

$$\lambda \rightarrow m \boxed{f_4}$$

## Wavelength (الطول الموجي)

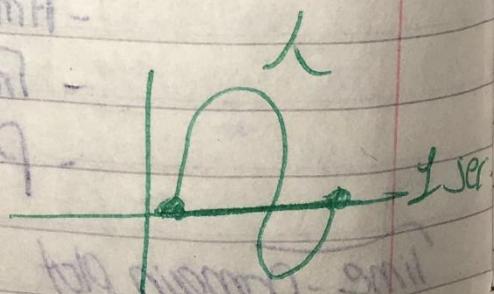
↳ Another characteristic of Signal Travelling through a Transmission Medium.

Wave length = Propagation speed  $\times$  period.

$$\text{period} = \frac{1}{\text{Frequency}}$$

$$\text{Wavelength} = \frac{\text{Speed}}{\text{Frequency}} - (\text{speed of light})$$

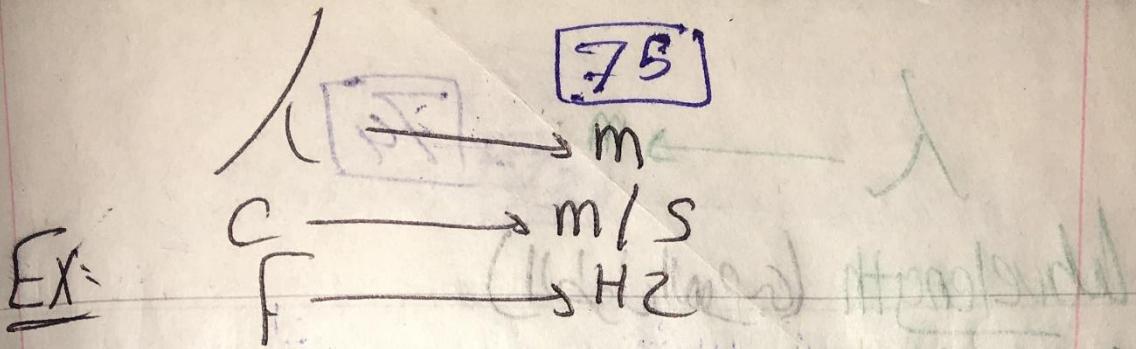
$$\lambda = \frac{c}{f} = C.T$$



Wavelength: is The Distance that a simple signal can travel in one period.

$$C = 3 \times 10^8 \text{ m/s}$$

$$\lambda = \frac{C}{f} = C.T$$



$$Speed = 3 \times 10^8 \text{ m/s}$$

$$P. \text{frequency} = 4 \times 10^{14} \text{ Hz}$$

$$\lambda = \frac{c}{f} = \frac{3 \times 10^8}{4 \times 10^{14}} = \boxed{\quad} \text{ m}$$

### \* Time & Frequency Domains:

Sine wave represented by:

- Amplitude
- Frequency / period
- phase.

#### Time - Domain plot

Shows changes in signal amplitude with respect to time.

Amplitude ~~versus~~ Time

#### Frequency Domain plot

Concerned with peak Amplitude value & the Frequency

changes

Amplitude

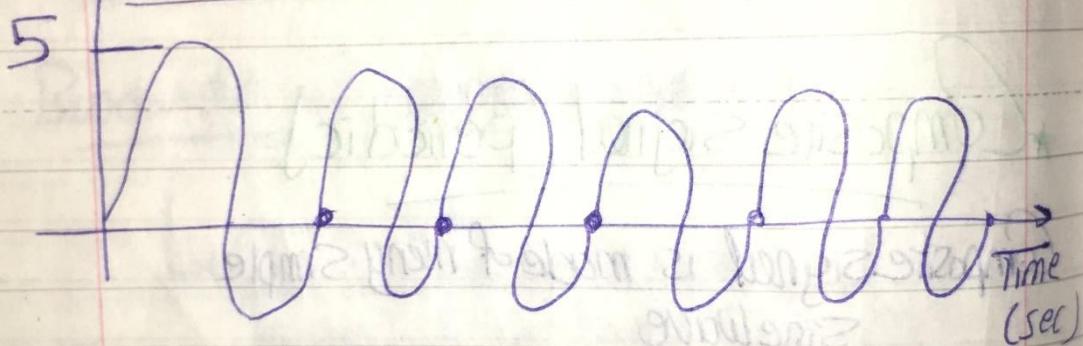
Frequency

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Amplitude (V)

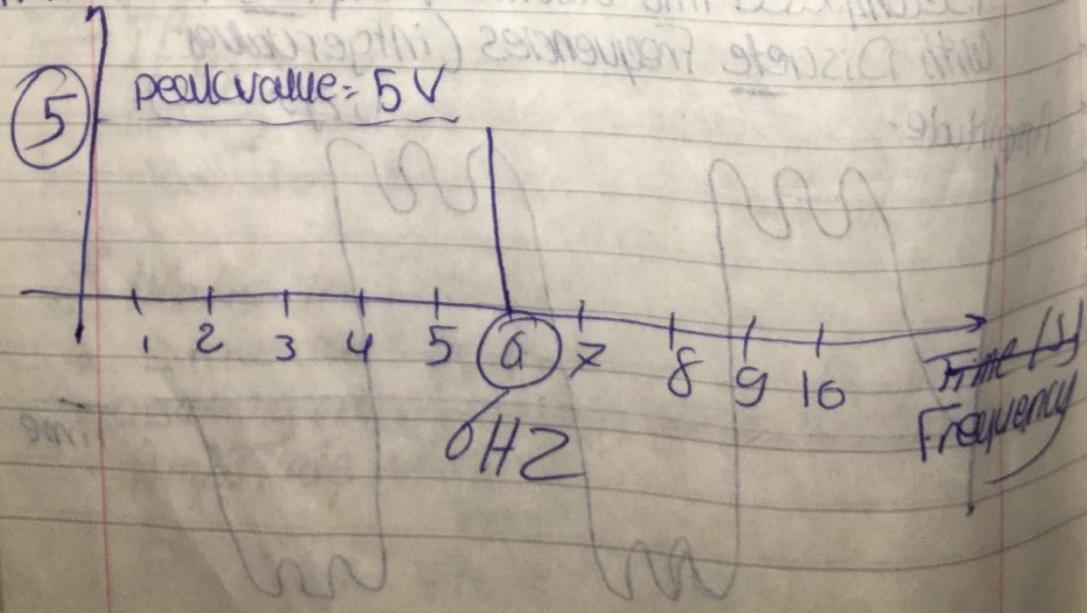
$$T = \frac{1}{f} = \frac{1}{6} = \text{sec.}$$

