



<b>TITLE OF PROJECT</b>	IMAGE & AUDIO DIGITAL PROCESSING
<b>COURSE</b>	SIGNALS & SYSTEMS (ELC 2030)
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## Abstract

In this report, we present our work on the signals project supervised by Dr. Michael Melek which concentrated on some concepts in the Signals & Systems course, especially the Fourier Transform and discrete Fourier Transform represented in the Fast Fourier Transform. The concepts of convolution, signal transmission, and modulation were also strongly planted in the project's core.

We worked on this project in two directions, which were image Filtration & Restoration and communication system simulation. In the first direction, we aimed to do some specific filtration processes on a specific image and restore the image after a specific filter. In the other direction, we aimed to record our voice, apply a filter to it, and then transmit it to a higher frequency and get it back.

We can say that the skills gained from practicing Matlab through such a practical project, in addition to writing the report in latex, were of invaluable benefit to us in various ways.

# 1 Image Filtration and restoration

We did this part with the help of the following built-in functions:

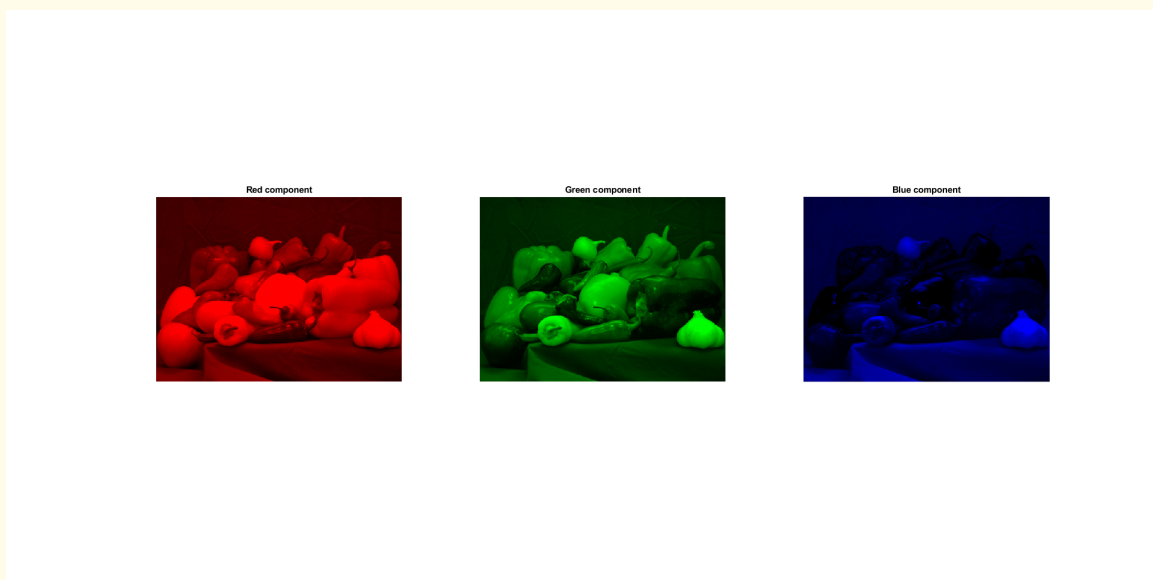
- `conv2` [1]
- `fft2`
- `ifft2`
- `im2double` [2]
- `imshow` [3]
- `subplot` [4]
- `zeros`
- `ones`
- `rgb2gray`

## 1.1 Getting the three color components of the image

### 1.1.1 Working idea

From the previously known information every image consists of three images of different colors (Red, Green, and Blue) concatenated at each other, We extracted each component alone and concatenated it with the other two black components to get full three images of different colors forming the original image.[5]

### 1.1.2 The processed images



**Figure 1:** The three components of the color

## 1.2 Edge Detection

In edge detection, we decided to work by convolving the image with the Laplacian kernel, as the Laplacian is a measure of the spacial derivative of an image which can detect the great changes in the pixel value of an image and get the edges.[6]

### 1.2.1 How to apply the kernel?

We should conserve the realization of some conditions:

- The kernel is a square Matrix.
- The sum of kernel elements equals zero.
- We can apply the kernel on the gray image or each component of the image and concatenate them.

### 1.2.2 The Kernel used

$$\begin{pmatrix} 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ -1 & -1 & -1 & -1 & 16 & -1 & -1 & -1 & -1 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \end{pmatrix}$$

### 1.2.3 The processed images

## 1.3 Sharpening

### 1.3.1 The working idea

The working idea of the kernel used to perform the sharpening is so simple that you add the edges you got from the edge-detected image and add to the original so that you can get the edges sharpened.



