



TRAINING

# Introduction to Anomaly Detection in Python & R



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# Course Outline

- Introduction
- Data Preparation
- Probability & Statistical Techniques
- Machine Learning Techniques
- Conclusion

# Course Outline

- Introduction
  - Who am I?
  - What are Anomalies?
  - Anomaly Detection Analytical Framework
- Data Preparation
- Probability & Statistical Techniques
- Machine Learning Techniques
- Conclusion

# Course Outline

- Introduction
- Data Preparation
  - Feature Engineering
  - Recency and Frequency
  - Categorical Feature Engineering
- Probability & Statistical Techniques
- Machine Learning Techniques
- Conclusion

# Course Outline

- Introduction
- Data Preparation
- Probability & Statistical Techniques
  - Benford's Law
  - Z-scores and Robust Z-scores
  - IQR Rule and Its Adjustment
  - Mahalanobis Distances and Robust Mahalanobis
- Machine Learning Techniques
- Conclusion

# Course Outline

- Introduction
- Data Preparation
- Probability & Statistical Techniques
- Machine Learning Techniques
  - k-Nearest Neighbors (k-NN)
  - Local Outlier Factor (LOF)
  - Isolation Forests
  - Classifier-Adjusted Density Estimation (CADE)
  - One-Class Support Vector Machine (SVM)
- Conclusion

# Coding in Action

Example

# Introduction



The background is split diagonally. The left side is a solid green gradient. The right side is dark grey with a white circuit board pattern. The circuit includes various lines, nodes, and binary code snippets. The word 'Introduction' is centered in white text.

101010110110

1010101

101101110

101010101010  
10101011101101  
11011101110111  
0111010100010001  
000100

101010101010  
110101000100

1101



# Introduction

- Introduction
  - Who am I?
  - What are Anomalies?
  - Anomaly Detection Analytical Framework

# Introduction

Who Am I?

- Introduction
  - Who am I?
  - What are Anomalies?
  - Anomaly Detection Analytical Framework

# Who Am I?

- 4-time North Carolina State University graduate:
  - BS in Statistics
  - BS in Economics
  - MS in Statistics
  - PhD in Statistics with minor in Economics

# Who Am I?

- 4-time North Carolina State University graduate
- Former Senior Data Scientist and Director at Elder Research Inc.
  - Passionate about helping people solve challenges using their data.
  - Mentored a team of data scientists and software engineers to work closely with clients and partners to solve problems in predictive modeling, advanced analytics, forecasting, and risk management.

# Who Am I?

- 4-time North Carolina State University graduate
- Former Senior Data Scientist and Director at Elder Research Inc.
- Associate Professor of Analytics at Institute for Advanced Analytics at NC State University
  - Nation's first master of science in analytics degree program
  - Helped design the innovative program to prepare a modern work force to wisely communicate and handle a data-driven future.
  - Developed and taught courses in statistics, mathematics, finance, risk management, and operations research.

# Who Am I?

- 4-time North Carolina State University graduate
- Former Senior Data Scientist and Director at Elder Research Inc.
- Associate Professor of Analytics at Institute for Advanced Analytics at NC State University
- Find me online:
  - <https://www.linkedin.com/in/ariclabarr/>
  - <https://www.youtube.com/c/AricLaBarr/>
  - <https://www.ariclabarr.com/>

# Introduction

What are Anomalies?

- Introduction
  - Who am I?
  - What are Anomalies?
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# What is an Anomaly?

anomaly

***noun***

/ə'näməlē/

something that **deviates** from what is **standard, normal, or expected**



# Why Detect Anomalies?

- Anomalies in data can lead to incorrect or out of date decisions to be made.
- Need to find these **outliers** before they become too much of a problem.
- Anomaly detection techniques used in variety of areas:
  - Cleaning data
  - Monitoring health of computer systems
  - Cybersecurity threats
  - Fraudulent claims or transactions

# Why Detect Anomalies?

- Anomalies in data can lead to incorrect or out of date decisions to be made.
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  - Cybersecurity threats
  - Fraudulent claims or transactions

# What is Fraud?

fraud

***noun***

/frôd/

**Wrongful** or criminal **deception** intended to result in financial or personal **gain**

# Fraud Problem

- In 2022, the ACFE (Association of Certified Fraud Examiners) Report to the Nations estimated that organizations lose approximately 5% of their revenues to fraud.
- Based on 2022 estimated world GDP (IMF estimates) this would mean approximately \$5.19 trillion is lost each year due to fraud.

# Fraud Characteristics

1. Uncommon
2. Concealed and trying to be avoided
3. Ever changing and adapting
4. Thought out and organized
5. Doesn't all look the same

# Fraud Characteristics

1. Uncommon
  2. Concealed and trying to be avoided
  3. Ever changing and adapting
  4. Thought out and organized
  5. Doesn't all look the same
- Because of these characteristics, fraud is a tough anomaly problem to solve.
  - Data science can help aid in this problem!

# Introduction

Anomaly Detection Analytical  
Framework

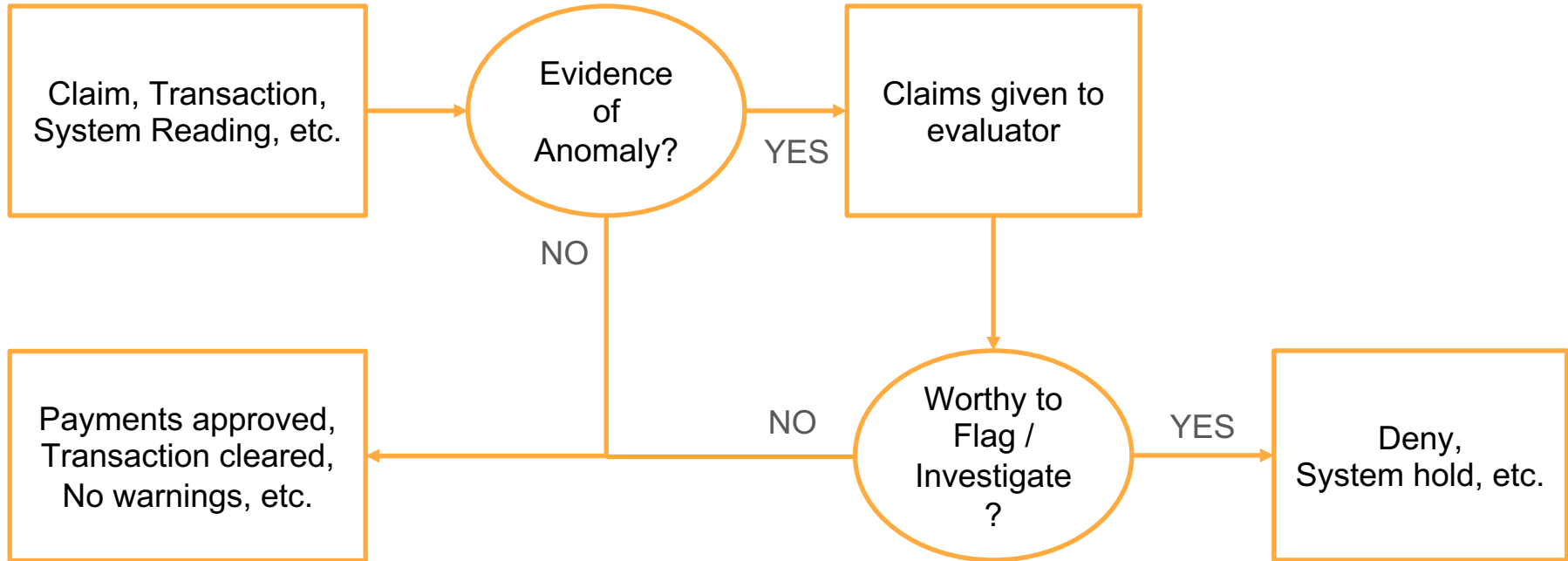
- Introduction
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# Anomaly Detection Systems

- Regardless of the industry, two things are important for any anomaly detection solution or system:
  1. **DETECTION** – able to identify current anomalies in the system
  2. **PREVENTION** – able to flag potentially new anomalies in the system



# Anomaly Detection Systems



# Anomaly Detection Maturity – Card Transaction

- New / young anomaly detection solutions are based on **business rules**.
- Example:
  - IF:
    - Amount of transaction above threshold
  - THEN:
    - Flag as suspicious AND
    - Alert evaluator

# Anomaly Detection Maturity – Cybersecurity

- New / young anomaly detection solutions are based on **business rules**.
- Example:
  - IF:
    - System pinged at unusual time
  - THEN:
    - Flag as suspicious AND
    - Alert evaluator

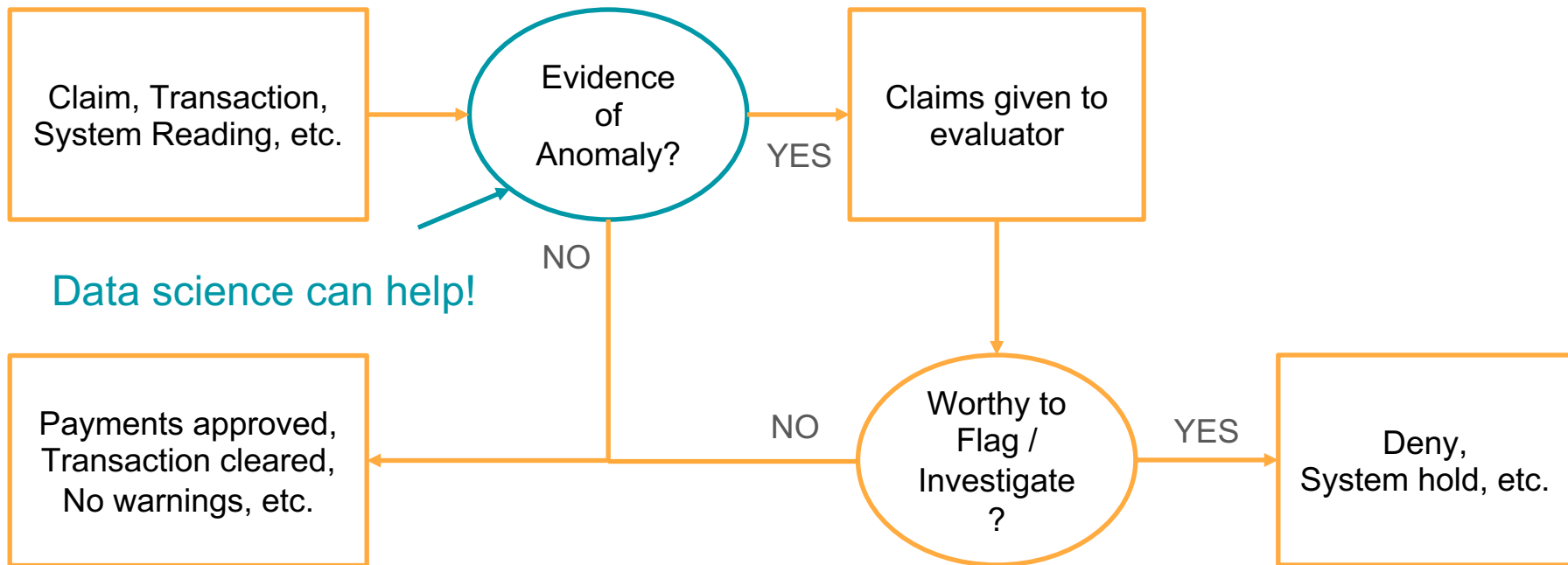
# Anomaly Detection Maturity – Insurance Fraud

- New / young anomaly detection solutions are based on **business rules**.
- Example:
  - IF:
    - Severe injury but no doctor report
  - THEN:
    - Flag as suspicious AND
    - Alert evaluator

# Business Rule Approach

- Advantages:
  - Simple
  - Easy to implement
- Disadvantages:
  - Expensive
  - Difficult to maintain and manage
  - Completely historical
  - Threats discover rules

# Anomaly Detection Systems



# Analytical Anomaly Detection Framework

- Advantages

1. **Precision**

- Increased detection power
- More information used in decisions
- More anomalies evaluated

# Analytical Anomaly Detection Framework

- Advantages
  1. **Precision**
  2. **Efficiency in Operations**
    - Automated processing of claims
    - Ranked cases for evaluators



# Analytical Anomaly Detection Framework

- Advantages
  1. **Precision**
  2. **Efficiency in Operations**
  3. **Efficiency in Costs**
    - Cheaper to long-run maintain
    - Quicker evaluation
    - Higher return on evaluations

# Introduction

Conclusion

- Introduction
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# Data Preparation

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# Data Preparation

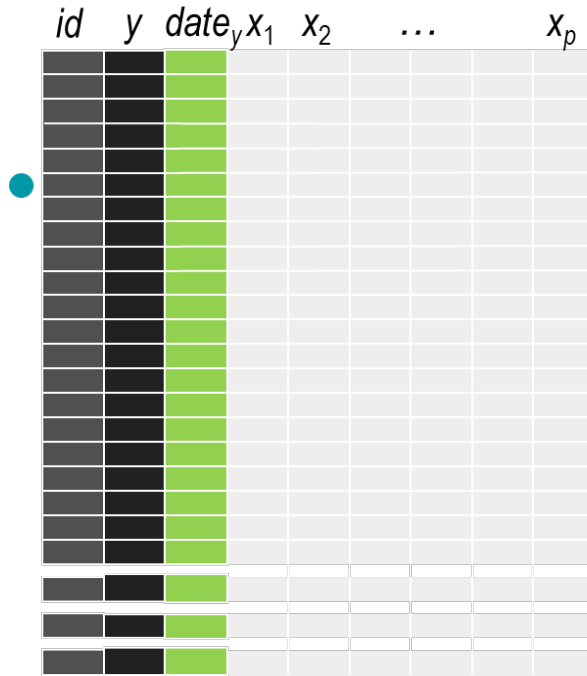
- Data Preparation
  - Feature Engineering
  - Recency and Frequency
  - Categorical Feature Engineering

# Data Preparation

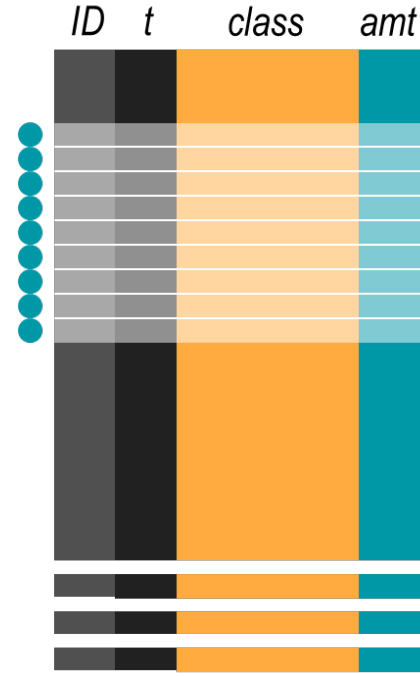
Feature Engineering

- Data Preparation
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# Transaction Data



Model Development Data



Transaction Data

# Transaction Data Examples

- There are many fields where transactional data plays an important role:
  - Credit card purchasing data
  - Medical / insurance claims data
  - Supply chain and logistics data
  - Sensor / systems monitoring data
  - Etc.