6 cycles  
6 periods Frequency = 6Hz



peak Amplitude = 5 Frequency = 6Hz

Amplitude:



Note:

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(v) about QM

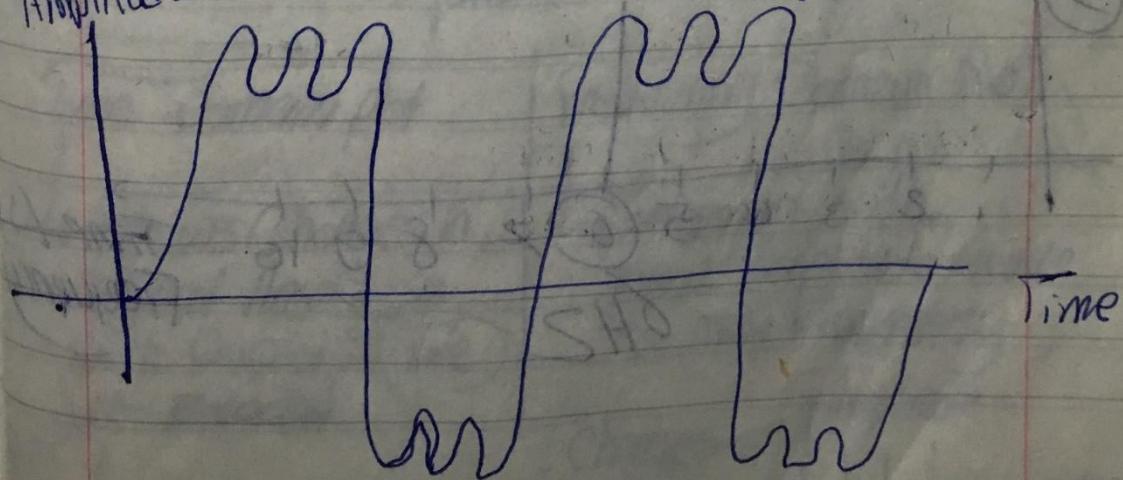
A Complete Sine Wave in the Time Domain Can be Represented by one single Spike in The Frequency Domain.

### \* Composite Signal (periodic):

Composite signal is made of many simple Sine wave

- \* A Composite periodic signal can be Decomposed into a series of Simple Sine waves with Discrete Frequencies (integer values).

Amplitude-



~~Ex 78~~ Composite Signal

\* Bandwidth →

↳ Bandwidth The Range of Frequencies  
Contained in Composite Signal.

Bandwidth of Composite Signal

↳ The Difference Between The  
Highest & The Lowest Frequencies  
in The Signal.

~~Ex:~~ If a periodic Composite Signal is Decomposed  
into 5 Sine Waves with Frequencies

100 300 500 700 900 Hz

\* What is the Bandwidth?

\* Draw the spectrum

- assuming all Components have a maximum  
Amplitude of 10 V

$$B = 800 \quad A = 10$$

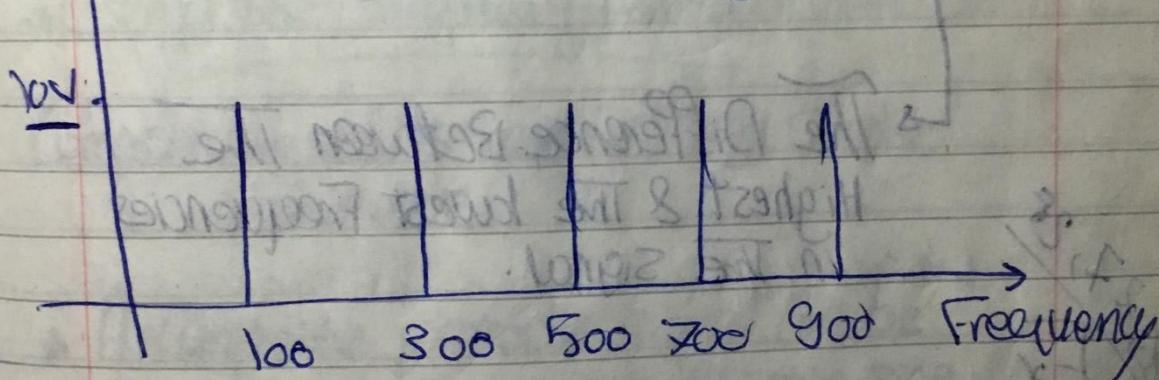
18. [79]

Solution:

$$\text{Bandwidth} = \text{High F} - \text{Low F}$$
$$= 900 - 100 = 800 \text{ Hz}$$

Amplitude:

+ The spectrum



Ex:

A periodic signal has Bandwidth of 20 Hz, The highest Frequency is 60 Hz, what is the lowest Frequency?

Draw the spectrum. of all Frequencies have The same Amplitude.

Frequency  
60  
+  
High

Bandwidth = 20 Hz   low f = ???  
High f = 60 Hz   180

Solution:

