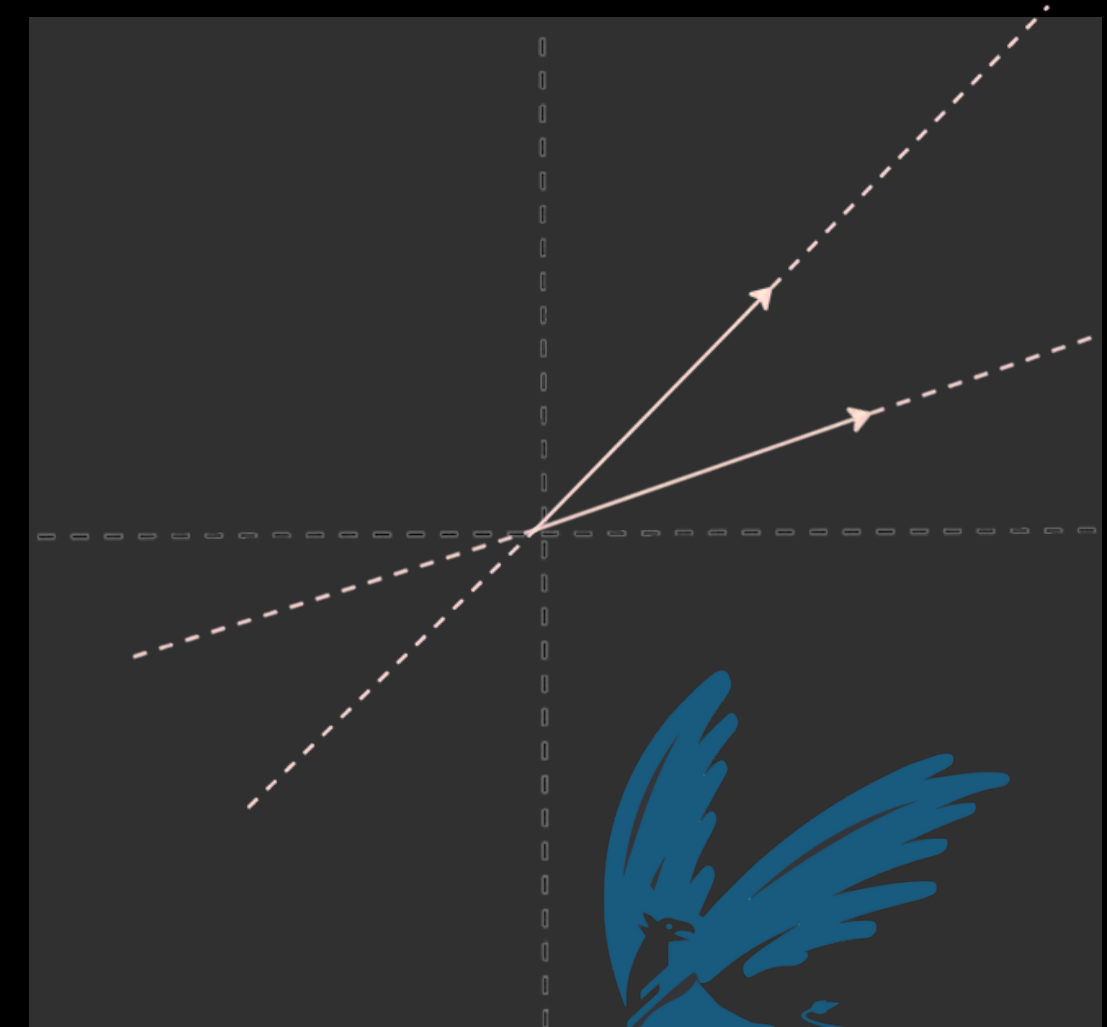
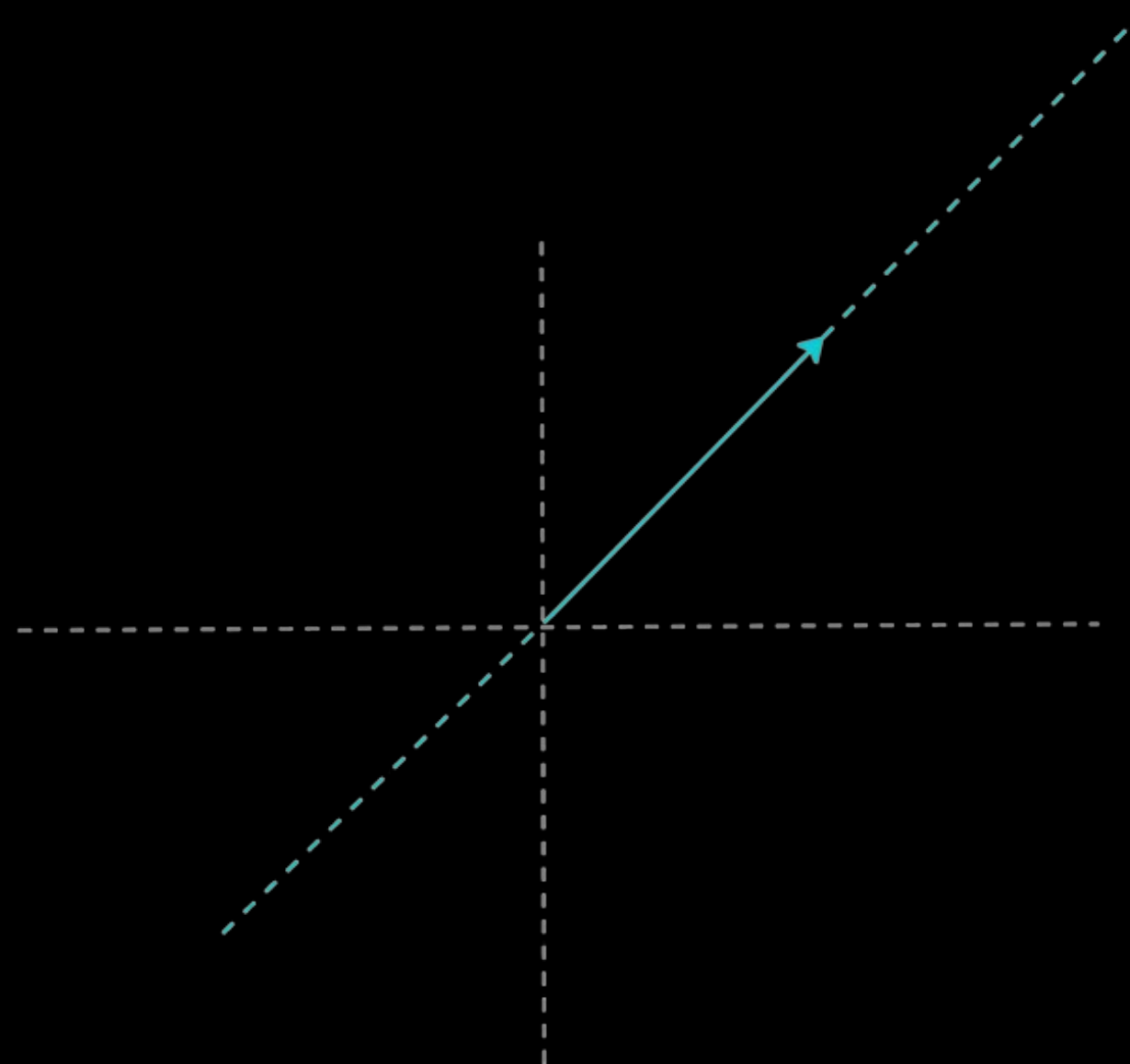
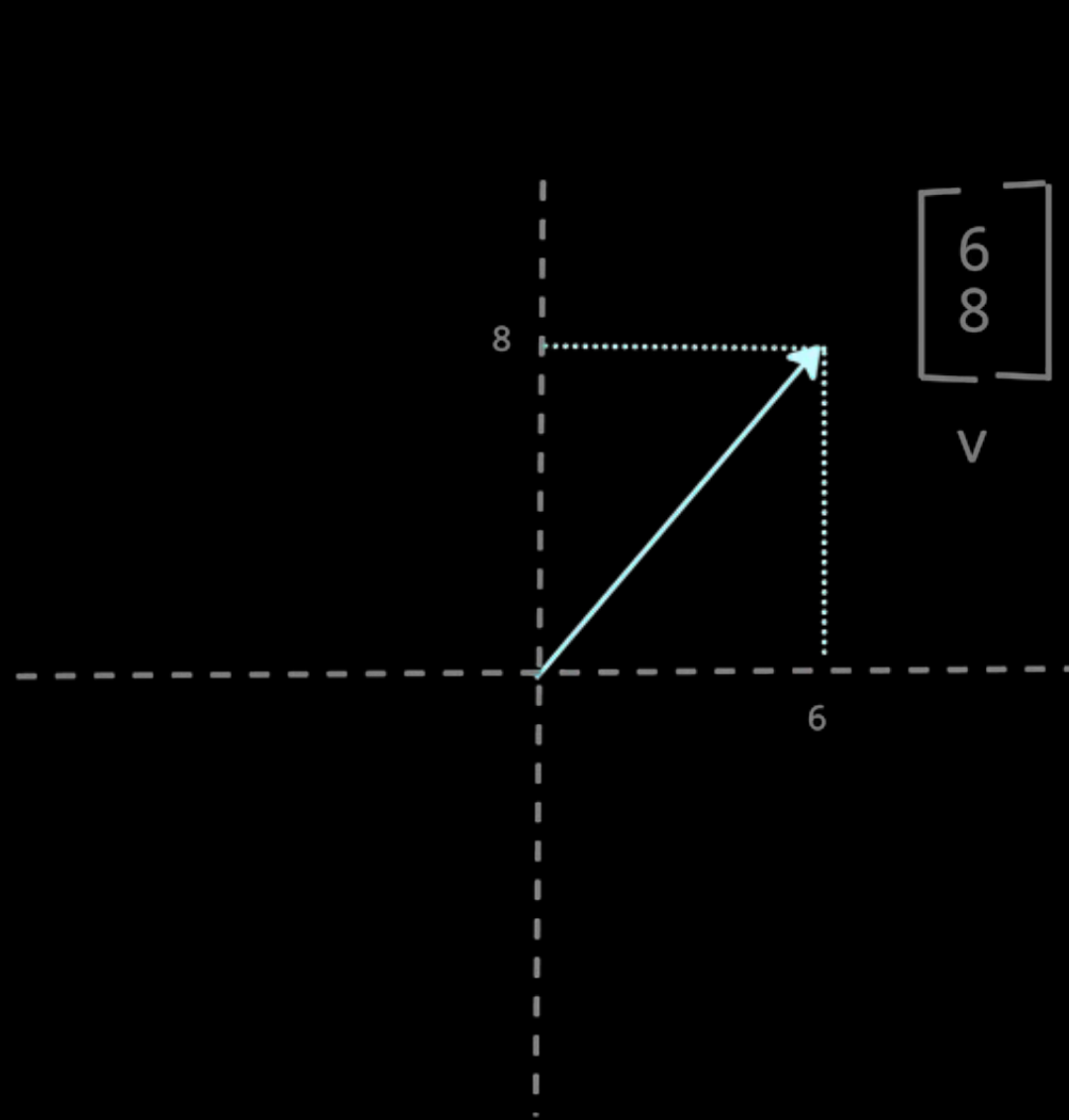