# Transactions Data

- Advantages

- Highly detailed
- Captures individual behavior
- Strong prediction possible

- Challenges

- Highly detailed
- Difficult to obtain
- Difficult to process

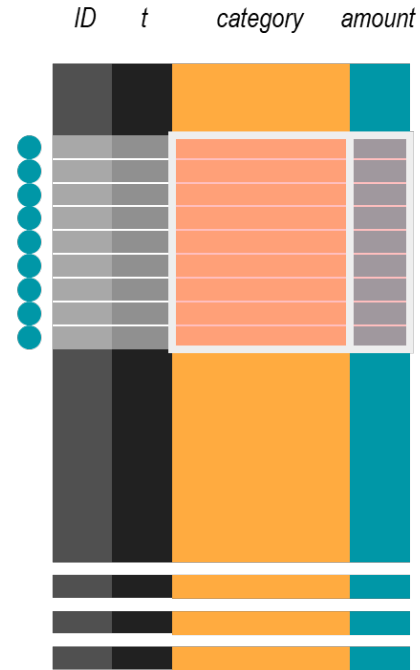
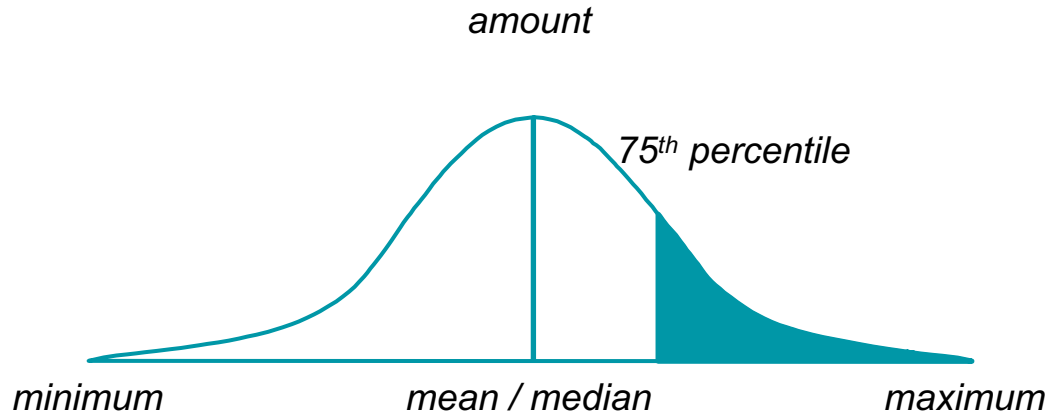


# Input Possibilities: Tabulations

|   |                           |                          |
|---|---------------------------|--------------------------|
|   |                           |                          |
|   |                           |                          |
| ● | <i>Number in category</i> | <code>sum(amount)</code> |
|   |                           |                          |
|   |                           |                          |
|   |                           |                          |
|   |                           |                          |

## Transaction Data

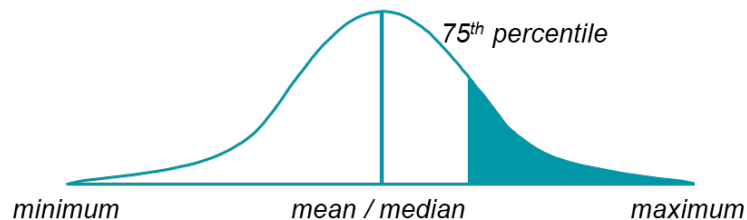
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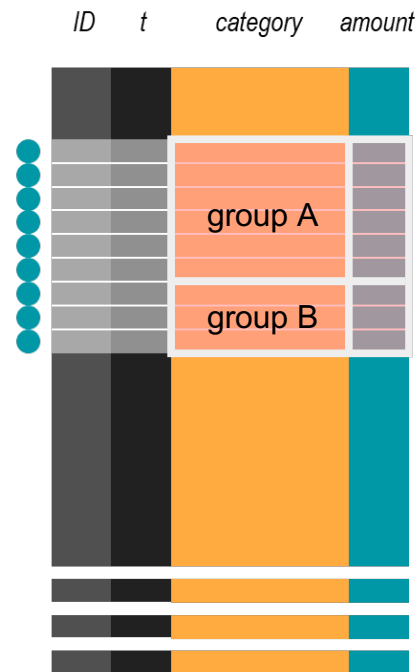
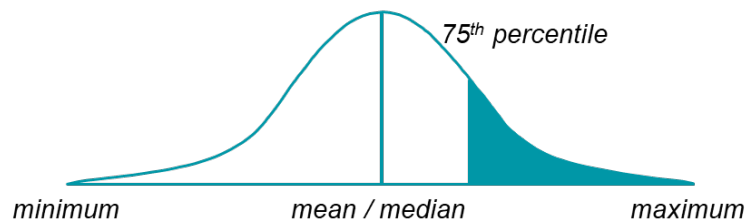
Transaction Data

# Input Possibilities: Tabulations

amount – group A

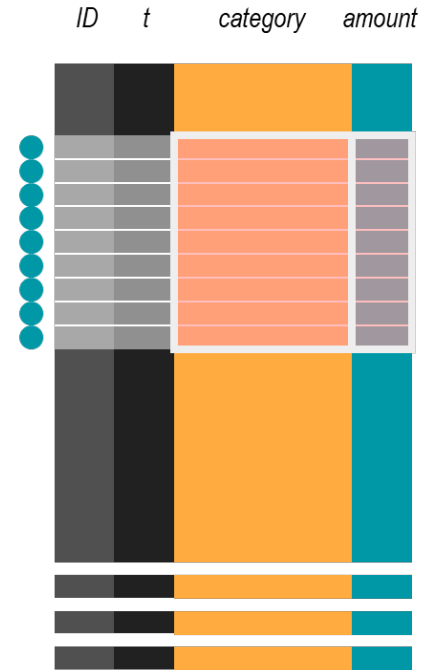
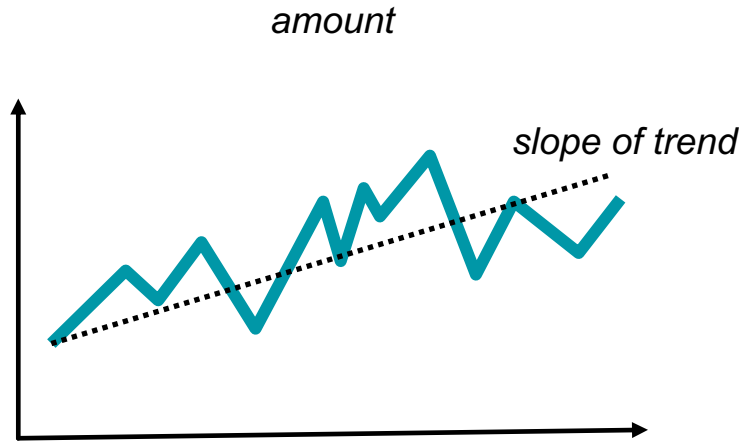


amount – group B



Transaction Data

# Input Possibilities: Tabulations



Transaction Data

# Coding in Action

Data Preparation – Feature Engineering

# Data Preparation

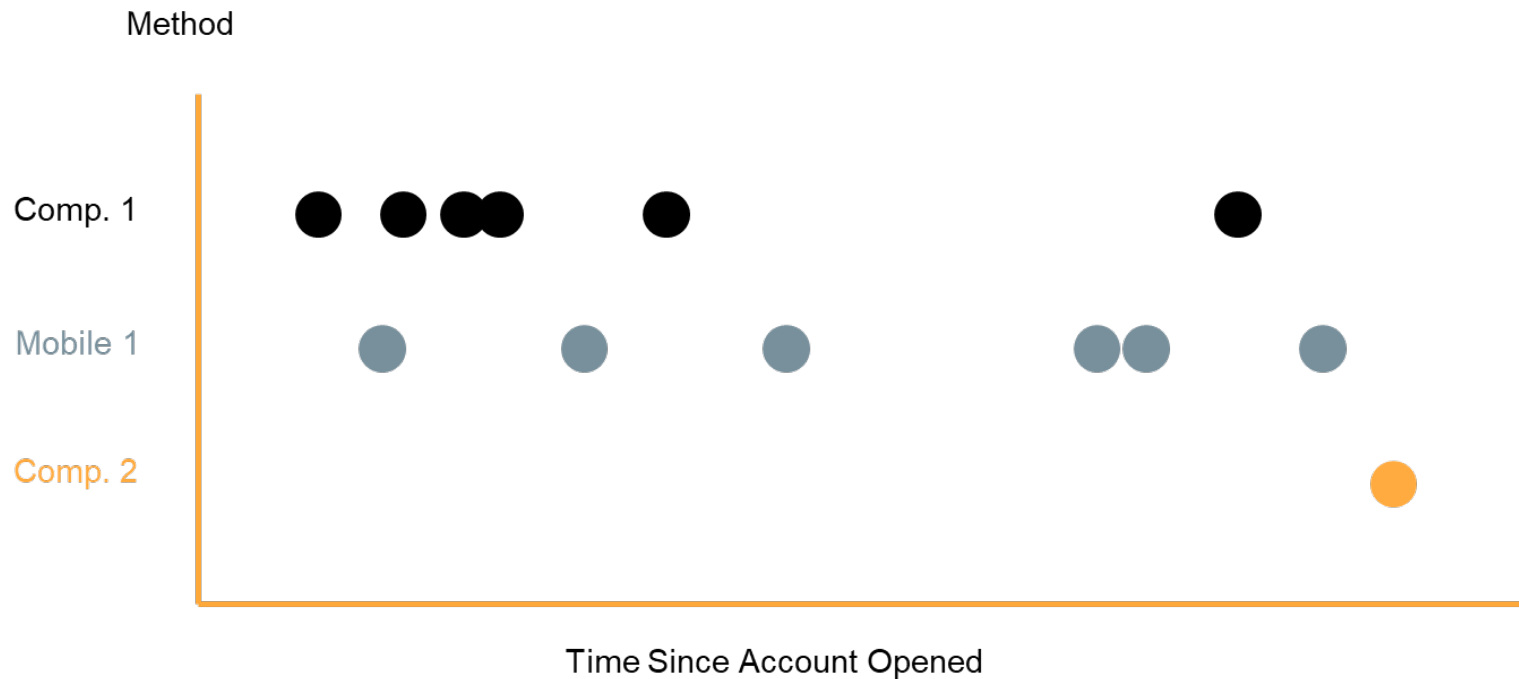
Recency and Frequency

- Data Preparation
  - Feature Engineering
  - Recency and Frequency
  - Categorical Feature Engineering

# Recency & Frequency

- Transactional data provides extensive information.
- Two of the most important things in fraud detection (as well as other fields) are **recency** and **frequency** of transaction.
- **Recency** – time in between transactions
- **Frequency** – how often transactions occur