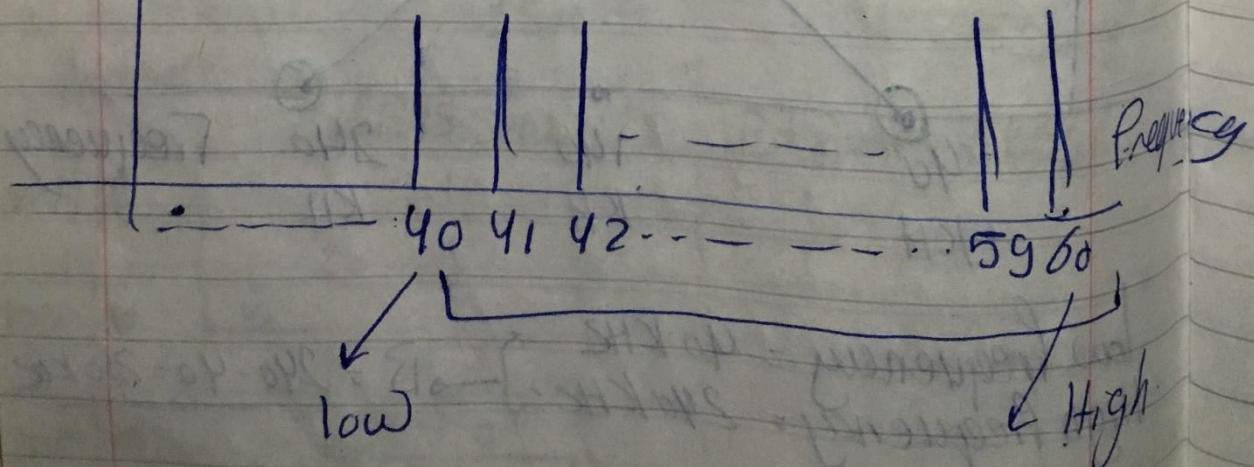
Bandwidth, High f - low f

$$20 = 60 - \text{low } f$$

$$\text{low } f: 60 - 20 = 40 \text{ Hz}$$

Spectrum:

↑ Amplitude -



SSSS - Ques) SH od = Attributed no. 3

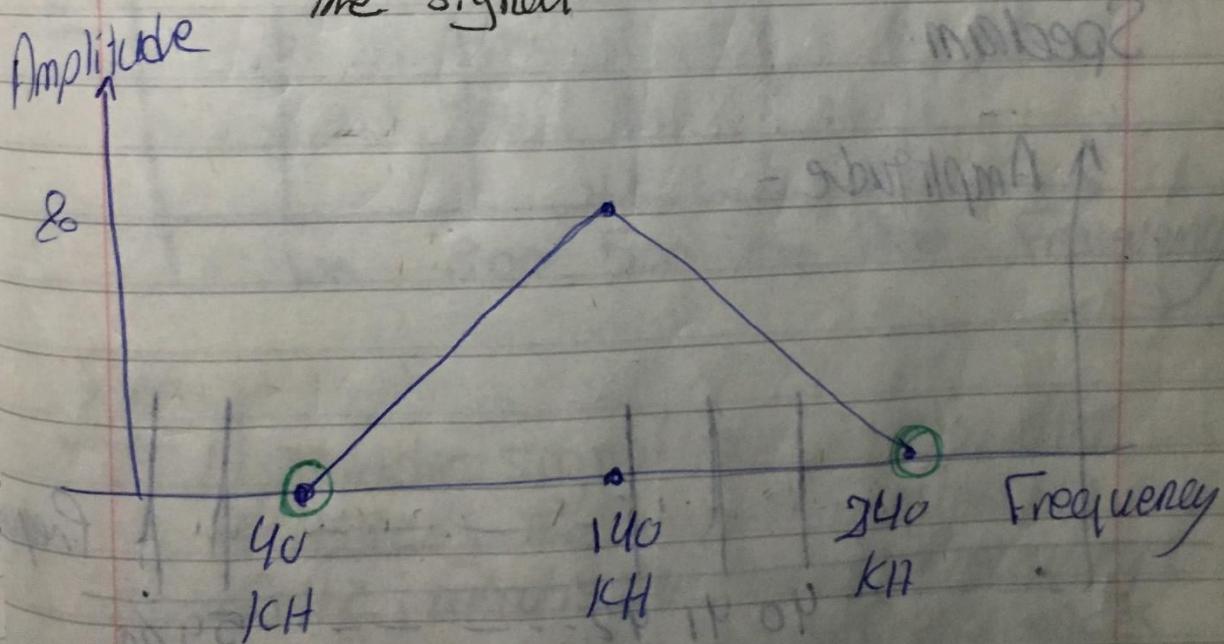
81

SH od = Q. dpt/

Ex: 3.12

A nonperiodic Composite signal has Bandwidth 200 kHz, with a Middle Frequency of 140 kHz & peak Amplitude of 20 V.

The two Extreme Frequencies have an amplitude of 0. Draw the frequency domain of the signal.