# Applied Linear Algebra Series

## Part 1 : Vectors



# What are vectors ??

lets take an example : suppose a person can have many features such as its height , weight



Person(1)

Person / Features	Height <sub>cm</sub>	Weight <sub>kg</sub>
Person (1)	135 cm	75 Kg
Person (2)	98cm	58 Kg



Person(2)

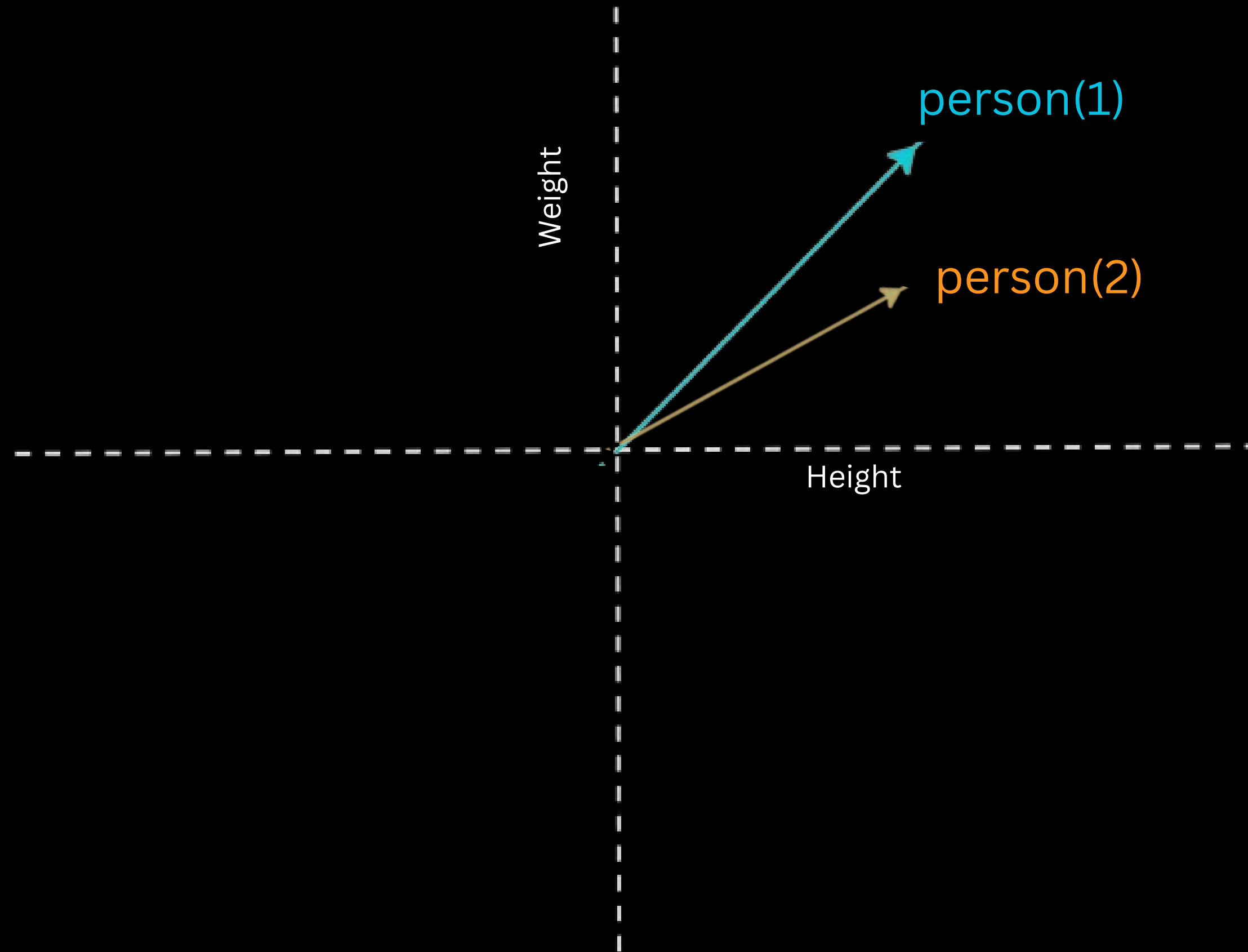
# Lets model a person in vector space |R -2

$$\text{person\_vector} = \begin{bmatrix} \text{Height} \\ \text{Weight} \end{bmatrix} = \begin{bmatrix} X \\ Y \end{bmatrix}$$

$$\text{Person(1)} = \begin{bmatrix} 135\text{cm} \\ 75\text{kg} \end{bmatrix} \quad \text{Person(2)} = \begin{bmatrix} 98\text{cm} \\ 58\text{kg} \end{bmatrix}$$

lets model x-axis as height and y-axis as weight





“ so a person can be represented as a vector based on its feature such as weight, height “



# Lets Extend this idea of vector's to a 3-dimensional vector space |R-3

we add another dimension by adding another feature of the person “Age”



Person(1)

Person / Features	Height <sub>cm</sub>	Weight <sub>kg</sub>	Age (y)
Person (1)	135 cm	75 Kg	30 years
Person (2)	98cm	58 Kg	25 years