**Figure 2:** Edge Detection for colored images



**Figure 3:** Edge Detection for gray images

### 1.3.2 The Kernel used

$$\begin{pmatrix} 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ -1 & -1 & -1 & -1 & 17 & -1 & -1 & -1 & -1 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \end{pmatrix}$$

### 1.3.3 The processed images



**Figure 4:** Sharpening colored images



**Figure 5:** Sharpening gray images

## 1.4 Blurring

### 1.4.1 The working idea

Blurring basically means averaging, as when you want to blur a photo, you want to make it smoother, less detailed, and not sharpened. So, you just can make every pixel dependent on the value of the pixels around it.

We can make the dependency of the pixel on other pixels dependent also on the distance between the two pixels[7], but we will just be satisfied by the simple averaging kernel. The averaging kernel is characterized that we divide the whole kernel by the sum of its elements.

### 1.4.2 The Kernel used

$$\frac{1}{100} * \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \end{pmatrix}$$

### 1.4.3 The processed images



**Figure 6:** Blurring colored images



**Figure 7:** Blurring gray images

## 1.5 Motion Blurring

### 1.5.1 The working idea

By intuition, we can say that motion blurring has the idea of normal averaging, but we make every pixel depend on the pixels in the same direction of motion instead of all directions. The kernel can only be a vector of all ones divided by their number and directed in the direction we want the motion in.

### 1.5.2 The Kernel used

$\frac{1}{50} * \text{vector of length (50) containing only ones}$



### 1.5.3 The processed images



**Figure 8:** Motion blurring colored images



**Figure 9:** Motion blurring gray images

## 1.6 Restoring the image from motion blurring

### 1.6.1 Working idea

The idea of restoring the original image is based on the Fourier Transform concept to reflect the impact of convolution, we can't do this in the time domain easily so, we have to convert to the frequency domain as convolution turns into multiplication in frequency domain, so we can reflect the impact of convolution by using division.

### 1.6.2 the restoring process



**Figure 10:** Reconstructing colored images



**Figure 11:** Reconstructing gray images

## 2 Communication System Simulation

### 2.1 Recording the voice

In order for the voice to be of good quality, the sampling rate must be more than double the frequency of the sound that humans can hear (which ranges from 20 Hz to 20 kHz). So, we chose a sampling rate of 44100 Hz, which is a widely used number worldwide.

We can use a higher sampling rate to get more quality sound, such as 96 kHz or 192 kHz, which are widely used in higher-quality communication systems.

In low-quality voice, 8-bit is widely used but to make the voice of an acceptable quality range, we used 16-bit depth. For higher quality, we use 24-bit or 32-bit depth.[8]

### 2.2 Filtering the voice

We used the Butterworth filter because it has no ripples[9]. At first, we used  $F_{pass} = 8000Hz$  and  $F_{stop} = 8500Hz$ , but it interfered with the communication part as MATLAB has a limited range in the carrier, so we dropped the value a little to make sure the whole communication system works well, and also decreasing the frequency doesn't affect the voice so much as the frequency of the human most power exists in the range of 300 to 3400 Hz. So, we used  $F_{pass} = 6000Hz$  and  $F_{stop} = 6500Hz$  .[10]