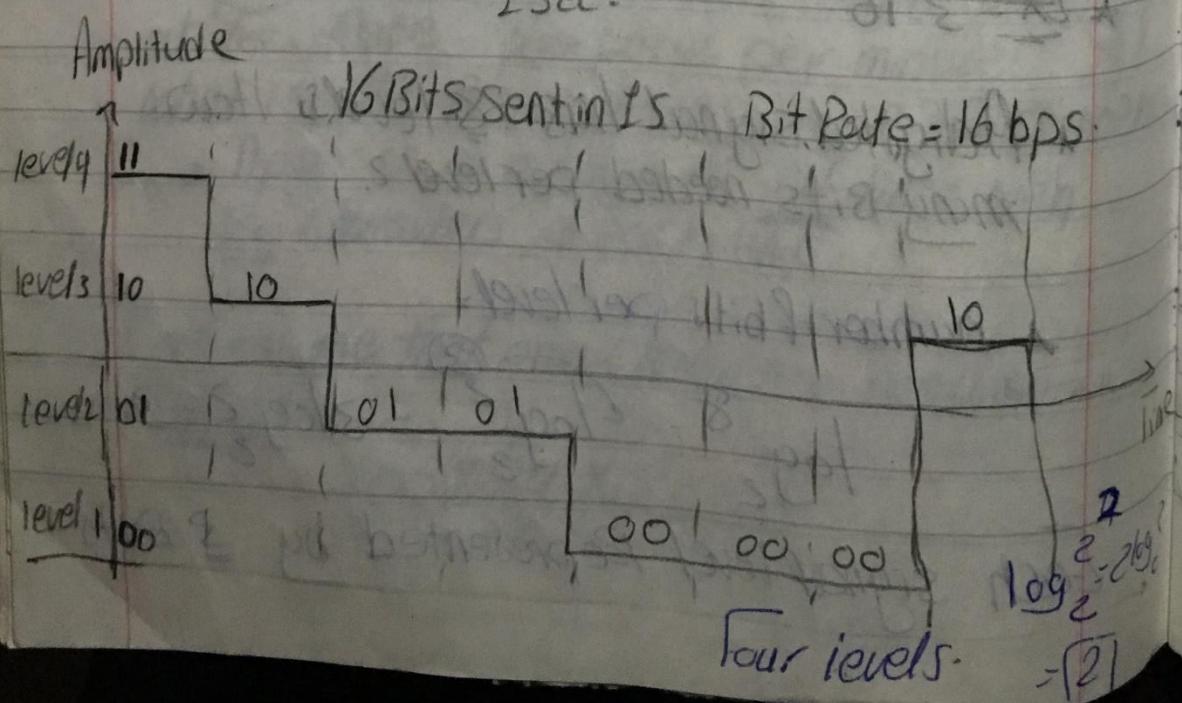
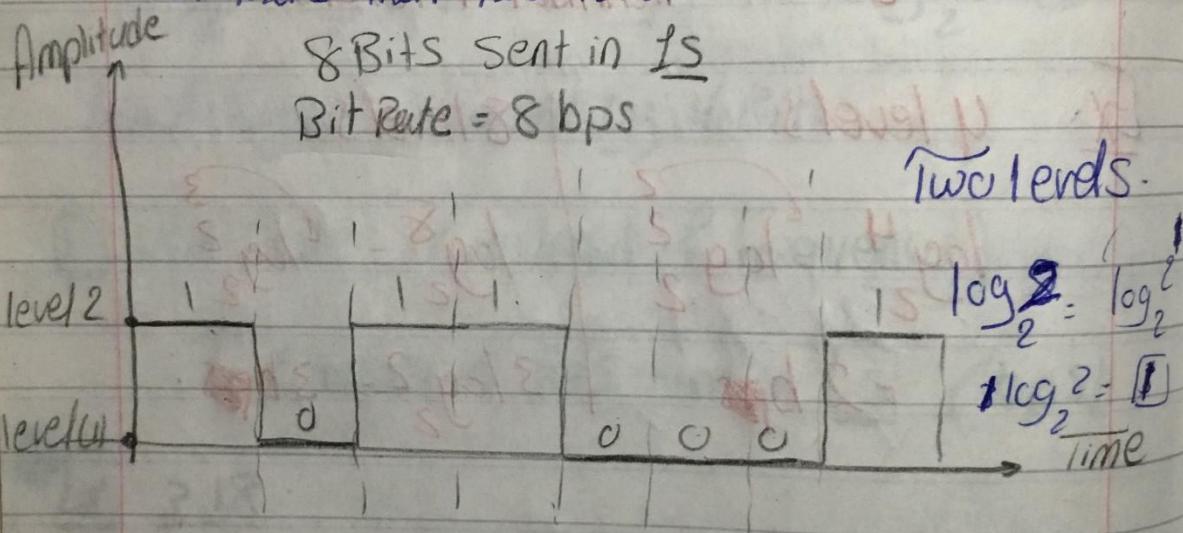
$$\text{Low frequency} = 40 \text{ kHz}$$
$$\text{High frequency} = 240 \text{ kHz}$$
$$B = 240 - 40 = 200 \text{ kHz}$$

$$2^x = 2 \log_2$$

→ Discrete Signal Values  
 → Finite Values  
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### \* Digital signal:

- Digital signal can have more than two levels or more than two levels.



(83)

\* Number of Bits per level =

$$\log_2 \text{number of levels}$$

Ex. 4 levels

$$\log_2 4 = \log_2 2^2$$

= 2 bits

8 levels.

$$\log_2 8 = \log_2 2^3$$

= 3 bits

\* Ex. 3.16

\* A digital signal has 8 levels, how many bits needed per level?

\* number of bits per level:

$$\log_2 8 = \log_2 2^3 = 3 \log_2 2 = 3$$

Each signal level represented by 3 bits.

Ex: 3.17

- A Digital signal has 9 levels.  
How many bits need per level?

$$\log_2 9 \xrightarrow{\text{use log}} \log_2^2 = 4 \log_2 2 = 4$$

Each signal represent by 4 Bits

II Bit Rate: (instead of Frequency)

↳ Number of Bits sent in 1s (bps).

Ex: 3.18

- Assume we need Download text documents at the rate 100 page per minute.
- what is the required bit rate of the channel
- \* A page is an average of 24 lines with 80 characters in each line.

∴ we assume that one character requires 8 bits.

$$100 \times 24 \times 80 \times 8 =$$

J bps.

$B = 4\text{ kHz}$ . Analogue voice  
 Digital signal

Ex. 3.19

A Digitized voice channel, is made by a 4kHz Bandwidth Analogue Voice signal.

We need to sample the signal at twice the highest frequency (Two samples per hertz). We assume that each sample requires 8 bits, what is the required bit rate.

Bit rate:

$$2 \times 8 \times 4000 = \boxed{\quad} \text{ bps.}$$

→ <sup>Two samples</sup>  $\downarrow$   $4\text{ kHz} = 4000$  <sup>81.8</sup>  
 for each sample → Bandwidth

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### \* Bit length:

↳ The Distance one Bit occupies  
on the Transmission Medium -

22, 23

$$\text{Bit length} = \text{propagation speed} \times \text{Bit Duration}$$

### \* Digital signal as Composite Analog Signal.

- Based on Fourier Analysis.

Note ↳ Digital signal is a Composite Analog  
Signal with infinite Bandwidth.