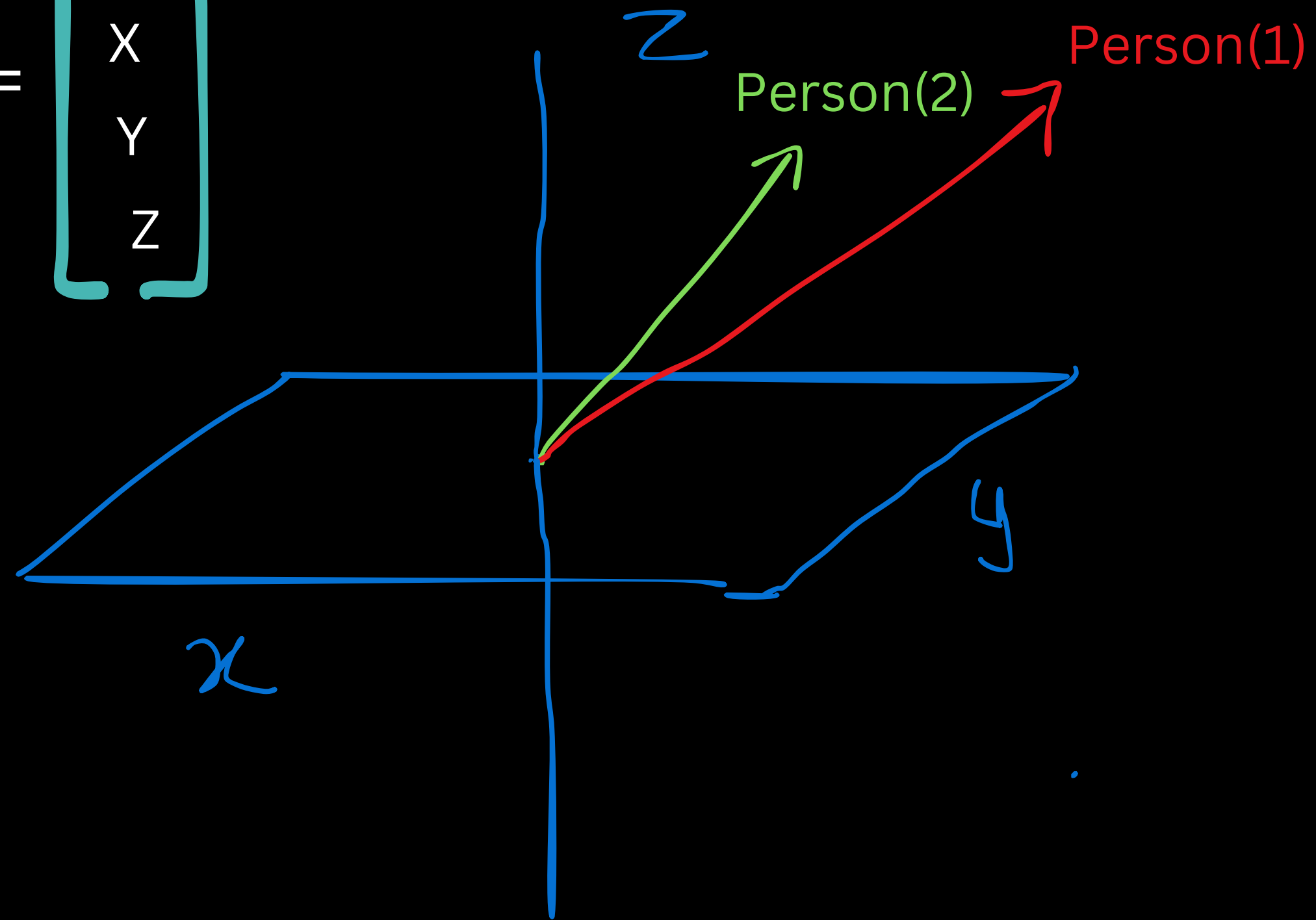
Person =  $\begin{bmatrix} \text{Height} \\ \text{Weight} \\ \text{Age} \end{bmatrix}$



Person(2)



$$\text{Person} = \begin{bmatrix} \text{Height} \\ \text{Weight} \\ \text{Age} \end{bmatrix} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

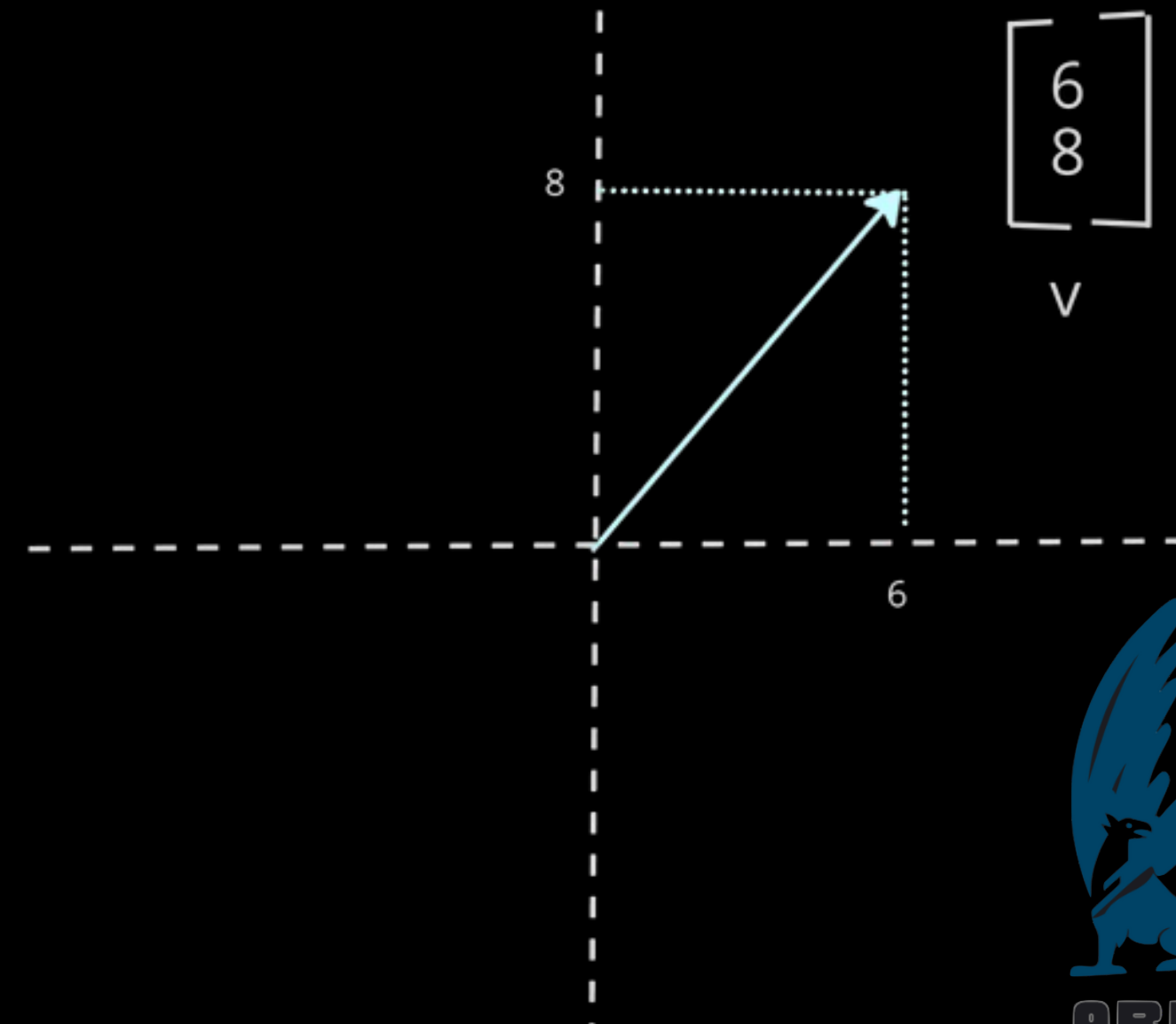
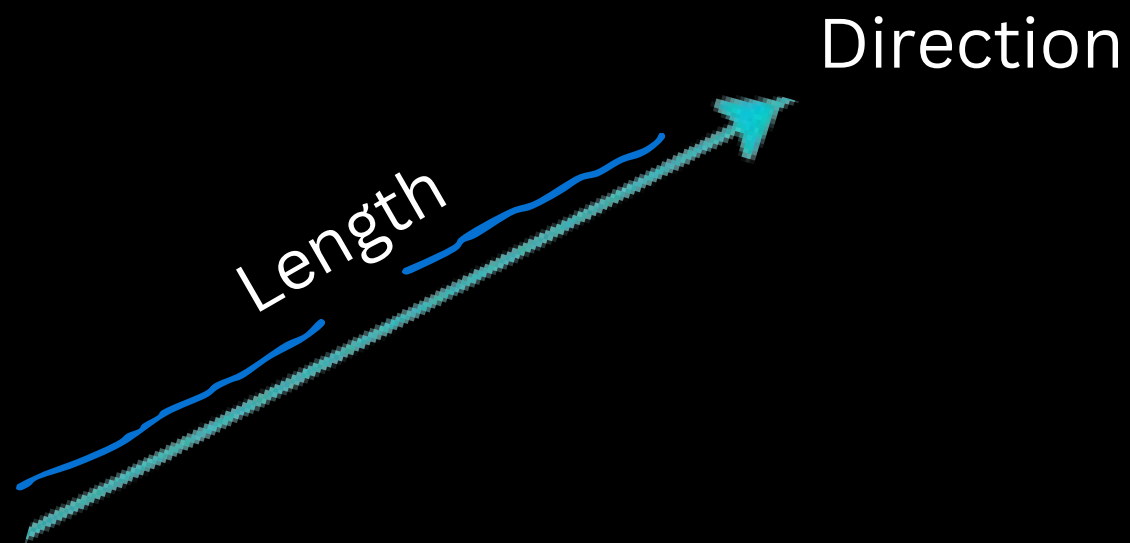


