

# Optimizing Shared Mobility: A survey of models and algorithms for people and freight transportation

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## Abstract

Research on shared mobility systems has grown in popularity in recent years. Emerging challenges, such as finite oil supplies, rising gas prices and traffic congestion, going in hand with environmental concerns have attracted the attention of the operational research community towards more sharable systems of transportation. Shared mobility systems can be seen in two main streams: mobility systems where people can share rides and mobility systems where the transportation of parcels can be combined with people transportation. This survey aims, on the one hand, at summarizing the recent research in this area including different optimization approaches and, on the other hand, providing guidelines and promising directions for further research. Furthermore, a distinction between static and dynamic problems and their solution methods is made. The survey also gives an overview of applications to real cases that correspond to the research area considered.

**Keywords:** Optimization, people and freight transportation, static and dynamic ride-sharing, exact and heuristic methods.

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## 1. Introduction

## 2. People Sharing Rides

### 2.1. Ride-Sharing with Non-Autonomous Vehicles

#### 2.1.1. Static Ride-Sharing

- [17]: Design and Management of Vehicle Sharing Systems: A Survey of Algorithmic Approaches (2015).
- [36]: Enhancing Urban Mobility: Integrating Ride-sharing and Public (2016).
- [15]: Ridesharing: The state-of-the-art and future directions (2013).
- [35]: The benefits of meeting points in ride-sharing systems (2015).
- [19]: The shared-taxi problem: Formulation and solution methods (2014).

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### 2.1.2. *Dynamic Ride-Sharing*

- [1]: Optimization for Dynamic Ride-Sharing: A Review.
- [16]: Dynamic ride sharing service: are users ready to adopt it? (2015).
- [31]: Taxi and Ride Sharing: A Dynamic Dial-a-Ride Problem with Money as an Incentive (2015).
- [42]: Effective and Efficient: Large-scale Dynamic City Express (2015).
- [20]: Large Scale Real-time Ridesharing with Service Guarantee on Road Networks (2013).
- [37]: Making dynamic ride-sharing work: The impact of driver and rider flexibility (2016).
- [26]: Real-Time City-Scale Taxi Ridesharing (2015).
- [21]: Towards Scalable Processing for a Large-Scale Ride Sharing Service (2012).
- [41]: Where to Find My Next Passenger? (2011).
- [39]: A fast heuristic for solving a large-scale static dial-a-ride problem under complex constraints (2006).
- [40]: The study of a dynamic dial-a-ride problem under time-dependent and stochastic environments (2008).

### 2.1.3. *Applications*

- [28]: An Agent-based model to assess the impacts of introducing a shared-taxi system in Lisbon (Portugal) (2015).
- [5]: An optimization framework for the development of efficient one-way car-sharing systems (2013).
- [22]: Assessing the viability of enabling a round-trip carsharing system to accept one-way trips: Application to Logan Airport in Boston (2015).
- [2]: Dynamic ride-sharing: A simulation study in metro Atlanta (2011).
- [27]: Large-scale microscopic simulation of taxi services. Berlin and Barcelona case studies (2016).

## 2.2. *Ride-Sharing with Autonomous Vehicles*

### 2.2.1. *Static Ride-Sharing*

- [23]: Preferences for shared autonomous vehicles (2016).
- [7]: A methodology for planning a new urban car sharing system with fully automated personal vehicles (2014).
- [13]: Preparing a nation for autonomous vehicles: opportunities, barriers and policy recommendations (2015).

### 2.2.2. *Dynamic Ride-Sharing*

- [3]: On-demand high-capacity ride-sharing via dynamic trip-vehicle assignment (2017).
- [10]: Solving the User Optimum Privately Owned Automated Vehicles Assignment Problem (UO-POAVAP): A model to explore the impacts of self-driving vehicles on urban mobility (2016).

### 2.2.3. Applications

- [4]: Simulation of city-wide replacement of private cars with autonomous taxis in Berlin (2016).
- [24]: Autonomous cars: The tension between occupant experience and intersection capacity (2015).
- [18]: Assessing the Long-Term Effects of Autonomous Vehicles: a speculative approach (2016).
- [42]: Exploring the impact of shared autonomous vehicles on urban parking demand: An agent-based simulation approach (2015).
- [14]: Dynamic ride-sharing and fleet sizing for a system of shared autonomous vehicles in Austin, Texas (2016).
- [8]: Operations of a shared, autonomous, electric vehicle fleet: Implications of vehicle and charging infrastructure decisions (2016).

## 3. People and Freight Transportation

### 3.1. Freight Transportation

- [33]: City Logistics: Challenges and Opportunities (2016).
- [9]: Hands-on testing of last mile concepts (2016).
- [34]: Multimodal freight transportation planning: A literature review (2014).
- [38]: New opportunities and challenges for city logistics (2016).
- [12]: Review of intermodal freight transportation in humanitarian logistics (2017).
- [29]: A review of dynamic vehicle routing problems (2013).
- [30]: A Survey on Dynamic and Stochastic Vehicle Routing Problems (2014).
- [6]: Vehicle routing problems for city logistics (2015).