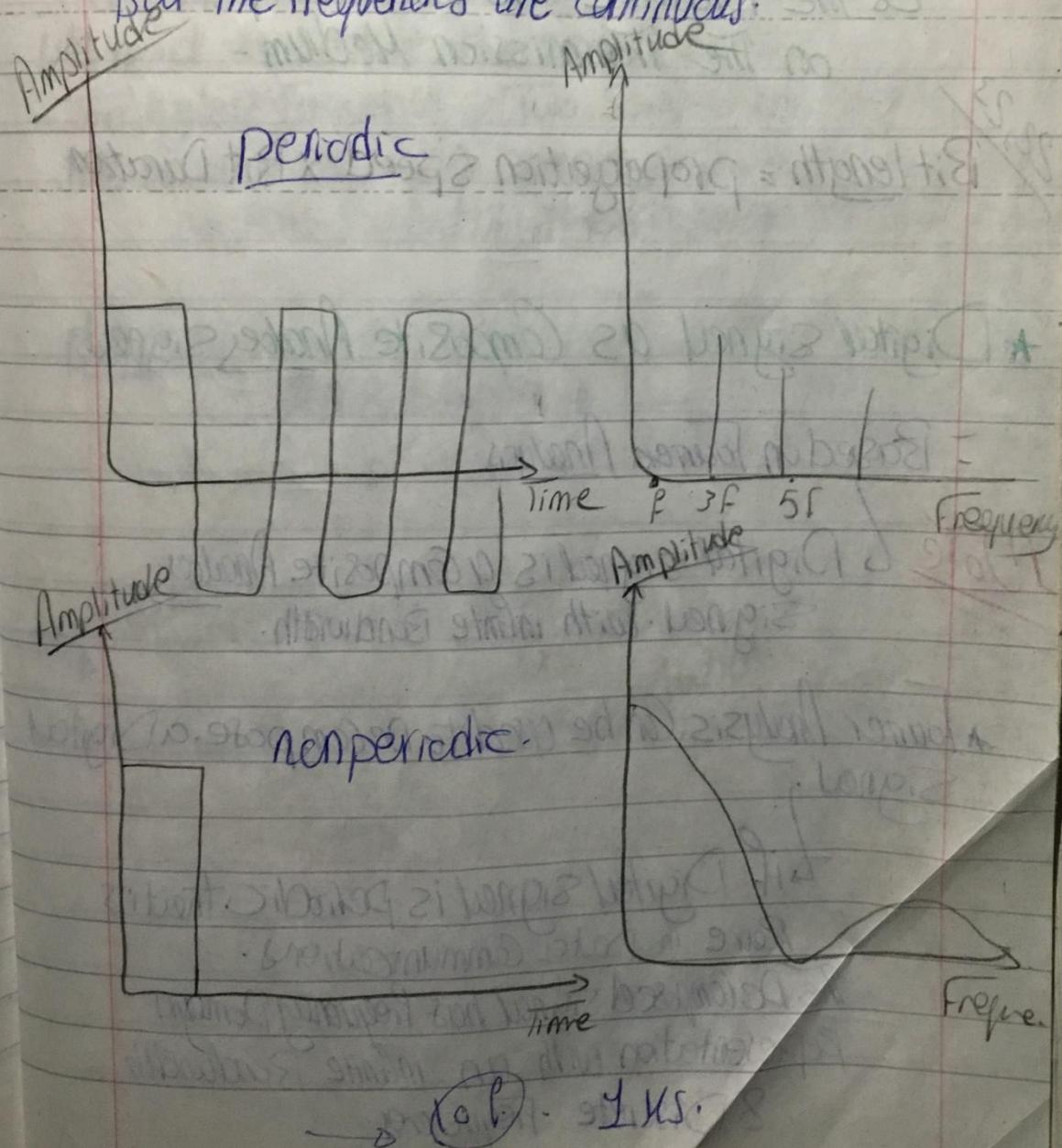
\* Fourier Analysis can be used to Decompose a Digital  
Signal;

↳ If Digital signal is periodic that is  
Rare in Data Communications.

The Decomposed signal has Frequency Domain  
Representation with an infinite Bandwidth  
8 Discrete Frequencies.

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If The Digital Signal is Nonperiodic  $\rightarrow$  The  
Decomposed signal has an infinite Bandwidth  
But the Frequencies are Continuous.



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## \* Transmission of Digital Signals

### (1) Baseband.

- means sending a digital signal over a channel without changing the digital signal to an analog signal.

### \* Low path channel

(Bandwidth starts from zero)

Note: Baseband transmission of a digital signal that preserves the shape of the digital signal is possible only if we have a low pass channel with an infinite or very wide bandwidth.

### Note:

In baseband transmission, the required bandwidth is proportional to the bit rate. If we need to send bits faster, we need more bandwidth.

### (2) Broadband (Modulation)

- means changing the digital signal to an analog signal for the transmission.

### \* band-pass channel

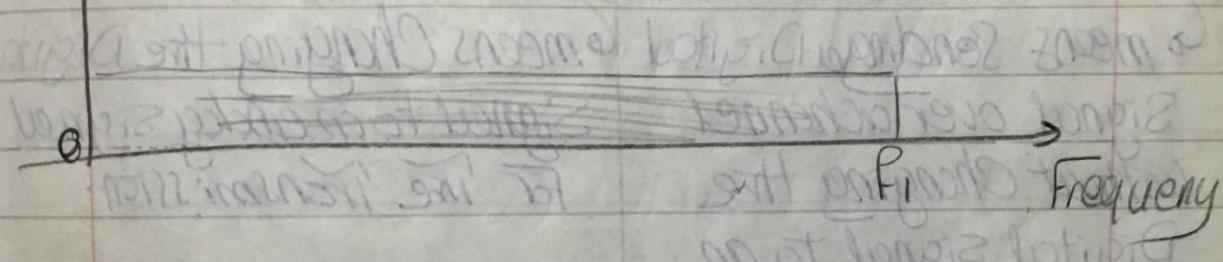
Bandwidth doesn't start from zero.

Amplitude

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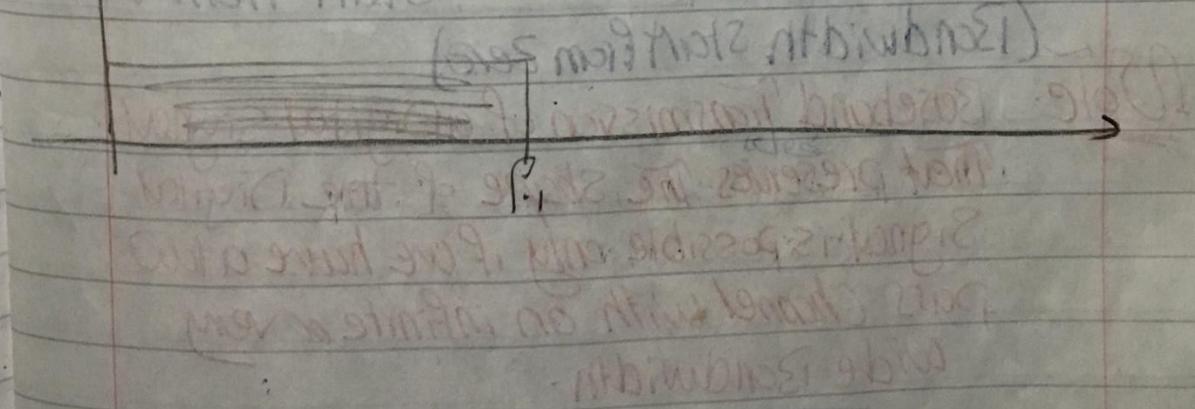
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(predominant) Low pass Channel, Wide Bandwidth.