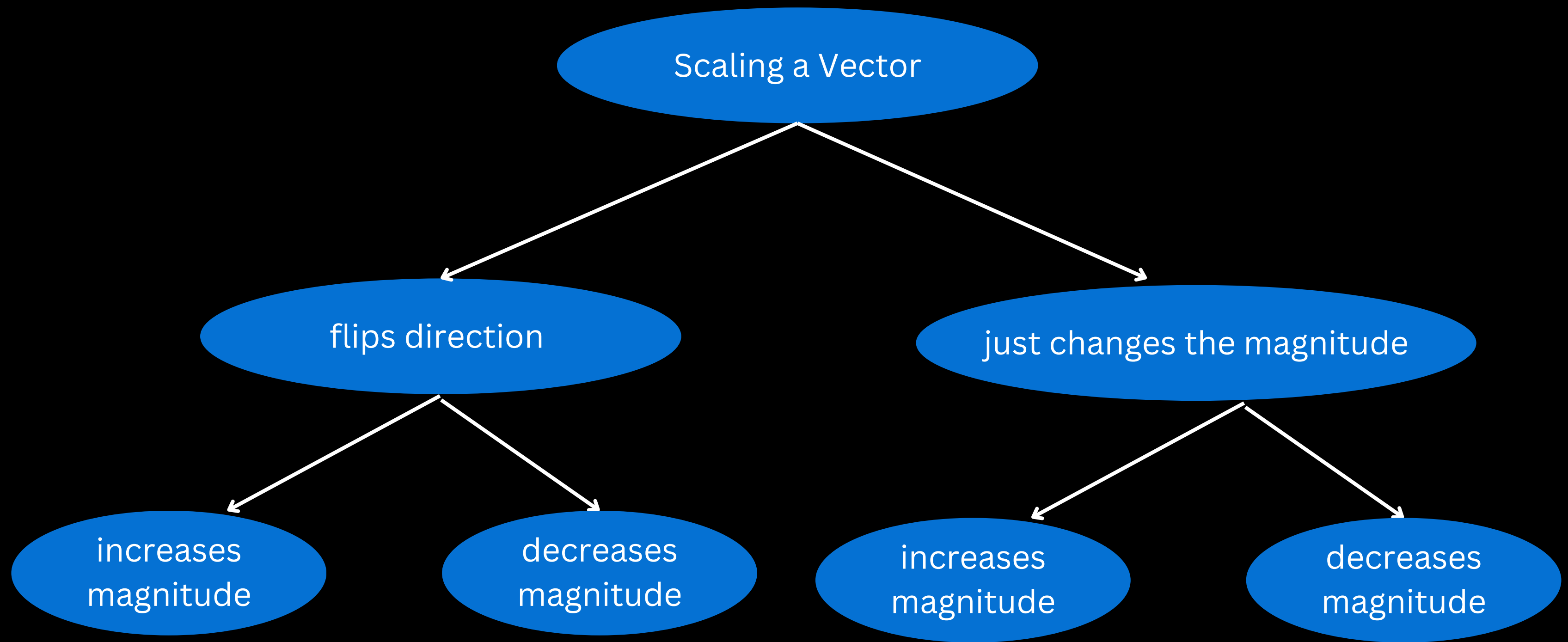
here the person is represented as a vector in R3 with the help of features such as height ,weight and age



**Vector's:** vectors can be represented as an arrow in a vector space where its tail sits at the origin and its head is pointing towards the direction of the vectors

- a vector has two properties one its magnitude the other one is its direction
- a vector can be used to represent an entity in n-dimension , and that entity has n features