# Online Account Access Example

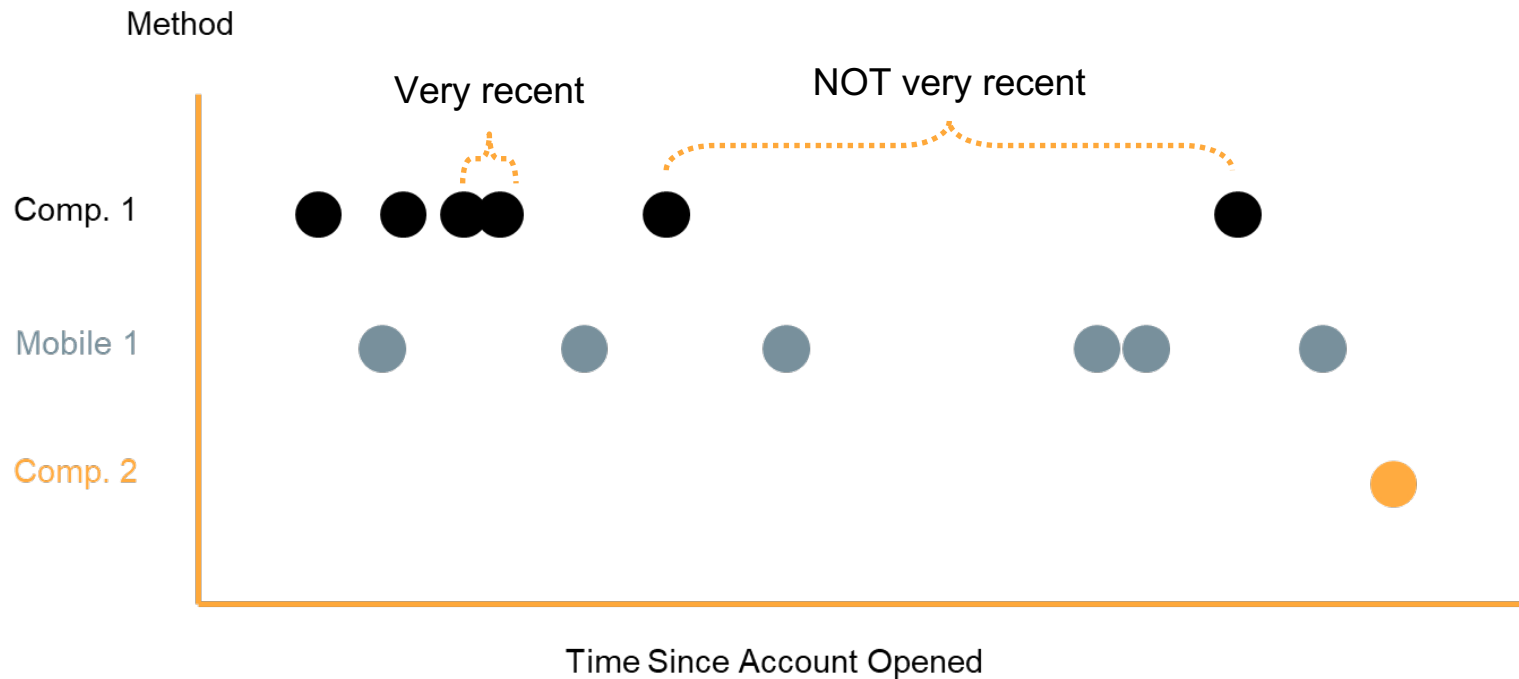




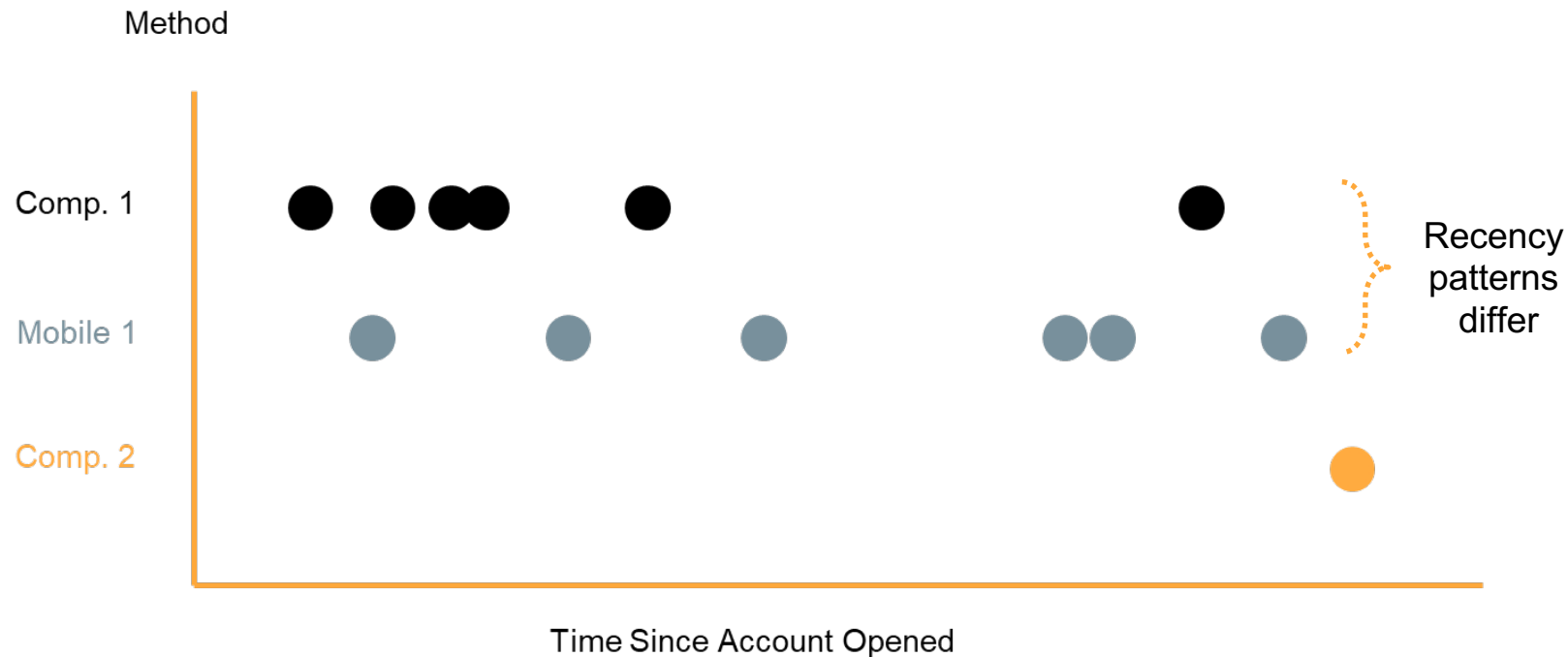
# Recency

- **Recency** – time in between transactions
- Easy features:
  - Time in between transactions
  - Time since last transaction


# Online Account Access Example



# Online Account Access Example



# Recency

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- What if you want to standardize these across different groups (authentication methods)?
- Is time symmetric? 

# Recency

- **Recency** – time in between transactions
- Easy features:
  - Time in between transactions
  - Time since last transaction
- What if you want to standardize these across different groups (authentication methods)?
- Is time symmetric? **NO – Careful how you standardize!**

# Exponential Distribution

- Weight transactions based on their recency, but all on similar scale.
- **Exponential Distribution for Recency:**

$$Recency = e^{-\gamma t}$$

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Tuning parameter  
for decline rate

# Exponential Distribution

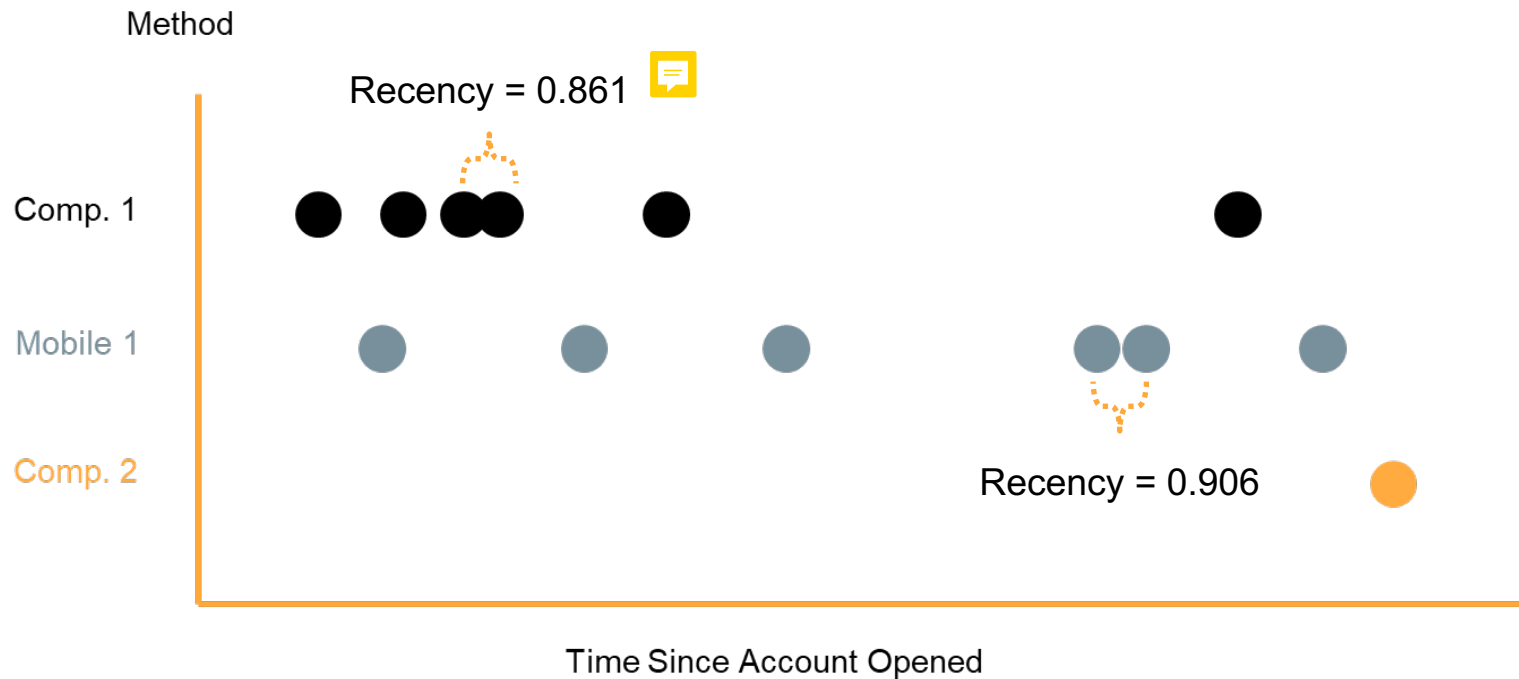
- Weight transactions based on their recency, but all on similar scale.
- **Exponential Distribution for Recency:**

$$\textit{Recency} = e^{-\gamma t}$$

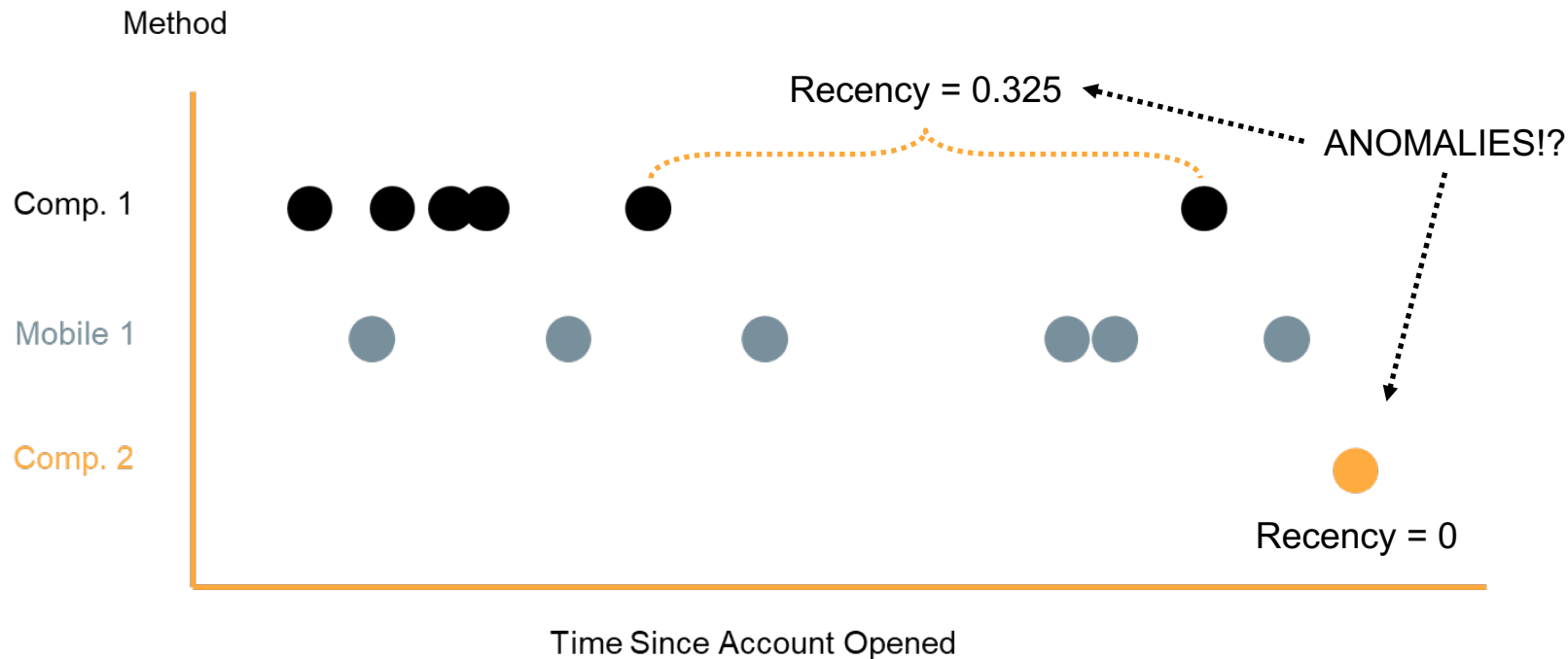
- This forces recency to be bounded between 0 and 1.



# Online Account Access Example



# Online Account Access Example



# How to Pick $\gamma$ ?

- Computer can optimize the parameter  $\gamma$  based solely on your data.
- Authentication Method:
  - Computer 1:  $\gamma = -0.075$
  - Mobile 1:  $\gamma = -0.0492$