Graphs, Wdg-band\*

Low pass Channel, Narrow Bandwidth



Opposite of low pass channel, band edge at  
high frequencies & minimum at low frequencies  
in case of narrow band

Bit (Data) Rate = ~~Bandwidth~~ Bits / sec

Table: Show How Much Bandwidth we need to send Data at Different Rates

Bit Rate (bps)	Harmonic 1.	Harmonics 1, 3	Harmonics 1, 3, 5
$n = 1 \text{ kbps}$	$B = 500 \text{ Hz}$	$B = 1.5 \text{ kHz}$	$B = 2.5 \text{ kHz}$
$n = 10 \text{ kbps}$	$B = 5 \text{ kHz}$	$B = 15 \text{ kHz}$	$B = 25 \text{ kHz}$
$n = 100 \text{ kbps}$	$B = 50 \text{ kHz}$	$B = 150 \text{ kHz}$	$B = 250 \text{ kHz}$

Ex:

What is The Required Bandwidth of a low-pass Channel if we need to send 1 Mbps by using Baseband transmission?

① The minimum Bandwidth

$$\text{② BitRate}/2 \quad 1 \text{ Mbps}/2 = 500 \text{ kHz}$$

We need low-pass channel with Frequencies between 0 to 500 kHz

[Go]

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- ① A better result achieved by using  
the first 8 third harmonics with  
the required bandwidth.

$$B = 3 \times 500 \text{ kHz} = 1.5 \text{ MHz}$$

- ③ A better result can be achieved by  
using 1, 3, 5 harmonics.

$$B = 5 \times 500 = 2500 \text{ kHz} = 2.5 \text{ MHz}$$

Ex 2.23

We have a low-pass channel with  
bandwidth 100 kHz, what is the  
maximum bit rate of this channel?

The maximum bandwidth bit rate can be  
achieved if we use the first harmonic.

$$\text{Bit Rate} = 2 * \text{Bandwidth}$$
$$2 \times 100 = \underline{200 \text{ kbps}}$$

Bit Rate  $\boxed{1}$  / 2  
Minimum Frequency

$$\text{Maximum Frequency} = 2 \times \text{Bit Rate}$$

Ex

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## \* Causes of impairment -

Attenuation

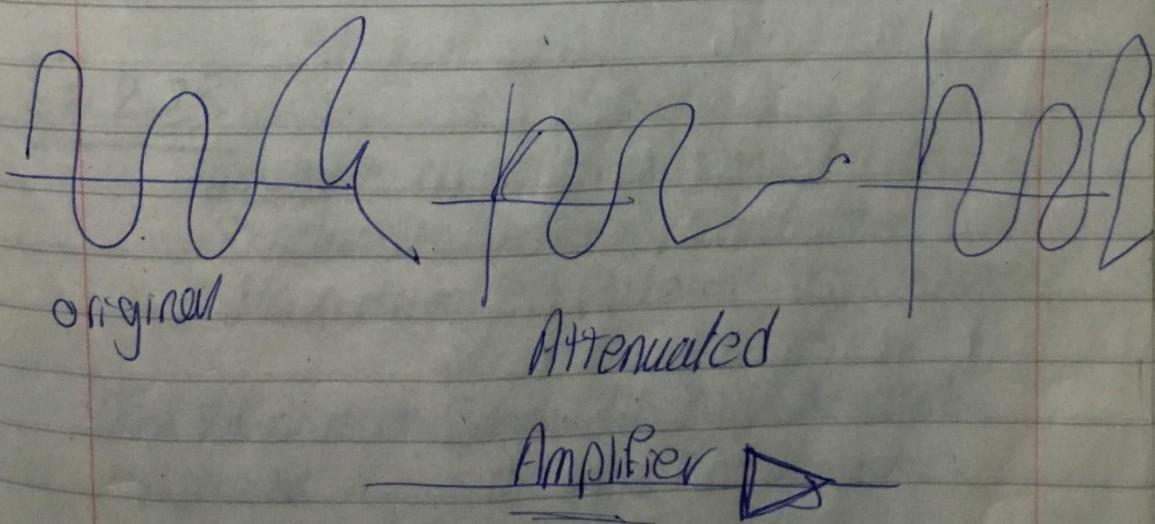
Distortion

Noise.

### ① Attenuation:

It means a loss of energy.

\* When a signal (single / composite) travels through a medium, it loses some of its energy in overcoming the resistance of the medium.



9c1

## \* Decibel (dB)

Measures the Relative strengths of  
Two signals or one signal at  
Two Different Points.

Note:

Decibel is + if signal is Amplified

- if signal is Attenuated

$$dB = 10 \log_{10} \frac{P_2}{P_1} \rightarrow \begin{array}{l} \text{Attenuation} \\ \text{original signal power} \end{array}$$

$P_2, P_1 \rightarrow$  the powers of a signal at points 1, 2

Ex: (3.26) Suppose a signal Travels Through a medium & its power is Reduced to one-half

$P_2 = \frac{1}{2} P_1$ , Calculate The Attenuation

$$= 10 \log_{10} \frac{P_2}{P_1} = \frac{0.5 P_1}{P_1} = 10 \log_{10} (0.5)$$

Ex 3.27

15e

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(a)

Decibels

A signal travels through Amplifier & its power is increased 10 times.

$$P_2 = 10 P_1$$

The Amplification (Gain of power) =

$$\log_{10} \frac{P_2}{P_1} = \log_{10} \frac{10 P_1}{P_1}$$

$$\log_{10} 10 = 10 \text{ dB}$$

Amplified

Ex: 3.30

The loss in a cable is usually defined in dB/km.

If the signal at the beginning of a cable with

-0.3 dB/km has a power 2 mW, what is the power of the signal at 5 km?