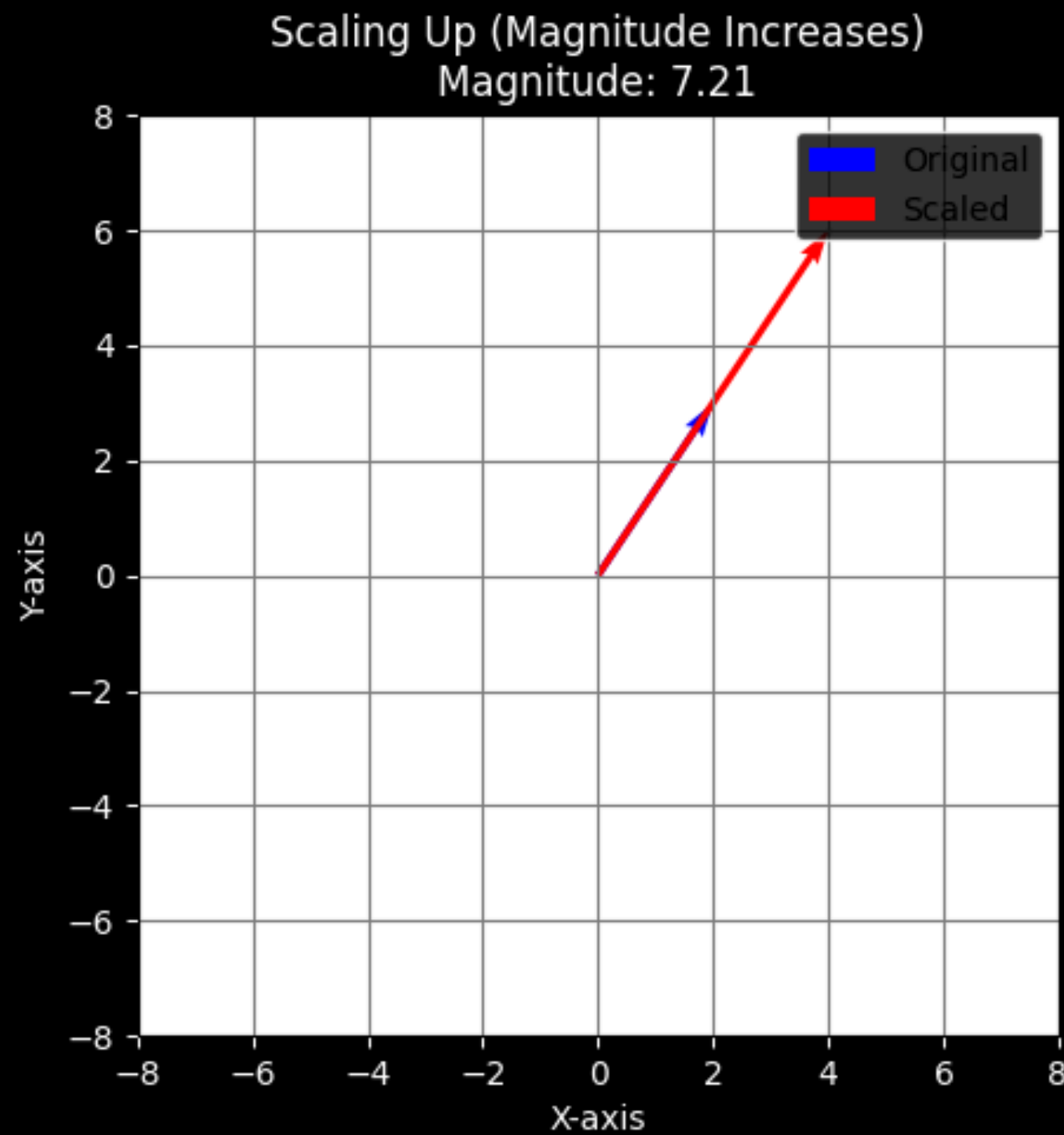






# lets see how we can scale vector

Increasing the magnitude / length



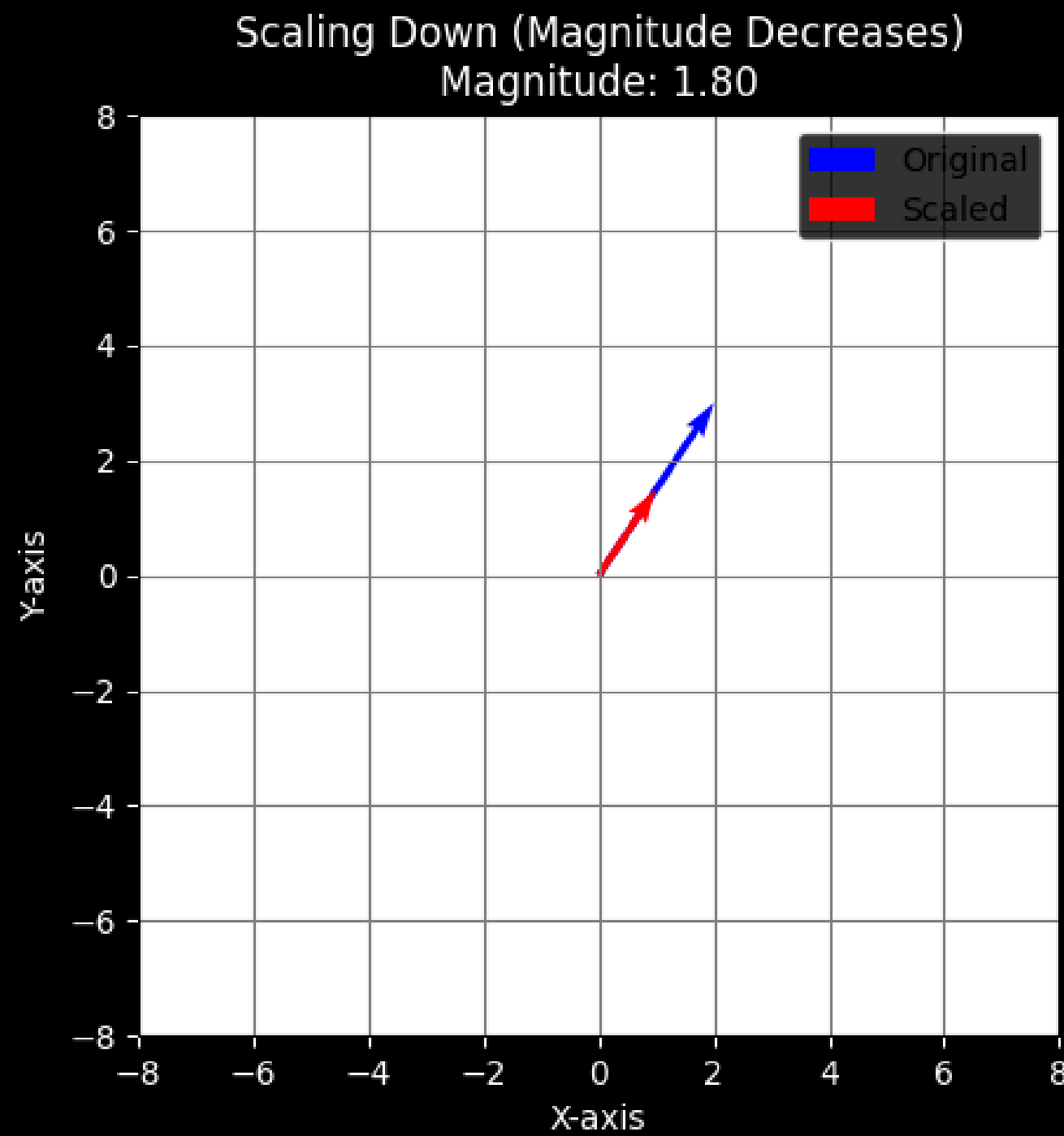
$$\vec{v} = \begin{bmatrix} 2 \\ 3 \end{bmatrix} \quad \vec{w} = \alpha \vec{v} \quad \alpha = 2$$
$$\vec{w} = 2 \cdot \begin{bmatrix} 2 \\ 3 \end{bmatrix} = \begin{bmatrix} 4 \\ 6 \end{bmatrix}$$

- (w) is the scaled vector where we increase the length of vector (v) by a scaling factor of 2



# lets see how we can scale vector

decreasing the magnitude / length

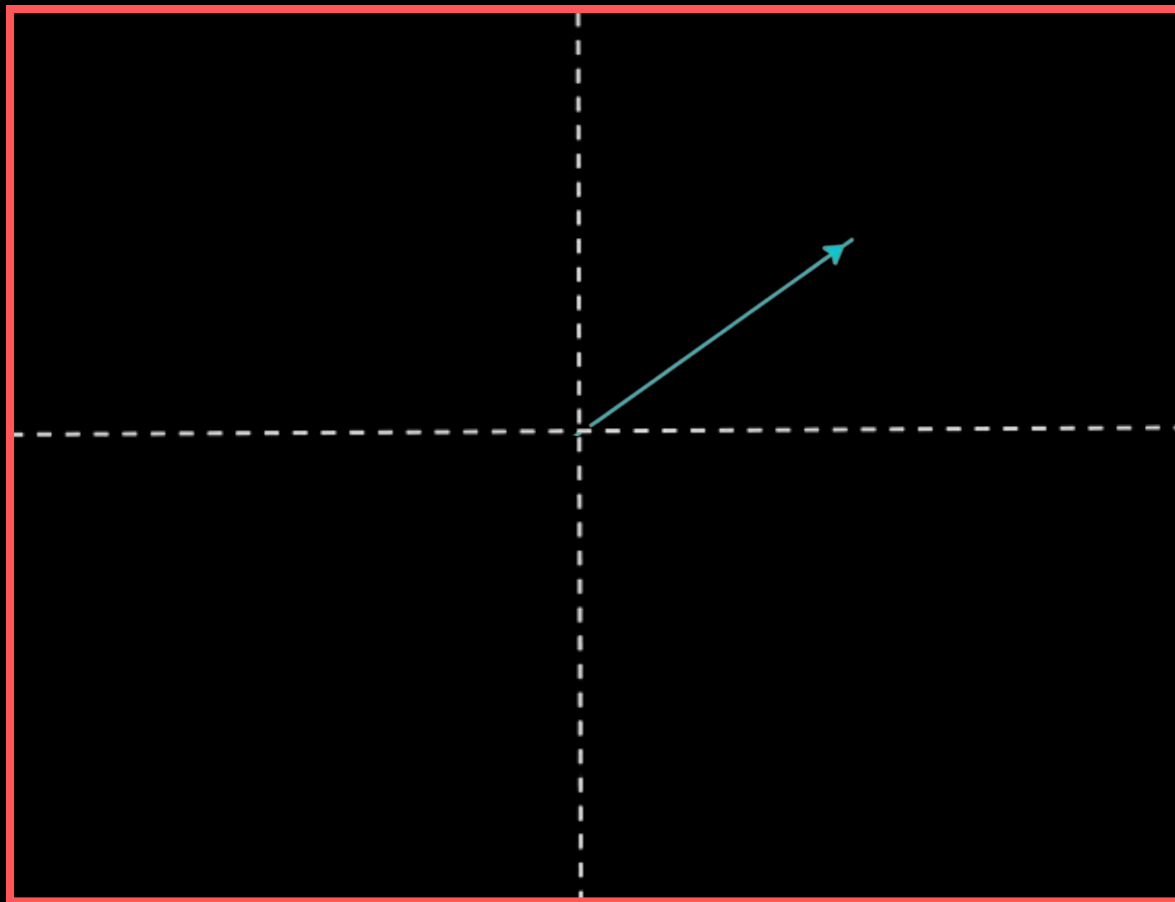


$$\vec{v} = \begin{bmatrix} 2 \\ 3 \end{bmatrix} \quad \vec{w} = \alpha \vec{v} \quad \alpha = \frac{1}{2}$$
$$\vec{w} = \frac{1}{2} \begin{bmatrix} 2 \\ 3 \end{bmatrix} \quad \vec{w} = \begin{bmatrix} 1 \\ 1.5 \end{bmatrix} = \begin{bmatrix} 1 \\ 1.5 \end{bmatrix}$$