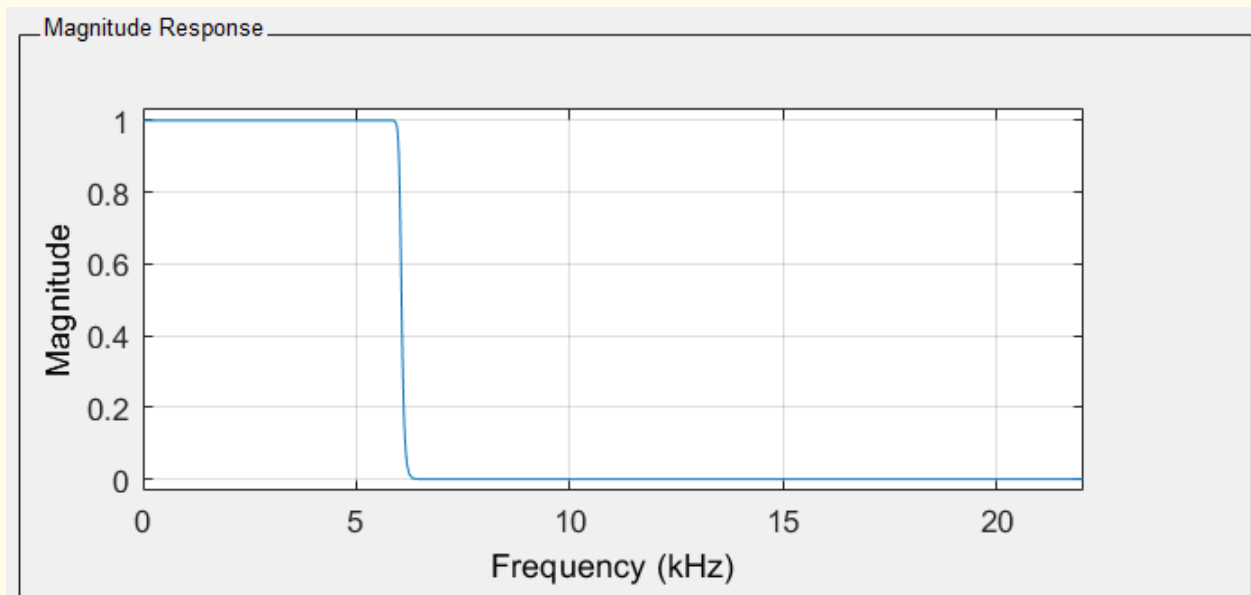
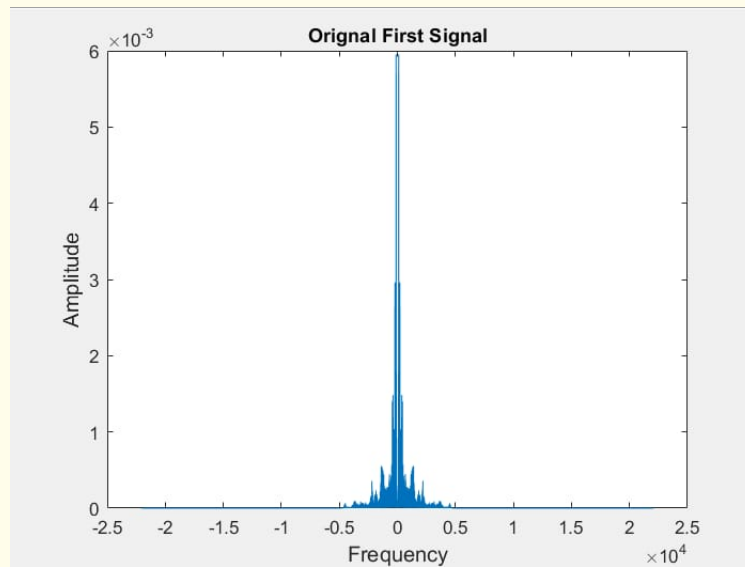
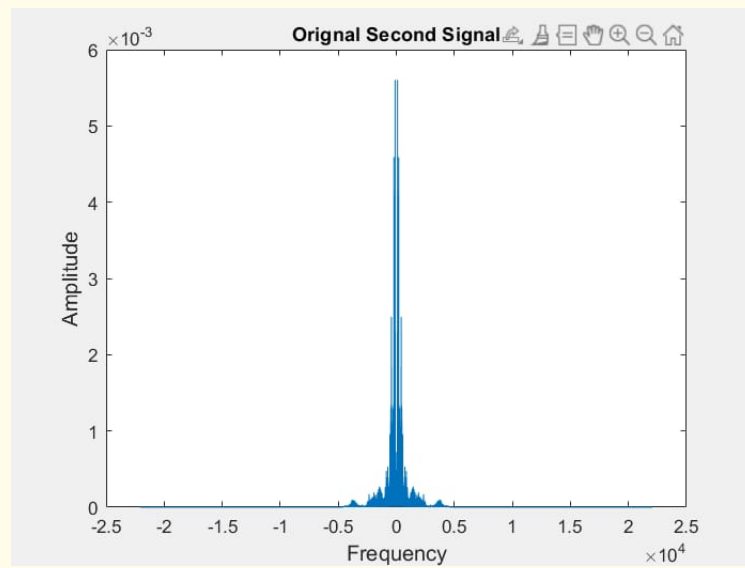


Figure 12: Magnitude vs Frequency

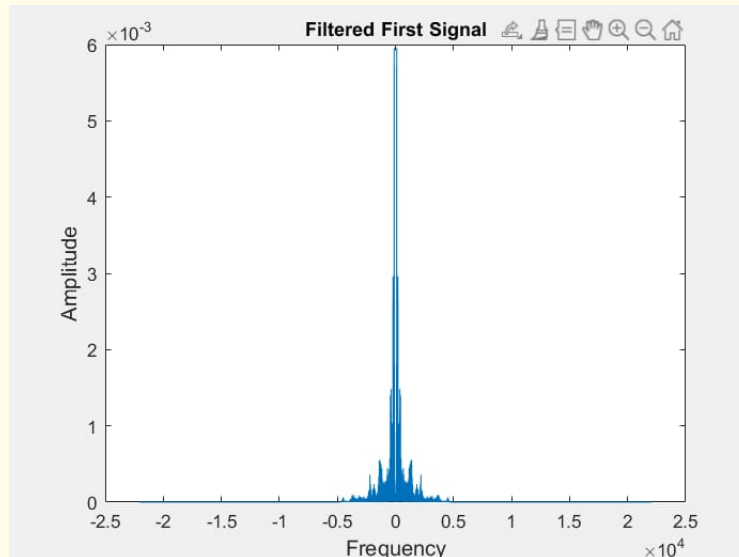
## 2.3 Plotting the spectrum of the signals