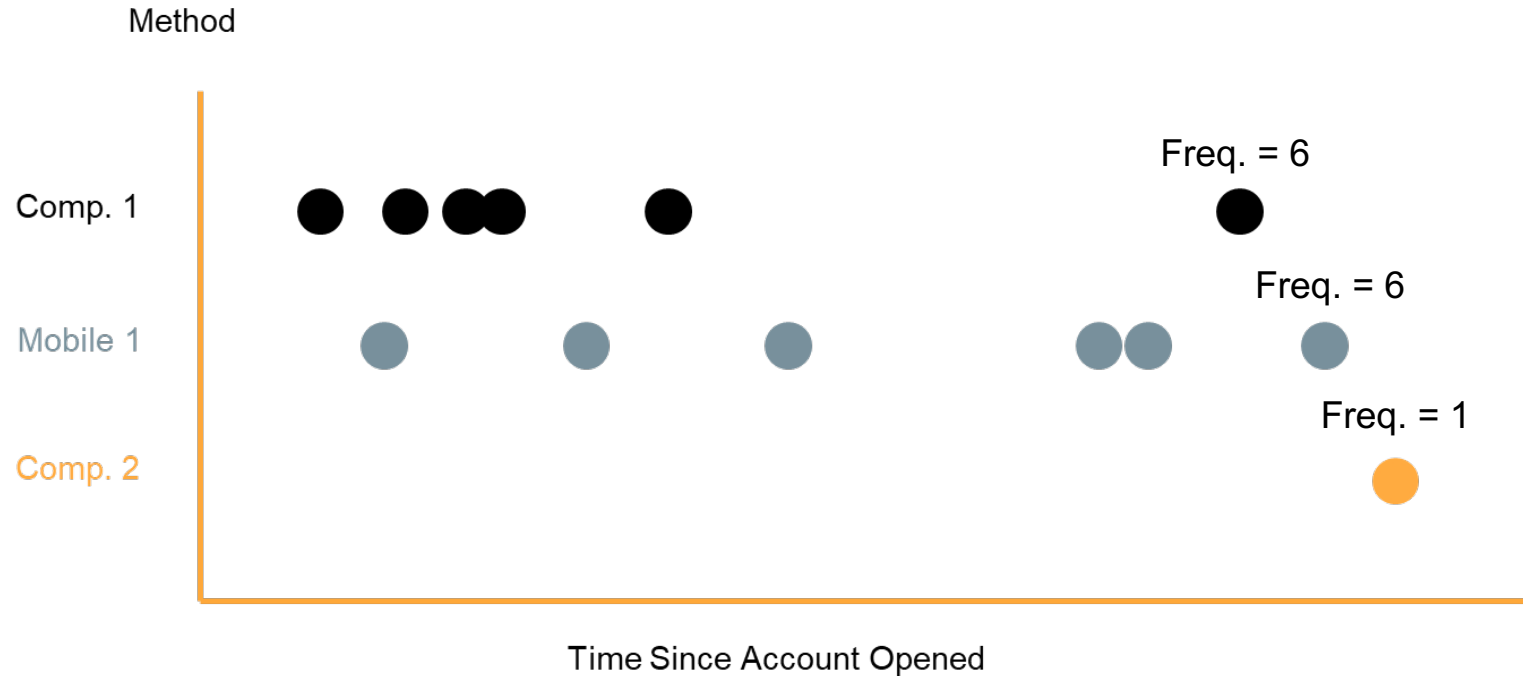
# Coding in Action

Data Preparation – Recency

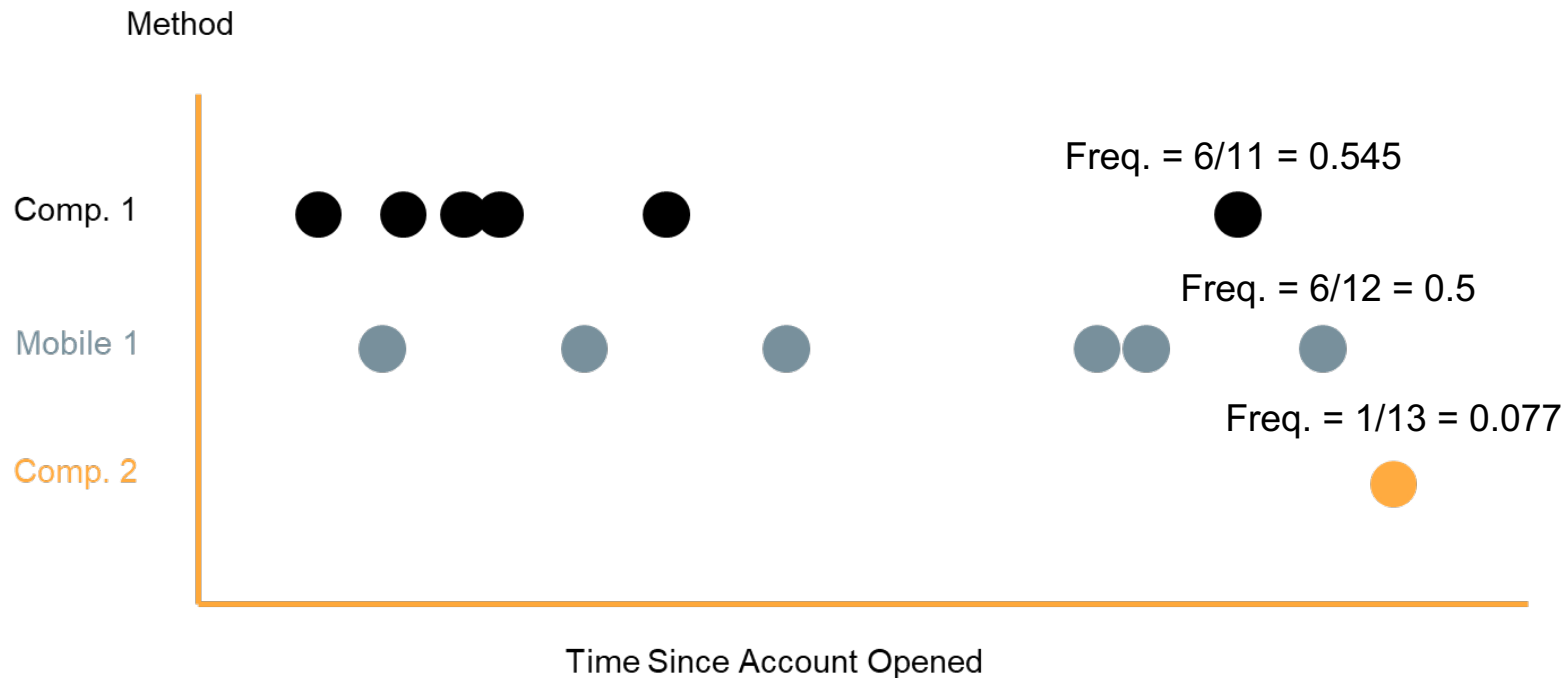
# Frequency

- **Frequency** – how often transactions occur
- Easy features:
  - How many transactions total
  - How many transactions per group
  - Ratio of frequency by group to days active

# Online Account Access Example



# Online Account Access Example



# Coding in Action

Data Preparation – Frequency



# Data Preparation

Categorical Feature  
Engineering

- Data Preparation
  - Feature Engineering
  - Recency and Frequency
  - Categorical Feature Engineering

# Categorical Data

Number of Possible  
Categories

Loyalty program

⋮

Education level

⋮

State

⋮

Medical codes

Free-form text

2



*infinite*

One-hot encoding

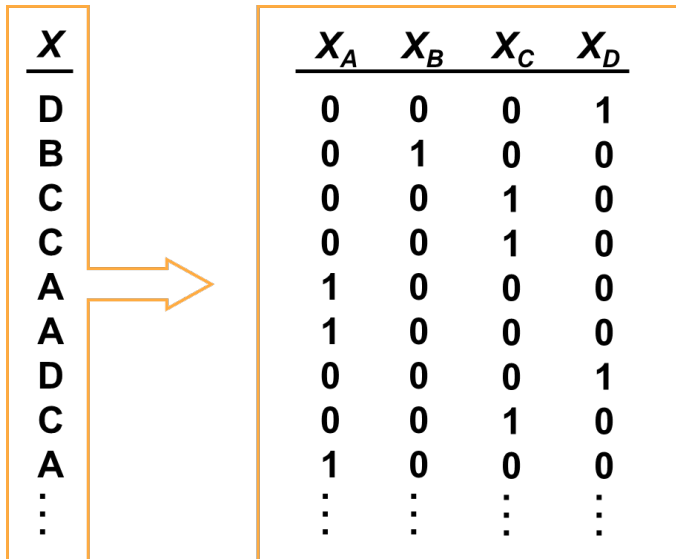
Thresholding

Target-based  
enumeration

Text mining

# One-Hot Encoding

- With limited number of categories, it is easiest to just create binary representations of the categories in separate variables.



| <u>X</u> | <u>X<sub>A</sub></u> | <u>X<sub>B</sub></u> | <u>X<sub>C</sub></u> | <u>X<sub>D</sub></u> |
|----------|----------------------|----------------------|----------------------|----------------------|
| D        | 0                    | 0                    | 0                    | 1                    |
| B        | 0                    | 1                    | 0                    | 0                    |
| C        | 0                    | 0                    | 1                    | 0                    |
| C        | 0                    | 0                    | 1                    | 0                    |
| A        | 1                    | 0                    | 0                    | 0                    |
| A        | 1                    | 0                    | 0                    | 0                    |
| D        | 0                    | 0                    | 0                    | 1                    |
| C        | 0                    | 0                    | 1                    | 0                    |
| A        | 1                    | 0                    | 0                    | 0                    |
| ⋮        | ⋮                    | ⋮                    | ⋮                    | ⋮                    |
| ⋮        | ⋮                    | ⋮                    | ⋮                    | ⋮                    |

# Thresholding

- When you have many categories, you can take the “important” categories (maybe ones with the largest counts) and let all the others be aggregated into an “other” category.

| Level | Sample Size | Default |
|-------|-------------|---------|
| A     | 1562        | 332     |
| B     | 970         | 53      |
| C     | 223         | 17      |
| D     | 111         | 10      |
| E     | 85          | 4       |
| F     | 50          | 10      |
| G     | 23          | 1       |
| H     | 17          | 0       |
| I     | 12          | 1       |
| J     | 5           | 1       |

Recombine into “Other” category

# Target-Based Enumeration

- You can also represent categorical pieces of information numerically through target-based enumeration. Instead of the original categories, we now have a continuous variable for proportion of default.

| Level | Sample Size | Default | Prop. of Default |
|-------|-------------|---------|------------------|
| A     | 1562        | 332     | 0.21             |
| B     | 970         | 53      | 0.05             |
| C     | 223         | 17      | 0.08             |
| D     | 111         | 10      | 0.09             |
| E     | 85          | 4       | 0.05             |
| F     | 50          | 10      | 0.10             |
| G     | 23          | 1       | 0.04             |
| H     | 17          | 0       | 0.00             |
| I     | 12          | 1       | 0.08             |
| J     | 5           | 1       | 0.20             |

# Level Clustering

- However, these new numeric representations can also be ordered and combined into new categories as well.

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# Level Clustering

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| Level | Sample Size | Default | Prop. of Default | New Level |
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| H     | 17          | 0       | 0.00             | D         |

# Derived Fields from Text

- Text mining can provide an immense amount of data when limited data may seem to exist.
- Mining the text data may reveal patterns that can be adapted into input variables.
- Text mining is not covered in this course.



# Coding in Action

Data Preparation – Categorical Feature Engineering

# Data Preparation

Conclusion

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# Probability and Statistical Approaches

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# Probability and Statistical Approaches

- Probability and Statistical Approaches
  - Benford's Law
  - Z-scores and Robust Z-scores
  - IQR Rule and Its Adjustment
  - Mahalanobis Distances and Robust Mahalanobis

# Probability and Statistical Approaches

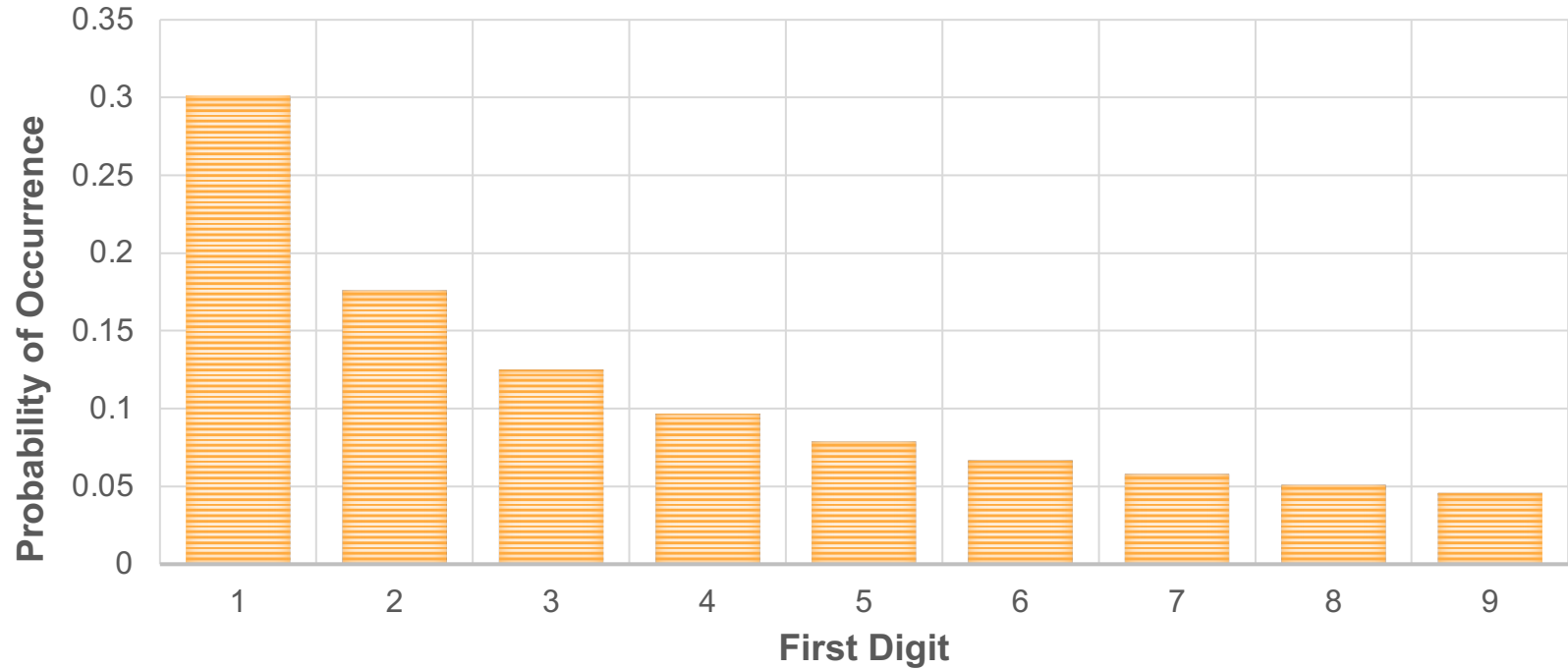
Benford's Law

- Probability and Statistical Approaches
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# Benford's Law

- Certain numbers do not occur uniformly despite what we might think.
- Digits of certain numbers follow Benford's Law.
- Example:
  - First digit of house/building numbers in addresses.
  - First digit of transaction amounts.