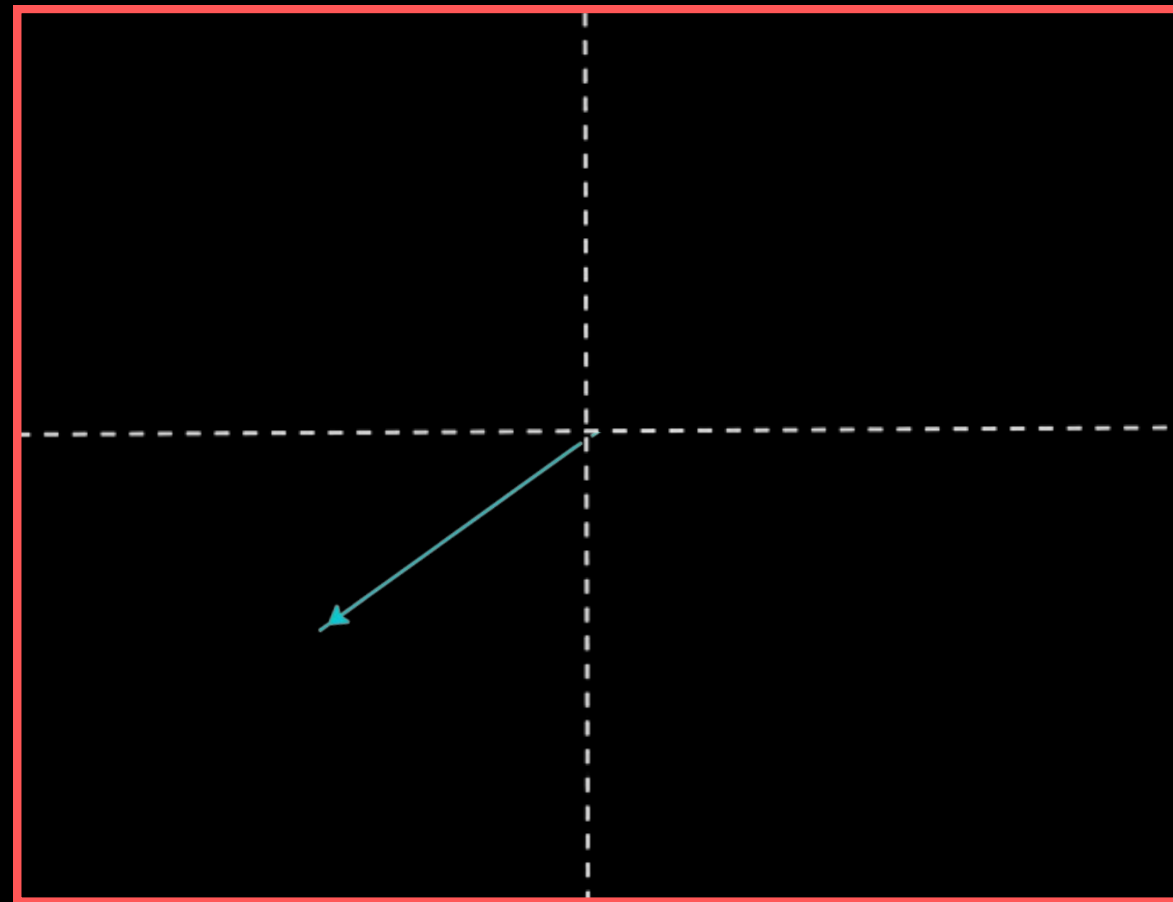
- (w) is the scaled vector where we decrease the length of vector (v) by a scaling factor of (1/2)



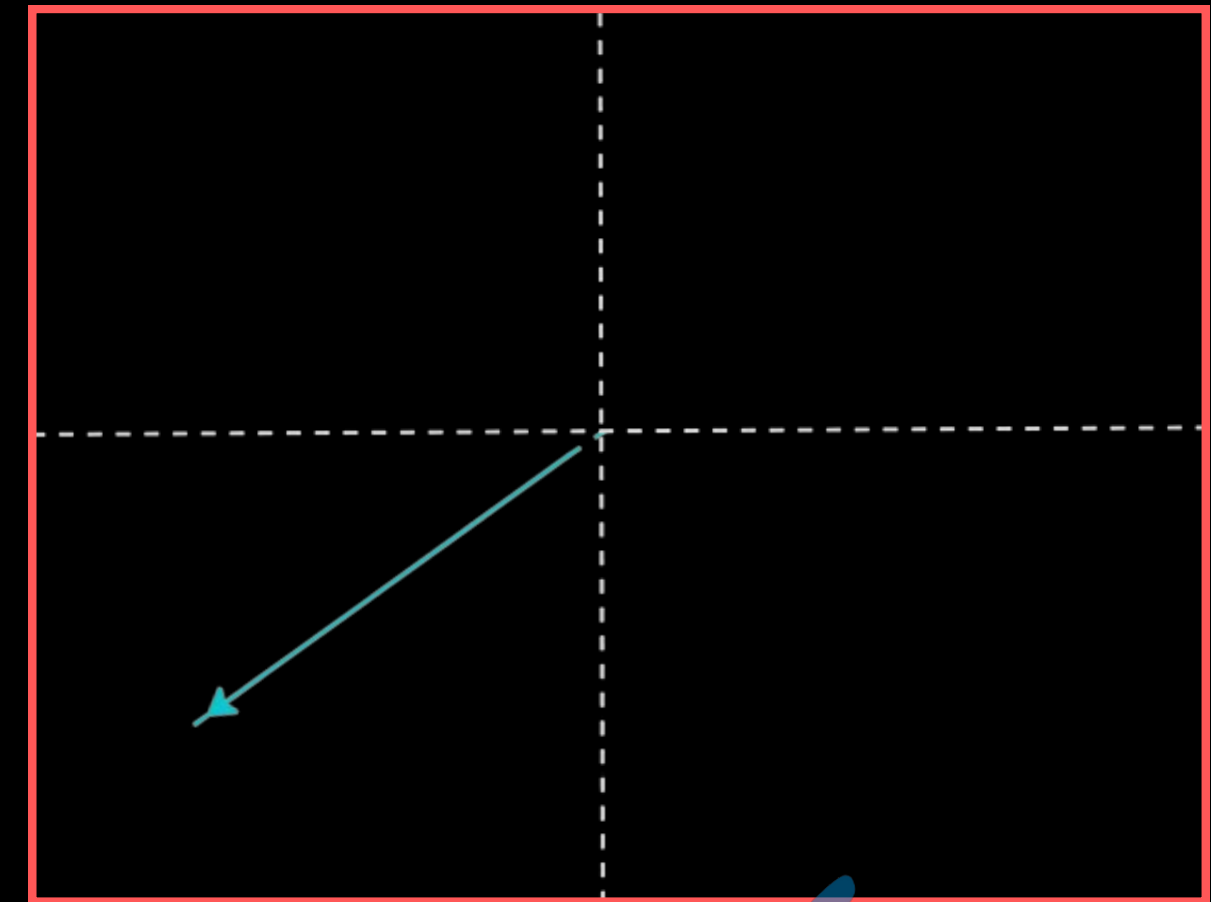
Lets see Flipping the direction and then scaling the vector



Original Vector ( $v$ )



Flipped vector ( $-v$ )