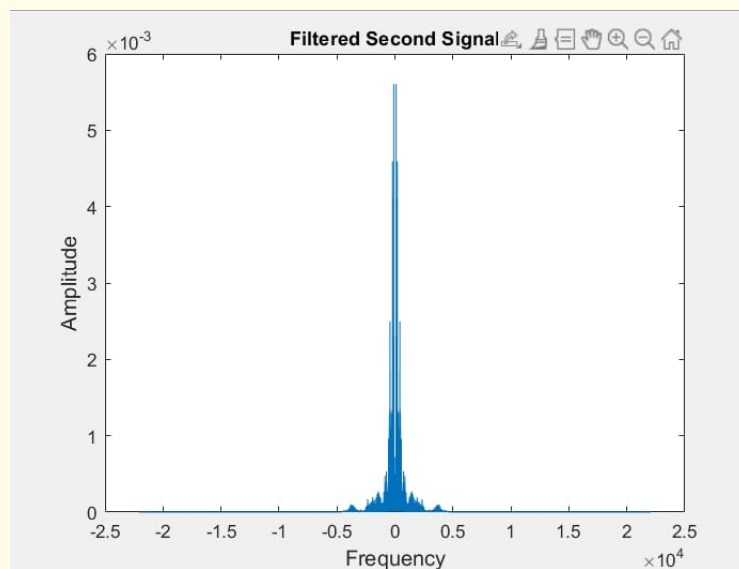
**Figure 13:** original first signal



**Figure 14:** original second signal



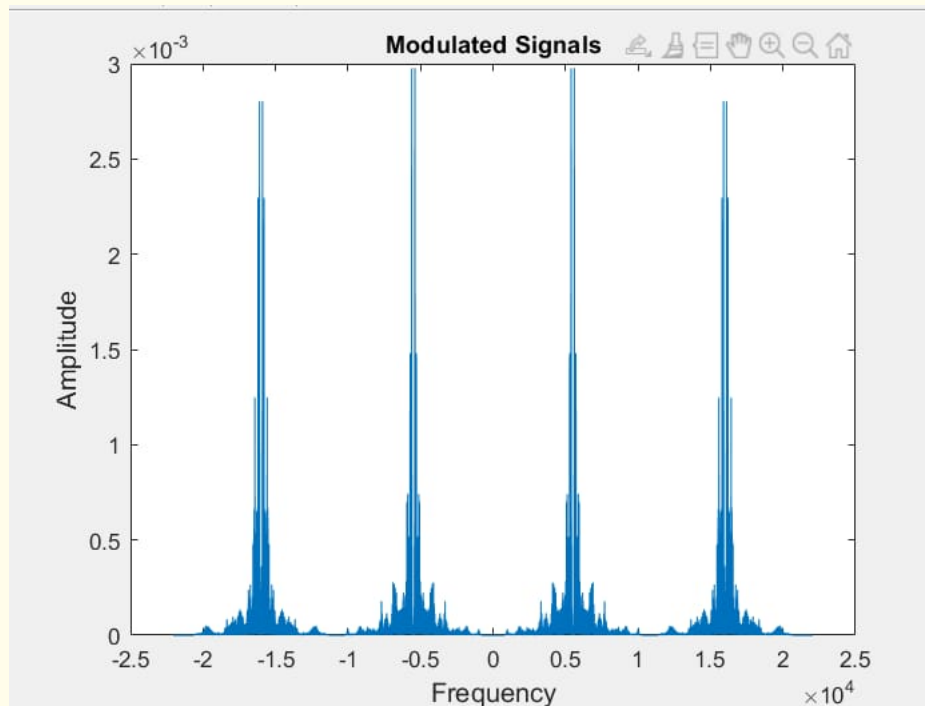
**Figure 15:** Filtered first signal



**Figure 16:** Filtered second signal

## 2.4 Modulation

In carrier, we used the frequency values  $F_{c1} = 5500Hz$  and  $F_{c2} = 16000Hz$  to make the two frequencies away from each other to not interfere and could filter them by non-ideal filter easily[11]. Also, MATLAB can't put the signal on the higher carrier so we don't have a lot of frequency space here[12]



