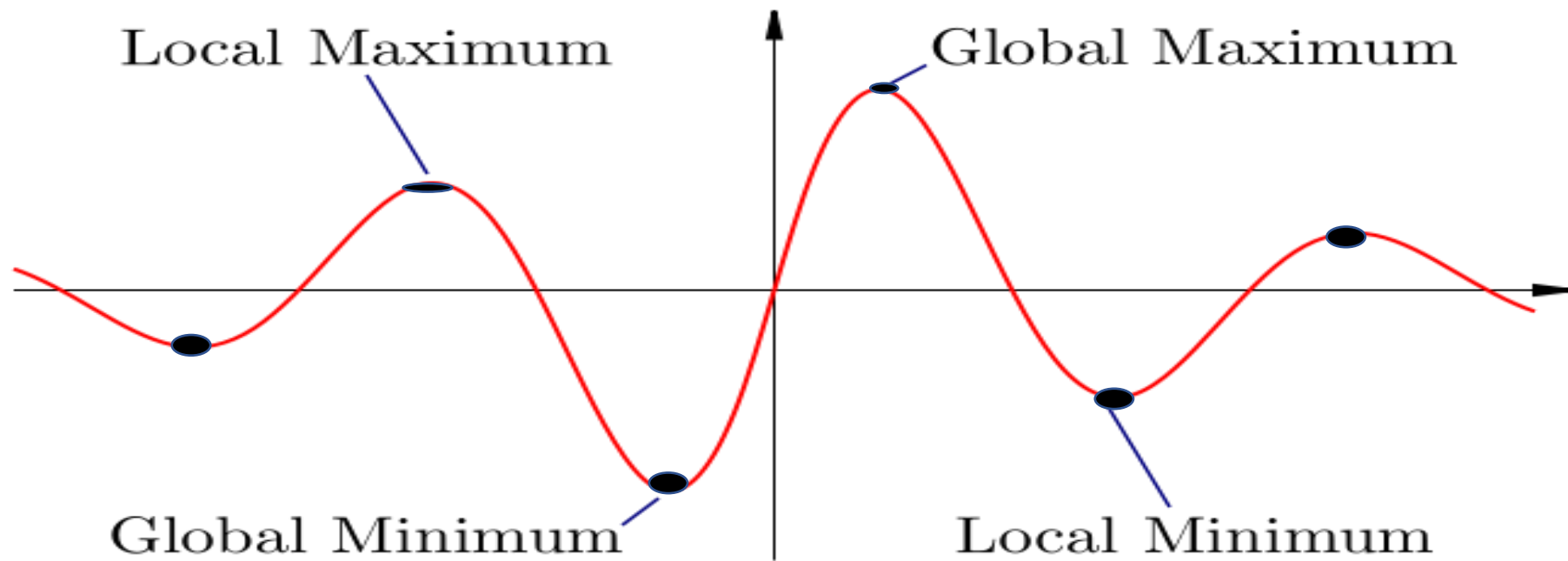
Gradient descent is an efficient optimization algorithm that attempts to find a local or global minima of a function. At this point the model has optimized the weights such that they minimize the cost function. Gradient descent enables a model to learn the gradient or direction that the model should take in order to reduce errors

$$\text{Weight}_{\text{new}} = W_{\text{old}} - \eta \frac{\partial \text{Loss}}{\partial W_{\text{old}}}$$

↗



Minimizing the cost function:  
*Gradient Descent*



*Let's Implement Linear Regression with Python*

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