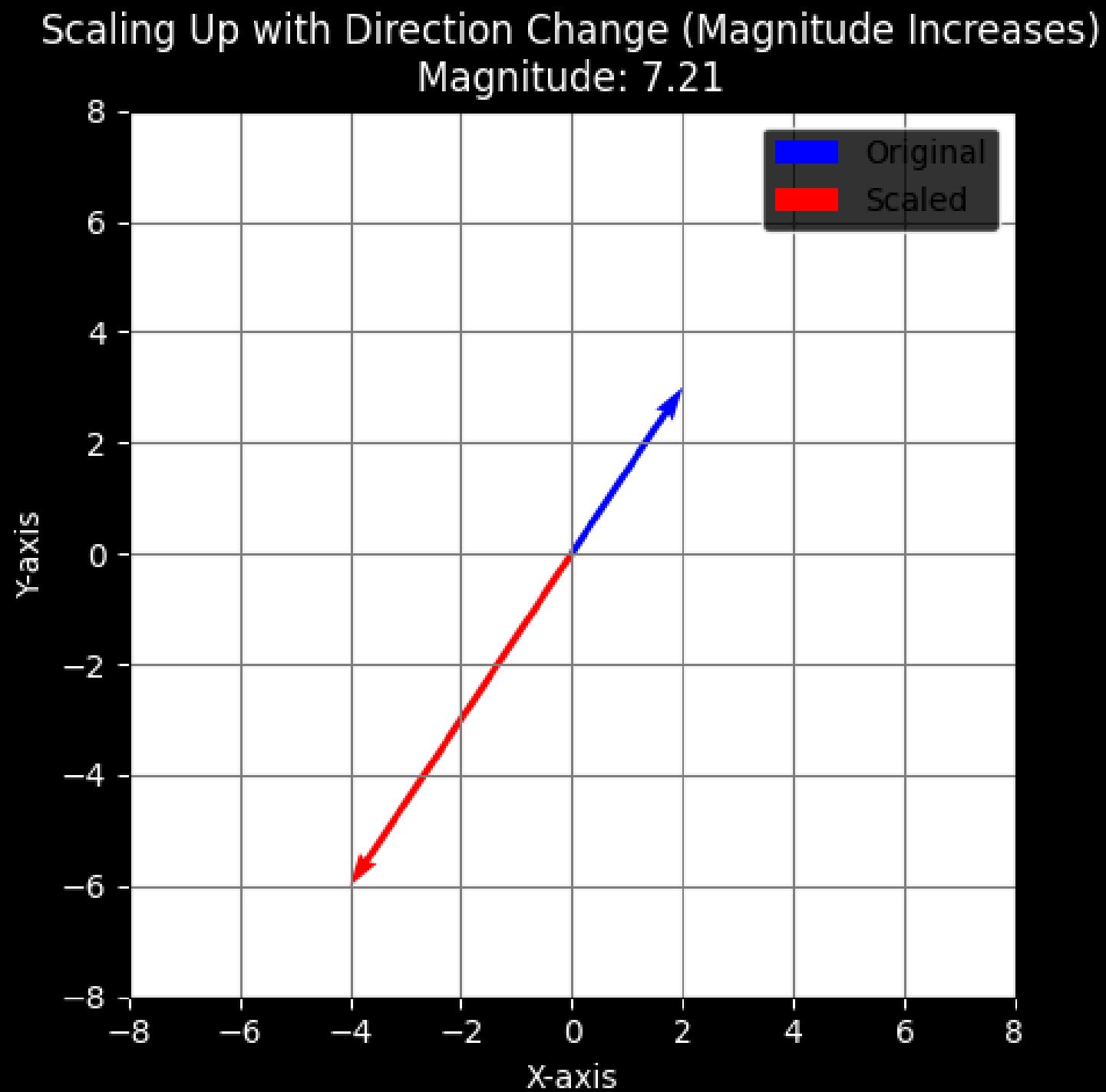


Scaled vector



# lets see how we can scale vector

## Flipping the direction (increasing magnitude)



$$\vec{v} = \begin{bmatrix} 2 \\ 3 \end{bmatrix} \quad \vec{w} = \alpha \vec{v} \quad \alpha = -1 \times 2$$
$$\vec{w} = -2 \begin{bmatrix} 2 \\ 3 \end{bmatrix} \quad \vec{w} = \begin{bmatrix} -4 \\ -6 \end{bmatrix}$$

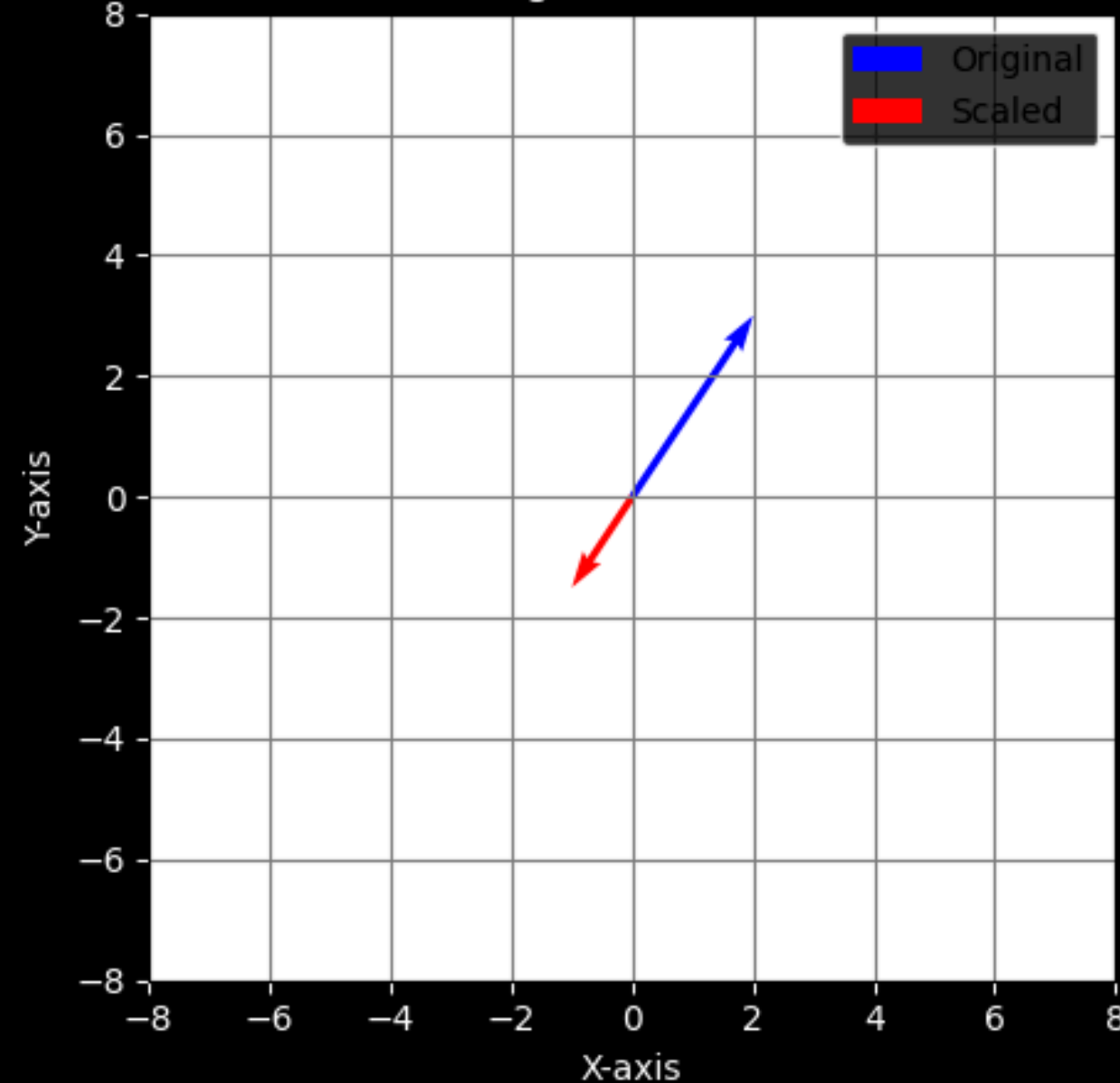
- (w) is the flipped scaled vector where we increase the length of vector (v) by a scaling factor of (-2)



# lets see how we can scale vector

## Flipping the direction (decreasing magnitude)

Scaling Down with Direction Change (Magnitude Decreases)  
Magnitude: 1.80



$$\vec{v} = \begin{bmatrix} 2 \\ 3 \end{bmatrix} \quad \vec{w} = \alpha \vec{v} \quad \alpha = -\frac{1}{2}$$
$$\vec{w} = -\frac{1}{2} \begin{bmatrix} 2 \\ 3 \end{bmatrix} \quad \vec{w} = \begin{bmatrix} -1 \\ -1.5 \end{bmatrix}$$