**Figure 17:** Modulated signals

## 2.5 Demodulation

In the receiver stage, first we need to separate the two signals by applying a bandpass filter to separate the two signals (demultiplexing). the first bandpass frequencies values are  $F_{stop1} = 100\text{Hz}$ ,  $F_{pass1} = 1100\text{Hz}$ ,  $F_{pass2} = 10000\text{Hz}$ ,  $F_{stop2} = 15000\text{Hz}$  and the second one values were  $F_{stop1} = 10200\text{Hz}$ ,  $F_{pass1} = 11400\text{Hz}$ ,  $F_{pass2} = 20800\text{Hz}$ ,  $F_{stop2} = 22000\text{Hz}$ .

second, we multiply the signal with the carrier signal, then apply a low pass filter with gain of 2 to restore original audios (demodulation). the signal operates in different domains:

1. time domain:

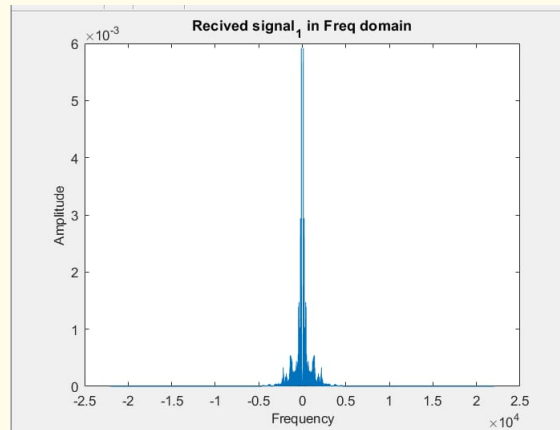
$$r(t) = y(t) * c(t)$$

Where,  $r(t)$ : received signal,  $y(t)$ : the signal came from bandpass filter,  $c(t)$ : the carrier

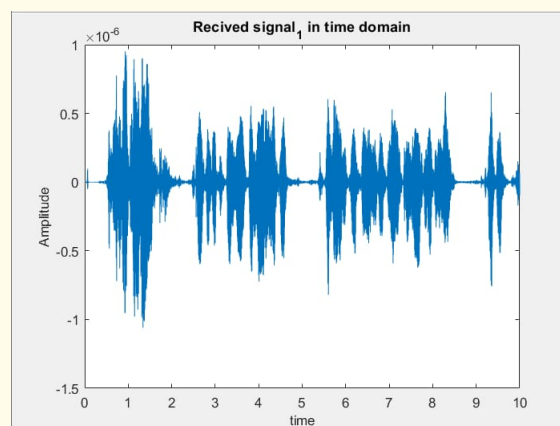
2. Frequency domain:

$$R(\omega) = \frac{Y(\omega - \omega_o) + Y(\omega + \omega_o)}{2}$$

- $R(\omega)$ : received signal
- $Y(\omega)$ : the signal came from bandpass filter