### 3.2. People and Parcels Sharing Rides

#### 3.2.1. Static Case

- [25]: The Share-a-Ride Problem: People and parcels sharing taxis.
- [11]: Physical internet enabled Hyperconnected City Logistics (2016).
- [32]: Vehicle Routing with Roaming Delivery Locations (2015).

#### 3.2.2. Dynamic Case

- [25]: The Share-a-Ride Problem: People and parcels sharing taxis.

### 3.2.3. Applications

## 4. Conclusion

### Bibliography

- [1] Niels Agatz, Alan Erera, Martin Savelsbergh, and Xing Wang. Optimization for dynamic ride-sharing: A review. *European Journal of Operational Research*, 223(2):295–303, 2012.
- [2] Niels A H Agatz, Alan L. Erera, Martin W P Savelsbergh, and Xing Wang. Dynamic ride-sharing: A simulation study in metro Atlanta. *Transportation Research Part B: Methodological*, 45 (9):1450–1464, 2011.
- [3] Javier Alonso-Mora, Samitha Samaranayake, Alex Wallar, Emilio Frazzoli, and Daniela Rus. On-demand high-capacity ride-sharing via dynamic trip-vehicle assignment. *Proceedings of the National Academy of Sciences*, page 201611675, 2017.
- [4] Joschka Bischoff and Michal Maciejewski. Simulation of City-wide Replacement of Private Cars with Autonomous Taxis in Berlin. *Procedia Computer Science*, 83(June):237–244, 2016.
- [5] Burak Boyaci, Konstantinos G. Zografos, and Nikolas Geroliminis. An optimization framework for the development of efficient one-way car sharing systems. *European Journal of Operational Research*, 240(3):718–733, 2013.
- [6] Diego Cattaruzza, Nabil Absi, Dominique Feillet, and Jesús González-Feliu. Vehicle routing problems for city logistics. *EURO Journal on Transportation and Logistics*, pages 1–29, 2015.
- [7] Elvezia M. Cepolina and Alessandro Farina. A methodology for planning a new urban car sharing system with fully automated personal vehicles. *European Transport Research Review*, 6(2):191–204, 2014.
- [8] T. Donna Chen, Kara M. Kockelman, and Josiah P. Hanna. Operations of a shared, autonomous, electric vehicle fleet: Implications of vehicle & charging infrastructure decisions. *Transportation Research Part A: Policy and Practice*, 94:243–254, 2016.
- [9] Uwe Clausen, Christiane Geiger, and Moritz Pötting. Hands-on testing of last mile concepts. *Transportation Research Procedia*, 14:1533–1542, 2016.
- [10] Gonçalo Homem de Almeida Correia and Bart van Arem. Solving the User Optimum Privately Owned Automated Vehicles Assignment Problem (UO-POAVAP): A model to explore the impacts of self-driving vehicles on urban mobility. *Transportation Research Part B: Methodological*, 87:64–88, 2016.
- [11] Teodor Gabriel Crainic and Benoit Montreuil. Physical Internet Enabled Hyperconnected City Logistics. *Transportation Research Procedia*, 12(June 2015):383–398, 2016.
- [12] M A Ertem, M İşbilir, and A Şahin Arslan. Review of intermodal freight transportation in humanitarian logistics. *European Transport Research Review*, 9(1), 2017.
- [13] Daniel J. Fagnant and Kara Kockelman. Preparing a nation for autonomous vehicles: Opportunities, barriers and policy recommendations. *Transportation Research Part A: Policy and Practice*, 77:167–181, 2015.
- [14] Daniel J. Fagnant and Kara M. Kockelman. Dynamic ride-sharing and fleet sizing for a system of shared autonomous vehicles in Austin, Texas. *Transportation*, pages 1–16, 2016.
- [15] Masabumi Furuhashi, Maged Dessouky, Fernando Ordóñez, Marc Etienne Brunet, Xiaoqing Wang, and Sven Koenig. Ridesharing: The state-of-the-art and future directions. *Transportation Research Part B: Methodological*, 57:28–46, 2013.
- [16] Eleonora Gargiulo, Roberta Giannantonio, Elena Guercio, Claudio Borean, and Giovanni Zenezini. Dynamic Ride Sharing Service: Are Users Ready to Adopt it? *Procedia Manufacturing*, 3(Ahfe):777–784, 2015.
- [17] Damianos Gavalas, Charalampos Konstantopoulos, and Grammati Pantziou. Design and Management of Vehicle Sharing Systems: A Survey of Algorithmic Approaches. page 38, 2015.
- [18] Wolfgang Gruel and Joseph M. Stanford. Assessing the Long-term Effects of Autonomous Vehicles: A Speculative Approach. *Transportation Research Procedia*, 13:18–29, 2016.
- [19] Hadi Hosni, Joe Naoum-Sawaya, and Hassan Artail. The shared-taxi problem: Formulation and solution methods. *Transportation Research Part B: Methodological*, 70:303–318, 2014.
- [20] Yan Huang, Ruoming Jin, Favyen Bastani, and Xs Wang. Large Scale Real-time Ridesharing with Service Guarantee on Road Networks. *arXiv preprint arXiv:1302.6666*, 7(14):2017–2028, 2013.
- [21] Beihong Jin and Jiafeng Hu. Towards scalable processing for a large-scale ride sharing service. *Proceedings - IEEE 9th International Conference on Ubiquitous Intelligence and Computing and IEEE 9th International Conference on Autonomic and Trusted Computing, UIC-ATC 2012*, pages 940–944, 2012.
- [22] Diana Jorge, Cynthia Barnhart, and Gonçalo Homem de Almeida Correia. Assessing the viability of enabling a round-trip carsharing system to accept one-way trips: Application to Logan Airport in Boston. *Transportation Research Part C: Emerging Technologies*, 56:359–372, 2015.
- [23] Rico Krueger, Taha H. Rashidi, and John M. Rose. Preferences for shared autonomous vehicles. *Transportation Research Part C: Emerging Technologies*, 69:343–355, 2016.