Rule:

$$\log_a b = \boxed{x}$$

$$a^x = b$$

The loss is cable

$$5 \times 0.3 = -1.5 \text{ dB}$$

$$dB = 10 \log_{10} \frac{P_2}{P_1} = -1.5$$

$$10 \log_{10} \left( \frac{P_2}{P_1} \right) = -1.5$$

$$\frac{P_2}{P_1} = 10^{-0.15} = 0.71$$

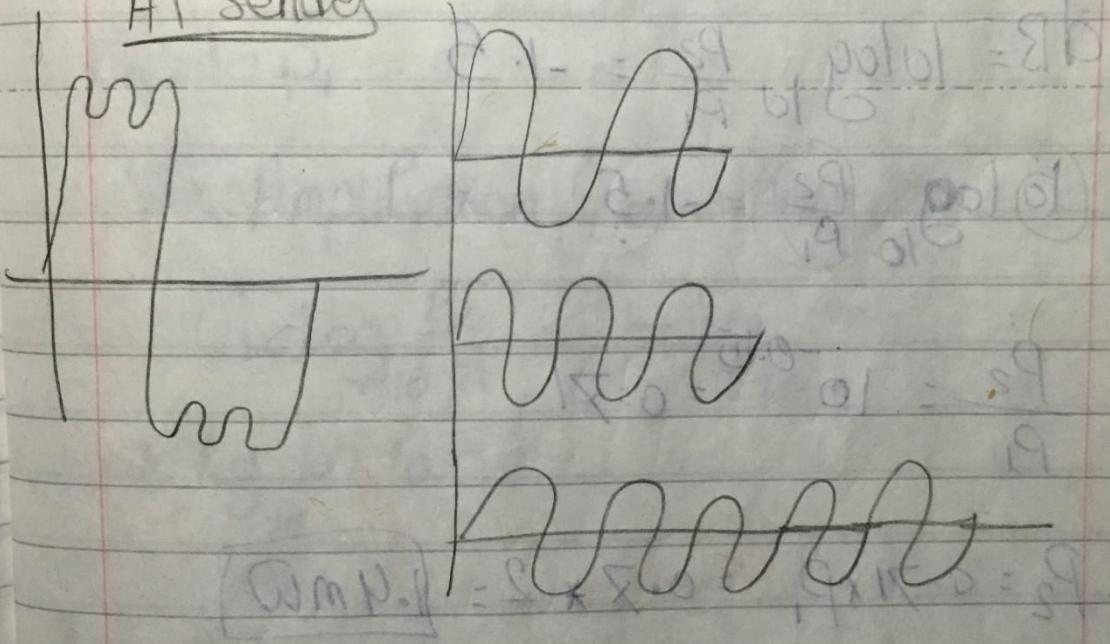
$$P_2 = 0.71 \times P_1 = 0.71 \times 2 = \boxed{1.4 \text{ mW}}$$

## 2) Distortion:

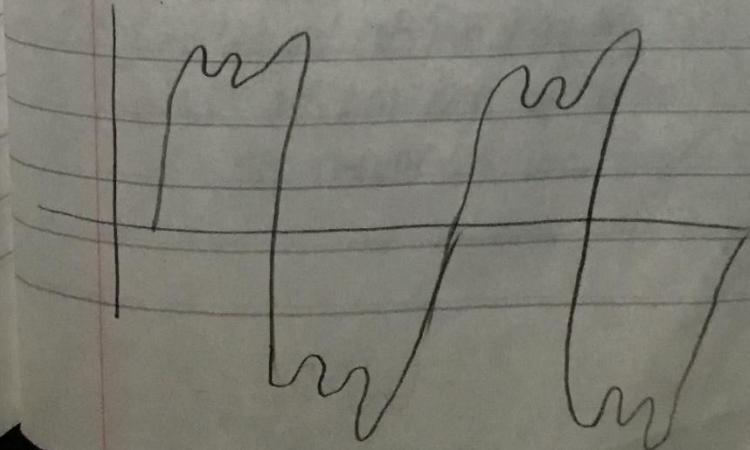
means that signal changes its form or shape.

- Distortion can occur in a composite signal made of different frequencies

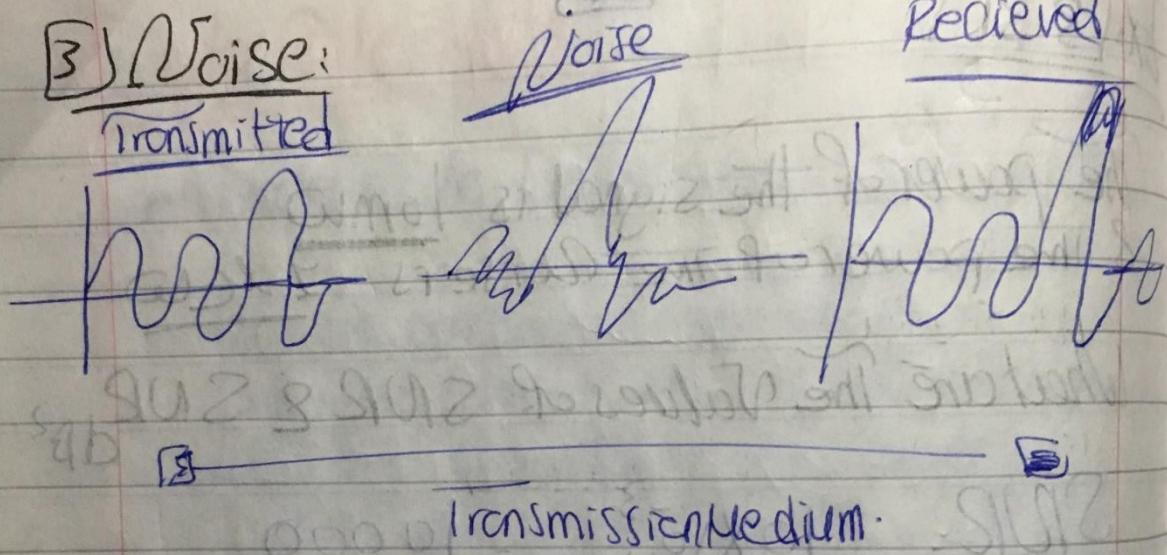
At Sender



At Receiver



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- SNR (Signal-To-Noise Ratio).