**Figure 18:** Received first signal in frequency domain

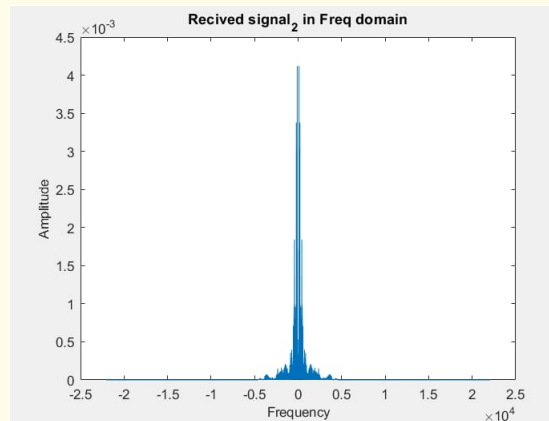


**Figure 19:** Received first signal in time domain

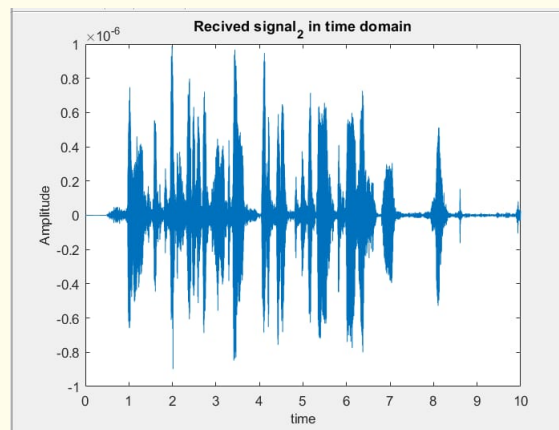
## A References

### A.1 Bibliography

- [1] 2-d convolution - matlab conv2. <https://www.mathworks.com/help/matlab/ref/conv2.html>, 2024. Accessed: 2024-01-02.
- [2] Convert image to double precision - matlab im2double. <https://www.mathworks.com/help/matlab/ref/im2double.html>, 2024. Accessed: 2024-01-02.
- [3] Display image - matlab imshow. [https://www.mathworks.com/help/images/ref/imshow.html?searchHighlight=imshow&s\\_tid=srchtitle\\_support\\_results\\_1\\_imshow](https://www.mathworks.com/help/images/ref/imshow.html?searchHighlight=imshow&s_tid=srchtitle_support_results_1_imshow), 2024. Accessed: 2024-01-02.
- [4] Create axes in tiled positions - matlab subplot. [https://www.mathworks.com/help/matlab/ref/subplot.html?searchHighlight=subplot&s\\_tid=srchtitle\\_support\\_results\\_1\\_subplot](https://www.mathworks.com/help/matlab/ref/subplot.html?searchHighlight=subplot&s_tid=srchtitle_support_results_1_subplot), 2024. Accessed: 2024-01-02.
- [5] r g b components of an image - matlab answers - matlab central. <https://www.mathworks.com/matlabcentral/answers/90908-r-g-b-components-of-an-image>, 2024. Accessed: 2024-01-02.



**Figure 20:** Received second signal in frequency domain



**Figure 21:** Received second signal in time domain

- [6] Spatial filters - laplacian/laplacian of gaussian. <https://homepages.inf.ed.ac.uk/rbf/HIPR2/log.htm>, 2024. Accessed: 2024-01-02.
- [7] Blurring an image — apple developer documentation. [https://developer.apple.com/documentation/accelerate/blurring\\_an\\_image](https://developer.apple.com/documentation/accelerate/blurring_an_image), 2024. Accessed: 2024-01-02.
- [8] (98) how to record audio in matlab (with complete code) - youtube. <https://www.youtube.com/watch?v=C05tMF2kvpM>, 2024. Accessed: 2024-01-02.
- [9] 1-d digital filter - matlab filter. <https://www.mathworks.com/help/releases/R2021a/matlab/ref/filter.html>, 2024. Accessed: 2024-01-02.
- [10] (98) design fir in matlab — fir iir filters in matlab - youtube. <https://www.youtube.com/watch?v=Jf9NvCU6siU>, 2024. Accessed: 2024-01-02.
- [11] Transpose vector or matrix - matlab transpose '. <https://www.mathworks.com/help/releases/R2021a/matlab/ref/transpose.html>, 2024. Accessed: 2024-01-02.
- [12] (98) amplitude modulation - matlab tutorial (amplitude modulation in matlab with code) 2016 - youtube. [https://www.youtube.com/watch?v=dEG\\_hv5E8VQ](https://www.youtube.com/watch?v=dEG_hv5E8VQ), 2024. Accessed: 2024-01-02.



## B Matlab code for image processing

```
1 peppers_img=imread('peppers.png');
2
3 %-----
4
5 %Extracting the three color components
6
7 red_component=peppers_img(:,:,1);%red component of the image
8 green_component=peppers_img(:,:,2);%green component of the image
9 blue_component=peppers_img(:,:,3);%red component of the imageSeS
10
11 %-----
12
13 %Creating a black image
14
15 Black= zeros(size(peppers_img,1),size(peppers_img,2));
16
17 %-----
18
19 %Creating colored images of the image
20
21 red_image =cat(3,red_component,Black,Black);
22 green_image =cat(3,Black,green_component,Black);
23 blue_image =cat(3,Black,Black,blue_component);
24
25 %-----
26
27 %Displaying color components
28
29 subplot(1,3,1)
30 imshow (red_image)
31 fontsize= 18;
32 title('Red component');
33 subplot(1,3,2)
34 imshow (green_image)
35 fontsize= 18;
36 title('Green component');
37
38 subplot(1,3,3)
39 imshow (blue_image)
40 fontsize= 18;
41 title('Blue component');
42
43 %-----
44
45 %getting a gray image out of the original one
46 grey_image=rgb2gray(peppers_img);
```

```

47
48 %-----
49
50 %Converting image components into double
51 Red_double=im2double(red_component);
52 Blue_double=im2double(blue_component);
53 Green_double=im2double(green_component);
54 Gray_double= im2double(grey_image);
55
56 %-----
57
58 %Edge Detection
59 Edge_Detection_kernel=[
60     0  0  0  0  -1  0  0  0  0
61     0  0  0  0, -1 ,0  0  0  0 ;
62     0  0  0  0  -1  0  0  0  0;
63     0  0  0  0  -1  0  0  0  0;
64    -1 -1 -1 -1  16 -1 -1 -1 -1;
65     0  0  0  0  -1  0  0  0  0 ;
66     0  0  0  0  -1  0  0  0  0 ;
67     0  0  0  0  -1  0  0  0  0;
68     0  0  0  0  -1  0  0  0  0 ];
69
70
71 %-----
72
73 %Edge detection for a gray image
74
75 Gray_edge_detection = conv2( Gray_double,Edge_Detection_kernel);
76 figure;
77 imshow(Gray_edge_detection);
78
79 %-----
80 %Edge detection for the original image
81 figure;
82 Red_edge_detectioned_image=conv2(Red_double,Edge_Detection_kernel);
83 Blue_edge_detectioned_image=conv2(Blue_double,Edge_Detection_kernel);
84 Green_edge_detectioned_image=conv2(Green_double,Edge_Detection_kernel);
85
86 Img_processed =cat(3,Red_edge_detectioned_image,Green_edge_detectioned_image,
87     Blue_edge_detectioned_image);
88 imshow(Img_processed);
89
90 %-----
91
92
93 %Sharpening image
94