- [24] Scott Le Vine, Alireza Zolfaghari, and John Polak. Autonomous cars: The tension between occupant experience and intersection capacity. *Transportation Research Part C: Emerging Technologies*, 52:1–14, 2015.
- [25] Baoxiang Li, Dmitry Krushinsky, Hajo A. Reijers, and Tom Van Woensel. The Share-A-Ride Problem: People and parcels sharing taxis. *European Journal of Operational Research*, 238(1):31–40, 2014.
- [26] S Ma, Y Zheng, and O Wolfson. Real-time city-scale taxi ridesharing. 27(7):1782–1795, 2015.
- [27] Michal Maciejewski, Josep Maria Salanova, Joschka Bischoff, and Miquel Estrada. Large-scale microscopic simulation of taxi services. Berlin and Barcelona case studies. *Journal of Ambient Intelligence and Humanized Computing*, 7(3):385–393, 2016.
- [28] Luis M Martinez. An Agent-based model to assess the impacts of introducing a shared-taxi system in Lisbon ( Portugal ). *Journal of Advanced Transportation*, 49(3):475–495, 2015.
- [29] Victor Pillac, Michel Gendreau, Christelle Gu??ret, and Andr??s L. Medaglia. A review of dynamic vehicle routing problems. *European Journal of Operational Research*, 225(1):1–11, 2013.
- [30] Ulrike Ritzinger, Jakob Puchinger, and Richard F Hartl. A Survey on Dynamic and Stochastic Vehicle Routing Problems. 00(00):1–19, 2014.
- [31] Douglas O. Santos and Eduardo C. Xavier. Taxi and ride sharing: A dynamic dial-a-ride problem with money as an incentive. *Expert Systems with Applications*, 42(19):6728–6737, 2015.
- [32] Martin Savelsbergh and Alejandro Toriello. Vehicle Routing with Roaming Delivery Locations. pages 1–24, 2015.
- [33] Martin Savelsbergh and Tom Van Woensel. City Logistics : Challenges and Opportunities. *Optimization Online*, pages 1–19, 2016.
- [34] M. Steadieseifi, N. P. Dellaert, W. Nuijten, T. Van Woensel, and R. Raoufi. Multimodal freight transportation planning: A literature review. *European Journal of Operational Research*, 233(1):1–15, 2014.
- [35] Mitja Stiglic, Niels Agatz, Martin Savelsbergh, and Mirko Gradisar. The benefits of meeting points in ride-sharing systems. *Transportation Research Part B: Methodological*, 82:36–53, 2015.
- [36] Mitja Stiglic, Niels Agatz, Martin Savelsbergh, and Mirko Gradisar. Enhancing Urban Mobility : Integrating Ride-sharing and Public Transit. pages 1–20, 2016.
- [37] Mitja Stiglic, Niels Agatz, Martin Savelsbergh, and Mirko Gradisar. Making dynamic ride-sharing work: The impact of driver and rider flexibility. *Transportation Research Part E: Logistics and Transportation Review*, 91:190–207, 2016.
- [38] Eiichi Taniguchi, Russell G. Thompson, and Tadashi Yamada. New Opportunities and Challenges for City Logistics. *Transportation Research Procedia*, 12(June 2015):5–13, 2016.
- [39] Zhihai Xiang, Chengbin Chu, and Haoxun Chen. A fast heuristic for solving a large-scale static dial-a-ride problem under complex constraints. *European Journal of Operational Research*, 174(2):1117–1139, 2006.
- [40] Zhihai Xiang, Chengbin Chu, and Haoxun Chen. The study of a dynamic dial-a-ride problem under time-dependent and stochastic environments. *European Journal of Operational Research*, 185(2):534–551, 2008.
- [41] Jing Yuan, Yu Zheng, Liuhan Zhang, XIng Xie, and Guangzhong Sun. Where to find my next passenger? *Proceedings of the 13th international conference on Ubiquitous computing - UbiComp '11*, pages 109–118, 2011.
- [42] Siyuan Zhang, Lu Qin, Yu Zheng, and Hong Cheng. Effective and efficient: Large-scale Dynamic City Express. *Proceedings of the 23rd SIGSPATIAL International Conference on Advances in Geographic Information Systems - GIS '15*, pages 1–4, 2015.