The Ratio Between the Signal power  
to the Noise power.

SNR =  $\frac{\text{Average Signal Power}}{\text{Average Noise Power}}$ .

\* Low SNR → More Noise.

\* High SNR → less Noise.

Ex. 3.31

The power of the signal is 10 mW  
& the power of the noise is 1 mW

What are the values of SNR & SNR<sub>dB</sub>?

$$SNR = \frac{10 \times 10^{-3}}{1 \times 10^{-6}} = 10000$$

$$SNR_{dB} = 10 \log_{10} (10000) = 40 dB$$

$$10 \log_{10} (10^4) = 4 \times 10 (\log_{10}) \\ = \underline{\underline{40 \text{ dB}}}$$

## \* Data Rate limits:

1.  $\sqrt{100}$

\* Data Rate Depends on 3 factors.

- 1) The bandwidth Available.
- 2) The level of the signals we use.
- 3) The Quality of the channel  
(The level of Noise).

\* Noiseless Channel (Nyquist Bit Rate)

→ The Nyquist Bit Rate Define The Maximum Bit Rate.

$$\text{Bit Rate} = 2 \times \text{Bandwidth} \times \log_2 (l)$$

→ Number of signal levels

(101)

Ex: (3-36)

We need to send 265 Kbps over a noiseless channel with bandwidth of 20 kHz  
How many signal levels do we need?

$$\text{Bit Rate} = 2 \times \text{Bandwidth} \times \log_2 L$$

$$265 \times 10^3 = 2 \times [20 \times 10^3] \times \log_2 L$$

$$\log_2 L = \frac{265}{20} = 6.625 \quad \begin{cases} \text{Rule} \\ \log_b a = c \\ a^c = b \end{cases}$$

$$2^{(6.625)} = L$$

$$L = 2^{6.625} = 98.7$$

$\approx$  [99 levels]

$$2^{\square} \approx 99 \quad 2^7 = 128$$

Each signal represents 7 bits.

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## \* Noisy Channel: Shannon Capacity

- We can't have a noiseless channel.

The channel is always Noisy.

## \* Shannon Capacity:

To determine the highest Data Rate for Noisy channel

$$\text{Capacity} = \text{Bandwidth} \times \log_2 (1 + \text{SNR})$$

Ex: (3-39)

The SNR Ratio is given in decibels.

SNR<sub>dB</sub> = 36 dB The channel Bandwidth

is 2 MHz. Calculate The channel capacity?

$$\log_a b = c$$

$$SNR_{dB} = 10 \log_{10} SNR$$

$$SNR = 10^{SNR_{dB}/10}$$

$$SNR = 10^{\frac{36}{10}} = 10^{3.6} = 3981.$$

$$\text{Capacity} = \text{Bandwidth} \times \log_2 (1+SNR)$$

$$= 2 \times 10^6 \times \log_2 (1 + 3981)$$

$$= \underline{\underline{84 \text{ Mbps}}}$$

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Ex- 3.4(d) for practical

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When The SNR is very High, we can assume that  $\text{SNR}+1$  is almost the same As SNR

In These Cases, The Theoretical Channel Capacity can be simplified as:

$$C = \text{Bandwidth} \times \frac{\text{SNR}_{\text{dB}}}{3}$$

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Ex: [3-41] We have a channel with 14 Hz Bandwidth  
the SNR for this channel is 63

What are the Appropriate Bit Rate & signal levels?

$$\text{Bit Rate (Nyquist)} = 2 \times B \times \log_2 (1 + \frac{S}{N})$$

$$\Rightarrow \text{Bit Rate} = 2 \times 14 \times \log_2 L$$

$\xrightarrow{\text{using Shannon}}$  upper limit rate.

$$[1] C = B \times \log_2 (1 + \text{SNR})$$

$$\text{C} = [2 \times 10^6] \log_2 (1 + 63) = 10^6 \log_2 64 = 6 \text{ Mbps}$$

[2] For better performance we choose something lower 4 Mbps.

$$[3] \text{Nyquist/Bit Rate} = 2 \times 2 \times 10^6 \times \log_2 L$$

$$4 \times 10^6 = 2 \times 10^6 \log_2 L$$

$$2 = \log_2 L$$

$$L = 2^2 = 4 \text{ levels}$$

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[Note]

The Shanon Capacity gives us the upper limit

The Nyquist formula tells us how many signal levels we need.

Ex:

\* Performance

- ① Bandwidth
- ② Throughput
- ③ Latency (Delay)

\* Bandwidth

Bandwidth (Hz)

↳ used in Composite signal  
the range of frequency

That a channel can pass

b (Analogue signal)

b (Digital signal)

Bandwidth (bps)

↳ the speed of  
bit transmission in  
a channel or link.

1

2

3

2) Throughput:

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A measure of How fast we can actually send Data Through a network.

Ex 3.44

- Network Bandwidth of 10 Mbps Can passally on Average of 12000 Frames per minute with each frame carrying an Average of 10,000 Bits.

What is the Throughput:

$$\text{Throughput: } \frac{12000 \times 10000}{60} = 2 \times 10^6 \text{ bps}$$

24 bps

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### ③ Latency (Delay)

Define How long it takes for an entire Message to Completely arrive at Destination From the time the First bit is sent out from the Source.

### Latency (Delay)

- ↳ Propagation Time
- ⊕ Transmission Time.
- ⊕ Queuing Time
- ⊕ Processing Delay

#### ① Propagation Time.

The time required for a bit to travel from the source to the Destination

$$\text{Propagation Time} = \frac{\text{Distance}}{\text{Propagation Speed}}$$

## ② Transmission Time

Time Between The first bit leaving the sender  
& The last bit arriving at the Receiver.

$$\text{Transmission Delay} = \frac{\text{Message Size}}{\text{Bandwidth}}$$

## ③ Queuing Time

The Time needed for each intermediate  
or end Device to hold message before  
it can be processed.

\* Propagation Time (Delay) =

$$\frac{\text{Distance}}{\text{propagation speed}}$$

\* Transmission Delay =  $\frac{\text{Message Size}}{\text{Bandwidth}}$