# Benford's Law



# Benford's Law

- This wasn't mathematically proven until the mid-90's.
- <http://testingbenfordslaw.com/>
- Benford's Law – First Digit

$$P(d_1) = \log_{10} \left( 1 + \frac{1}{d_1} \right)$$

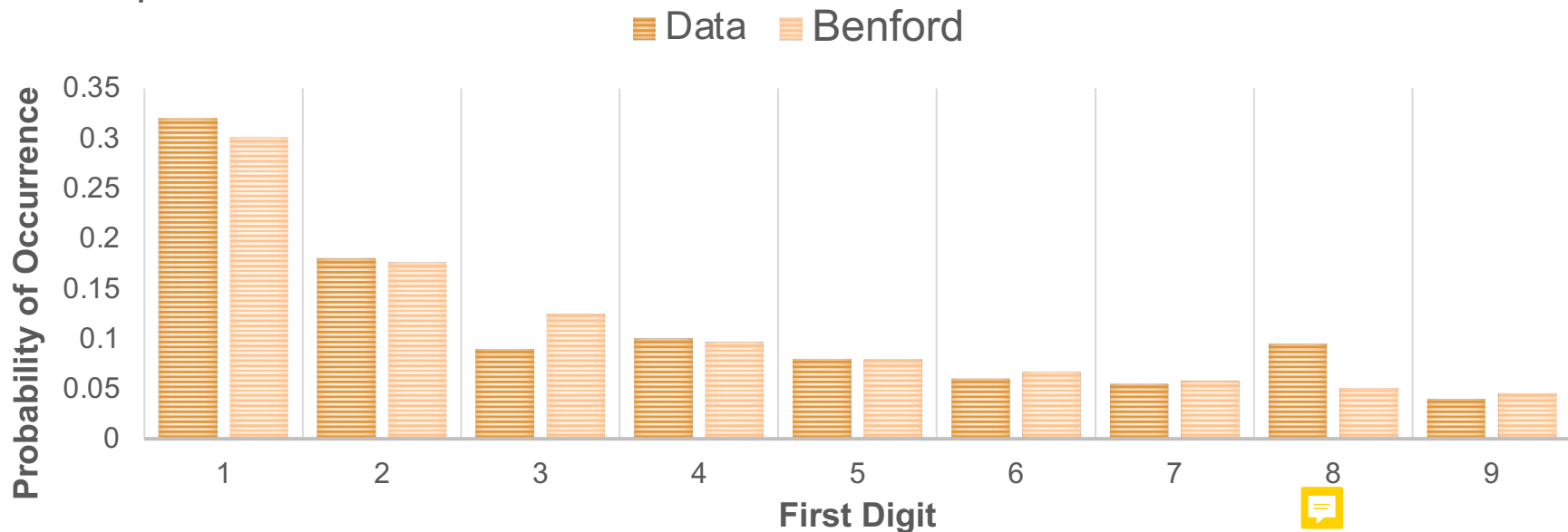


# Benford's Law – Fraud Detection

- Fraud transactions typically involve inventing new numbers or changing real transactions into fraudulent ones.
- Legally admissible in Federal, State, and Local courts in United States as evidence.

# Benford's Law – Fraud Detection

- Example transaction amounts submitted for reimbursement from scanned receipts



# Benford's Law

- Fraud detection typically uses the first two digits in Benford's Law.
- Benford's Law – First Two Digits

$$P(d_1 d_2) = \log_{10} \left( 1 + \frac{1}{d_1 d_2} \right)$$

$$d_1 d_2 \in [10, 11, 12, 13, \dots, 99]$$

# Coding in Action

Probability and Statistical Techniques – Benford's Law

# Probability and Statistical Approaches

Z-scores and Robust Z-scores

- Probability and Statistical Approaches
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# Statistical Methods

- Basic fraudulent systems look for abnormal observations from a statistical standpoint.
- Univariate analysis can help identify fraudulent **transactions** or **people** (aggregated transactions).

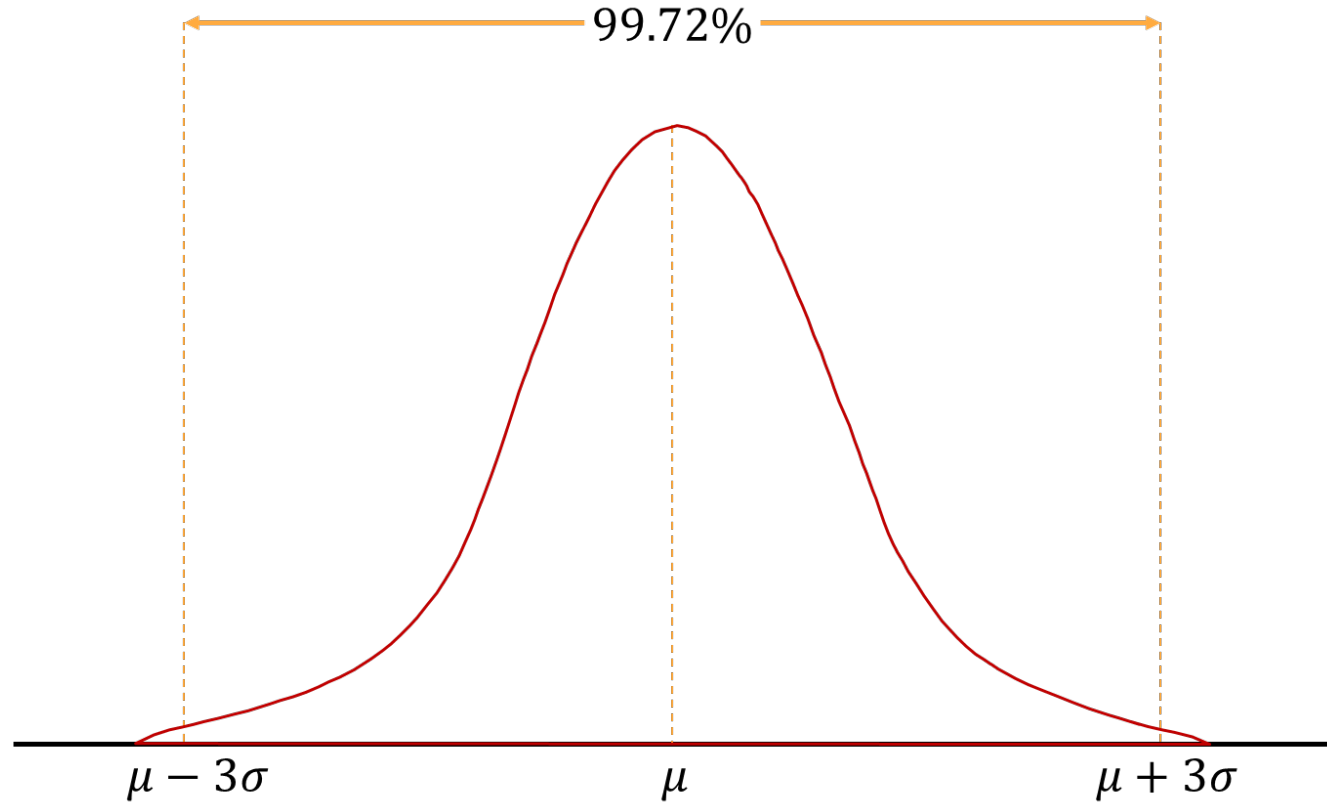
# Z-Scores

- Typical with Normal distributions.

$$z_i = \frac{x_i - \bar{x}}{s}$$

- Measures how many standard deviations away from mean each point is.
- Works best with **symmetric** distributions.

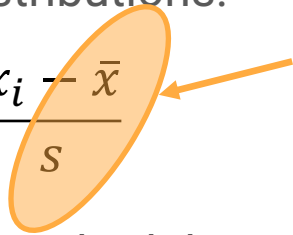
# Empirical Rule





# Z-Scores

- Typical with Normal distributions.

$$z_i = \frac{x_i - \bar{x}}{s}$$


Bothered by  
outliers

- Measures how many standard deviations away from mean each point is.
- Works best with **symmetric** distributions.

# Robust Statistics

- Outliers can greatly influence results.
- Robust techniques
  1. Reliable when outliers present
  2. Reliable when outliers **not** present (ideally)

# Robust Z-Scores

- Robust adjustments to mean and standard deviation.

$$z_{R,i} = \frac{x_i - \text{median}(x)}{\text{MAD}(x)}$$

- Median Absolute Deviation (MAD):

$$\text{MAD}(x) = k \times \text{median}(|x_i - \text{median}(x)|)$$

# Robust Z-Scores

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Adjustment factor per  
distribution

# Robust Z-Scores

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$$z_{R,i} = \frac{x_i - \text{median}(x)}{\text{MAD}(x)}$$

- Median Absolute Deviation (MAD):

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1.4826 for Normal  
distribution

# Coding in Action

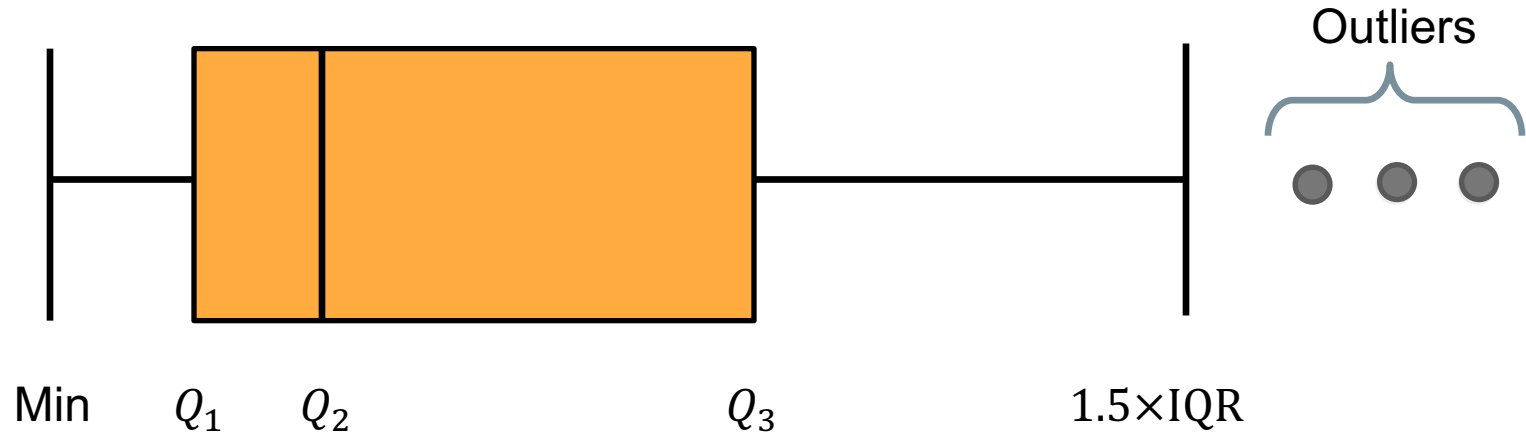
Probability and Statistical Techniques – Z-Scores and Robust Z-Scores

# Probability and Statistical Approaches

IQR Rule and Its Adjustment

- Probability and Statistical Approaches
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## 1.5 IQR Rule





## 1.5 IQR Rule

- Works best for **symmetric** distributions.
- Severely skewed distributions tend to report large number of outliers.
- Some software (like R) can use **adjusted boxplot** instead – more robust to skewed distributions.

# Coding in Action

Probability and Statistical Techniques – IQR Rule and Its Adjustment

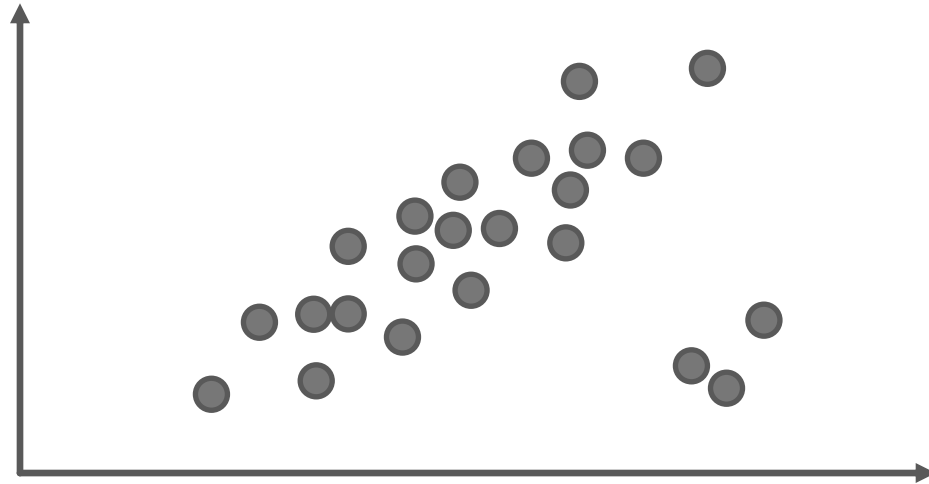
# Probability and Statistical Approaches

Mahalanobis Distances and Robust Mahalanobis

- Probability and Statistical Approaches
  - Benford's Law
  - Z-scores and Robust Z-scores
  - IQR Rule and Its Adjustment
  - Mahalanobis Distances and Robust Mahalanobis

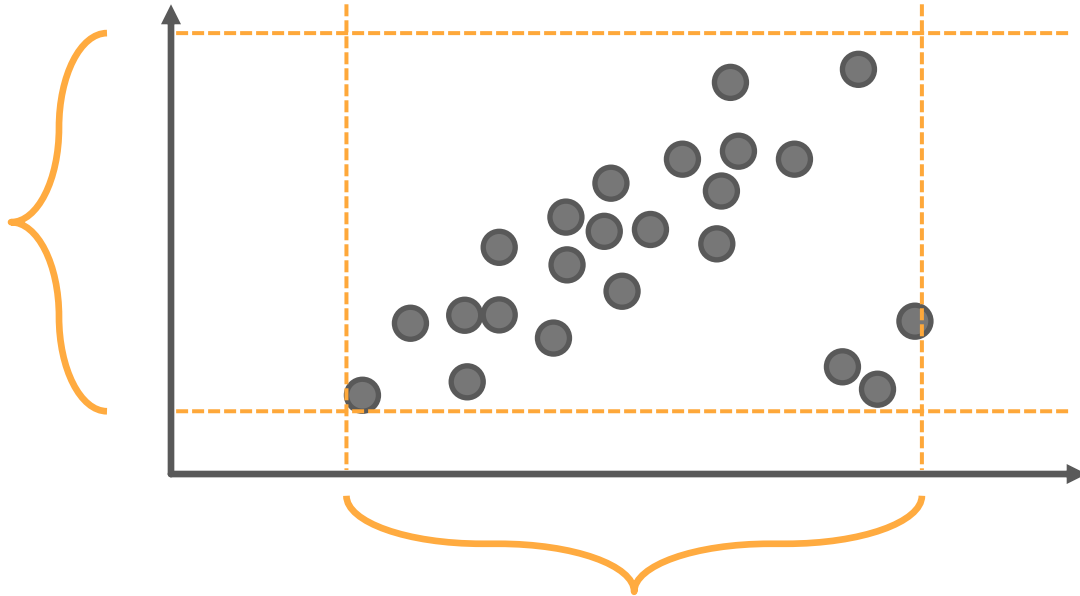
# Multiple Dimensions

- Outliers in one dimension are possibly restrictive.