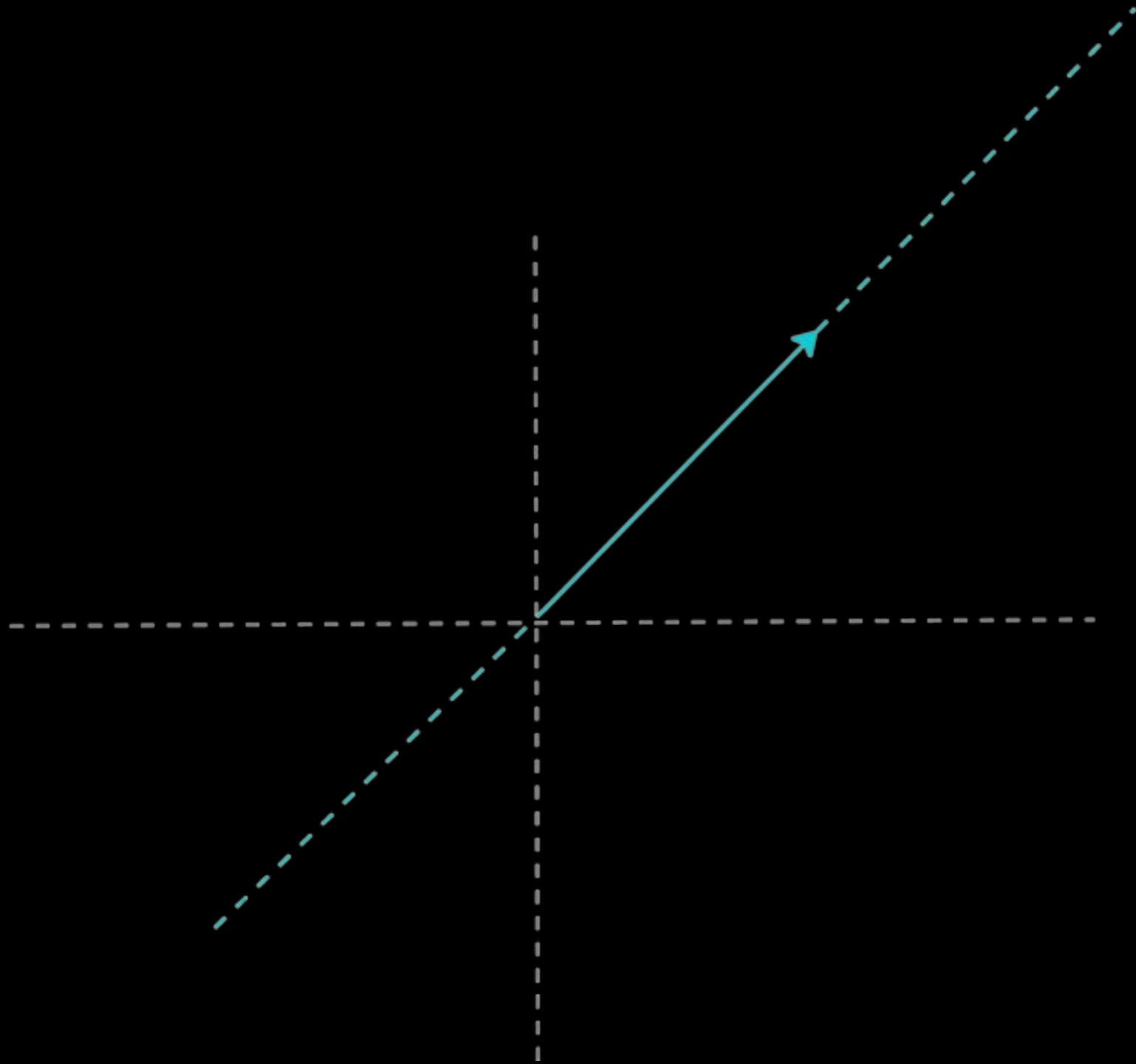
- (w) is the flipped scaled vector where we decrease the length of vector (v) by a scaling factor of (-1/2)



## Lets Summarize Vector scaling

$$\vec{w} = \alpha \vec{v}$$

NOTE : for any values of  $\alpha$  the vector  $\vec{w}$  stays on this dashed line



# Vector Addition

< what does it mean to add two vectors in linear algebra

$$\vec{s} = \vec{v} + \vec{w}$$

$$\vec{s} = \begin{bmatrix} a_1 \\ a_2 \\ a_3 \end{bmatrix} + \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}$$

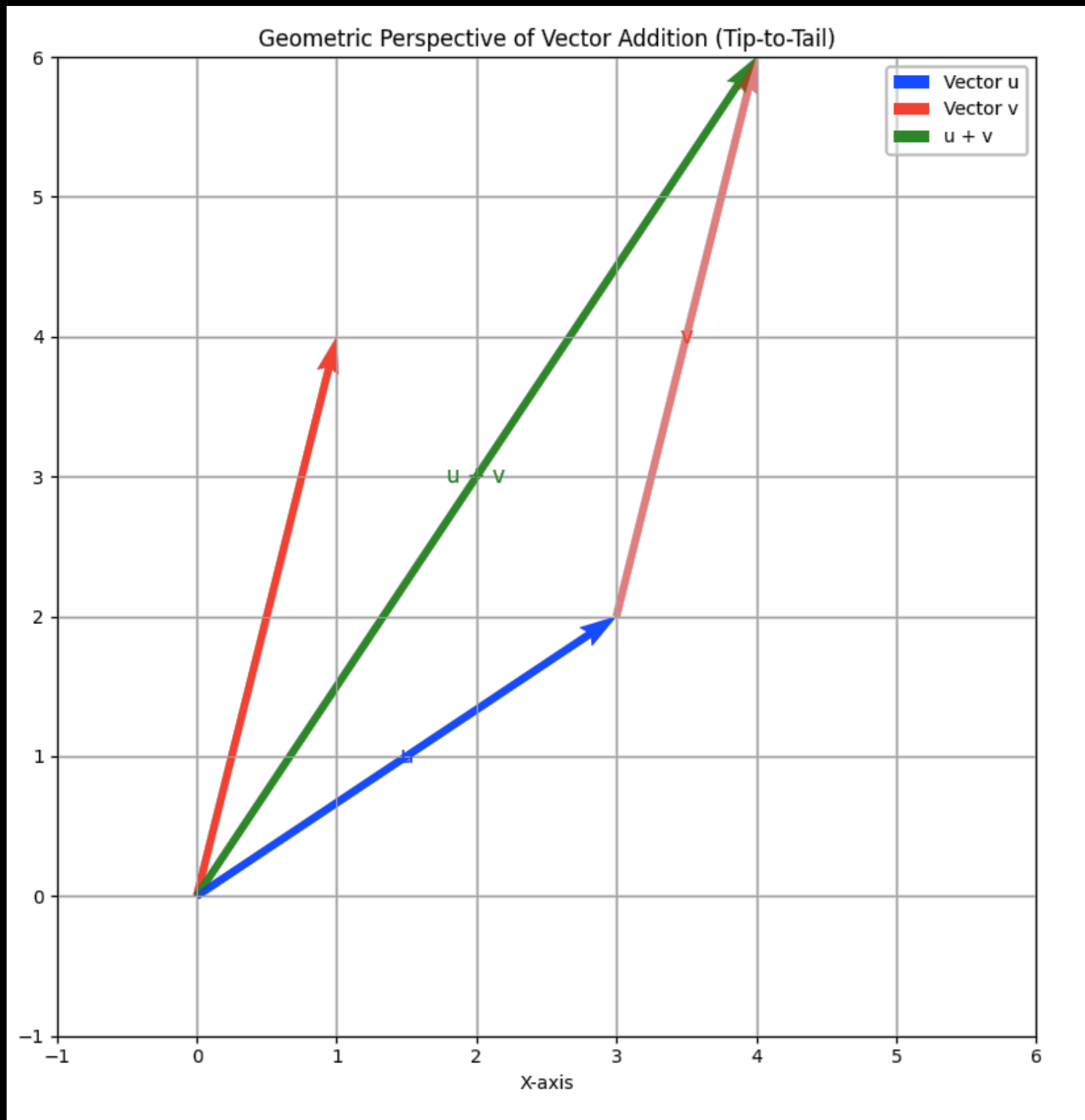
$$\vec{s} = \begin{bmatrix} a_1 + b_1 \\ a_2 + b_2 \\ a_3 + b_3 \end{bmatrix}$$

Vector addition is similar to scalar addition it works element wise



# Vector Addition

## Geometric definition of vector addition



- Tip-to-Tail Addition: To add the vectors, place the tail of (v) at the tip of (u). The resultant vector, ( $u+v$ ), is drawn from the tail of (u) to the tip of (v). This vector is shown in green.