```

```

95 Sharpening_Kernel = [
96     0  0  0  0  -1  0  0  0  0 ;
97     0  0  0  0, -1 ,0  0  0  0 ;
98     0  0  0  0  -1  0  0  0  0 ;
99     0  0  0  0  -1  0  0  0  0 ;
100    -1 -1 -1 -1  17 -1 -1 -1 -1 ;
101     0  0  0  0  -1  0  0  0  0 ;
102     0  0  0  0  -1  0  0  0  0 ;
103     0  0  0  0  -1  0  0  0  0 ;
104     0  0  0  0  -1  0  0  0  0 ];
105
106
107 %-----
108
109 %%Sharpening the gray image
110
111 Gray_sharpened_image = conv2( Gray_double,Sharpening_Kernel);
112 figure;
113 imshow(Gray_sharpened_image);
114
115 %-----
116
117 %%Sharping the original image
118
119 figure;
120 Red_sharpened_image=conv2(Red_double,Sharpening_Kernel);
121 Blue_sharpened_image=conv2(Blue_double,Sharpening_Kernel);
122 Green_sharpened_image=conv2(Green_double,Sharpening_Kernel);
123
124 Sharpened_image =cat(3,Red_sharpened_image,Green_sharpened_image,Blue_sharpened_image);
125 imshow(Sharpened_image);
126
127
128 %-----
129
130
131 % Bluring image
132
133 Gz=(1/100 )*ones(10,10);
134
135 %-----
136
137 %Bluring the gray image
138 Blured_gray_image = conv2( Gray_double,Gz);
139 figure;
140 imshow(Blured_gray_image);
141
142 %-----
143

```

```

144 %Bluring the original image
145
146 figure;
147
148 Blured_red_image=conv2(Red_double,Gz);
149 Blured_blue_image=conv2(Blue_double,Gz);
150 Blured_green_image=conv2(Green_double,Gz);
151
152 Blured_image =cat(3,Blured_red_image,Blured_green_image,Blured_blue_image);
153 imshow(Blured_image);
154
155
156 %-----
157
158 %Motion bluring
159
160 Motion_bluring_kernel=(1/50)*ones(1,50)
161
162 %-----
163
164 %Motion blur of gray image
165
166 Motion_blured_gray_image = conv2( Gray_double,Motion_bluring_kernel);
167 figure;
168 imshow(Motion_blured_gray_image);
169
170 %-----
171
172 %Motion blur of the original image
173
174
175 figure;
176
177 Motion_blured_red_image=conv2(Red_double,Motion_bluring_kernel);
178 Motion_blured_blue_image=conv2(Blue_double,Motion_bluring_kernel);
179 Motion_blured_green_image=conv2(Green_double,Motion_bluring_kernel);
180
181 Motion_blured_image =cat(3,Motion_blured_red_image,Motion_blured_green_image,
    Motion_blured_blue_image);
182 imshow(Motion_blured_image);
183
184 %-----
185
186 %Adjusting the size of the motion_bluring kernel to suit the divisioin in
187 %frequency domain
188
189 The_widened_motion_bluring_kernel=zeros(size(Motion_blured_image,1),size(Motion_blured_image,2));
190 The_widened_motion_bluring_kernel(1,1:50)=Motion_bluring_kernel;
191