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# Mahalanobis Distances

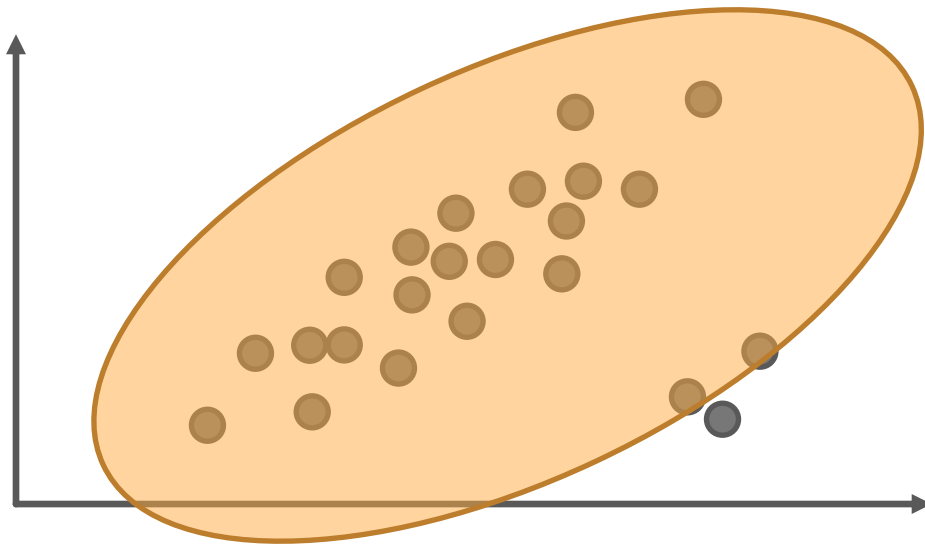
- Generalization of z-scores to multi-dimensional space.
  - Replace univariate mean with **multivariate mean**
  - Replace standard deviation with **covariance matrix**

# Mahalanobis Distances

- Generalization of z-scores to multi-dimensional space.
  - Replace univariate mean with **multivariate mean**
  - Replace standard deviation with **covariance matrix**
- Euclidean Distance (L2):  $D_{L2} = \sqrt{(x - \mu)^T (x - \mu)}$
- Mahalanobis Distance:  $D_M = \sqrt{(x - \mu)^T \Sigma^{-1} (x - \mu)}$

# Confidence Ellipsoids

- Still bothered by outliers since standard mean and covariance matrix used.





# Robust Mahalanobis Distances

- Mahalanobis distances use mean and covariance matrix influenced by outliers.
- Use **robust** calculations of mean vector and covariance matrix instead:

$$D_M = \sqrt{(x - \mu_{MCD})^T \Sigma_{MCD}^{-1} (x - \mu_{MCD})}$$

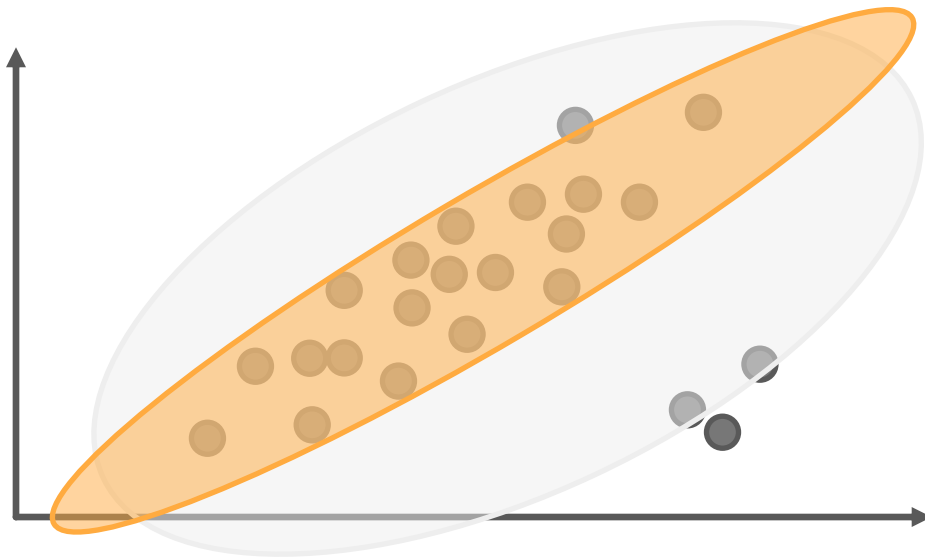
# Robust Mahalanobis Distances

$$D_M = \sqrt{(x - \mu_{MCD})^T \Sigma_{MCD}^{-1} (x - \mu_{MCD})}$$

- MCD: Minimum Covariance Determinant
  - Find  $h$  ( $< n$ ) observations that have MCD (essentially the tightest cloud)
  - Typically  $h = 0.75 \times n$
  - Problem: How to find the right  $h$  observations?
  - Fast algorithms exist

# Confidence Ellipsoids

- Robust version isn't impacted by outliers as drastically.



# Coding in Action

Probability and Statistical Techniques –

Mahalanobis Distance & Robust Mahalanobis

# Probability and Statistical Approaches

Conclusion

- Probability and Statistical Approaches
  - Benford's Law
  - Z-scores and Robust Z-scores
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  - Mahalanobis Distances and Robust Mahalanobis

# Machine Learning Approaches



# Machine Learning Approaches

- Machine Learning Approaches
  - k-Nearest Neighbors (kNN)
  - Local Outlier Factor (LOF)
  - Isolation Forests
  - Classifier-Adjusted Density Estimation (CADE)
  - One-Class Support Vector Machine (SVM)

# Machine Learning Approaches

k-Nearest Neighbors (kNN)

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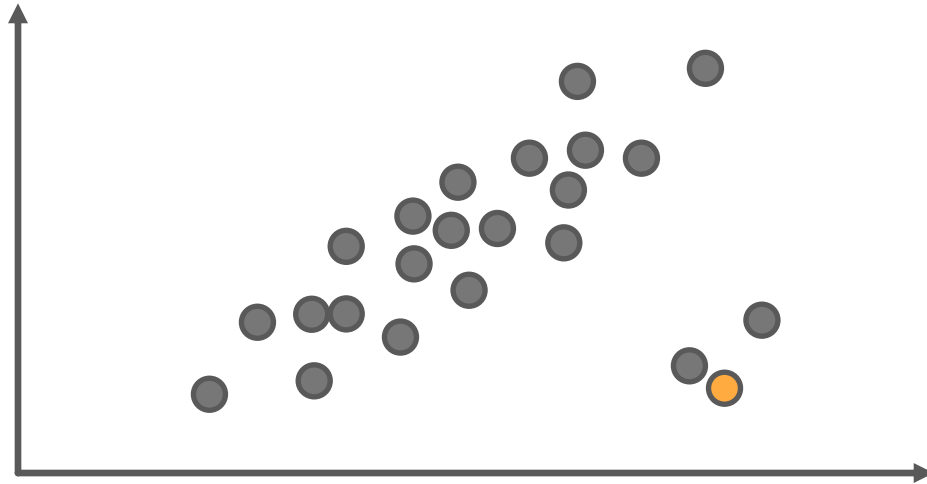


# k-Nearest Neighbors

- Want to discover points that are “not close” to the rest.
- Instead of distance from center of cloud, k-NN looks at distance from close points.
- Measure **average** distance from a point to each of the k-closest points.
  - Default: Euclidean distance

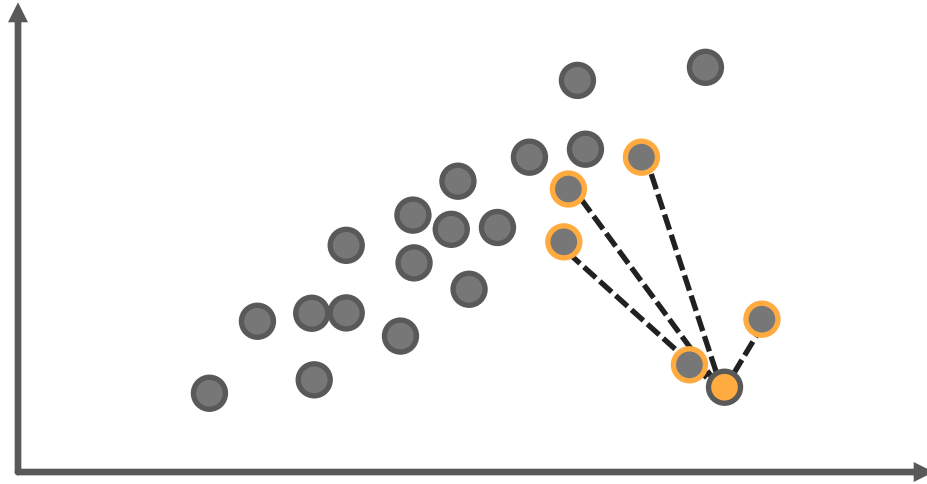
# k-Nearest Neighbors

- Need to measure distances to  $k$  nearest observations.



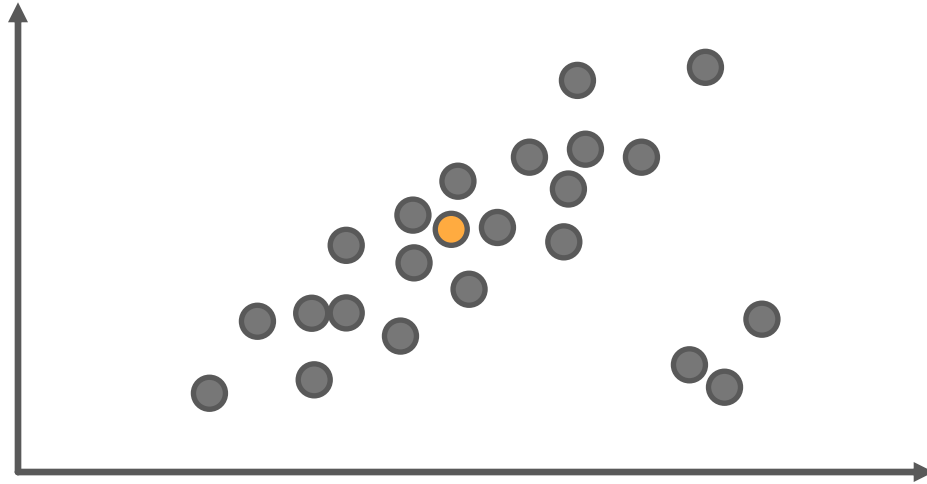
# k-Nearest Neighbors

- Need to measure distances to 5 nearest observations.



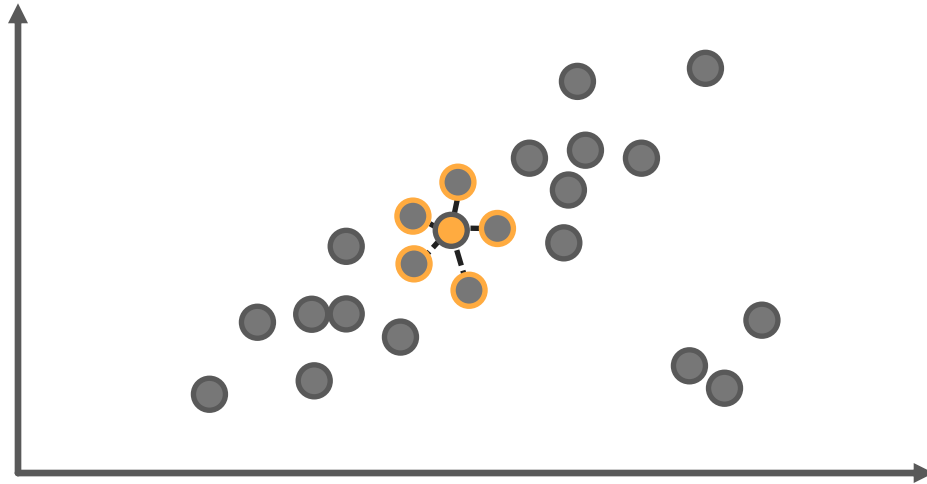
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# k-Nearest Neighbors

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# Coding in Action

Machine Learning Techniques – k-Nearest Neighbors

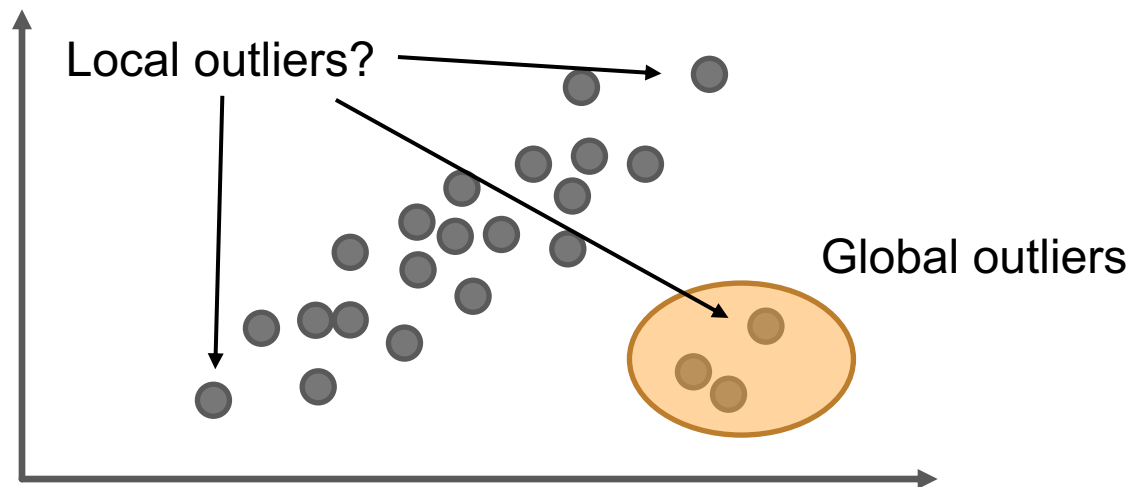
# Machine Learning Approaches

Local Outlier Factor (LOF)

- Machine Learning Approaches
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# Global vs. Local Outliers

- k-NN great at detecting **global** outliers, but not **local** outliers.





# Local Outlier Factor (LOF)

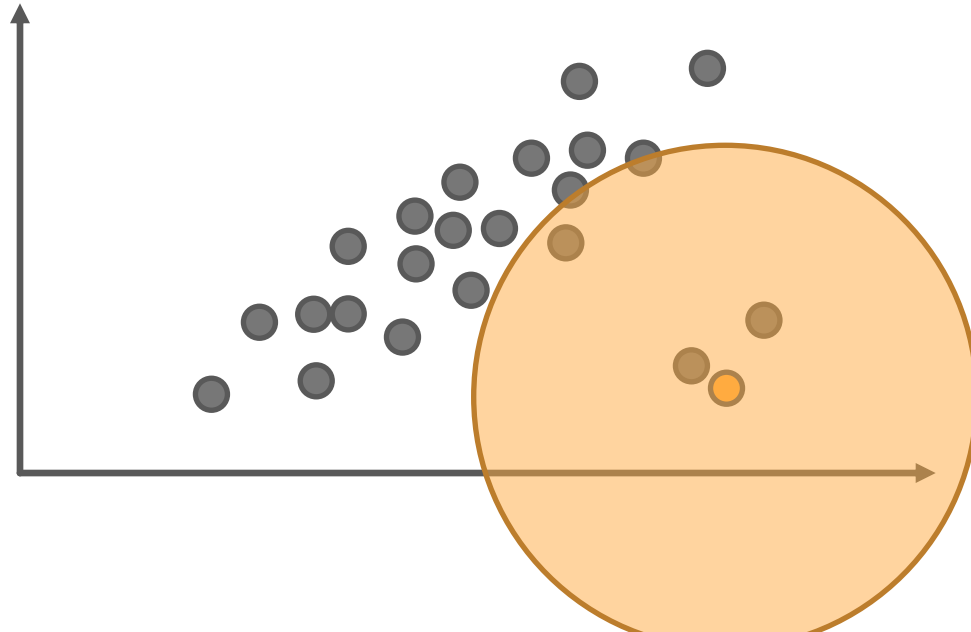
- LOF:
  - Ratio (comparison) of the average **density** of the k-NN of an observation to the **density** of the observation itself.
  - $> 1$  means more likely to be anomaly
  - $< 1$  means less likely to be anomaly

# Local Outlier Factor (LOF)

- LOF:
  - Ratio (comparison) of the average **density** of the k-NN of an observation to the **density** of the observation itself.
- Density:
  - Inverse of the average **reachability** (distances) from observation to all of its k-NN.
  - Essentially, how far do we have to travel to nearest point, so less dense means farther travel.

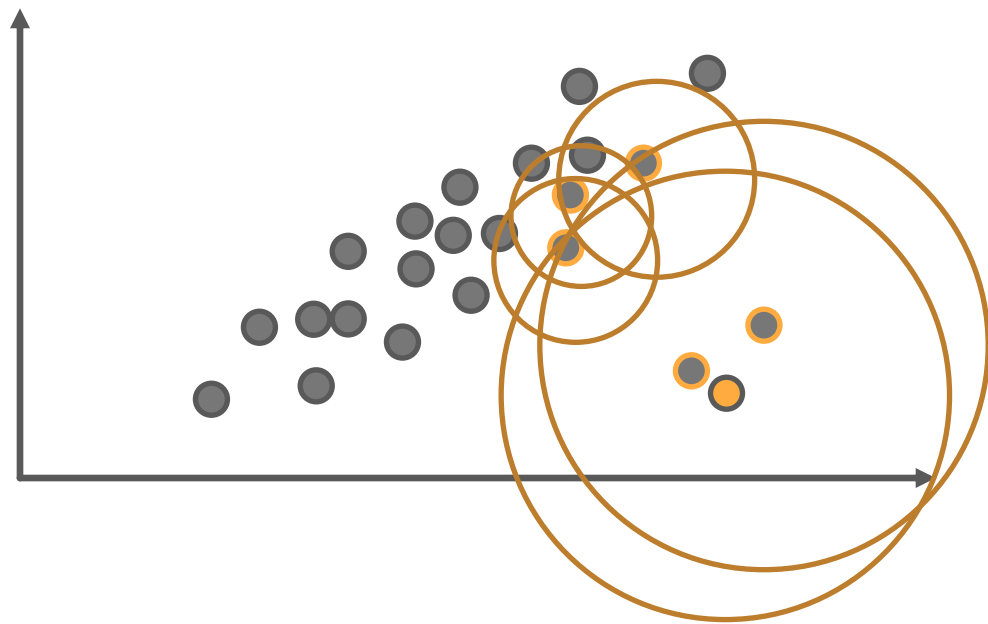
# Local Outlier Factor (LOF)

- Density of observation of interest



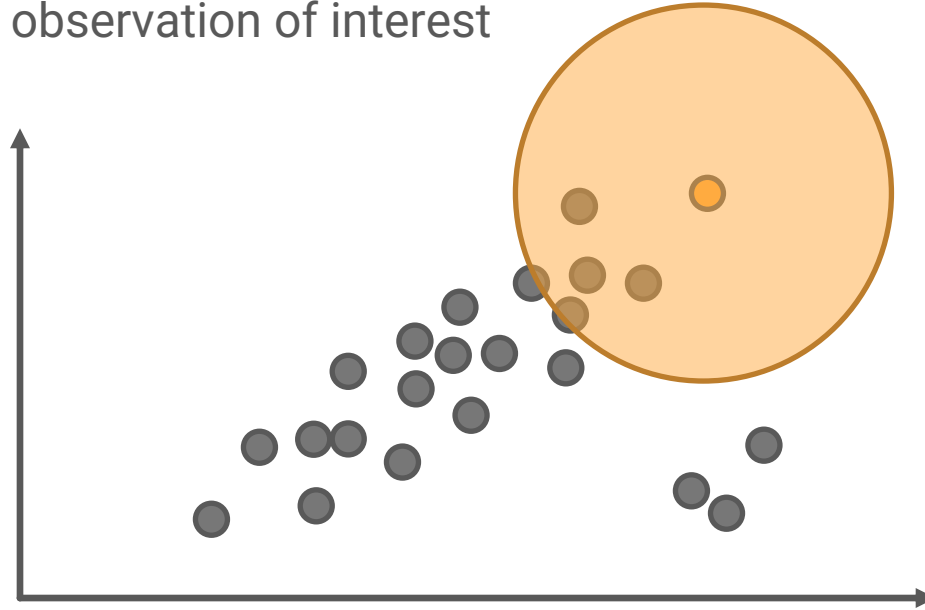
# Local Outlier Factor (LOF)

- Need to average the densities of the k-NN observations.



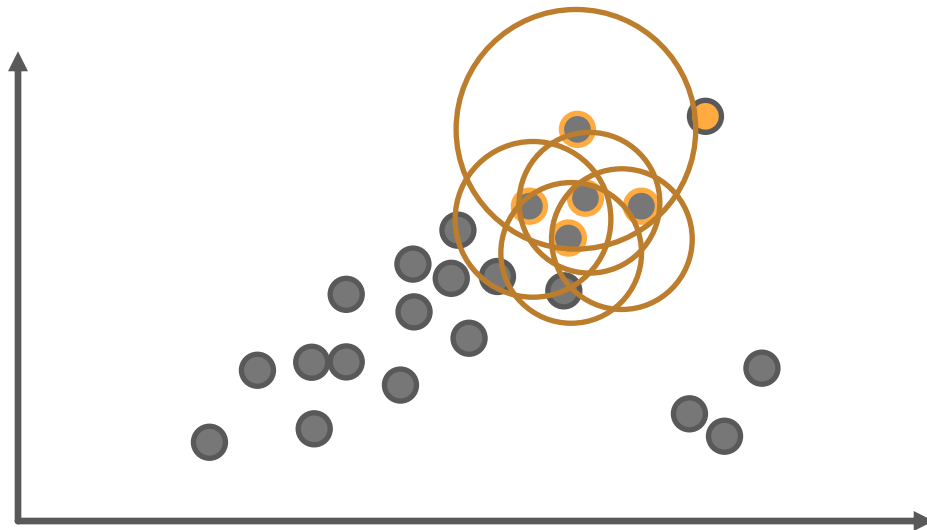
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# Coding in Action

Machine Learning Techniques – Local Outlier Factor (LOF)

# Machine Learning Approaches

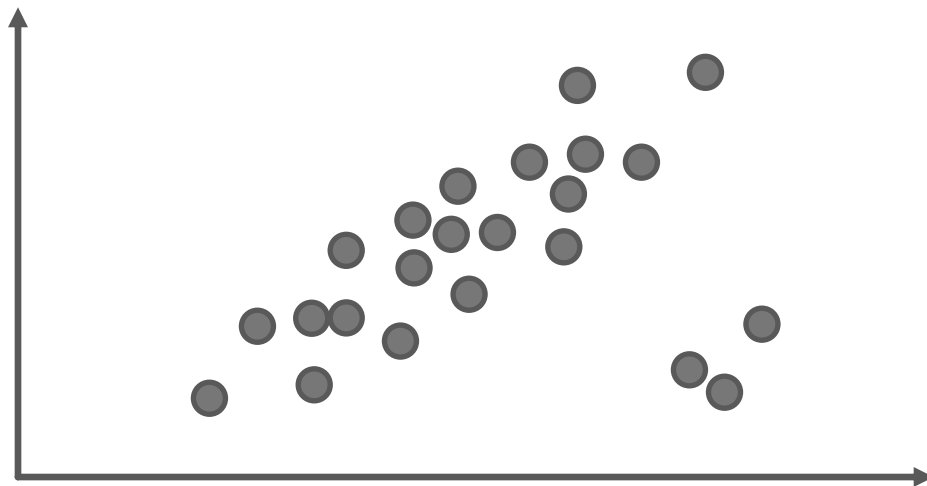
Isolation Forests

- Machine Learning Approaches
  - k-Nearest Neighbors (kNN)
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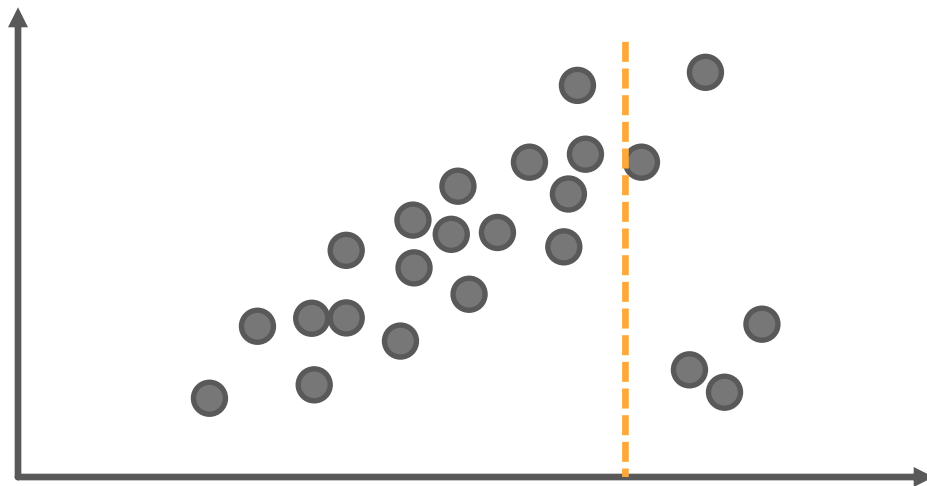
# Isolation Tree

- Tree-based algorithm to isolate observations.
- Easier the isolation  $\rightarrow$  More likely an anomaly!



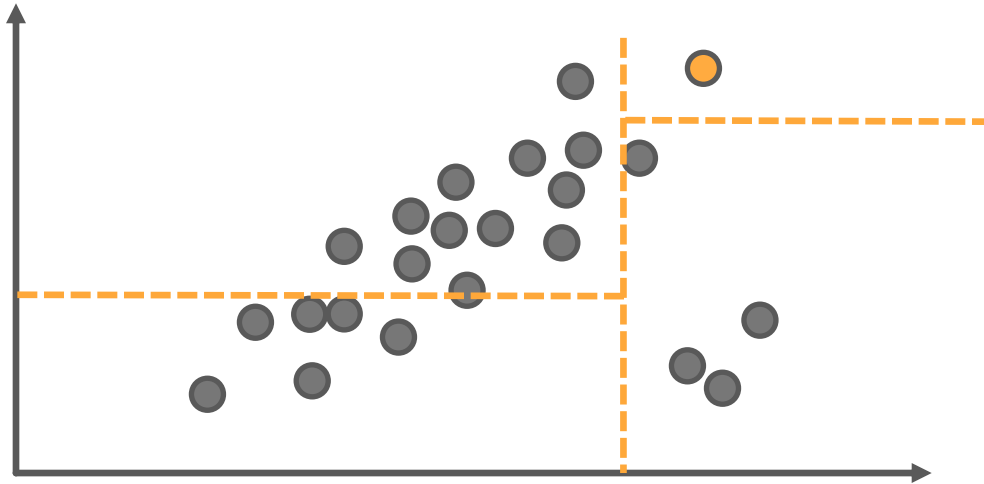
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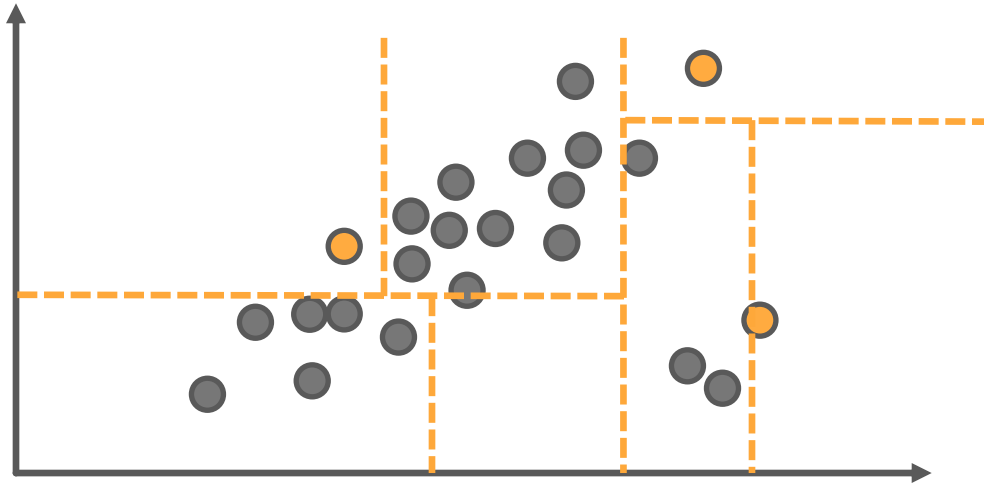
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# Isolation Tree

- Tree-based algorithm to isolate observations.
- Easier the isolation → More likely an anomaly!
- Isolation score is inversely related to number of needed splits to isolate observation.
  - Bounded between 0 and 1.
  - Closer to 1 → more likely an anomaly
  - Closer to 0 → less likely an anomaly
  - All observations  $\sim 0.5$ , no real anomalies

# Isolation Forest

- Since the isolation trees are based on random splits on random dimensions, outlier might get lucky and survive longer than it really should.
- Isolation forest – combination of MANY isolation trees with averaged scores.
- Look for convergence of scores for optimal number of trees.