```

```

192
193 %-----
194
195 %Reconstructing the image from the motion-blured one in frequency domain
196
197 %Converting into Fourier domain
198
199 Frequency_domain_motion_blured_kernel=fft2(The_widened_motion_bluring_kernel);
200 Frequency_domain_motion_blured_red_image=fft2(Motion_blured_red_image);
201 Frequency_domain_motion_blured_blue_image=fft2(Motion_blured_blue_image);
202 Frequency_domain_motion_blured_green_image=fft2(Motion_blured_green_image);
203 Frequency_domain_motion_blured_gray_image=fft2(Motion_blured_gray_image);
204
205 %-----
206
207
208 %Getting the original image in fourier domain
209
210
211 reconstructed_red_in_frequendy_domain=Frequency_domain_motion_blured_red_image./
    Frequency_domain_motion_blured_kernel;
212 reconstructed_blue_in_frequency_domain=Frequency_domain_motion_blured_blue_image./
    Frequency_domain_motion_blured_kernel;
213 reconstructed_green_in_frequency_domain=Frequency_domain_motion_blured_green_image./
    Frequency_domain_motion_blured_kernel;
214 reconstructed_gray_in_frequency_domain=Frequency_domain_motion_blured_gray_image./
    Frequency_domain_motion_blured_kernel;
215
216 %-----
217
218 %Getting inverse Fourier Transform of the image
219
220 Reconstructed_red=ifft2(reconstructed_red_in_frequendy_domain);
221 Reconstructed_green=ifft2(reconstructed_green_in_frequency_domain);
222 Reconstructed_blue=ifft2(reconstructed_blue_in_frequency_domain);
223 Reconstructed_gray=ifft2(reconstructed_gray_in_frequency_domain);
224
225 Reconstructed_gray=Reconstructed_gray(1:384,1:512,:);
226 %-----
227
228 %The reconstructed image
229
230 Reconstructed_image=cat(3,Reconstructed_red,Reconstructed_green,Reconstructed_blue);
231
232 Reconstructed_image=Reconstructed_image(1:384,1:512,:);
233
234 %-----
235
236 %displaying the original image besides the motion_blured and reconstructed

```

```
237 %one
238
239 figure;
240 subplot(1,3,1);
241 imshow (peppers_img);
242 fontsize= 18;
243 title('Original Image');
244
245 subplot(1,3,2);
246 imshow (Motion_blured_image);
247 fontsize= 18;
248 title('Motion-Blured Image');
249
250 subplot(1,3,3);
251 imshow (Reconstructed_image);
252 fontsize= 18;
253 title('Reconstructed Image');
254
255 figure;
256 subplot(1,3,1);
257 imshow (grey_image);
258 fontsize= 18;
259 title('Original Gray Image');
260
261 subplot(1,3,2);
262 imshow (Motion_blured_gray_image);
263 fontsize= 18;
264 title('Motion-Blured Gray Image');
265
266 subplot(1,3,3);
267 imshow (Reconstructed_gray);
268 fontsize= 18;
269 title('Reconstructed Gray Image');
270
271
272 %------%
273
274 %-----Thank you doctor Michael-----%
```

## C Matlab code for Simulating Communication Systems

```
1 %% check no error
2 clc;
3 clear ;
4 close all;
5 %to make sure that no previous data interrupt and no error happended and
6 %clear the command window
7 %% variable setting
8 ch=1;%Number of channels--2 options--1 (mono) or 2 (stereo)
9 Fs=44100;%Sampling frequency in hertz
10 datatype='int16';
11 Nseconds=10;
12 nbits=16;%8,16,or 24
13
14 % as the doctor say in the first lecture sampling time for telefon is 8khz
15 % and in music in CDs is 44.1 khz
16 % if you want a high quality resulation audio sampling frequency would be
17 % 96khz or 196khz
18
19 % the numbers of bit used in quantzion are 8 bits for low quality voices
20 % like in telefon and 16 bit for CDs used in music as shown in the first
21 % lecture of the term and also there are 24 and 32 bits which used in high
22 % quality resulatuiion and professional
23
24 %% recording audio and saving it
25 recorder=audiorecorder(Fs,nbits,ch);
26 disp('Start speaking..')
27 %Record audio to audiorecorder object,hold control until recording completes
28 recordblocking(recorder,Nseconds);
29 disp('End of Recording.');
```

30 %Store recorded audio signal in numeric array

```
31 x=getaudiodata(recorder,datatype); % datatype could be int16 or uint8 or int8 or
32 %Write audio file
33 audiowrite('input1.wav',x,Fs);
34
35 %% Ex
36 % first voice parameteres fs 44100 hz and 16 bit for quantization with no
37 % noise
38
39 % second voice as the previous but external noise is 25000 hz sound
40
41
42 % after trying some prameters i choose this to make the sound clear and not
43 % with high space
```

## D Names and codes in Arabic

ID	Section	الاسم
9220720	3	محمد عصام عبد العظيم ابراهيم
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