# Coding in Action

Machine Learning Techniques – Isolation Forest

# Machine Learning Approaches

Classifier-Adjusted Density Estimation (CADE)

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# CADE

- Newer technique for density estimation.
- Value been found in anomaly detection and fraud applications.

# CADE

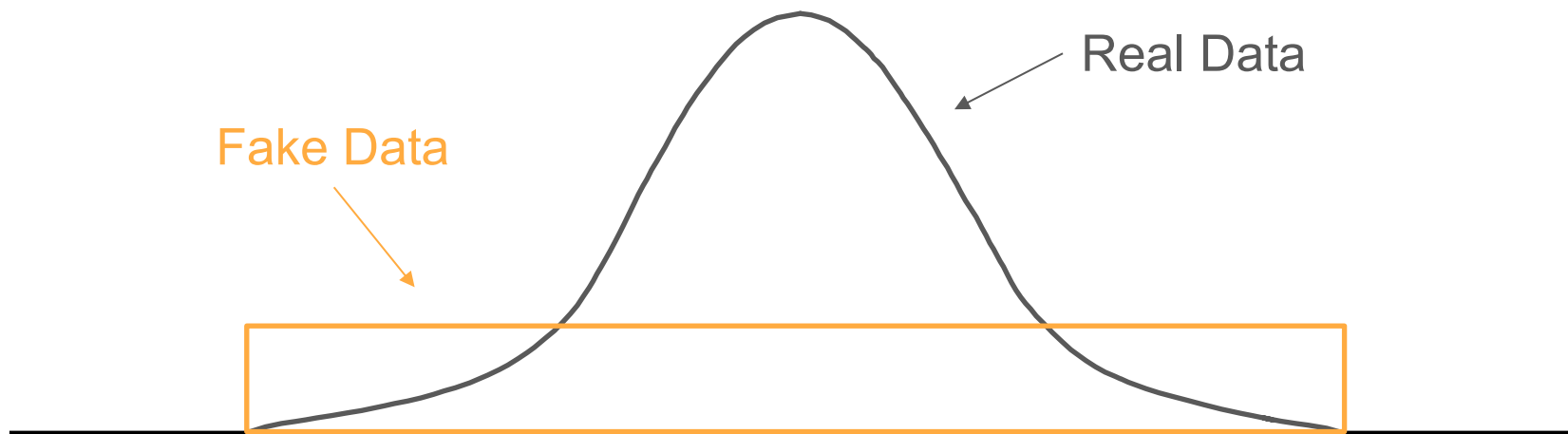
- Process:
  1. Label all original data as **not outliers**
  2. Create new observations (same  $n$  as data) but variables are all uniformly distributed
  3. Label all new data as **outliers**, merge old and new data
  4. Use classification model to predict “outliers” (1’s).
  5. Score original data

# CADE

- High predicted probabilities → More likely an anomaly!
- Observation looks more like fake uniform data than actual distribution from which it came in multivariate space.

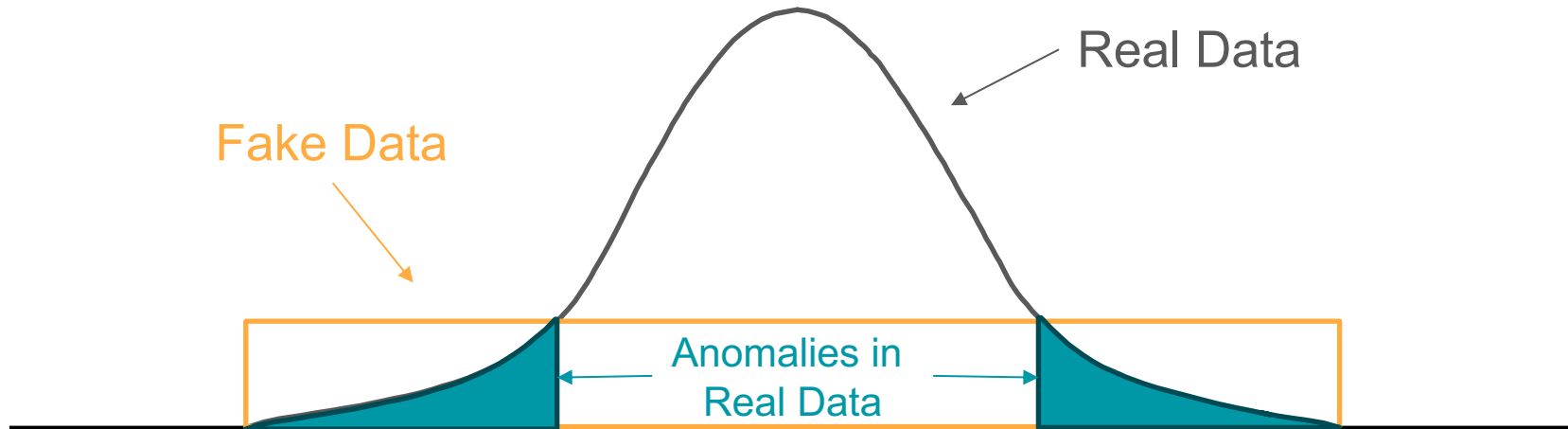
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# CADE

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# Coding in Action

Machine Learning Techniques – Classifier-Adjusted Density Estimation

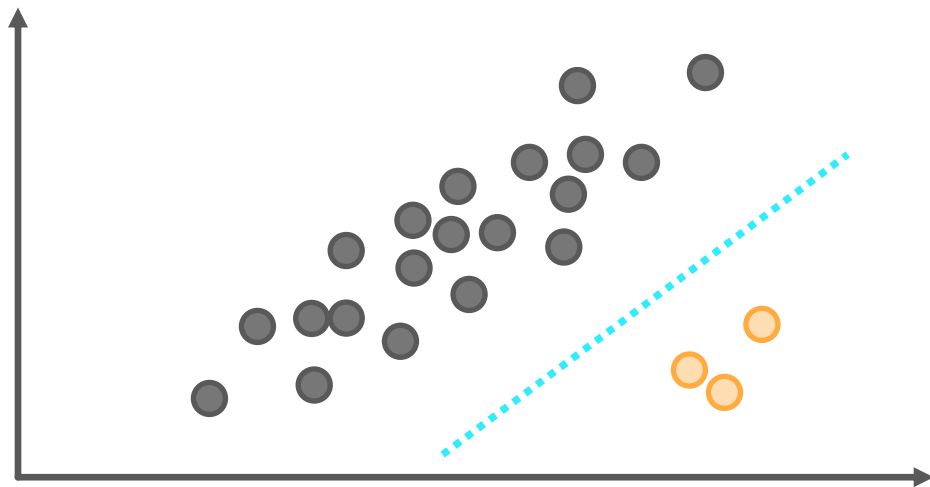
# Machine Learning Approaches

One-Class Support Vector Machine (SVM)

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# Support Vector Machines (SVM)

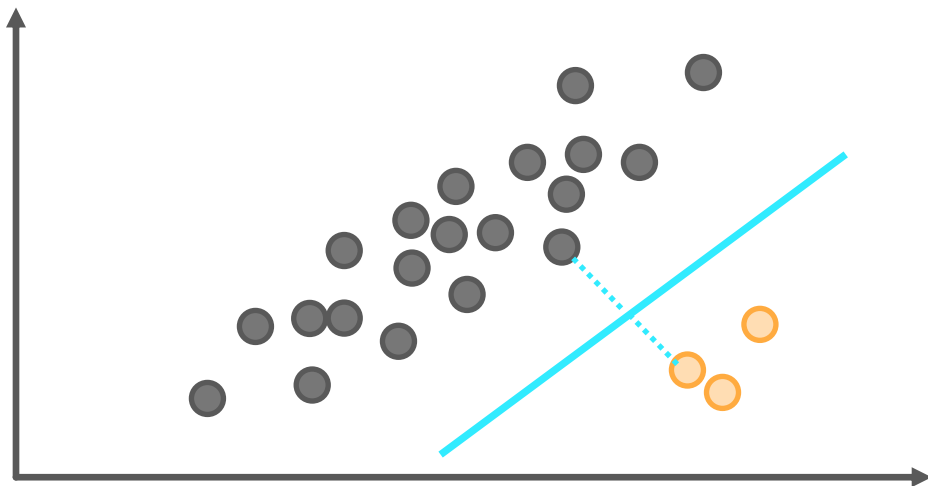
- A traditional two-class SVM is a classifier.
- It creates a hyperplane that “best” separates the two classes.





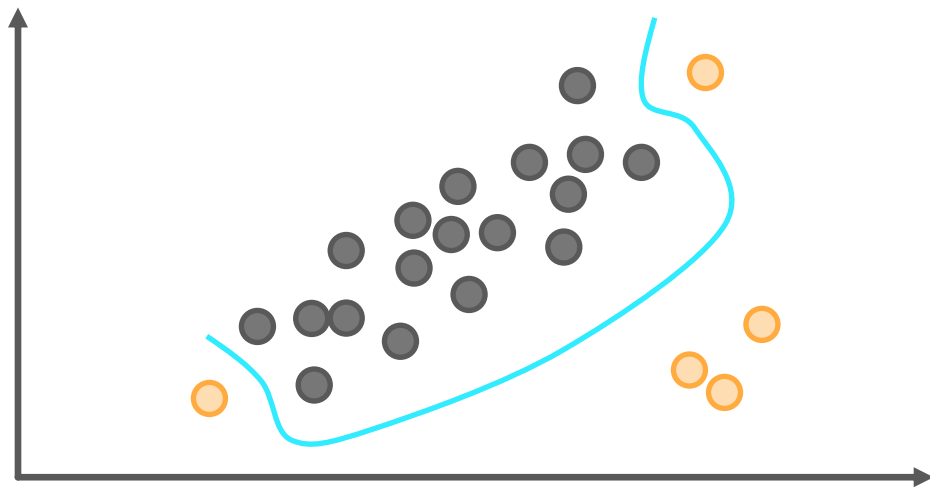
# Support Vector Machines (SVM)

- A traditional two-class SVM is a classifier.
- It creates a hyperplane that “best” separates the two classes.
- “Best” is maximizing the distance (in every dimension) from the two classes.



# Support Vector Machines (SVM)

- A traditional two-class SVM is a classifier.
- Not limited to linear separation! Kernels are used to make hyperplanes nonlinear.

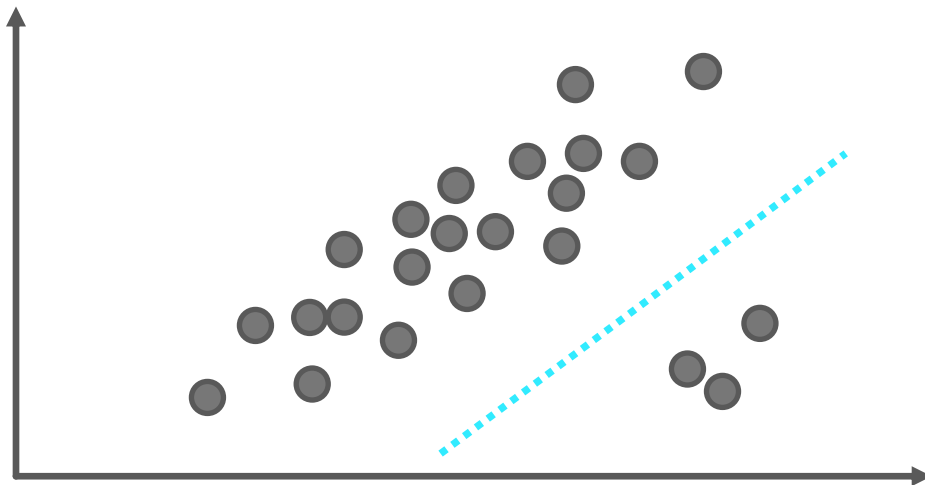


# One-Class Support Vector Machines

- SVM's are also used in an unsupervised learning scenario as well.
- Instead of thinking about two classes, we can take one of two approaches:
  1. Tell the SVM to isolate the X% of observations. If we think we have 5% anomalies, we tell the SVM to isolate the “most” anomalous 5% of observations.
  2. Train the SVM on all data as normal and score new data to see if it falls “within normal”.

# One-Class Support Vector Machines

- Tell the SVM to isolate the X% of observations. If we think we have 5% anomalies, we tell the SVM to isolate the “most” anomalous 5% of observations.



# Coding in Action

Machine Learning Techniques – One-Class Support Vector Machine

# Machine Learning Approaches

Conclusion

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# Conclusion

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# Course Outline

- Introduction
- Data Preparation
- Probability & Statistical Techniques
- Machine Learning Techniques
- Conclusion



# Course Outline

- Introduction
  - Who am I?
  - What are Anomalies?
  - Anomaly Detection Analytical Framework
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# Course Outline

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# Where Am I?

- Find me online:
  - <https://www.linkedin.com/in/ariclabarr/>
  - <https://www.youtube.com/c/AricLaBarr/>
  - <https://www.ariclabarr.com/>



Thank you

